$$\begin{split} & & \text{In} [10] := & \textbf{r} = \textbf{4}; \\ & & \textbf{f} [\textbf{x}_{\_}] = \textbf{r} \, \textbf{x} \, (\textbf{1} - \textbf{x}) \, ; \\ & & \mu [\textbf{x}_{\_}] = \frac{\textbf{1}}{\pi \, \sqrt{\textbf{x} \, (\textbf{1} - \textbf{x})}} \, ; \\ & & \textbf{D} [\textbf{f} [\textbf{x}]_{\texttt{x}} \, \textbf{x}] \\ & & \textbf{Out} [13] = \\ & & \textbf{4} \, (\textbf{1} - \textbf{x})_{\texttt{x}} - \textbf{4} \, \textbf{x} \\ & & \textbf{In} [15] := & \textbf{Integrate} [\mu [\textbf{x}]_{\texttt{x}} \, \textbf{Log} [\textbf{Abs} [\textbf{D} [\textbf{f} [\textbf{x}]_{\texttt{x}}, \textbf{x}]_{\texttt{x}}]_{\texttt{x}}, \, \textbf{0}, \, \textbf{1} \}] \\ & & \textbf{Out} [15] = \\ & & \textbf{Log} \, [\textbf{2}] \end{split}$$