Population models, springs, general differential equations.

1. A population model is defined by the differential equation:

$$\frac{dP}{dt} = 1.2P(1 - \frac{P}{4200}).$$

- (a) For what values of P is the population increasing;
- (b) For what values of P is the population decreasing;
- (c) What are the equilibrium solutions.

2.

- (a) For what values of k does the function $y = \cos kx$ satisfy the differential equation 4y'' = -25y?
- (b) For those values of k, verify that every member of the family of functions $y = A \sin kt + B \cos kt$ is also a solution.

3. A function y(t) satisfies the differential equation:

$$\frac{dy}{dt} = y^4 - 6y^3 + 5y^2.$$

- (a) What are the constant solutions of the equation?
- (b) For what values of y is y increasing?
- (c) For what values of y is y decreasing?