

Linear algebra originated from solving linear systems, through row reductions. There are three basic row reduction operations:

- Linear combination of two rows;
- Scalar multiple of a row;
- Interchange two rows.

Also, make sure that you are clear about the two concepts:  
Echolon form and Reduced Echolon form

1. Try to explain to your group mates what is the span of  $n$  vectors.
2. What conditions on  $a, b, c, d$  will guarantee that the following system has exactly one solution?

$$\begin{aligned} ax + by &= 1 \\ cx + dy &= 0 \end{aligned}$$

3. For which  $\lambda$  does the following system have more than one solutions:

$$\begin{aligned} (\lambda - 3)x + y &= 0 \\ x + (\lambda - 3)y &= 0 \end{aligned}$$

4. Let  $u = [2, -1], v = [2, 1]$ , show that  $[h, k]$  is in the span of  $u, v$  for arbitrary  $h$  and  $k$ .

5. Solve  $Ax = b$ :

$$A = \begin{bmatrix} 2 & 0 & 6 \\ -1 & 8 & 6 \\ 1 & -2 & 1 \end{bmatrix}, \quad b = \begin{bmatrix} 10 \\ 3 \\ 7 \end{bmatrix}$$

6. Solve  $Ax = b$ :

$$A = \begin{bmatrix} 1 & 0 & -4 \\ 0 & 3 & -2 \\ -2 & 6 & 3 \end{bmatrix}, \quad b = \begin{bmatrix} 4 \\ 1 \\ -4 \end{bmatrix}$$

7. For what value of  $h$  is  $y$  in the span of  $v_1$  and  $v_2$ :

$$v_1 = \begin{bmatrix} 1 \\ 0 \\ -2 \end{bmatrix} \quad v_2 = \begin{bmatrix} -2 \\ 1 \\ 7 \end{bmatrix} \quad y = \begin{bmatrix} h \\ -3 \\ -5 \end{bmatrix}$$