

A Right not Granted<sup>1</sup>. A Wrong not Righted. Spending and performance in Texan Public Schools

## 1 Introduction

The economics of public education remains a deeply contested field. Essential questions like the impact of class sizes on student performance, the importance of teacher quality and the fairness of local taxation continue to provoke disputes between leading economists in the field [hedges vs hanushek]. Few can doubt the importance of these questions in designing policy.

I use two methods to estimate the educational return to spending in Texan public schools, which to my knowledge are previously unexplored. Arbitrary restrictions on tax rates due to the unconstitutionality of state-wide taxes induced some cash-starved districts to max out their tax rates, presenting windows in which their revenue was completely dependent on property values and state aid. Thus changes in revenue may have been exogenous to changes in school performance. Further to this, random fluctuations in the oil price provided positive and negative revenue shocks which may constitute a viable instrument for district revenue, allowing for a more plausible estimate of the causal impact of spending on school performance. Further to this I exploit the arbitrary nature of district borders to estimate the impact the prevalence of student and teacher sorting between districts in response to district changes.

[actual estimation details]

Texas is a strong subject for this study for several reasons. It sets a state-

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<sup>1</sup>footnotes working fine

wide curriculum and requires common standardised testing by its primary and secondary students, removing the possibility of test or curriculum variation from biasing estimates of resource effects. It has a school finance system with several quirks which provide the possibility of exogenous variation in spending and other independent variables. Size

[results]

These results may be externally valid within American states which operate a hybrid local/state-funded education system.

### 1.1 Within district, one time period

Almost twenty years would pass until Texans would successfully sue the Texan Commissioner of Education for discrimination against students in poor districts[3] in Edgewood Independent School District v. Kirby (Tex 1989). During the trial it was found that the "[the] wealthiest district [have] over 14,000,000 of property wealth per student, while the poorest [have] approximately 20,000; this disparity reflects a 700 to 1 ratio"[4]. While as Americans the students in Edgewood ISD had no right to education, as Texans it was decided they did. The solution forged by the wrestle between parents, lawmakers and judges which followed was finance-equalisation legislation passed in 1993 and taken into effect in the 1993/94 school year. Though nicknamed 'Robin Hood' by the press, this belied the widespread ire the legislation would draw from economists[5], lawmakers[6] and parents[7] (rich and poor alike), and the two further rounds of lawsuits it would face. In January 2019 Republican Governor Greg Abbott tweeted: "We must put Robin Hood school funding on a path of extinction", later congratulating himself (more

mutedly) for "reform" on the issue as the 86th Legislative Session ended [8]. Far from being a unique, arcane example, interesting only in its novelty, Texas' school finance system mirrors dozens [9] of other states which rely on similar local funding models; as do its problems.

The "byzantine" [10] nature of the system presents two intriguing settings to the econometrician, which to my knowledge are previously unexplored. Arbitrary restrictions on tax rates due to the unconstitutionality of statewide taxes induced some cash-starved districts to max out their tax rates, presenting windows in which their revenue was completely dependent on property values and state aid. Further to this, random fluctuations in the oil price provided positive and negative revenue shocks which may constitute a viable instrument for district revenue, allowing for a more plausible estimate of the causal impact of spending on school performance. These combined with the time-series, campus-level nature of the data allows for estimates which plausibly address some endogeneity concerns which plague other educational production function estimates. Many remain, and are addressed in due course.

## **2 The Educational Landscape**

### **3 Literature Review**

Texas' education system has been the subject of several previous studies, most notably Hoxby '04, Hanushek and Rivkin '05 and

Our ultimate aim is to estimate a production function of the form:

$$Score = f(ability, resources, teacher, family, peers, community) + \epsilon$$

Once we have done this policy questions can be answered by investigating the parameters obtained from this estimate. For example how does the effect of class size differ in different communities, what proportion of the variation in expenditure estimates can be attributed to district-level effects?

[Obviously I'll need to put the general background, data and theory here too. (Importantly I need to talk about data selection and assumptions about sampling process. That is, that the data I have dropped were dropped randomly).]

## 4 Model

Consider a simple linear model for academic performance over campuses  $i = 1, \dots, n$ ; school districts  $j = 1, \dots, 957$ ; and periods  $t = 2003, \dots, 2011$  (where 2003 represents the academic year '02-'03):

$$\begin{aligned} \text{Gr5.Avg}_{ijt} = & \beta_0 + \beta_1 \text{Gr4.Avg}_{ijt-1} + \beta_2 \text{Gr3.Avg}_{ijt-2} \\ & + \beta_3 \text{Per.Pupil.Exp}_{ijt} + \beta_4 \text{Econ.Disadv.Per}_{ijt} \\ & + \beta_5 \text{T.Avg.Sal}_{ijt} + \beta_6 \text{T.Avg.Exp}_{ijt} \\ & + \beta_7 \text{Gr5.Class.Size}_{ijt} + \epsilon_{ijt} \end{aligned}$$

Before estimating this model it is instructive to restrict it to more specialised cases and clearly step through the assumptions required for OLS to be an efficient, unbiased estimation strategy. This makes suggesting alternative estimation strategies much more intuitive.

## 4.1 Within district, one time period

Let the first restriction be  $j = 1$  (WLOG let this represent DALLAS ISD) and  $t = 2006$ . These are arbitrary parameter values. The model then can be simplified to:

$$\begin{aligned}\text{Gr5.Avg}_i &= \beta_0 + \beta_1 \text{Gr4.Avg.Lag1}_i + \beta_2 \text{Gr3.Avg.Lag2}_i \\ &+ \beta_3 \text{Per.Pupil.Exp}_i + \beta_4 \text{Econ.Disadv.Per}_i \\ &+ \beta_5 \text{T.Avg.Sal}_i + \beta_6 \text{T.Avg.Exp}_i \\ &+ \beta_7 \text{Gr5.Class.Size}_i + \epsilon_i\end{aligned}$$

In making these restrictions we can automatically rule out concerns due to time-trends and some spatial autocorrelation, however we must still be confident that the GM assumptions are satisfied.

### 4.1.1 Multicollinearity

We require that the matrix  $\mathbf{X}'\mathbf{X}$  where

$$\mathbf{X} = \begin{pmatrix} 1 & x'_1 \\ 1 & x'_2 \\ \vdots & \vdots \\ 1 & x'_n \end{pmatrix}$$

,

$$x_i = \begin{pmatrix} \text{Gr4.Avg.Lag1}_i \\ \text{Gr3.Avg.Lag2}_i \\ \vdots \\ \text{Gr5.Class.Size}_i \end{pmatrix}$$

be invertible.

#### 4.1.2 Exogeneity

Measurement error, simultaneity.

#### 4.1.3 Homoskedasticity

Downward bias, local spatial autocorrelation.

#### 4.1.4 Normality

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### 4.2 Within district, panel

A simple linear model for performance in Dallas ISD:

$$\begin{aligned}\text{Gr5.Avg}_{it} = & \beta_0 + \beta_1 \text{Gr4.Avg.Lag1}_{it} + \beta_2 \text{Gr3.Avg.Lag2}_{it} \\ & + \beta_3 \text{Per.Pupil.Exp}_{it} + \beta_4 \text{Econ.Disadv.Per}_{it} \\ & + \beta_5 \text{T.Avg.Sal}_{it} + \beta_6 \text{T.Avg.Exp}_{it} \\ & + \beta_7 \text{Gr5.Class.Size}_{it} + \epsilon_{it}\end{aligned}$$

### 4.3 Across districts, one time period

A simple linear model for performance in 2006:

$$\begin{aligned}\text{Gr5.Avg}_{ij} = & \beta_0 + \beta_1 \text{Gr4.Avg.Lag1}_{ij} + \beta_2 \text{Gr3.Avg.Lag2}_{ij} \\ & + \beta_3 \text{Per.Pupil.Exp}_{ij} + \beta_4 \text{Econ.Disadv.Per}_{ij} \\ & + \beta_5 \text{T.Avg.Sal}_{ij} + \beta_6 \text{T.Avg.Exp}_{ij} \\ & + \beta_7 \text{Gr5.Class.Size}_{ij} + \epsilon_{ij}\end{aligned}$$

#### 4.4 Across districts, panel

This linear model utilises all our data.

$$\begin{aligned}\text{Gr5.Avg}_{ijt} = & \beta_0 + \beta_1 \text{Gr4.Avg}_{ijt-1} + \beta_2 \text{Gr3.Avg}_{ijt-2} \\ & + \beta_3 \text{Per.Pupil.Exp}_{ijt} + \beta_4 \text{Econ.Disadv.Per}_{ijt} \\ & + \beta_5 \text{T.Avg.Sal}_{ijt} + \beta_6 \text{T.Avg.Exp}_{ijt} \\ & + \beta_7 \text{Gr5.Class.Size}_{ijt} + \epsilon_{ijt}\end{aligned}$$

where  $\epsilon_{ijt} = \alpha_i + \mu_j + v_{ijt}$  and

$$v_{ijt} \sim \mathcal{N}(0, \sigma^2) \text{ for all } i, j, t.$$

That is our errors are composed of time-invariant, campus-level and district-level heterogeneity and an idiosyncratic error.

#### 4.5 Other Concerns

##### 4.5.1 Hierarchical Error Structure

##### 4.5.2 Parameter Heterogeneity

### 5 Estimation Strategy

Fixed effects is likely not to be appropriate in the presence of time trends.

#### 5.1 Non-Linear Models

GMM estimation.

#### 5.2 Dynamic Panel Model

Small T (9), large N (957).

## References

- [1] Michel Goossens, Frank Mittelbach, and Alexander Samarin. *The L<sup>A</sup>T<sub>E</sub>X Companion*. Addison-Wesley, Reading, Massachusetts, 1993.
- [2] Albert Einstein. *Zur Elektrodynamik bewegter Körper*. (German) [*On the electrodynamics of moving bodies*]. Annalen der Physik, 322(10):891–921, 1905.
- [3] Knuth: Computers and Typesetting,  
<http://www-cs-faculty.stanford.edu/~uno/abcde.html>