

Problem 2 : Determine $T(n)$ & Big-O.

(a) There are 3 ifs, but the first 2 are exclusive:

- $total = 1 \rightarrow 1 \text{ op.}$
- $n > 0 \rightarrow 1 \text{ op.}$
- $i > 1$: last iteration $\rightarrow 1 \text{ op.}$
- $i = n$: $\rightarrow 1 \text{ op.}$
- $i > 1, i--$: $\rightarrow 2n.$
- $total = total * i$: $\rightarrow n.$

$$\Rightarrow T_1(n) : 3n + 4$$

The last if :

- $n \% 2 == 0 \rightarrow 1 \text{ op.}$
- $i = 0 \rightarrow 1 \text{ op.}$
- $i < n$ (last iteration) $\rightarrow 1 \text{ op.}$
- $i < n, n += 2$: $\frac{n}{2} (2) \text{ op.}$
- $total = total + i$: $\rightarrow \frac{n}{2} \text{ op.}$

$$\Rightarrow T_2(n) : 3 + n + \frac{n}{2}$$

$$\Rightarrow \boxed{T(n) = T_1(n) + T_2(n) = 7 + 4n + \frac{n}{2}} \Rightarrow \boxed{O(n)} = O(n)$$

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