

Yokoi connectivity number



Description

1. Problem Formation

- I. Binarize the benchmark image Lena as in HW2 by 128
- II. using 8x8 blocks as a unit, take the topmost-left pixel as the down-sampled data,
Down-sample Lena from 512x512 to 64x64
- III. Count the Yokoi connectivity number
- IV. Result of this assignment is a 64x64 matrix. Please **align** the matrix within 1 single
A4 page (using 4-connected).

2. Method of Algorithms

For 4-connectivity:

$$h(b, c, d, e) = \begin{cases} q & \text{if } b = c \text{ and } (d \neq b \vee e \neq b) \\ r & \text{if } b = c \text{ and } (d = b \wedge e = b) \\ s & \text{if } b \neq c \text{ and } (d = b \wedge e = b) \end{cases}$$

$$f(a_1, a_2, a_3, a_4) = \begin{cases} 5 & \text{if } a_1 = a_2 = a_3 = a_4 = r \\ n & \text{where } n = \text{number of } \{a_k | a_k = q\}, \text{ otherwise} \end{cases}$$

3. 本次作業使用 python, IDE 為 Spyder

4. Source Code [HW6.py]說明如下

主程式:

1. 先import會用到的library
2. 將lena圖讀進來
3. 進行binary 處理
4. 進行downsample, 8個取一個值
5. 進行yokoi 演算法
6. 最後將結果存為txt檔

```

86 if __name__ == '__main__':
87     from PIL import Image
88     import numpy as np
89
90     lena = Image.open("lena.bmp")
91     binary_lena = lena.point(lambda x: 0 if x < 128 else 255, '1')
92     downsamplingImage = downsampling(binary_lena, 8)
93     downsamplingImage.save('downsampling.bmp')
94     YokoiConnectivityNumber = Yokoi(downsamplingImage)
95     np.savetxt('YokoiConnectivityNumber.txt', YokoiConnectivityNumber, delimiter=',', fmt='%s')
96

```

```

1  # -*- coding: utf-8 -*-
2  """
3  Created on Sun Oct 20 10:32:58 2019
4
5  @author: vincent黃國郡
6  """
7  def downsampling(originalImage, sampleFactor):
8      """
9      originalImage: Image, sampleFactor: int, return Image
10     """
11     from PIL import Image
12     downsamplingWidth = int(originalImage.size[0] / sampleFactor)
13     downsamplingHeight = int(originalImage.size[1] / sampleFactor)
14     downsamplingImage = Image.new('1', (downsamplingWidth, downsamplingHeight))
15     for x in range(downsamplingWidth):
16         for y in range(downsamplingHeight):
17             originalPixel = originalImage.getpixel((x * sampleFactor, y * sampleFactor))
18             downsamplingImage.putpixel((x, y), originalPixel)
19     return downsamplingImage
20
21 def getNeighborhood(originalImage, position):
22     """
23     originalImage: Image, position: tuple, return numpy array
24     """
25     neighborhood = np.zeros(9)
26     x, y = position
27     neighborhood = []
28     for xx in range(3):
29         for yy in range(3):
30             targetX = x + (xx - 1)
31             targetY = y + (yy - 1)
32             if ((0 <= targetX < originalImage.size[0]) and \
33                 (0 <= targetY < originalImage.size[1])):
34                 pixelValue = originalImage.getpixel((targetX, targetY))
35                 neighborhood.append(pixelValue)
36             else:
37                 neighborhood.append(0)
38     neighborhood = [
39         neighborhood[4], neighborhood[7], neighborhood[3],
40         neighborhood[1], neighborhood[5], neighborhood[8],
41         neighborhood[6], neighborhood[0], neighborhood[2]]
42     return neighborhood

```

1. 將每一個pixel 值附近的九宮個取出
2. 重新排列成yokoi會用到的九宮格順序

```

44 def Yokoi_h(b, c, d, e):
45     """
46     type of b,c,d,e: int return: str
47     """
48     if ((b == c) and (b != d or b != e)):
49         return 'q'
50     if ((b == c) and (b == d and b == e)):
51         return 'r'
52     if (b != c):
53         return 's'

```

$$h(b, c, d, e)$$

$$= \begin{cases} q & \text{if } b = c \text{ and } (d \neq b \vee e \neq b) \\ r & \text{if } b = c \text{ and } (d = b \wedge e = b) \\ s & \text{if } b \neq c \text{ and } (d = b \wedge e = b) \end{cases}$$

```

56 def Yokoi_f(a1, a2, a3, a4):
57     """
58     type of b,c,d,e: int return: str
59     0: Isolated 1: Edge 2: Connecting 3: Branching 4: Crossing 5:interior
60     """
61     if (a1 == a2 == a3 == a4 == 'r'):
62         return 5
63     else:
64         return [a1, a2, a3, a4].count('q')

```

$$f(a_1, a_2, a_3, a_4)$$

$$= \begin{cases} 5 & \text{if } a_1 = a_2 = a_3 = a_4 = r \\ n & \text{where } n = \text{number of } \{a_k | a_k = q\}, \text{ otherwise} \end{cases}$$

```

66 def Yokoi(originalImage):
67     """
68     type originalImage: Image ,return: numpy array
69     """
70     YokoiConnectivityNumber = np.full(downsamplingImage.size, ' ')
71
72     for x in range(originalImage.size[0]):
73         for y in range(originalImage.size[1]):
74             if (originalImage.getpixel((x, y))):
75                 neighborhood = getNeighborhood(originalImage, (x, y))
76                 YokoiConnectivityNumber[y, x] = Yokoi_f(
77                     Yokoi_h(neighborhood[0], neighborhood[1], neighborhood[6], neighborhood[2]),
78                     Yokoi_h(neighborhood[0], neighborhood[2], neighborhood[7], neighborhood[3]),
79                     Yokoi_h(neighborhood[0], neighborhood[3], neighborhood[8], neighborhood[4]),
80                     Yokoi_h(neighborhood[0], neighborhood[4], neighborhood[5], neighborhood[1]))
81             else:
82                 YokoiConnectivityNumber[y, x] = ' '
83
84     return YokoiConnectivityNumber

```

進行 yokoi 運算 · 對每一個 pixel 進行

f(h1(a,b,c,d), h2(a,b,c,d).....)

最後回傳 array