






## Answer

lena.bmp	(a) dilation_lena.bmp
	
(b) erosion_lena.bmp	(c) opening_lena.bmp
	
(d) closing_.bmp	(e) hitmiss_lena.bmp
	

Description
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## 1. Problem Formation

I. Write programs which do binary morphology on a binary image:

(a) Dilation (b) Erosion (c) Opening (d) Closing (e) Hit-and-miss transform

II. Binarize Lena with the threshold 128 (0-127,128-255).

III. Please use the octogonal 3-5-5-5-3 kernel.

IV. Please use the "L" shaped kernel (same as the text book) to detect the upper-right corner for hit-and-miss transform.

V. Please process the white pixels (operating on white pixels).

## 2. Method of Algorithms

(a) Dilation:

$$A \oplus B = \{c \in E^N \mid c = a + b \text{ for some } a \in A \text{ and } b \in B\}$$

(b) Erosion:

$$A \ominus B = \{x \in E^N \mid x + b \in A \text{ for every } b \in B\}$$

(c) Opening:

$$B \circ K = (B \ominus K) \oplus K$$

(d) Closing:

$$B \bullet K = (B \oplus K) \ominus K$$

(e) Hit-and-Miss:

$$A \otimes (J, K) = ((A \ominus J) \cap (A^c \ominus K))$$

## 3. 本次作業使用 python, IDE 使用 Spyder

## 4. Source Code [HW4.py]說明如下

```

1  # -*- coding: utf-8 -*-
2  """
3  Created on Thu Oct 17 20:56:19 2019
4
5  @author: vincent黃國郡
6  """
7  from PIL import Image
8  import numpy as np
9  import myMorphology
10 kernel = np.array([
11     [0, 1, 1, 1, 0],
12     [1, 1, 1, 1, 1],
13     [1, 1, 1, 1, 1],
14     [1, 1, 1, 1, 1],
15     [0, 1, 1, 1, 0]])
16 centerKernel = tuple([x // 2 for x in kernel.shape])
17
18 if __name__ == '__main__':
19     lena = Image.open("lena.bmp")
20     # binarization
21     binary_lena = lena.point(lambda x: 0 if x < 128 else 255, '1')
22
23     # HW4(a)
24     dilation_lena = myMorphology.dilation(binary_lena, kernel, centerKernel)
25     dilation_lena.save('dilation_lena.bmp')
26
27     # HW4(b)
28     erosion_lena = myMorphology.erosion(binary_lena, kernel, centerKernel)
29     erosion_lena.save('erosion_lena.bmp')
30
31     # HW4(c)
32     opening_lena = myMorphology.opening(binary_lena, kernel, centerKernel)
33     opening_lena.save('opening_lena.bmp')
34
35     # HW4(d)
36     closing_lena = myMorphology.closing(binary_lena, kernel, centerKernel)
37     closing_lena.save('closing_lena.bmp')
38
39     # HW4(e)
40     kernel_J = np.array([
41         [1, 1],
42         [0, 1]])
43     centerKernel_J = (1, 0)
44     kernel_K = np.array([
45         [1, 1],
46         [0, 1]])
47     centerKernel_K = (0, 1)
48     hitmiss_lena = myMorphology.hitmiss(binary_lena,
49                                         kernel_J, centerKernel_J,
50                                         kernel_K, centerKernel_K)
51     # Save image fo file.
52     hitmiss_lena.save('hitmiss_lena.bmp')

```

Import 需要用到的 library

宣告 kernel[35553]

定義 kernel 中心點

因為要 program on a binary image · 故先將 lena 二值化

呼叫我的 myMorphology.py 副函式進行處理作業

宣告 hitmiss 要用到的 Array

呼叫我的 myMorphology.py 副函式進行處理作業

5. Source Code (副程式) [[myMorphology.py](#)]說明如下

```

13 def dilation(originalImage, kernel, centerKernel):
14     dilationImage = Image.new('1', originalImage.size)
15     for r in range(originalImage.size[0]):
16         for c in range(originalImage.size[1]):
17             originalPixel = originalImage.getpixel((r, c))
18             # If this pixel is 1 which is white
19             if (originalPixel != 0):
20                 for ii in range(kernel.shape[0]):
21                     for jj in range(kernel.shape[1]):
22                         if (kernel[ii, jj]):
23                             targetX = r + (ii - centerKernel[0])
24                             targetY = c + (jj - centerKernel[1])
25                             if ((0 <= targetX < originalImage.size[0])
26                                 and (0 <= targetY < originalImage.size[1])):
27                                 dilationImage.putpixel((targetX, targetY), 1)
28     return dilationImage
29
30
31 def erosion(originalImage, kernel, centerKernel):
32     erosionImage = Image.new('1', originalImage.size)
33     for r in range(originalImage.size[0]):
34         for c in range(originalImage.size[1]):
35             matchFlag = 1
36             for ii in range(kernel.shape[0]):
37                 for jj in range(kernel.shape[1]):
38                     if (kernel[ii, jj] and matchFlag):
39                         targetX = r + (ii - centerKernel[0])
40                         targetY = c + (jj - centerKernel[1])
41                         if ((0 <= targetX < originalImage.size[0])
42                             and (0 <= targetY < originalImage.size[1])):
43                             if (originalImage.getpixel(
44                                 (targetX, targetY)) == 0):
45                                 matchFlag = False
46                                 break
47                             else:
48                                 matchFlag = False
49                                 break
50             if (matchFlag):
51                 erosionImage.putpixel((r, c), 1)
52     return erosionImage
53
54
55 def opening(originalImage, kernel, centerKernel):
56     return dilation(erosion(originalImage, kernel, centerKernel), kernel, centerKernel)
57
58
59 def closing(originalImage, kernel, centerKernel):
60     return erosion(dilation(originalImage, kernel, centerKernel), kernel, centerKernel)
61

```

先產生一張跟 input 一樣大的 binary original Image

掃過每一個 pixel 並判斷是否為 1(白色格子)

如果為 1(白色格子) · 並將 kernel 貼上去那個 pixel · 並將 kernel 中黑點的地方都填上 1(條件為在 dilation Image)大小內

將處理好的影像回傳

先產生一張跟 input 一樣大的 binary original Image

matchFlag 來判斷 kenel 是否和該 pixel 的鄰近 pixel 都符合

只要掃到和 kernel 不一樣的內容就 break 掉 · 以節省運算時間

只要通過檢核的 pixel · 一律填值 1 給他(白色) · 最後就可以得到我的 erosion Image

先 erosion 再 dilation

先 dilation 再 erosion

```
63 def complement(originalImage):
64     complementImage = Image.new('1', originalImage.size)
65     for r in range(originalImage.size[0]):
66         for c in range(originalImage.size[1]):
67             if (originalImage.getpixel((r, c)) == 0):
68                 complementImage.putpixel((r, c), 1)
69             else:
70                 complementImage.putpixel((r, c), 0)
71     return complementImage
72
73
```

先產生一張跟 input 一樣大的 binary original Image

一個一個 pixel 往下掃往右掃，如果是 1 就填 0，如果是 0 就填 1，做 complement

```
74 def intersection(image1, image2):
75     intersectionImage = Image.new('1', image1.size)
76     for r in range(image1.size[0]):
77         for c in range(image1.size[1]):
78             image1Pixel = image1.getpixel((r, c))
79             image2Pixel = image2.getpixel((r, c))
80             if (image1Pixel and image2Pixel):
81                 intersectionImage.putpixel((r, c), 1)
82             else:
83                 intersectionImage.putpixel((r, c), 0)
84     return intersectionImage
85
```

先產生一張跟 input 一樣大的 binary original Image

一個一個 pixel 往下掃往右掃，並同時比較兩張圖位置的 pixel 做交集，將結果存入 intersectionImage

```
87 def hitmiss(originalImage, kernel_J, centerKernel_J, kernel_K, centerKernel_K):
88     return intersection(erosion(originalImage, kernel_J, centerKernel_J),
89                         erosion(complement(originalImage), kernel_K, centerKernel_K))
```

最後進行 hit and miss，交集(被 erosion 過的 original Image 和被 erosion 過的 original complement Image)