

## **Following are the example problems in Probability**

**Probability:** It is the measure of possible occurrence of an event.

$$\text{Probability} = \frac{\text{No. of times an event can occur}}{\text{Total number of possible}}$$

- Tossing a coin and what is the probability of getting Head
  - $\Pr(H) = \frac{1}{2}$
- Rolling a dice and what is the probability of getting 1
  - $\Pr(1) = \frac{1}{6}$

**Mutual Exclusive Events:** In the experiment or event, one only possible outcome can be occurred.

- Tossing a coin possibility of Head or Tail is possible but Head and Tail is not possible.
- Rolling a die possibility of 1 or 2 or 3 or 4 or 5 or 6 is possible but both 1 and 2 or 2 and 3 or 3 and 4 similarly combination not possible.

### **Additive Rule for Mutual Exclusive Events (Formulae)**

$$\Pr(A \text{ or } B) = \Pr(A) + \Pr(B)$$

- Tossing a coin, probability of Head or Tail

$$\begin{aligned}\Pr(H \text{ or } T) &= \Pr(H) + \Pr(T) \\ &= \frac{1}{2} + \frac{1}{2} \\ &= 1\end{aligned}$$

- Rolling a die, probability of 1 or 2 or 3

$$\begin{aligned}\Pr(1 \text{ or } 2 \text{ or } 3) &= \Pr(1) + \Pr(2) + \Pr(3) \\ &= \frac{1}{6} + \frac{1}{6} + \frac{1}{6} \\ &= \frac{3}{6}\end{aligned}$$

**Non-mutual Exclusive Events:** In the experiment or event, more than one possible outcome can be occurred.

- Taking out a card from deck of pack possibility of King or Heart can be possible.

### **Additive Rule for Non-Mutual Exclusive Events (Formulae):**

$$\Pr(A \text{ or } B) = \Pr(A) + \Pr(B) - \Pr(A \cap B)$$

- Taking out a card from deck, what is the probability of value King or Heart

$$\begin{aligned}\Pr(K \text{ or } H) &= \Pr(K) + \Pr(H) - \Pr(K \cap H) \\ &= \frac{4}{52} + \frac{13}{52} - \frac{1}{52}\end{aligned}$$

$$\Pr(\text{King or Heart}) \text{ is } \frac{16}{52}$$

### **Multiplicative Rule (Formulae)**

**A. Independent Event:** Total number of Outcome will not reduce in the next trial.

- Tossing a coin 3 times independently, what is the probability of first time Head, second time Tail then third time Head

$$\begin{aligned}\Pr(\text{H and T and H}) &= \Pr(\text{H}) * \Pr(\text{T}) * \Pr(\text{H}) \\ &= \frac{1}{2} * \frac{1}{2} * \frac{1}{2} \\ &= \frac{1}{8}\end{aligned}$$

**B. Dependent Event (Conditional Event):** Total number of Outcome will reduce in the next trial.

$$\Pr(\text{A and B}) = \Pr(\text{A}) * \Pr(\text{B/A})$$

$\Pr(\text{B/A})$  means Probability of B given A

- What is the probability first remove King then Queen from deck of cards?

$$\Pr(\text{K and Q}) = \Pr(\text{K}) * \Pr(\text{Q/K})$$

$\Pr(\text{Q/K})$  means Probability of Q after taking K as first card  
 $= \frac{1}{52} * \frac{1}{51}$