

function  $x = f(n)$

$x = 1;$

for  $i = 1:n$

for  $j = 1:n$

$x = x + 1;$

1. Find the runtime of the algorithm mathematically

Inner loop

It executed  $n$  times for each phase in  
outer loop.

$\therefore n$  execution for inner loop

Outer loop

It executed  $n$  times from  $i = 1$  to  $i = n$

$\therefore n$  executions for outer loop

$$\text{Total execution} = \sum_{i=1}^n \sum_{j=1}^n 1$$

$$= \sum_{i=1}^n n$$

$$= n \times n$$

$$= n^2$$

$\therefore$  The total runtime of algorithm is  $\Theta(n^2)$

3) Find Polynomials that are upper and lower bounds on your curve. From this specify a big- $\Theta$ , big- $\Omega$ , and what big- $\Theta$  is.

Big-O - notation (upper bound)

$O(n^2)$  - function does not grow faster

than Quadratic

Big-Omega

$\Omega(n^2)$  - function does not grow

Slower than Quadratic

Big-Theta

$\Theta(n^2)$  - function grows asymptotically as  $n^2$

if I modified the function to be

$x = f(n)$

$x = 1;$

$y = 1;$

for  $i = 1: n$

for  $j = 1: n$

$x = x + 1;$

$y = y + j;$



4) Will this increase how long it takes the algorithm to run?

$y = i + j$ , actual time taken by the modified function will be slightly longer due to it.  
 $\therefore O(n^2)$  is the time complexity

5) Will it effect your result from first function?  
 It doesn't effect much in the time complexity.

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x = f(n)
x = 1
a = 1
for i = 1 to n
  for j = 1 to n
    x = x + i
    a = a + j
    
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