

Approximate integrals and improper integrals.

1. $\int_3^{\infty} \frac{1}{(x-2)^{3/2}} dx$

2. $\int_0^{\infty} \frac{1}{\sqrt[4]{x+1}} dx$

3. $\int_{-\infty}^{\infty} x e^{-x^2} dx$

4. $\int_0^3 \frac{1}{x^2 - 6x + 5} dx$

5. $\int_0^1 \frac{e^{1/x}}{x^3} dx$

6.

(a) Find the approximations T_8 and M_8 of the integral $\int_0^1 \cos(x^2)$.

(b) Estimate the errors in the approximations of part(a) (Error bound).

(c) How large do we have to choose n so that the approximations of T_n and M_n in part(a) are accurate to within 0.0001.

7. State Simpson's rule for approximation and its error bound.