# Model-Based Testing with Graph Grammars

MSc Thesis (Afstudeerscriptie)

written by

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#### Abstract

Graph Grammars describe system behavior through graphs and graph transformation rules. Graph Grammars have not been used for Model-Based Testing. However, Graph Grammars have many structural advantages, which are potential benefits for the model-based testing process. We describe a model-based testing setup with Graph Grammars. The result is a system for automatic test generation from Graph Grammars. A graph transformation tool, GROOVE, and a model-based testing tool using Symbolic Transition Systems, ATM, are used as the backbone of the system.

One result of this report is a technique for the generation of a Symbolic Transition System from a Graph Grammar. This technique is implemented in a tool, GRATiS, which can be used for model-based testing with Graph Grammars. This tool is shown to be useful for the model-based testing paradigm, a.o. by showing its effectiveness in five case studies. Furthermore, a complexity difference is revealed between Graph Grammars and Symbolic Transition Systems: the first uses a bigger vocabulary and the latter uses more repetition to model the same behavior.

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# Chapter 1

## Introduction

In this introduction, first the importance of testing and automation of testing is stressed. Then Model-Based Testing is shown to be a useful tool for automation of testing. Graph Grammars and graph transformation are argued to be useful as formalism for Model-Based Testing. Some leading tools for automatic test generation are set out, which include the tools used in this report. The research goals are given and finally a roadmap explains the basic structure of the rest of this report.

## 1.1 Testing

In software development projects, often time and budget costs are exceeded. Laird and Brennan [11] investigated in 2006 that 23% of all software projects are canceled before completion. Furthermore, of the completed projects, only 28% are delivered on time with the average project overrunning the budget with 45%. The cause of this often are the unclear ambigious requirements of the software system to develop.

Testing is an important part of software development, because it decreases future maintainance costs [17]. Testing is a complex process and should be done often [20]. Therefore, the testing process should be as efficient as possible in order to save resources.

Test automation allows repeated testing during the development process. The advantage of this is that bugs are found early and can therefore be fixed early. A widely used practice is maintaining a test suite, which is a collection of test-cases. However, when the creation of a test suite is done manually, this still leaves room for human error [14]. The process of deriving tests tends to be unstructured, barely motivated in the details, not reproducible, not documented, and bound to the ingenuity of single engineers [29].

## 1.2 Model-based Testing

The existence of an artifact that explicitly encodes the intended behaviour can help mitigate the implications of these problems. Creating an abstract representation or a *model* of the system is an example of such an artifact. What is meant by a model in this report, is the description of the behavior of a system. In particular, the term model will be often used to describe transition-based notations, such as finite state machines, labelled transition systems and I/O automata. Other notations, such as UML statecharts, are not considered as models in this report.

A model can be used to systematically generate tests for the system. This is referred to as *model-based testing*. Generating tests automatically leads to a larger test suite than if done manually. A large, systematically built test suite is bound to find more bugs than a smaller, manually built one.

Models are created from the specification documents provided by the end-user. These specification documents are 'notoriously error-prone' [16]. This implies that the model itself needs validation. Validating the model usually means that the requirements themselves are scrutinised for consistency and completeness [29]. This helps to clear up ambigious requirements early on, which allows better estimation of the budget and time demands.

The stakeholders evaluate the constructed model to verify its correctness. However, the visual or textual representation of large models may become troublesome to understand, which is referred to as the model having a low model transparency or high model complexity. The problem with transition systems is that a larger number of states and/or transitions decreases the model transparency. We think that low model transparency make errors harder to detect and that it obstructs the feedback process of the stakeholders. Using models with high transparency is therefore essential.

## 1.3 Graph Transformation

A formalism that claims to have higher model transparency is Graph Transformation. The system states are represented by graphs and the transitions between the states are accomplished by applying graph change rules to those graphs. These rules can be expressed as graphs themselves. A graph transformation model of a software system is therefore a collection of graphs, each a visual representation of one aspect of the system. This formalism may therefore provide a more intuitive approach to system modelling than traditional state machines. Graph Transformation and its potential benefits have been studied since the early '70s [21]. The usage of this computational paradigm is best described by the following quote from Andries et al. [1]:

Graphs are well-known, well-understood, and frequently used means to represent system states, complex objects, diagrams, and networks, like flowcharts, entity-relationship diagrams, Petri nets, and many more. Rules have proved to be extremely useful for describing computations by local transformations: Arithmetic, syntactic, and deduction rules are well-known examples.

An informative paper on graph transformations is written by Heckel et al. [9]. A quote from this paper:

Graphs and diagrams provide a simple and powerful approach to a variety of problems that are typical to computer science in general, and software engineering in particular.

#### 1.4 Tools

The testing tool developed by Axini<sup>1</sup> is used for the automatic test generation on *symbolic* models, which combine a state and data type oriented approach. This tool is referred to as Axini Test Manager (ATM) and is used in practice by several Dutch companies.

In Utting et al. [29], a taxonomy is done on different model-based testing tools:

• TorX [26]: accepts behaviour models such as I/O labelled transition systems. A version of this tool written in Java under continuous development is JTorX [2]. This version accepts the same kind of models as ATM.

 $<sup>^{1}\,</sup>htt\,p://\,www.ax\,in\,i.n\,l/$ 

- Spec Explorer[30]: provides a model editing, composition, exploration and visualization environment within Visual Studio, and can generate offline .NET test suites or execute tests as they are generated (online).
- JUMBL[22]: an academic model-based statistical testing that supports the development of statistical usage-based models using Markov chains, the analysis of models, and the generation of test cases.
- AETG[5]: implements combinatorial testing, where the number of possible combinations of input variables are reduced to a few 'representative' ones.
- STG tool[4]: implements conformance testing techniques to automatically derive symbolic test cases from formal operational specifications.

The choice was made to use ATM, because of the location of Axini, their willingness to support this project and the already available models for case studies. Another interesting option for our research would have been to use an open-source MBT tool. In particular JTorX was an interesting candidate due to its maturity and the available support at the University of Twente.

The graph transformation tool GROOVE<sup>2</sup> is used to model and explore graph grammars.

## 1.5 Research goals

The motivation above is given for using graph grammars as a modelling technique. The goal of this research is to create a system for automatic test generation on graph grammars. If the assumptions that graph grammars provide a more intuitive modelling and testing process hold, this new testing approach will lead to a more efficient testing process and fewer incorrect models. The system to be designed, once implemented and validated, should provide a valuable contribution to the testing paradigm. The tools GROOVE and ATM are used to create this system.

The research goals are split into a design and validation component:

- 1. **Design**: Design and implement a system using ATM and GROOVE which performs model-based testing on graph grammars.
- 2. Validation: Validate the design and implementation using case studies and performance measurements.

The result of the design goal is one system called the GROOVE-Axini Testing System (GRATiS). The validation goal uses case-studies with existing specifications from systems tested by Axini. Each case-study has a graph grammar and a symbolic model which describe the same system. GRATiS and ATM are used for the automatic test generation on these models respectively. Both the models and the test processes are compared as part of the validation.

The solution has to uphold three requirements:

- 1. A graph grammar must be used as the model; it must derive from the specification and be used for the testing.
- 2. It must be possible to measure the test progress/completion, by means of *coverage* statistics (explained in detail in section 2.1.2).
- 3. The solution must be efficient: it should be usable in practice, therefore the technique should be scalable and the imposed constraints reasonable from a practical view point.

<sup>&</sup>lt;sup>2</sup>http://sourceforge.net/projects/groove/

## 1.6 Roadmap

This report has five more chapters: first, the concepts described in this chapter are elaborated in chapter 2. The design of GRATiS is described in chapter 3. The implementation of GRATiS is covered in chapter 4. The validation of GRATiS is in chapter 5. Finally, conclusions are drawn and future work suggestions are made in chapter 6.

## Chapter 2

# Background

The structure of this chapter is as follows: the general model-based testing process is set out in section 2.1. Some basic concepts from algebra are described in section 2.2. Then the symbolic models used by ATM are described in section 2.3. Section 2.4 describes the Graph Grammar formalism. GROOVE and ATM are described in section 2.5.

## 2.1 Model-based Testing

Model-based testing is a testing technique where a System Under Test (SUT) is tested for conformance to a model description of the system. The general setup for this process is depicted as a UML sequence diagram in Figure 2.1. The specification of a system is provided as a model to a test derivation component which generates a test suite. The test suite is used by a test execution component to test the SUT. Tests are executed by providing input/stimuli to the SUT and monitoring the output/response. The test execution component evaluates whether the correct responses are given. It gives a 'pass' or 'fail' verdict depending on whether the SUT conforms to the model or not.

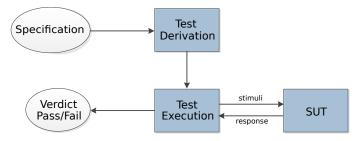


Figure 2.1: A general model-based testing setup

This type of model-based testing is called *batch testing* or *offline testing*. Another type of model-based testing is *on-the-fly* testing. The main difference is that no test cases are derived, instead a transition in the model is chosen and tested on the system directly. The general architecture for this process is shown in Figure 2.2. An example of an on-the-fly testing tool is TorX [26].

Variations of state machines and transition systems have been widely used as the underlying model for test generation. Other tools use the structure of data types to generate test data.

The stucture of the rest of this section is as follows. First, previous work on model-based testing is given. Then, Labelled Transition Systems are introduced. This is a basic formalism useful to

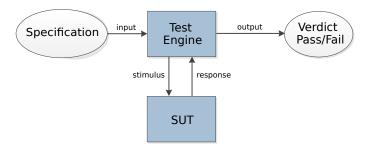


Figure 2.2: A general 'on-the-fly' model-based testing setup

understand the models in the rest of the paper, namely Graph Grammars and Symbolic Transition Systems. Next, an adaptation of Labelled Transition Systems, the Input-Output Transition System is described. This is a useful formalism for Model-Based Testing. Finally, the notion of *coverage* is explained.

#### 2.1.1 Previous work

Transition-based formal testing theory was introduced by De Nicola et al. [19]. The input-output behavior of processes is investigated by series of tests. Two processes are considered equivalent if they pass exactly the same set of tests. This testing theory was first used in algorithms for automatic test generation by Brinksma [3]. This led to the so-called *canonical tester* theory. Tretmans gives a formal approach to protocol conformance testing (whether a protocol conforms to its specifications) in [27] and an algorithm for deriving a sound and exhaustive test suite from a specification in [28]. A good overview of model-based testing theory and past research is given in "Model-Based Testing of Reactive Systems" [15].

#### 2.1.2 Labelled Transition Systems

A Labelled Transition System (LTS) is a structure consisting of states with labelled transitions between them.

**Definition 2.1.1.** Labelled Transition Systems An LTS is a 4-tuple  $\langle Q, L, T, q_0 \rangle$ , where:

- Q is a finite, non-empty set of states
- $\bullet$  L is a finite set of labels
- $T \subseteq Q \times (L \cup \{\tau\}) \times Q$ , with  $\tau \notin L$ , is the transition relation
- $q_0 \in Q$  is the initial state.

We write  $q \xrightarrow{\mu} q'$  if there is a transition labelled  $\mu$  from state q to state q', i.e.,  $(q, \mu, q') \in T$ . q, q' are called the source and target states of the transition respectively. The informal idea of such a transition is that when the transition system is in state q it may perform action  $\mu$ , and go to state q'.

**Input-Output Transition Systems** A useful type of transition system for model-based testing is the Input-Output Transition System (IOTS) by Tretmans [28]. Assuming that implementations communicate with their environment via inputs and outputs, this formalism is useful for describing system behavior. The system is regarded as a black box and the IOTS specifies the allowed inputs and outputs.

IOTSs have the same definition as LTSs with one addition: each label  $l \in L$  has a type  $\iota \in Y$ , where  $Y = \{input, output\}$ . Each label can therefore specify whether the action represented by the label is a possible input or an expected output of the system under test. An IOTS is formally defined as:

#### **Definition 2.1.2.** Input-Output Transition Systems

An IOTS is a 4-tuple  $\langle Q, L, T_Y, q_0 \rangle$ , where  $T_Y \subseteq T \times Y$  are the input-output transitions.

When the transition system is in the source state of an input transition, the input can be given to the SUT. When the transition system is in the source state of an output transition, the output should be observed from the SUT. In both cases, the transition system advances to the target state of the transition. The case where a state has both input and output transitions is not considered in this report.

An example of such an IOTS is shown in Figure 2.3a. This system allows an input of 20 or 50 cents and then outputs tea or coffee accordingly. The inputs are preceded by a '?', the outputs are preceded by an '!'. This system is a specification of a coffee machine. A test case can also be described by an IOTS with special pass and fail states.

A test case for the coffee machine is given in Figure 2.3b. The test case shows that when an input of '50c' is given, an output of 'coffee' is expected from the tested system, as this results in a 'pass' verdict. When the system responds with 'tea', the test case results in a 'fail' verdict. The pass and fail verdicts are two special states in the test case, which are sink states, i.e., once in either of those the test case cannot leave that state.

Test cases should always reach a pass or fail state within finite time. This requirement ensures that the testing process halts.

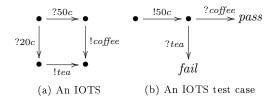


Figure 2.3: The specification of a coffee machine and a test case as an IOTS

Coverage The number of tests that can be generated from a model is potentially infinite. Therefore, there must be a test selection strategy to maximize the quality of the tests while minimizing the time spent testing. Coverage statistics help with test selection. Coverage statistics are calculated to indicate how adequately the testing has been performed [31]. These statistics are therefore useful metrics for communicating how much of a system is tested.

One type of coverage is *white-box coverage* or *code coverage*: This coverage statistic measures how much of the lines of codes in the implementation is tested. A line of code is considered tested when it is executed during the test run.

When the SUT is a black box, which often is the case, typical coverage metrics for LTSs are *state* and transition coverage [13, 18, 8]. This coverage statistic measures how much of the model is tested. A state in the model is considered tested when the transition system reaches the state during testing. A transition in the model is considered tested when the transition system is in the source state of the transition and either:

- 1. the transition is a stimulus and the input represented by the label of the transition is given to the SUT
- 2. the transition is a response and the output represented by the label of the transition is observed from the SUT

State coverage can be measured by dividing the tested states by the total states in the model. The same process applies to transition coverage. As an example, the coverage metrics of the IOTS test case example in 2.3b are calculated. The test case tests one path through the specification and passes through 3 out of 4 states and 2 out of 4 transitions. The state coverage is therefore 75% and the transition coverage is 50%.

This example shows that the total number of states and transitions in the transition systems has to be known; coverage statistics cannot be measured on an infinitely large LTS, for example.

## 2.2 Algebra

Some basic concepts from algebra are described here. For a general introduction into logic we refer to [10]. This section explains in order: multi-sorted signatures, algebrae, variables & terms and term-mapping & valuations. The algebra described here will be used in the next sections to formally define Symbolic Transition Systems and Graph Grammars.

#### **Definition 2.2.1.** Multi-sorted Signatures

A multi-sorted signature  $\langle S, F \rangle$  describes the sorts and function symbols of a formal language. S is a set of sorts. F is a set of function symbols. Each  $f \in F$  has an arity  $n \in \mathbb{N}$ , where a function symbol with arity n = 0 is called a constant symbol.  $F^i$  denotes the subset of F with function symbols of arity n = i. The sort of a function symbol  $f \in F$  with arity n is given by  $\sigma(f) = s_1...s_{n+1}$ , with  $s_i \in S$  for  $1 \le i \le n$ .  $s_{n+1}$  is the return sort. In this report,  $S = \{int, real, bool, string\}$  denoting the integer, real, boolean and string sorts respectively. F features the commonly used function symbols, which include, but are not restricted to, 'int:+', 'string:=', '¬', '1', which are the addition of integers, the equality of strings, the negation of a boolean and the integer 'one' respectively. The sorts and arities of these examples are given by:

```
1. \sigma(int :+) = \langle int, int, int \rangle

2. \sigma(string :=) = \langle string, string, bool \rangle

3. \sigma(\neg) = \langle bool, bool \rangle

4. \sigma(1) = \langle int \rangle
```

#### **Definition 2.2.2.** Algebrae

An  $algebra \mathcal{A} = \langle \mathbb{U}, \Phi \rangle$  has a non-empty set  $\mathbb{U}$  of values called a universe, partitioned into  $\mathbb{U}^s$  for each  $s \in S$ , and a set  $\Phi$  of functions. A function  $\phi_{\mathcal{A}}$  is typed  $\mathbb{U}^{s_1}_{\mathcal{A}} \times ... \mathbb{U}^{s_n}_{\mathcal{A}} \to \mathbb{U}^{s_{n+1}}_{\mathcal{A}}$ , where  $s_1...s_{n+1}$  is the sort of the function symbol given by the signature. For example,  $<_{\mathcal{A}}: \mathbb{U}^{int}_{\mathcal{A}} \times \mathbb{U}^{int}_{\mathcal{A}} \to \mathbb{U}^{bool}_{\mathcal{A}}$  represents the 'less-than' comparison of two integers.

#### **Definition 2.2.3.** Point algebra

We define a point algebra  $\mathcal{P}$  to be an algebra with  $\forall s \in S. |\mathbb{U}_{\mathcal{P}}^s| = 1$ .

#### **Definition 2.2.4.** Variables

We define  $\mathcal{V} = \mathcal{V}^{int} \uplus \mathcal{V}^{real} \uplus \mathcal{V}^{bool} \uplus \mathcal{V}^{string}$  to be the set of variables. Terms over V, denoted  $\mathcal{T}(V)$ , are built from function symbols F and variables  $V \subseteq \mathcal{V}$ . The definition of a term is:

```
t ::= f(t_1...t_n), where n is the arity of \phi, where x is a variable.
```

We write var(t) to denote the set of variables appearing in a term  $t \in \mathcal{T}(V)$ . Terms  $t \in \mathcal{T}(\emptyset)$  are called ground terms. An example of a term t is (x + (y - 1)), with  $var(t) = \{x, y\}$ . The type of a term is given by:

```
\sigma: t \mapsto s if t = x \in \mathcal{V}^s

s_{n+1} if t = f(t_1...t_n) and \sigma(f) = s_1...s_{n+1}, provided \sigma(t_i) = s_i
```

The set of terms with return type *bool*, is denoted as  $\mathcal{B}(\mathcal{V})$ . An example is (x < y), where the result is *true* or *false*.

#### **Definition 2.2.5.** Term-mapping

A term-mapping is a function  $\mu: \mathcal{V} \to \mathcal{T}(\mathcal{V})$ . A valuation  $\nu$  is a function  $\nu: \mathcal{V} \to \mathbb{U}$  that assigns values to variables. For example, given an algebra,  $\nu: \{(x \mapsto 1), (y \mapsto 2)\}$  assigns the values 1 and 2 to the variables x and y respectively. A valuation of a term given  $\mathcal{A}$  is defined by:

$$\begin{array}{cccc} \nu: & x & \mapsto & \nu(x) \\ & f(t_1...t_n) & \mapsto & f_{\mathcal{A}}(\nu(t_1)...\nu(t_n)) \end{array}$$

When every variable in a term is defined by a valuation, the term can be valuated to a value. Therefore, when every variable in a term-mapping is defined by a valuation, a new valuation can be obtained. Formally, this is defined as:  $\_after\_: (\mathcal{V} \to \mathbb{U}) \times (\mathcal{V} \to \mathcal{T}(\mathcal{V})) \to (\mathcal{V} \to \mathbb{U})$ . Given a valuation  $\nu$  and a term-mapping  $\mu$ , ( $\nu$  after  $\mu$ ):  $\nu \mapsto \nu(\mu(\nu))$ .

## 2.3 Symbolic Transition Systems

Symbolic Transition Systems (STSs) combine a state oriented and data type oriented approach. This formalism is a specification of system behavior like LTSs. These systems are used in practice in ATM and will therefore be part of GRATIS. In this section, previous work on STSs is reviewed. The definitions of STSs and IOSTSs follow. An example of an IOSTS is then given. Next, the mapping of an STS to an LTS is explained and illustrated by an example. This mapping is useful when comparing STSs to Graph Grammars, because both systems can be mapped to an LTS and then compared. Finally, different coverage metrics on STSs and the relation with LTS coverage metrics are explained.

#### 2.3.1 Previous work

STSs are introduced by Frantzen et al. [12]. This paper includes a detailed definition, on which the definition below is based. The authors also give a sound and complete test derivation algorithm from specifications expressed as STSs. Deriving tests from a symbolic specification, also called Symbolic test generation, is introduced by Rusu et al. [25]. Here, the authors use Input-Output Symbolic Transition Systems (IOSTSs). These systems are very similar to the STSs in [12]. However, the definition of IOSTSs we will use in this report is based on the STSs by [12]. A tool that generates tests based on symbolic specifications is the STG tool, described in Clarke et al. [4].

#### 2.3.2 Definition

An STS has locations and switch relations. If the STS represents a model of a software system, a location in the STS represents a state of the system, not including data values. A switch relation defines the transition from one location to another. The location variables are a representation of the data values in the system. A switch relation has a gate, which is a label representating the execution steps of the system. Gates have interaction variables, which represent some input or output data value. Switch relations also have guards and update mappings. A guard is a term  $t \in \mathcal{B}(\mathcal{V})$ . The guard disallows using the switch relation when the valuation of the term results in

false. When the valuation results in *true*, the switch relation of the guard is *enabled*. An update mapping is a term-mapping of location variables. After the system switches to a new location, the variables in the update mapping will have the value corresponding to the valuation of the term.

#### **Definition 2.3.1.** Symbolic Transition Systems

A Symbolic Transition System is a tuple  $\langle W, w_0, \mathcal{L}, i, \mathcal{I}, \Lambda, D \rangle$ , where:

- W is a finite set of locations.
- $w_0 \in W$  is the initial location.
- $\mathcal{L} \subseteq \mathcal{V}$  is a finite set of location variables.
- i is a term-mapping  $\mathcal{L} \to \mathcal{T}(\emptyset)$ , representing the initialisation of the location variables.
- $\mathcal{I} \subseteq \mathcal{V}$  is a set of interaction variables, disjoint from  $\mathcal{L}$ .
- $\Lambda$  is a finite set of gates. The unobservable gate is denoted  $\tau(\tau \notin \Lambda)$ ; we write  $\Lambda_{\tau}$  for  $\Lambda \cup \{\tau\}$ . The arity of a gate  $\lambda \in \Lambda_{\tau}$ , denoted  $arity(\lambda)$ , is a natural number. The parameters of a gate  $\lambda \in \Lambda_{\tau}$ , denoted  $param(\lambda)$ , are a tuple of length  $arity(\lambda)$  of distinct interaction variables. We fix  $arity(\tau) = 0$ , i.e. the unobservable gate has no interaction variables.
- $D \subseteq W \times \Lambda_{\tau} \times \mathcal{B}(\mathcal{L} \cup \mathcal{I}) \times (\mathcal{L} \to \mathcal{T}(\mathcal{L} \cup \mathcal{I})) \times W$ , is the switch relation. We write  $w \xrightarrow{\lambda, \gamma, \rho} w'$  instead of  $(w, \lambda, \gamma, \rho, w') \in D$ , where  $\gamma$  is referred to as the guard and  $\rho$  as the update mapping. We require  $(var(\gamma) \cup var(\rho)) \subseteq (\mathcal{L} \cup param(\lambda))$ . We define  $out(w) \subseteq D$  to be the outgoing switch relations from location w.

An IOSTS can now easily be defined. The same difference between the labels in LTSs and IOTSs apply, namely each gate has a type  $\iota \in Y$ . As with labels, each gate is preceded by an '?' or '!' to indicate whether it is an input or an output respectively. The full definition is as follows:

#### **Definition 2.3.2.** Input-Output Symbolic Transition Systems

An IOSTS is a 5-tuple  $\langle W, \mathcal{L}, i, \Lambda_Y, D \rangle$ , where  $\Lambda_Y \subseteq \Lambda \times Y$  are the input-output gates.

#### 2.3.3 Example

In Figure 2.4 the IOSTS of a simple board game is shown, where two players consecutively throw a die and move along four squares, which are situated in a circle. The 'init' switch relation is a graphical representation of the variable initialization i. The values in the tuple of the IOSTS are defined as follows:

```
\begin{array}{rcl} W & = & \{t,m\} \\ w_0 & = & t \\ \mathcal{L} & = & \{T,P1,P2,D\} \\ \imath & = & \{T \mapsto 0,P1 \mapsto 0,P2 \mapsto 2,D \mapsto 0\} \\ \mathcal{I} & = & \{d,p,l\} \\ \Lambda & = & \{?throw,!move\} \\ D & = & \{t \xrightarrow{?throw,1 \leq d \leq 6,D \mapsto d} m, \\ & & \frac{!move,T=1 \wedge l = (P1+D)\%4,P1 \mapsto l,T \mapsto 2}{m} \downarrow t, \\ & & & m \end{array}
```

The variables T, P1, P2 and D are the location variables symbolizing the player's turn, the positions of the players and the number of the die thrown respectively. The output gate !move has  $param = \langle p, l \rangle$  symbolizing which player moves to which location. The input gate ?throws has  $param = \langle d \rangle$  symbolizing which number is thrown by the die. The switch relation with gate ?throws has the restriction that the number of the die thrown is between one and six and the

update sets the location variable D to the value of interaction variable d. The switch relations with gate !move have the restriction that it must be the turn of the player moving and that the new location of the player is the number of steps ahead as thrown by the die. The update mapping sets the location of the player to the correct value and passes the turn to the next player.

Figure 2.4 shows the example visually. The gates, guards and updates are separated by pipe symbols '|' respectively. The initialization function is expressed by a switch relation with no source location, gate and guard.

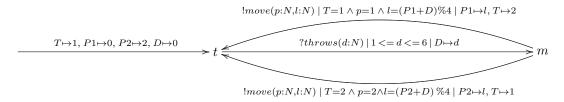


Figure 2.4: The IOSTS of a board game example

#### 2.3.4 STS to LTS mapping

This section shows the method of mapping an STS to an LTS.

Consider an STS J. We can construct an LTS K from J, such that K is an expansion of J. There exists a mapping from the location and location variable valuations to the states of K and from the switch relations and variable valuations of J to the transitions of K. These relations are defined as follows:

#### **Definition 2.3.3.** STS-to-LTS mapping

```
\begin{array}{ll} \mu_Q: & (W\times (\mathcal{L}\to \mathbb{U}))\to Q \\ \mu_L: & (\Lambda\times (\mathcal{I}\to \mathbb{U}))\to L \\ \\ \mu_T: & (w\xrightarrow{\lambda,\gamma,\rho} w',\nu: ((\mathcal{L}\cup \mathcal{I})\to \mathbb{U}))\mapsto (\mu_Q(w,\nu\upharpoonright \mathcal{L})\xrightarrow{\mu_L(\lambda,\nu\upharpoonright \mathcal{I})} \mu_Q(w',(\nu\ after\ \rho)\upharpoonright \mathcal{L})) \end{array}
```

When the number of possible valuations for  $\mathcal{L}$  and  $\mathcal{I}$  is finite, the transformation is always possible to an LTS with finite number of states. This often is the case when the guards of the switch relations provide bounds to the interaction variables and the update mappings do not infintely increase of decrease the location variables.

An example of this transformation is shown in Figure 2.5. The label 'do(1)' in the LTS is a textual representation of the gate 'do' plus a valuation of the interaction variable 'd'. The text on the nodes indicate from which location and valuation the state was created. The node labelled ' $w_0$ , N=2' is an example of an unreachable state.

#### 2.3.5 Coverage

Coverage metrics do not only apply to LTSs, they can also be used on STSs. The simplest metric to describe the coverage of an STS is the location and switch-relation coverage, which express the percentage of locations and switch relations tested. Measuring state and transition coverage of an STS is possible using the LTS from the STS-to-LTS mapping.

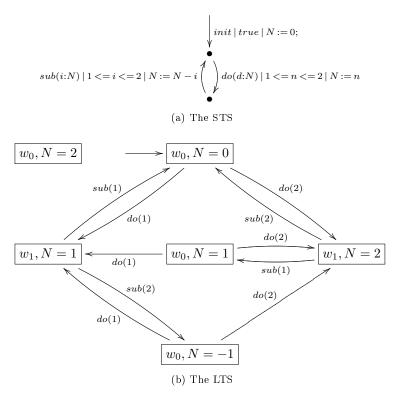


Figure 2.5: An example of a transformation of an STS to an LTS

## 2.4 Graph Grammars

A *Graph Grammar* (GG) is also a specification of system behavior like LTSs and STSs are. A GG is composed of a set of graph transformation rules. These rules indicate how a graph can be transformed to a new graph. These graphs are called *host graphs*. The rules are composed of graphs themselves, which are called *rule graphs*.

The rest of this section is ordered as follows: first, graphs, host graphs, rule graphs and graph transformation rules are explained. Then, the definition of a *Graph Transition System* (GTS) is given. An example of a GG and a GTS is then given. Finally, the definition of IOGGs is given. For a more detailed overview of GGs, we refer to [23, 9, 1].

#### **Definition 2.4.1.** Graphs

A graph is composed of nodes and edges. In this report, we assume a universe of nodes  $\mathbb{V} = \mathbb{W} \oplus \mathbb{U} \oplus \mathcal{V} \oplus 2^{\mathcal{T}}$ , where  $\mathbb{W}$  is the universe of standard graph nodes. The other symbols were introduced in section 2.2; these are the universe of values, the universe of variables and the power set of the universe of terms respectively.  $\mathbb{E} \subseteq \mathbb{V} \times L \times \mathbb{V}$  is the universe of edges.

#### **Definition 2.4.2.** Host graphs

A host graph G is a tuple  $\langle V_G, E_G \rangle$ , where:

- $V_G \subseteq (\mathbb{W} \uplus \mathbb{U})$  is the node set of G
- $E_G \subseteq (V_G \setminus \mathbb{U} \times L \times V_G)$  is the edge set of G

Figure 2.6 shows an example of a host graph. Here,  $n_1, n_2 \in \mathbb{W}$  are the *identities* of the nodes. The other four nodes are values in  $\mathbb{U}$ .

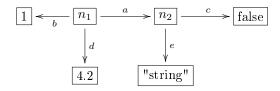


Figure 2.6: An example of a host graph

#### **Definition 2.4.3.** Rule graphs

A rule graph H is a tuple  $\langle V_H, E_H \rangle$ , where:

- $V_H \subset (\mathbb{V} \setminus \mathbb{U})$  is the node set of H
- $E_H \subseteq (V_H \times L \times V_H)$  is the edge set of H

In addition, the following must hold:

- $\forall z \in V_H \cap 2^T$ .  $var(z) \subseteq V_H$  The variables used in the terms must be present as nodes in the rule graph.
- $\forall z \in V_H \cap z \in \mathcal{V}$ .  $\exists (\_, \_, z) \in E_H$  If a variable is used in a rule graph, it needs context. Therefore, there must be an edge with the variable node as target.

Figure 2.7 shows an example of a rule graph. Here,  $r_1, r_2 \in \mathbb{W}$  are the node identities,  $x_1, x_2 \in \mathcal{V}^{int}$  and  $\{x_1 + 1, x_2\} \in 2^{\mathcal{T}}$ . The set of terms is mapped as a node to the same value. This mapping is explained in the next definition. The consequence is that this node implicitly expresses the relation  $x_1 + 1 = x_2$ .

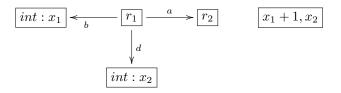


Figure 2.7: An example of a rule graph

#### **Definition 2.4.4.** Morphisms

A graph g has a morphism to a graph g' if there is a structure-preserving mapping from the nodes and the edges of g to the nodes and the edges of g' respectively. Elements of this mapping are called images in g' and pre-images in g. A graph g has a partial morphism to a graph g' if there are elements in g without an image in g'. For morphisms between host graphs and between rule graphs, the pre-image and image must be the same node. The next definition gives the rule for morphisms from rule graphs to host graphs.

#### **Definition 2.4.5.** Host graph images for rule graphs

A rule graph H to a host graph G morphism is a structure-preserving mapping, such that:

- A node  $z \in \mathbb{W}$  has an image i in G if i = z
- A value  $x \in \mathbb{U}$  has an image i in G if i = x
- A variable  $v \in \mathcal{V}^s, s \in S$  has an image i in G if  $i \in \mathbb{U}^s$ . This gives a valuation  $\nu$  for the variables in the rule graphs to the value nodes in the host graph.
- A node  $z \in 2^{\mathcal{T}}$  has an image i in G if i is the evaluation of all terms in z under  $\nu$ .

#### **Definition 2.4.6.** Transformation rules

A transformation rule r is a tuple  $\langle LHS, NAC, RHS, l \rangle$ , where:

- LHS is a rule graph representing the left-hand side of the rule
- NAC is a set of rule graphs representing the negative application conditions
- RHS is a rule graph representing the right-hand side of the rule
- $l \in L$  is the label of the rule

There exist implicit partial morphisms from the LHS to each rule graph in NAC and from the LHS to the RHS by means of the node identities. These morphisms are  $rule\ graph\ morphisms$ .

#### **Definition 2.4.7.** Creators and erasers

A *creator* is an edge or node in the RHS of a rule, that is not in the LHS of the rule. An *eraser* is an edge or node in the LHS of a rule that is not in the RHS of that rule.

#### **Definition 2.4.8.** Rule matches

A rule r has a rule match on a host graph G if its LHS has a morphism to G and none of the graphs in NAC have a morphism to G. The morphism of the LHS to a host graph is a match morphism  $m \in M$ .

#### **Definition 2.4.9.** Rule transitions

Let r be a rule, G a host graph and m a match morphism. After m is found, all nodes and edges in LHS that do not have an image in RHS, are removed from G. All elements in RHS that do not have a pre-image in LHS, are added to G. The result of this process is called a *rule transition*, denoted by:  $G \xrightarrow{r,m} G'$ .

Figure 2.8 shows an example of the initial graph  $G_0$ , one rule of a GG and the corresponding rule match.  $G_0$  can be represented by  $\langle \{n1,n2\}, \{\langle n1,a,n1\rangle, \langle n1,A,n2\rangle, \langle n2,B,n2\rangle \} \rangle$ . The *LHS* of the rule has a match in  $G_0$ . Neither *NAC1* and *NAC2* have a match in  $G_0$ , because the edge with label  $G_0$  does not exist in  $G_0$ . The new graph after applying the rule is  $G_1$ . The edge with label  $G_0$  is removed from the graph and an edge with label  $G_0$  is added with the same source and target node as the removed edge.

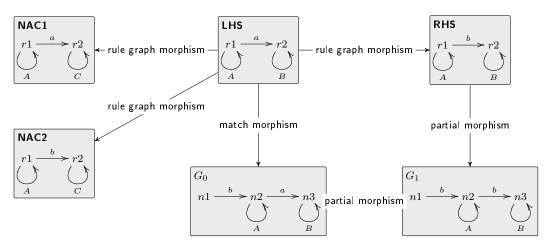


Figure 2.8: An example of a graph transformation

#### **Definition 2.4.10.** Graph Grammars

A graph grammar is a tuple  $\langle R, G_0 \rangle$ , where:

• R is a set of graph transformation rules

•  $G_0$  is the initial graph

By repeatedly applying graph transformation rules to the start graph and all its consecutive graphs, a GG can be explored to reveal a Graph Transition System (GTS). This transition system consists of graphs connected by rule transitions.

#### **Definition 2.4.11.** Graph Transition Systems

A graph transition system is a tuple  $\langle \mathcal{G}, R, M, U, G_0 \rangle$ , where:

- $\mathcal{G}$  is a set of graphs
- $L \subseteq R \times M$  is a set of labels
- $U \subseteq \mathcal{G} \times L \times \mathcal{G}$  is the rule transition relation
- $G_0 \in \mathcal{G}$  is the initial graph

Let  $K = \langle R, G_0 \rangle$ . A GTS  $O = \langle \mathcal{G}, R, M, U, G_0 \rangle$  is derived from K by the following.  $\mathcal{G}, M, U$  are the smallest sets, such that:

- $G_0 \in \mathcal{G}$
- if  $G \in \mathcal{G}$  and  $G \xrightarrow{r,m} G'$  then  $G' \in \mathcal{G}, (r,m) \in L, (G \xrightarrow{r,m} G') \in U$

In order to specify stimuli and responses with GGs, a definition is given for an Input-Output GG (IOGG).

#### Definition 2.4.12. Input-Output Graph Grammars

An IOGG is a tuple  $(R_Y, G_0)$ , where  $R_Y \subseteq R \times Y$  are input-output transformation rules.

Exploring an IOGG leads to an Input-Output Graph Transition System (IOGTS).

**Definition 2.4.13.** Input-Output Graph Transition Systems

An IOGTS is a tuple  $\langle \mathcal{G}, R_Y, M, U_Y, G_0 \rangle$ , where:

- $L_Y \subseteq R_Y \times M$  are the input-output labels
- $U_Y \subseteq \mathcal{G} \times L_Y \times \mathcal{G}$  are the input-output rule transitions

#### **Definition 2.4.14.** Rule priorities

A graph grammar with rule priorities P assigns a priority  $p \in \mathbb{N}$  to a  $r \in R$ , such that  $r \mapsto p \in P$ . The definition of GTSs is extended with this definition of rule priorities and the following:  $r_1, r_2 \in R, \ G \in \mathcal{G} \ . \ (G \xrightarrow{r_1, m_1} G') \in U \land P(r_1) > P(r_2) \to \nexists m_2, G'': \ (G \xrightarrow{r_2, m_2} G'') \in U$ 

$$r_1, r_2 \in R, G \in \mathcal{G} : (G \xrightarrow{r_1, m_2} G') \in U \land P(r_1) > P(r_2) \to \nexists m_2, G'' : (G \xrightarrow{r_2, m_2} G'') \in U$$

In the graph grammar in Figure 2.9, the 'add' rule produces a rule transition to a graph, where the sub rule produces a rule transition back to the start graph. Suppose P(add) > P(sub), then the 'sub' rule does not have a outgoing rule transition from the start graph.

#### 2.5Tooling

#### 2.5.1ATM

ATM is a model-based testing web application, developed in the Ruby on Rails framework. It has been used to test the software of several big companies in the Netherlands since 2006. It is under

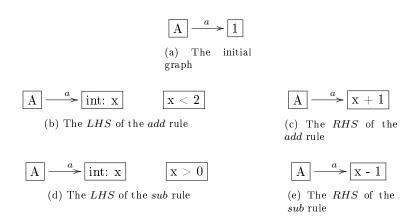


Figure 2.9: Priority rules

continuous development by Axini.

A UML sequence diagram for ATM is shown in Figure 2.10, depicting a test run from start to end.

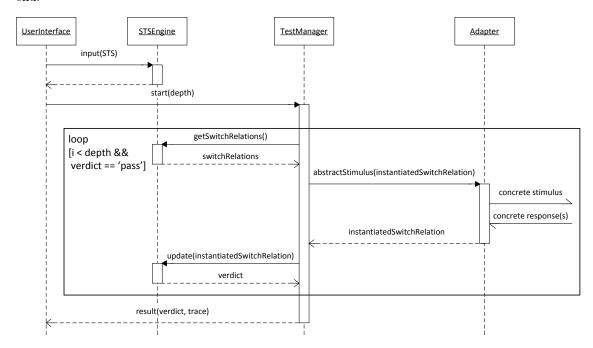


Figure 2.10: ATM sequence diagram

The tool functions as follows:

- 1. An STS is given to an STS Engine, which keeps track of the current location and variables. The user starts the test and gives a 'depth', indicating how many stimuli should be tested. The variable i stands for the current iteration of loop and is initially set to 0. The variable verdict is initially set to 'pass'.
- 2. The STS Engine gives the possible switch relations from the current location to the Test Manager. It chooses an enabled switch relation based on a test strategy, which can be a random strategy or a strategy designed to obtain a high location/switch relation coverage. The valuation of the variables in the guard are also chosen by a test strategy, which can be

- a random strategy or a strategy using boundary-value analysis. The choice is represented by an instantiated switch relation.
- 3. The instantiated switch relation is given to the Test Execution component as an abstract stimulus. The term abstract indicates that the instantiated switch relation is an abstract representation of some computation steps taken in the SUT. For instance, a transition with label '?connect' is an abstract stimulus of the actual setup of a TCP connection between two distributed components of the SUT.
- 4. The translation of an abstract stimulus to a concrete stimulus is done by the Adapter. This component has to be programmed by the tester such that the abstract stimulus is correctly translated to a concrete stimulus. This component provides the stimulus to the SUT. When the SUT responds, the Adapter translates this response to an abstract response. For instance, the Adapter receives an HTTP response that the TCP connect was successful. This is a concrete response, which the Adapter translates to an abstract response, such as an instantiated switch relation with gate '!ok'. The SUT can also give multiple responses. As with the stimuli, the tester has to program the translation from concrete responses to abstract responses. The Test Manager is notified with these abstract responses.
- 5. The Test Manager updates the STS engine with the chosen abstract stimuli and received abstract responses. If this is possible according to the STS, a pass verdict is given, otherwise a fail verdict is given. The Test Manager updates the *verdict* variable accordingly. The loop continues as long as all responses are according to the specification and the required number of tested stimuli has not been reached. The test is stopped at a fail verdict, because the SUT has entered an invalid state and the STS engine cannot give possible switch relations any more. For instance, an error could have occurred, which is an invalid response and makes continuing impossible.
- 6. When the Test Manager finishes it gives a pass verdict for this test if all verdicts given by the STS engine were a pass verdict. Otherwise, the result is a fail verdict. Also a trace is given of all chosen and observed instantiated switch relations. This can be used to calculate coverage information for the test and to allow the SUT or the STS to be fixed in case of a fail verdict.

#### 2.5.2 GROOVE

GROOVE is an open source, graph-based modelling tool, written in Java and in development at the University of Twente since 2004 [24]. It has been applied to several case studies, such as model transformations and security and leader election protocols [6]. A UML sequence diagram for GROOVE is shown in Figure 2.11, depicting a GG exploration to a GTS.

The tool functions as follows:

- 1. A graph grammar is given as input to a RuleApplier component, which determines the possible rule transitions.
- 2. The user selects an ExplorationStrategy from a list of possible strategies. This strategy explores all possible host graphs and rule transitions. The possible rule transitions from the initial graph state are obtained from the RuleApplier and a rule transition is chosen, based on the exploration strategy. The target host graph of the chosen rule transition is again given to the RuleApplier until no more new host graphs can be explored.
- 3. The ExplorationStrategy returns the explored GTS to the UserInterface.

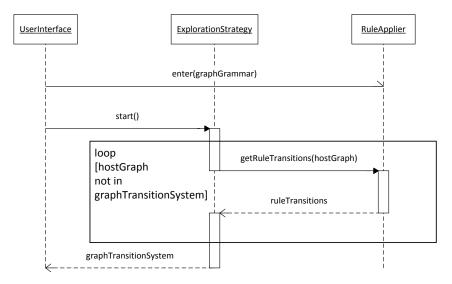


Figure 2.11: GROOVE sequence diagram

#### 2.5.3 GROOVE visual elements

Labels and flags Nodes in GROOVE have several kinds of labels: regular labels, type labels and flags. Figure 2.12 shows a node with a type label (bold), two flags (italic) and two regular labels. Nodes in GROOVE can have one type, indicated by the type label. Typing is not explained further in this report<sup>1</sup>. A node can have multiple regular labels and flags.



Figure 2.12: GROOVE labels and flags

Rule node matching Nodes in a rule graph in GROOVE can also match the same host graph node, by connecting them with an equals '=' labelled edge. This means that any images of both nodes have to be the same. Figure 2.13a shows an example of this. Nodes in a rule graph in GROOVE can also explicitly not match each other, by connecting them with an not-equals '!=' labelled edge. This means that any images of both nodes cannot be the same. Figure 2.13b shows an example of this.



Figure 2.13: Node matching in GROOVE rule graphs

Colors Rule graphs in GROOVE combine LHS, RHS and NAC into one rule graph. The colors on the nodes and edges in GROOVE rules represent whether they belong to the LHS, RHS or NAC of the rule. See Figure 2.14 for an example.

 $<sup>^1\</sup>mathrm{See}$  the documentation of GROOVE for more information:  $\mathrm{http://groove.cs.utwente.nl/doc/}$ 

- 1. normal line (black): This node or edge is part of both the LHS and RHS.
- 2. dotted line (red): This node or edge is part of the NAC only.
- 3. thick line (green): This node or edge is part of the RHS only.
- 4. dashed line (blue): This node or edge is part of the LHS only.

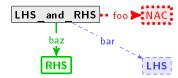


Figure 2.14: GROOVE rule graph colors

Variable nodes and terms Variable nodes in GROOVE are represented by their type: 'int', 'bool', 'real' and 'string' for integer, boolean, real and string variables respectively. Figure 2.15 shows two integer variable nodes and the constant integer node '1'. The diamond shaped node is a term node. It has two argument edges  $\pi_0, \pi_1$  and a result edge 'int:add'. The term represented here is the addition of two integers, the first one being an integer variable, the second being the number 1. When this rule matches a host graph, the target variable node of the result edge is set to the result of the term; in this case the image of the first variable node plus one.

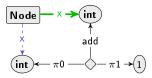


Figure 2.15: Terms in GROOVE rule graphs

**Term shorthand notation** A rule node with an edge to a constant is shortened to a label on the node. Figure 2.16a shows a node with an edge labelled 'x' to the constant '1'. Figure 2.16b shows the shorthand notation of this edge as the label 'x = 1' on the source node of the edge. Terms can also be shortened. The rule graph in Figure 2.15 can be shortened to the rule graph in Figure 2.17.



Figure 2.16: Constant shorthand notation in GROOVE

#### Wildcards

Rule transition parameters Rule transitions can have parameters in GROOVE. Figure 2.18a shows a rule where the node variables have a number in the top right of the node. These numbers indicate that the value of the variables are placed as parameters on the rule transition, in the order indicated by the numbers. This rule matches the host graph in Figure 2.18b. The result of applying the rule twice is the GTS in Figure 2.18c.



Figure 2.17: Term shorthand notation in GROOVE

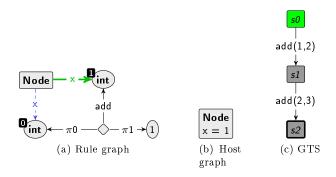


Figure 2.18: Rule transition parameters in GROOVE

Quantification GROOVE supports quantification operations over nodes in rule graphs. Figure 2.19 shows a simple example. The 'forall' operator here matches all nodes typed 'Node'. GROOVE also supports the 'exists' operator and nesting of operators, however this is out of scope for this report. The 'forall' operator will be used in the model examples to perform operations over sets of nodes, such as in this rule: all self-edges labelled 'x' on nodes typed 'Node' are deleted from the host graph.



Figure 2.19: An example of quantification in GROOVE

#### 2.5.4 Example GROOVE graph grammar

The running example from Figure 2.4 is displayed as a graph grammar, as visualized in GROOVE, in Figure 2.20. Figures 2.20b, 2.20c and 2.20d show three rules. Figure 2.20a shows the start graph of the system.

The rules can be described as follows:

- 1. 2.20b: 'if a player has the turn and he has not thrown the die yet, he may do so.'
- 2. 2.20c: 'if a player has the turn and he has thrown the die and this number is larger than zero, he may move one place and then it is as if he has thrown one less.'
- 3. 2.20d: 'if a player has finished moving (number thrown is zero), the next player receives the turn.'

The graph is transformed after the rule is applied. The resulting graph after the transformation is the new state of the system and the rule is the transition from the old state (the graph as it was before the rule was applied) to the new state. Figure 2.21 shows the IOGTS of one ?throws rule application on the start graph. Note that the ?throws is an input, as indicated by the '?'. State

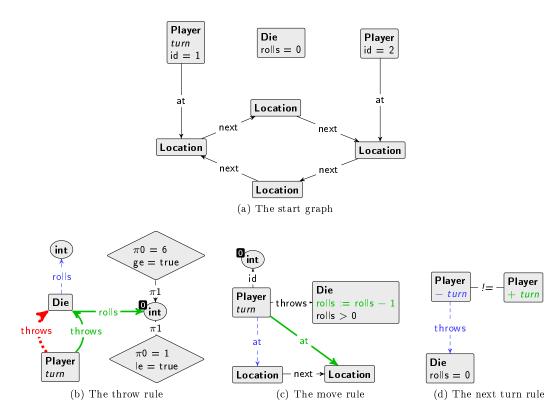


Figure 2.20: The graph grammar of the board game example in Figure 2.4

 $s_1$  is a representation of the graph in Figure 2.20a. Figure 2.22 shows the graph represented by  $s_2$ .



Figure 2.21: The GTS after one rule application on the board game example in Figure 2.20

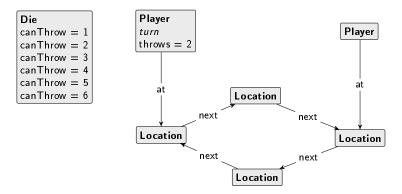


Figure 2.22: The graph of state s2 in Figure 2.21

## Chapter 3

# From Graph Grammar to STS

## 3.1 Requirements considerations

As described in secitor 1.5, the GRATiS tool needs to fulfill three requirements:

- 1. A graph grammar must be used as the model; it must derive from the specification and be used for the testing.
- 2. It must be possible to measure the test progress/completion, by means of coverage statistics.
- 3. The solution must be efficient: it should be usable in practice, therefore the technique should be scalable and the imposed constraints reasonable from a practical view point.

**IOGGs** In order to fulfill the first requirement, stimuli and responses have to be obtained from a GG. ATM uses an IOSTS, where the instantiated switch relations represent a stimulus to or a response from the SUT. GGs have no notion of inputs and outputs, therefore IOGGs have to be used as the model formalism. IOGGs can be explored to IOGTSs and the I/O labels of the IOGTS can be used to represent abstract stimuli/responses.

On-the-fly vs. offline exploration The exploration of a GG can be done in two ways: on the fly, rule transitions are explored only when chosen by ATM, or offline, the GG is first completely explored and then sent to ATM. On-the-fly model exploration works well on large and even infinite models. However, coverage statistics cannot be calculated with this technique. The number of states (graphs) and rule transitions the model has when completely explored are not known, so a percentage cannot be derived. As coverage statistics are an important metric, the offline model exploration is chosen for GRATiS.

**Data values** An IOGTS can potentially be infinitely large, due to the range of data values. This is a potential risk for the validation of the system. A model that is more efficient with data values is an STS. The setup of GRATiS is therefore to transform the IOGG directly to an IOSTS. This transformation should be done efficiently to fulfill the third requirement. Note that the second requirement is still met, because location and switch relation coverage can be calculated on the IOSTS.

**Steps** Taking these requirements into account, the method to achieve the goal of model-based testing on GGs is the following three steps:

- 1. Create an IOGG by assigning I/O types to the graph transformation rules of a GG
- 2. Create an IOSTS from the IOGG
- 3. Perform the model-based testing on the IOSTS

The rest of this chapter describes a declaritive definition for creating an IOSTS from an IOGG.

#### 3.2 From IOGG to IOSTS

#### 3.2.1 Variables in GGs

The location variables in an STS represent an aspect of the modelled system. For instance, if a system keeps track of the number of items in containers, the STS modelling this system could have integer location variables  $items_1..items_n$ . GGs do not have this kind of variables. The variable nodes in rule graphs are used to match a value in a host graph, which is only available to that rule. A definition of persistent variables in GGs is needed in order to define location variables from an IOGG.

#### **Definition 3.2.1.** GG variables

A GG variable is a tuple  $\langle l_a, l_v \rangle$ , where:

- $l_a$  is the variable label, which is part of an edge  $(z_a, l_a, z_a)$ , where  $z_a$  is called the variable
- $l_v$  is the value label, which is part of a value edge:  $(z_a, l_v, z)$ , with  $z \in \mathbb{U}$ .

The item/container example modelled in a graph grammar could be a graph node representing a container with an edge labelled 'items' to an integer node. This is shown in Figure 3.1a. The variable (var1, items) is now represented by this graph. Figure 3.1b shows the same example in GROOVE. The variable edge is omitted here and the variable label is represented by the flag var1. This convention for GROOVE is used in the rest of this report.



Figure 3.1: Example of a GG variable

#### 3.2.2 Graph exploration with point algebra

The IOGG cannot be directly made into an IOSTS, without using the IOGTS. To avoid the problem of a potentially infinitely large IOGTS, the point algebra is used. Using the point algebra when exploring a GG has two effects:

- 1. The host graphs that differ only in value nodes are collapsed into one
- 2. The variable nodes in rule graphs can have at most one image in the host graph

The actual values of the value nodes in host graphs and of the variable nodes in rule graphs are not needed to make the IOSTS, which is explained in the next section. Using the point algebra for the exploration poses some constraints, which are explained in section 3.4.

#### 3.2.3 The IOGG to IOSTS definition

First the declaritive definition is given, then each part of the definition is described in more detail.

#### **Definition 3.2.2.** IOGG to IOSTS

Let K be an IOGG. From K we define an IOSTS J. The first step is to explore K using the point algebra  $\mathcal{P}$  to an IOGTS  $O_{\mathcal{P}}$ . The elements of J can be obtained as follows:

- $W = \mathcal{G}$
- $w_0 = G_0$
- $\mathcal{L} = \mathcal{V}_{GG}$
- $i = \phi_i$ , where  $\phi_i$  is defined below
- $\Lambda = R$
- $\mathcal{I} = \mathcal{V}$
- D = U, where  $\gamma, \rho$  are given by functions defined below

**Locations** The locations abstract from data values, exactly like host graphs do under the point algebra. Therefore, the set of locations in J are the set of host graphs in  $O_{\mathcal{P}}$ . The initial location in J is also equal to the start graph of  $O_{\mathcal{P}}$ .

**Location variables** GG variables were defined to have location variables in GGs. Therefore, it is no surprise that the set of location variables in J is exactly the set of GG variables in  $O_{\mathcal{P}}$ . This poses some constraints on creators/erasers for the variable anchors, variable edges and value edges. This is explained in detail in section 3.4.

**Initialization function** The initial value of the location variables is defined by the start graph. The start graph contains the GG variables and their initial values. This poses a constraint on the start graph, which is explained in section 3.4.

**Definition 3.2.3.** Initialization function

$$\phi_i: (l_a, l_v) \mapsto z \mid (z_a, l_a, z_a) \in E_{G_0} \land (z_a, l_v, z) \in E_{G_0}$$

**Gates** The gate of a switch relation represents the stimulus to or response from the SUT. In an IOGG, the rules represent the stimuli and responses. Therefore, the set of gates  $\Lambda$  is equal to the set of rules R.

Interaction variables Interaction variables are used by the gates to represent a stimulus or response variable. The variable nodes in rule graphs are this representation. The set of interaction variables  $\mathcal{I}$  is equal to the set of variable nodes  $\mathcal{V}$ . The arity of a rule is defined by the variable nodes in the LHS of the rule:

$$arity(r) = |\mathcal{V} \cap V_{LHS}|$$

**Switch relations** A rule transition  $G \xrightarrow{r,m} G' \in U$  is mapped to a switch relation  $(G \xrightarrow{r,\phi_{\gamma},\phi_{\rho}} G') \in D$ . Note that the set of locations is the set of host graphs, therefore G and G' represent the source and target location of the switch relation. Also, the set of rules is chosen to be the set of

gates, therefore r represents the gate of the switch relation. The function  $\phi_{\gamma}$  obtains the guard as a term and  $\phi_{\rho}$  replaces the  $\rho$  function. These functions are defined in the next paragraphs.

**Guard** The guard of a switch relation restricts the use of the switch relation based on the values of the variables. In a GG, a rule is restricted by the terms. The variables used in the terms are interaction variables. Therefore, the first part of the guard is constructed by joining the terms for each term node.

#### Definition 3.2.4. First guard function

$$\phi 1_{\gamma}: \bigwedge_{z \in V_{LHS} \cap 2^{\mathcal{T}}, t_1 \in z, t_2 \in z} t_1 = t_2$$

We apply this to the rule graph in Figure 3.2. This rule graph contains one term node, which in turn contains two terms. Formally, the first part of the guard for this rule graph is:

$$(x_1+1=x_1+1) \land (x_1+1=x_2) \land (x_2=x_2) \land (x_2>3=x_2>3) \land (x_2>3=true) \land (true=true)$$

When  $t_1 = t_2$ , the equation for this part is not useful, therefore it is omitted from now on.

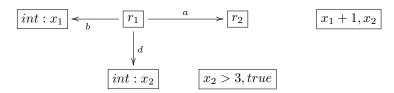


Figure 3.2: a rule graph

This first part of the guard contains only the interaction variables. In an STS, the values for  $x_1$  and  $x_2$  can be chosen such that the guard holds. However, the variable nodes cannot have just any value; their value is determined by their image in the host graph. This image can be the value of a GG variable. Therefore we add a second part to the guard to link the interaction and location variables.

#### **Definition 3.2.5.** Second guard function

$$\phi 2_{\gamma}: \ \bigwedge_{(l_a, l_v) \in \mathcal{V}_{GG}, \ z \in \mathcal{V} \cap V_{LHS} \ | \ (z_a, l_a, z_a) \in E_G \land (z_a, l_v, m(z)) \in E_G}(l_a, l_v) = z$$

We apply this to the rule graph in Figure 3.2 and the host graph in Figure 3.3. The rule has a match in the host graph. The second part of the guard for this rule is:

$$(var1, b) = x_1 \wedge (var1, d) = x_2$$

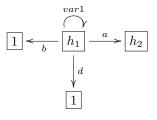


Figure 3.3: a host graph

#### **Definition 3.2.6.** Guard function

The complete guard is created by:

$$\phi_{\gamma}: \phi 1_{\gamma} \wedge \phi 2_{\gamma}$$

**Update mapping** When a value edge is erased from a graph and a new value edge is created with the same label and variable anchor, this inidicates an update for the corresponding GG variable. The update mapping for the switch relation represented by this rule transition should map the matched GG variable to the interaction variable represented by the target of the new value edge.

**Definition 3.2.7.** Update mapping function

$$\phi_{\varrho}: (l_a, l_v) \mapsto z' \mid (z_a, l_a, z_a) \in E_G \land (z, l_v, z') \in E_{RHS} \land m(z) = z_a$$

This poses some constraints on the eraser/creator edges for value edges, which are explained in section 3.4. These constraints ensure that  $\phi_{\rho}$  is bijective.

## 3.3 Rule priorities

Rule priorities are not taken into account in the definition above. First, we show why the definition above does not work with rule priorities. Then we show a method of including rule priorities in the IOSTS.

We apply the definition to the GG in Figure 2.9. We assume the rules both are stimuli, i.e. each is a I/O transformation rule (r, input), where r is the respective rule. All host graphs explored by this GG are isomorphic under the point algebra, so they represent the same location. The IOSTS obtained from this IOGG is in Figure 3.4, with  $i = \{x \mapsto 25\}$ . This IOSTS is wrong, because the '?sub' switch relation can be taken from the start, whereas the '?sub' rule in the IOGG cannot be applied to the start graph, because it has a lower priority than the '?add' rule.

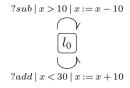


Figure 3.4: A wrong STS transformation of the graph grammar in Figure 2.9

The solution is shown in Figure 3.5. The negated guard of the '?add' switch relation is added to the '?sub' switch relation. The optimized guard for this switch relation is 'x >= 30' of course, but this shows the main principle: for a rule transition u and a set of rule transitions U with higher priority rules and the same source graph as u, the negated guard of the switch relations represented by U must be added to the guard of the switch relation represented by u. In the example, the 'x < 30' guard is negated to '!(x < 30)' and added to yield the 'x > 10 && !(x < 30)' guard.

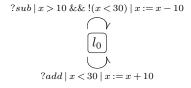


Figure 3.5: A correct STS transformation of the graph grammar in Figure 2.9

This problem only arises when the switch relation represented by the rule transition has a guard; if the rule has no constraints on data and if it is applicable on one graph state, it is applicable on

all isomorphic graph states under the point algebra. Therefore, rule transitions with lower priority rules do not exist from that graph state and the respective switch relations also do not exist.

#### 3.4 Constraints

In order for the definition in section 3.2 to work, four constraints are made for the IOGGs used in GRATiS. This section describes those constraints.

**GG** variable persistency All location variables in an STS are initialized to some value and no new variables are added. In a GG, it is possible to erase and create new variables in the transformation rules. Therefore, we pose the following constraints:

- All GG variables must be present in the start graph
- Variable anchors and variable edges cannot be erased or created
- A transformation rule may erase a value edge if and only if it creates a new edge with the same source node and label as the erased value edge. The target node of the new edge must be a value node of the same sort as the target node of the erased edge

Unique GG variables The GG variables to location variables mapping has to be bijective. The previous constraints ensure the GG variables are always present, however they do not ensure their uniqueness. Therefore, we pose the following constraints:

- The variable labels have to be unique; there cannot be two variable edges with the same label in the start graph
- The value labels for the value edges with the same source node have to be unique; there cannot be two edges with the same variable anchor with the same label in the start graph

No GG variables in NACs In graph transformation rules, it is common to create restrictions on data using a NAC. For example, the rule graph in Figure 3.6a as a NAC expresses that the rule cannot be applied when the system is in state 'done'. When using the point algebra, a problem occurs when a value edge is part of a NAC. The rule containing such a NAC will never match any host graph, because:

- (a) the value edge is present in every host graph as stated in the previous constraints
- (b) the target value node of the value edge will always be an image of the target variable node of the pre-image of the value edge. This is assuming the variable node in the NAC is of the same sort as the value node, otherwise the NAC would never have a match, because of the constraint on the sort of the value node of a value edge. Such a NAC would add nothing to the rule.

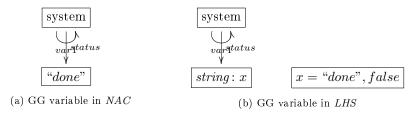


Figure 3.6: Node creating rule without structural constraint

Therefore we pose the following constraint: A NAC may never match the value edge and value node of a GG variable.

The correct way of modelling the example when using the point algebra is shown as the LHS of a rule in Figure 3.6b. Under the point algebra, both terms x = "done" and false evaluate to the same boolean value. Therefore, an image for this term node can always be found, when the term node is in the LHS of the rule.

The guard of the switch relation will be (x = "done") = false. This leads to a case where the guard of the switch relation can never be satisfied. The following paragraph describes such a case.

Data constraints in node creating rules A case where a guard can no longer be satisfied is shown in Figure 3.7. This figure shows the *LHS* and *RHS* of a rule in the container-items example. The rule adds an item to the container unless it is full, i.e. has five items. If an item is added, a new node labelled 'new' is created in the host graph. Under the point algebra, this rule always matches the host graph and thus this rule creates an infinite number of nodes. Therefore, the exploration never ends. This means that an IOGG with such a rule has an infinite number of graphs and the corresponding IOSTS has an infinite number of switch relations. However, the guards of the switch relations can no longer be satisfied when the location variable corresponding to the GG variable (*var1*, *items*) reaches 5.

The rules in an IOGG which create new nodes or edges and have constraints on data should either:

- erase the same amount of nodes and edges as it creates
- have a constraint on the created node or edge, e.g. the node to create is part of the NAC of the rule

The first constraint guarantees the exploration halts. The second constraint is only a guarantee if the node is the only element in the NAC, otherwise it is possible that the NAC does not match the graph even with the node in it.

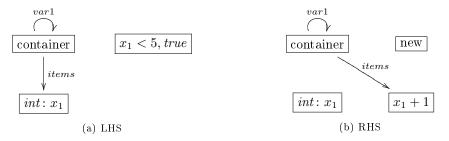


Figure 3.7: Node creating rule with data constraint

# Chapter 4

# Implementation

This chapter covers the general implementation of GRATiS. GROOVE and ATM, explained in section 2.5, are used for most of the functionality. Therefore, first a general overview of the workings of GRATiS and how GROOVE and ATM fit in the picture is explained in section 4.1. The added functionality is then explained in more detail in section ??.

## 4.1 General setup

Figure 4.1 shows a UML sequence diagram of GRATIS, depicting a general test run. This figure shows a combination of the UML sequence diagrams of GROOVE in Figure 2.11 and ATM in Figure 2.10. The interactions between GROOVE components and between ATM components as described in those figures is omitted where possible. The 'RemoteExploration' component replaces the 'ExplorationStrategy' in Figure 2.11 and the 'ATMInterface' component is added. These are briefly included in the step-by-step explanation and explained in more detail later.

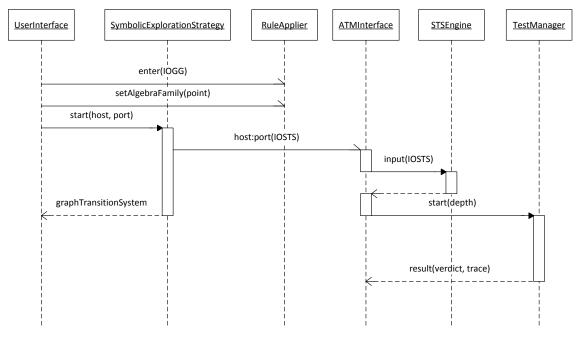


Figure 4.1: GRATiS sequence diagram

- 1. The user enters an IOGG in the RuleApplier of the GROOVE tool. The input/output rules are defined by prefixing the given rule names with '?' and '!'.
- 2. In the settings menu of GROOVE, the user sets the algebra family of the IOGG to to the point algebra, which is used by the RuleApplier.
- 3. The user selects the Symbolic Exploration Strategy from the available strategies in GROOVE. This strategy gives input options to a host name and port number. The strategy is then started by the user. The communication between the Rule Applier and the strategy is omitted here, this is the same as in the GROOVE diagram. The result of the exploration is an IOGTS under the point algebra.
- 4. The RemoteExplorationStrategy creates an IOSTS in Java objects from this IOGTS with the method described in chapter 3. It then creates a message with the IOSTS and sends this message to the ATMInterface
- 5. The ATMInterface receives the message and gives the IOSTS to the STSEngine.
- 6. The ATMInterface starts the testing with the default 'depth' parameter; making this configurable is not implemented yet. The communication between the TestManager, STSEngine and Adapter is omitted here.
- 7. The TestManager returns the test results to the ATMInterface. The test results are stored in a database and are viewable by starting the user interface of ATM (ommitted here).

## 4.2 Description of added functionality

This section covers in detail the added functionality to GROOVE and ATM.

**GROOVE exploration strategy** Figure 4.2 shows the class diagram of the added exploration strategy interface. The RemoteExplorationStrategy extends a *SymbolicStrategy*. The Symbolic-ExplorationStrategy has a *closing* exploration strategy, which is a strategy that explores all graph states and rule transitions, such as the BreadthFirstStrategy.

The user starts the RemoteExplorationStrategy with a host and port, as described above. This strategy starts a ClosingStrategy. This strategy explores the IOGG and notifies the remote strategy when there are no more rule transitions to explore. The SymbolicStrategy implements the method described in chapter 3 to build the IOSTS in Java objects using the explored IOGTS from the ClosingStrategy. The class diagram of this IOSTS is given in next.

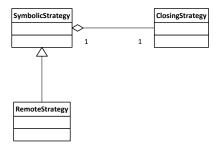


Figure 4.2: The class diagram of the exploration strategy interface

IOSTS in GROOVE Figure 4.3 shows the class diagram of the IOSTS in GRATIS. The IOSTS is composed of Location, SwitchRelation, Gate, Interaction- and LocationVariable classes. A Location object can be the start and target of any number of SwitchRelation objects. A SwitchRelation

object has two Location objects; the start and target location. It also has one Gate object, which can belong to any number of SwitchRelation objects. A Gate object can have any number of InteractionVariable objects, but an InteractionVariable object belongs to only one Gate object. The IOSTS class has one singleton object, the RuleInspector, which contains the functionality of building guards and updates from rule graphs, i.e. the  $\phi_{\gamma}$  and  $\phi_{\rho}$  functions defined in ?? and ?? respectively.

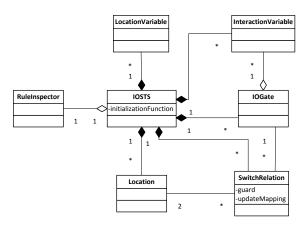


Figure 4.3: The class diagram of the IOSTS in GRATIS

Figure 4.4 shows the object relations in accordance with the class diagram for the IOSTS in Figure 2.4. Note that the links between the *BoardGame* object and the Location, SwitchRelation, IOGate and InteractionVariable classes are not drawn for the sake of clarity. Note that the created objects, inter-object relations and object parameters are in accordance with the method described in chapter 3. The IOSTS itself is the composite object, which also holds the initialization function. The RuleInspector is not part of the IOSTS, therefore the Boardgame object does not show the relation with this object.

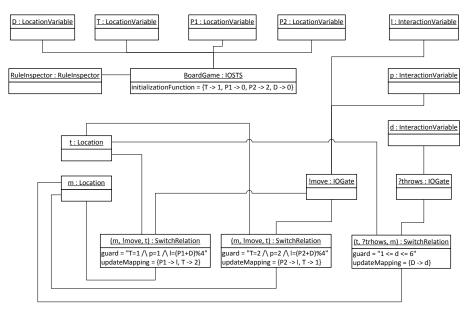


Figure 4.4: The object diagram of the IOSTS in Figure 2.4

**GROOVE-ATM Interface** The RemoteExplorationStrategy sends a HTTP POST request with the IOSTS in JSON format to the interface of ATM. The ATM interface is one component

in the Ruby on Rails framework. The interface is a controller in this Model-View-Controller framework. Controllers handle the HTTP requests given by the framework. The interface receives the IOSTS POST request, builds the IOSTS as Ruby objects and initiates the test using this IOSTS as model.

### Chapter 5

### Validation

This chapter covers the validation of GRATiS. The validation is done through examples and a case-study. Possible measurements on models and the performance are investigated in section 5.1. The examples, case-study and models are given in section 5.2.

### 5.1 Measurements

This section describes possible measurements on the execution of GRATiS and comparisons between IOSTSs and IOGGs. This is done to compare the effectiveness of both formalisms in MBT. The comparisons between the models are set out in the next sections, which are:

- 1. Simulation and redundancy
- 2. Model complexity
- 3. Extendability

The measurements on the performance of GRATiS follow.

### 5.1.1 Simulation and redundancy

The generated IOSTS and the modelled IOSTS can be compared. It can be observed whether the generated IOSTS simulates the modelled IOSTS and vice versa. When either is not the case, the models show a different possible behavior for the SUT.

Simulation between two STSs can be done by creating the LTSs from the STSs first. LTSMin <sup>1</sup> is a tool which can check the (bi)simulation on LTSs. However, creating the LTSs from STSs becomes difficult on large models. Therefore, another solution is chosen.

ATM can be used to find diffrences between two IOSTSs, by using one as the model and the other as the SUT. The SUT tries to copy the stimuli done by the model and the model tries to copy responses done by the SUT. ATM can then find differences in behavior between both IOSTSs. This technique is used to find non-conformance between the generated and modelled IOSTSs. This is done by letting the test run reach 100% switch relation coverage on both models. For purposes of the next measurement, we assume then that a bisimulation exists between both models.

**Definition 5.1.1.** Model redundancy

It is possible that a generated IOSTS s is larger than a modelled IOSTS t, even if both simulate

<sup>&</sup>lt;sup>1</sup>http://fmt.cs.utwente.nl/tools/ltsmin/

each other. If t simulates s, it is measured whether the set of switch relations or location variables is strictly smaller in t than in s, while the other set is at least as small in t as in s. Formally:

$$traces(s) \subseteq traces(t) \land ((|D_t| < |D_s| \land |\mathcal{L}_t| \le |\mathcal{L}_s|) \lor (|D_t| \le |D_s| \land |\mathcal{L}_t| < |\mathcal{L}_s|)$$

This indicates the the IOSTS s has redundancy.

### 5.1.2 Model complexity

A good way of testing the complexity of the IOSTS and the IOGG is to hold an extensive social experiment, where groups create and maintain models in either formalism. However, this is out of the scope for this report. More is written about this social experiment in the Future Work section 6.2.

Instead of a social experiment, we investigated software complexity measurements in the literature and tested their applicability for IOGGs and IOSTSs. The investigated complexity measurements are:

- 1. Halstead's software science
- 2. Cyclomatic complexity
- 3. System complexity

Halstead's software science The complexity of the generated IOSTS and the IOGG can be measured using Halstead's software science [7]. This method is used in measuring software complexity and the prediction of faults. However, it can also be used in analyzing model complexity. In Halstead's software science, the operators and operands in the program code are counted. The operators are the function symbols, the operands are the identifiers. However, in order to apply these concepts to our setting, we have to identify what we consider to be operators and operands.

IOSTSs and IOGGs both have identifiers and function symbols. However, they also have nodes and edges. In an IOSTS, the locations are counted as nodes, the switch relations as edges. Nodes and edges are considered to be operands. In GROOVE, colors indicate a restriction or node/edge removal/creation. The node and edge colors are therefore considered as operators.

The distinct number of operators  $(n_1)$  and operands  $(n_2)$  are counted as well as the total number of operator occurrences  $(N_1)$  and operand occurrences  $(N_2)$ . These metrics combined lead to the Volume (V) of the models.

**Definition 5.1.2.** Halstead's Volume (V) function 
$$(N_1 + N_2) * log_2(n_1 + n_2)$$

In Halstead's software science, the volume of a program and a constant for the number of faults per volume unit are combined to give the expected faults in a program. Therefore, comparing the volumes of the IOSTS and IOGG gives an indication of the relative model complexity.

Cyclomatic Complexity COMMENT Ik heb intensief emails gewisseld met Lodewijk Bergmans over de toepassing van cyclomatic complexity, maar dit lijkt niet geschikt hier. Ik zal het wel behandelen /COMMENT

System Complexity COMMENT mooie, simple metric voor OO. Niet toepasbaar hier, want onmogelijk om modules te definieren /COMMENT

### 5.1.3 Extendability

The models can be extended to include more functionality. In this measurement, a realistic scenario is introduced where additional functionality is required. It is then measured how much the complexity increases, using the measurement in section 5.1.3.

#### 5.1.4 Performance

The performance on runtime and heap-size on the IOSTS generated by GRATiS is measured. After the IOSTS is generated we assume the run-time and heap-size for the testing part are the same for both the generated IOSTS and the modelled IOSTS. Therefore, only the runtime and heap size of the IOSTS generation are measured. When dividing the results for each model by the corresponding volume of the model, a relative measurement is obtained which can be compared, to see how the algorithm scales.

### 5.2 Models

This section shows the IOGG and IOSTS for each model example and the case study. There are four examples; the last one shows the example can only modelled by violating the constraints in section 3.4.

### 5.2.1 Example 1: boardgame

The boardgame is the running example of which the IOSTS and IOGG are given in Figures 2.4 and 2.20 respectively. In order to be consistent with the GG variable definition, the two *Player* and *Die* nodes receive the flags var1, var2, var3 respectively, representing the variable labels.

### 5.2.2 Example 2: farmer-wolf-goat-cabbage

In this puzzle, a farmer, wolf, goat and cabbage are on one side of a river. The farmer can take upto one item to the other side. If the wolf and goat are on one side of the river without the farmer, the wolf eats the goat and the puzzle is reset. This also holds for the goat and the cabbage. The goal is to move all four to the other side of the river. The stimuli accepted by the puzzle are:

- ?n Move the farmer to the other river bank
- ?w Move the wolf to the other river bank
- ?g Move the goat to the other river bank
- ?c Move the cabbage to the other river bank

The responses given by the puzzle are:

- !retry When ?w,?g or ?c is given but the farmer is not on the same river bank as the item
- !eaten An item eats another item on one river bank, with the farmer on the other river bank
- !done When all four items are on the other river bank

The IOGG of this puzzle is in Figures A.1 and A.2. The response rules '!retry', '!eaten' and '!done' have a higher priority. This ensures that a proper response is given after a move, before allowing more stimuli.

The IOSTS of this puzzle is given in the formal definition in Figure A.4. It uses boolean location variables to indicate whether the item is on the other side. These are ?N, W, G, C for the farmer, wolf, goat and cabbage respectively. These are checked to see if an invalid move is done, an item is being eaten or the puzzle has been completed.

### 5.2.3 Example 3: bar tab system

This example models a bar tab system, where customers can order beer, wine and coke, costing \$1.50, \$2.10 and \$0.80 respectively. The price of the order adds to the customer's tab. Customers can pay their tab with money; they receive cash back if the payment exceeds the tab. The models are abstracted to include three customers. Furthermore, a customer can order only one drink. Drinks and payments are processed immediately before other drinks or payments can occur. The stimuli accepted by the system are:

- ?o(i,d) for ordering a drink d on bar tab i
- ?p(i, p) for paying amount p on bar tab i

The responses given by the system are:

- !po(b) for processing an order giving the new bar tab balance b
- !pp(b,r) for processing a payment giving the new account balance b and the return funds r

The IOGG of the bar tab system is in Figure B.1. The '!po' and '!pp' rules have a higher priority than the '?o' and '?p' rules, to ensure an order is processed before a new one is made.

The formal definition for the IOSTS of the bar tab system is given in Figure B.3. The IOSTS uses the variables  $T_1, T_2, T_3$  to keep track of the bar tabs of the three people. It uses the variables I, P as temporary variables for the id and payment/price respectively. The function max takes the maximum value of its parameters.

### 5.2.4 Example 4: restaurant reservations

In this example, a restaurant with three tables allow customers to reserve tables for a certain time slot, given by a start and end time. The reserved time should be at least an hour. The models abstract again from the number of customers, setting it to two. The time span in which reservations can be made is a week. The maximum number of reservations is therefore bounded to 7\*24=168.

Figure 5.1a shows the initial graph of three tables at a restaurant and two potential customers. Figure 5.1b shows part of a rule that allows people to make reservations. The start and end times are timestamps represented by integers. This rule allows people to make multiple reservations. However, The reservations cannot be GG variables or this rule violates the unique GG variables constraint in section 3.4, because it has to assign a variable label to the *Reservation* node.

Variables can be one of four sorts, as described in section 2.2. Allowing a dynamic amount of reservations per person means that variables need to be introduced dynamically as well or variables with more complex sorts have to be used, such as arrays. This also holds for the IOSTS of this system. This example is to show the limitations on data and the abstractions that both models are required to make. It is included in the measurements wherever possible.

### 5.2.5 Case study: Scanflow Cash Register Protocol

The system used for this case study is a *self-scan register*, which allows customers of a supermarket to scan and pay for their products without help of an employee. Figure 5.2 shows this self-scan

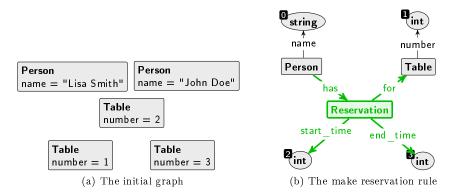


Figure 5.1: Part of the IOGG for the restaurant reservation system

register. The system contains a scanflow unit, which scans the products, and a cash register, which handles the payment. The communication protocol between the register and the scanflow unit is the system which is tested. The register is the SUT, the scanflow unit gives stimuli to and receives responses from the register. The code of the register is available in a simulator, which is used for the actual testing.



Figure 5.2: A self-scan register

Axini has provided an IOSTS and an Adapter component for this case study. These are used for the testing and measurements.

**Stimuli and responses** Appendix C gives the most relevant parts of the specification document for this communication protocol. From this document, the following stimuli were designed:

?SIGNON(id, password)	Requests the register to sign on with the login and password given by id and password
2CICNOEE	•
?SIGNOFF	Requests the register to sign off
?OPEN(account)	Opens the account given by <i>account</i> or a new account if <i>account</i> is not set
?ARTREG(barcode)	Requests registration of an article, with <i>barcode</i> representing its
:All In EG (varcoue)	key
?STAMPREG	Requests registration of loyalty points
?ARTID(barcode)	Requests identification of an article, with $barcode$ representing its key
?ARTRET(barcode)	Returns an article where barcode is the article being returned
?CLOSE	Closes the account
?ENDTOT	Requests the end total of the registered articles
$?TRANS(trans\_id)$	Inform the register that the payment was made, where $tr\_method$ represents the payment method, e.g. cash, credit card
?RECEIPT	Requests the register return the receipt.
?PRINT(account)	Requests the register to print additional information on the receipt for $account$
?IDLE	Requests rounding-up of the account
?RESUME	Requests the register to continue operation from an error state
?RHCOPY(account)	Requests the register to print a hardcopy of a receipt for account
?RESETCR	Requests the register to execute a reset
$?GET(var\_name)$	Requests to get the value of a certain register variable represented by $var\_name$

The SCRP responses follow a coding scheme, much like the definition for FTP. The responses are a 3-digit status code, where each digit has a special significance. The first digit denotes the essence of the related action:

- 2yz Ok Command has been accepted and the action is successfully completed. A new command may be issued.
- 4yz Again Command was not a accepted as a result of a temporary error condition. It is encouraged to request the same action again.
- 5yz Fail Command was not accepted as a result of a permanent error condition. It is discouraged to request the same action again.

The following function categories are encoded in the second digit:

- $\bullet$  x0z Syntax Command contained a syntax error (50z), or default indication if no other function category applies (10z, 20z, 30z, 40z)
- x1z Information Response related to access of information.
- $\bullet~$  x2z Connection Response related to connection/service.
- x3z Account Response related to account management.
- $\bullet\,$  x4z Transaction Response related to (payment) transaction.
- x5z Signing Response related to sign on/off operations.
- x6z Printing Response related to receipt printing.

The third digit gives a finer gradation in each of the function categories, which leads to the complete list of responses:

1202   Cash   1210(cr_variable, cr_value)   Gives   1212(description, price)   Gives   1213(description, price)   Gives   1220   SCRI   1220   SCRI   1221   SCRI   1230(endtotal)   Gives   1232   Article   1233   According   1240   Trans   1250   Signe   1251   Signe   1251   Signe   1260   Data   1261(html_text)   Gives   1450   Signi   1500   Unkn   1501   Synta   1502   Commulation   1503   Error   1503   Error   1510   No su   1511   No su   1512   No st   1512   No st   1531   Invali   1540   No su   1541   Busy   1542   Trans   1550   Not st   1542   Trans   1550   Not st   1	d On printed sthe receipt as HTML ng rejected own command ax error mand failed state nch variable nch article able weight nch account ad account state nch transaction method transacting saction failed igned on
	_
!550 Not s	igned on
!551 Author	entication failed
	rinting inactive
<u> </u>	printing inactive
:901 2t O-	printing mactive

**Database testing** The available barcodes of articles are stored in a database. There are no stimuli to manipulate this database, nor is it feasible to let the model perform SQL statements to obtain barcodes. However, the model should know if an existing or non-existing barcode is given. The Adapter component is given access to the database and the stimuli with barcode as internaction variable are replaced by:

```
?ARTID_EXISTRequests identification of an existing article?ARTRET_EXISTRequests identification of a non-existing article?ARTRET_NEXISTReturns an existing article?ARTREG_EXISTRequests the registration of an existing article?ARTREG_NEXISTRequests the registration of a non-existing article?ARTREG_REFUNDRequests registration of a special type of article, the refund?ARTREG_LOYALTYRequest registeration of a special type of aricle, the loyalty points
```

A similar abstraction is made for the *account* interaction variable:

$?OPEN\_EXIST$	Opens an existing account
$?OPEN\_NEXIST$	Opens a non-existing account
$?PRINT\_EXIST$	Requests the register to print additional information on the receipt for an existing account
$?PRINT\_NEXIST$	Requests the register to print additional information on the receipt for a non-existing account
?RHCOPY EXIST	Requests the register to print the receipt for an existing account
?RHCOPY_NEXIST	Requests the register to print additional information on the receipt for
	a non-existing account

And also for the login and password for the signing on:

```
?SIGNON_EXIST Sign on with a correct login/password ?SIGNON NEXIST Sign on with an incorrect login/password
```

IOGG Some selected rules of the IOGG of this communication protocol are shown in Figure 5.3. In total the IOGG has 94 rules. They are all listed in Appendix D. Figure 5.3a shows the initial graph. The CR node is the cash register, the SFU is the scanflow unit. The first node has the flag  $SS\_OFF$  representing that the register is off. There is one account which can be in states idle, open, closed and transing. When the customer places items on the belt, a new account is opened. Figure 5.3b shows the general request structure. As long as there is no request, a request can be sent. This rule requests the opening of an account. Figure 5.3c shows the rule for giving a success response. The request node is deleted such that new request nodes can be created again. The rule checks if an account is not already opened and opens an idle account. Figure 5.3d shows the rule for the error message received when an account is already opened.

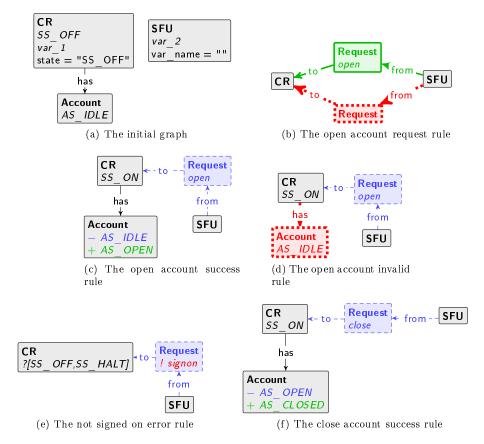


Figure 5.3: A few selected rules from the IOGG of the Scanflow Cash Register Protocol

For all these rules, the CR node has to have the flag  $SS\_ON$  representing the register to be signed on. Figure 5.3e shows the response to a request when the register is not signed on. Apart from the signon request, no other request is allowed in this state. Figure 5.3f shows the rule closing the account.

**IOSTS** The IOSTS of the system as created by Axini is shown in a seperate document. It has 907 locations, 1302 switch relations and 2 location variables.

### 5.3 Measurements on examples

### 5.3.1 Simulation and redundancy

Table ?? shows the results for this measurement. It contains all examples in the 'Example' column and 'Model' contains 'Generated' and 'Modelled' to indicate which IOSTS counterpart of the example the measurements are for. The 'Simulates?' column contains 'Yes' if the model simulates its counterpart in the same example or 'No' otherwise. 'Switch relations' and 'Location variables' give the number of these for each model. Using this information for both counterparts, the model is declared redundant or not in 'Redundant', as described in definition ??. The results are discussed in the next paragraphs, followed by the conclusions for this measurement

Example	Model	Simulates?	Switch relations	Location variables	Redundant?
Boardgame	Generated	No	??	??	-
	Modelled	No	??	??	-
FWGC	Generated	Yes	50	0	No
	Modelled	Yes	11	4	No
Bar tab	Generated IOSTS	${ m true}$	24	13	true
	Modelled IOSTS	${ m true}$	10	5	false
Reservation	Generated IOSTS	-	-	-	-
	Modelled IOSTS	-	-	-	-
SCRP	Generated IOSTS	??	540	2	??
	Modelled IOSTS	??	1302	2	??

Table 5.1: Simulation and redundancy results

**Boardgame** The responses used by the IOSTS and by the IOGG are different. Both models, used as examples to clarify the IOSTS and IOGG formalisms, were built with a different behavior in mind. Both allow a die to be thrown, after which the IOSTS directly moves the player to the correct location and passes the turn and the IOGG moves the player by a series of responses ended with a !nextTurn. Therefore, both IOSTSs do not simulate each other.

**Farmer-wolf-goat-cabbage puzzle** The IOGG does not use variables to track the location of each item. Therefore, the generated IOSTS has a location per state of the puzzle. Since on neither side both the number of switch relations and location variables are higher, both models are not redundant.

**Bar-tab system** The modelled IOSTS keeps the name and price of drinks as location variables, whereas the generated IOSTS hard-codes these into the guards and updates. The generated IOSTS builds a switch relation with gate ?o for each combination of customer and drink. It also builds a switch relation with gate ?p for each customer. The target locations of all these switch relations

have one switch relation back to the initial location. Therefore, the number of switch relations is 3\*3\*2+3\*1\*2=24. This could have been avoided by modelling GG variables for the price and drinks. However, this would make the IOGG more complex.

#### **SCRP**

Conclusions The farmer-wolf-goat-cabbage puzzle shows that IOGGs can often be better expressed using no variables. The bar-tab system shows that the generated IOSTS can be redundant compared to the IOSTS created by hand.

conclusies
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### 5.3.2 Model complexity

Table 5.5 shows the measurements on the operators and operands of all models. The differences in complexity differ between the models. However, the  $n_2$  and  $N_1$  column jump out: the distinct number of operands is much higher for the IOGG models, but the total number of operators  $N_1$  is much higher in the IOSTS models. This is based on the last three models, which express the same behavior.

Example	Model	$n_1$	$n_2$	$N_1$	$N_2$	Volume
Boardgame	IOGG	7	12	20	90	467.27
	IOSTS	6	9	14	27	160.18
FWGC	IOGG	3	12	31	190	863.42
	IOSTS	6	8	103	130	887.11
Bar tab	IOGG	9	31	40	188	1213.40
	IOSTS	8	15	66	134	904.7
Reservations	IOGG	??	??	??	??	??
	IOSTS	-	-	-	-	-
SCRP	IOGG	3	69	207	1506	10569.10
	IOSTS	3	6	730	2594	10536.83

Table 5.2: The Halstead measurements on the models

### 5.3.3 Extendability

The next paragraphs contain a hypothetical extension to each example. New models are given which feature the extension. In the last paragraph, the increase in model complexity for each example is given in a table. The restaurant reservation system is omitted from this measurement, as is SCRP.

**Boardgame** The boardgame is extended to include one more player and one more location. For the IOGG, this means adding new locations and players to the initial graph. The players get a fixed order in which they play. This means that the next turn rule also has to be extended. The rest of the rules stay as they are. The extended rules are in Figure 5.4.

The IOSTS gains a variable and a switch relation for the new player:

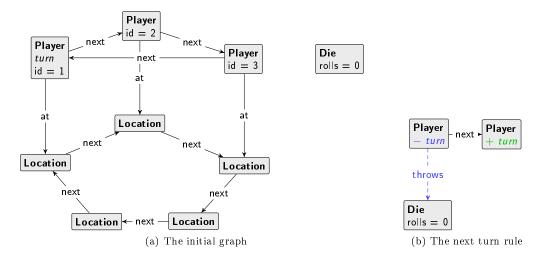


Figure 5.4: The extended IOGG of the board game example in Figure 2.20

```
\begin{array}{lll} W & = & \{t,m\} \\ w_0 & = & t \\ \mathcal{L} & = & \{T,P1,P2,P3,D\} \\ \imath & = & \{T\mapsto 0,P1\mapsto 0,P2\mapsto 2,P3\mapsto 0,D\mapsto 0\} \\ \mathcal{I} & = & \{d,p,l\} \\ \Lambda & = & \{?throw,!move\} \\ D & = & \{t & \frac{?throw,1<=d<=6,D\mapsto d}{m} & m, \\ & & \frac{!move,T=1\land l=(P1+D)\%5,P1\mapsto l,T\mapsto 2}{m} & t, \\ & & & \frac{!move,T=2\land l=(P2+D)\%5,P2\mapsto l,T\mapsto 3}{m} & t, \\ & & & & \frac{!move,T=3\land l=(P3+D)\%5,P3\mapsto l,T\mapsto 1}{m} & t \} \end{array}
```

**FWGC** In another variant of this puzzle, when one of the items is eaten, the puzzle can reset, but it can also undo the last action. The !eaten rule can have either effect. In Figure A.3 shows this extension for the IOGG in five rules. The rules keep track of the last moved items. When an item gets eaten, the last move can be undone.

The IOSTS in Figure A.5 keeps extra variables for the previous positions of the items and adds one switch relation that restores the items to their previous positions when an item gets eaten.

**Bar tab system** The system is extended to allow ordering multiple drinks of different types. Also, a customer can purchase the option of receiving 10% discount on all ordered drinks for 50 euros, which is added to the tab of the customer.

- $?o(i, d_1, q_1, d_2, q_2, d_3, q_3)$  is used to order a quantity  $q_n$  of drink  $d_n$  on bar tab i.
- ?d(i) is used to order the discount on bar tab i.
- !pd(b) process the discount where b is the new balance.

Figure B.2 shows the extended rules and initial graph. The ?p and !pp rules have remained the same. The bar tabs track their discount. When processing an order, the discount is applied to the total price.

The IOSTS in Figure B.4 gains three location variables to track the discount for each tab. An order discount and process discount switch relations are added. Like with the IOGG, the discount

is applied to the total price of the ordered drinks.

**SCRP** An extended version for the IOSTS of SCRP by Axini is not available as there is no extended version of the SUT. Creating an extended IOSTS for SCRP and a corresponding SUT is out of scope for this report. Therefore the extension measurement is not done on the models for SCRP.

Model complexity increase Table 5.6 shows the measurements on the operators and operands of all extended models and the increase in model complexity. The differences in complexity differ between the models. The volume increase does not show one trend; it is much higher for the IOSTS in the farmer-wolf-goat-cabbage puzzle and much higher for the IOGG in the bar tab system.

Example	Model	$n_1$	$n_2$	$N_1$	$N_2$	Volume	Volume increase
boardgame	IOGG	6	12	20	105	521.24	53.97
	IOSTS	6	10	24	39	252.0	91.82
farmer-wolf-goat-cabbage puzzle	IOGG	4	12	38	217	1020.00	156.58
	IOSTS	6	12	146	247	1638.78	751.67
bar-tab system	IOGG	9	36	65	290	1949.61	736.21
	IOSTS	8	23	88	156	1208.82	304.12
Reservations	IOGG	??	??	??	??	??	
	IOSTS	-	-	-	-	-	

Table 5.3: The Halstead measurements on the extended models

#### 5.3.4 Performance

The performance of GRATiS on all models is in Table 5.4.

Example	runtime (ms)	heap-size (MB)	$\mathbf{m}\mathbf{s}/\mathbf{V}$	${f MB/V}$
boardgame	300	1.9	??	??
farmer-wolf-goat-cabbage puzzle	770	5.2	??	??
bar-tab system	250	2.1	??	??
SCRP	9530	6.6	??	??

Table 5.4: Performance measurements

Comparing to the examples the case-study shows little increase in heap-size and approximately 20 times higher runtime. The algorithm scales reasonably well, considering the generated IOSTS is approximately 10 times larger in size than those of the examples.

### Chapter 6

### Conclusion

### 6.1 Research goals

This report shows the usability of Graph Grammars in model-based testing. The motivation to use GGs is supported by literature, emphasizing the understandibility of graphs and the usefulness of graphs to express system states. Symbolic Transition Systems are a useful formalism which are easily used by computers. This supports using a GG for testers to model a software system and generating the IOSTS from the IOGG for the computer to use during testing. The point algebra was shown to be useful for achieving the generation of an IOSTS. The design requirements for GRATiS are all met, because:

- the technique proved effective for model-based testing in several example cases and a larger case study
- coverage can be measured on the generated IOSTS
- the performance measurements show that the IOSTS can be generated from large models in a negligible time and that the technique scales well

### 6.2 Contributions

Generating the location variables in an STS meant creating an extra definition for GGs, which allowed persistent variables. The definition lets edges to data values to be considered as variables; this was a choice needed to generate the IOSTS. GGs can dynamically add these variables or delete them; something which was frequently desired to obtain the smallest and most intuitive models, but which complicates the generation of the IOSTS. Hence, constraints on GG transformation rules were defined mostly to accomdate the GG variable definition.

One of the example cases, the reservation system, suffered from the constraints the most. This example could not be modelled, because dynamically deleting and creating GG variables was required. The puzzle example on the other hand shows the strength of GGs the most, through simple, intuitive rules opposed to a complicated transition system. This shows that some systems are more suitable to be modelled in GGs than others.

The case study done in this report on the self-scan register shows a real life example of a software system, succefully modelled as an IOGG. Here, the strength of behavioral rules is apparent: instead of state-transition thinking, the graph transformation rules allow each behavioral aspect of a software system to be modelled by one rule. For example, the 'not signed on' error, given when

the register is in the 'not signed on' state. This error can be given in numerous states in the IOSTS, but simply described in the IOGG by matching the state of the register. Additional restrictions of where this rule applies can be easily added to the rule. In state-transition based models, high many states and transitions are often needed to model the same behavior described by one GG rule. This shows that IOGGs are very useful when it comes to changing requirements: only few rules need to be adjusted to accommodate these changes.

Model complexity measurements were done on the IOGGs and IOSTSs of the example cases and case study. This did not reveal a clear difference in overall model complexity. However, it did show that IOGGs generally have more distinct operands, but less overall operators. The first part is due to the labels on nodes and edges, which describe the nature of the nodes and the relation between the nodes; these operands are not present in the IOSTSs. The second part can be explained by the repetition needed in IOSTSs to describe the same behavior as one IOGG rule.

### 6.3 Future work

Better measurements to evaluate model complexity, such as sociological experiments, can be used to improve the usefulness of GGs in model-based testing. For instance, these measurements can be used to improve tools such as GROOVE, by making the GGs easier to create and understand.

When STSs are extended to allow more complex data structures, such as sets, maps and arrays, the definition of GG variables can also be extended. This should allow testers to viably model IOGGs for more software systems. Alternatively, other strengths of GGs can be explored, such as combining the consecutive application of the same rule into one, as was shown in the boardgame example.

More case studies on real-life software systems should be done, in order to establish and improve the usefulness of GRATiS to the model-based testing paradigm.

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# List of Symbols

d	A switch relation	
f	A function symbol	
l	A label	
$l_v$	A value label	
$l_a$	A variable label	
m	A graph transformation rule match on a graph	
$q_0$	An initial state	
r	A graph transformation rule	
s	A sort	
t	A transition	
u	A rule transition	17
v	A variable	10
$w_0$	An initial location	12
ι	An I/O type	9
$z_a$	A variable anchor	26
D	Set of switch relations	12
F	Set of function symbols	10
G	A graph	14
$G_0$	An initial graph	17
H	A rule graph	15
L	Set of labels	. 8
L	Set of input-output labels	17
M	Set of graph transformation rule matches	16
Q	Set of states	
$\dot{R}$	Set of graph transformation rules	16
$R_{Y}$	Set of input-output graph transformation rules	
$S^{1}$	Set of sorts	
T	Set of transitions	. 8
$T_Y$	Set of I/O transitions	9
$\dot{W}$	Set of locations	
U	Set of rule transitions	
$U_Y$	Set of input-output rule transitions	
$Y^{'}$	Set of I/O types	
$\mathbb{U}$	A universe	
$\mathbb{V}$	The universe of graph nodes	14
$\mathbb{E}$	The universe of graph edges	
W	The universe of standard graph nodes	
i	Term mapping for location variable initialization	
$\mathcal{A}$	An algebra	
$\mathcal{B}$	Set of terms with boolean type	
$\mathcal{G}$	Set of graphs	

${\mathcal I}$	Set of interaction variables	. 12
$\mathcal L$	Set of location variables	
${\mathcal P}$	A point algebra	. 10
$\mathcal T$	Set of terms	.10
$\mathcal{V}$	Set of variables	. 10
$\gamma$	Guard of a switch relation	. 12
$\phi$	A function	. 10
$\lambda$	A gate of a switch relation	. 12
$\mu$	Term-mapping function	. 11
$\nu$	Valuation function	. 11
$\rho$	Update mapping of a switch relation	. 12
Φ	Set of functions	. 10
Λ	Set of gates	. 12
$\Lambda_V$	Set of I/O gates	.12

## Appendix A

## Farmer-Wolf-Goat-Cabbage Models

This appendix contains IOGGs and IOSTSs for the Farmer-Wolf-Goat-Cabbage puzzle. This puzzle is explained in section ??. The IOGG for the puzzle is in Figures A.1 and A.2, the extended IOGG for the puzzle is in Figure A.3, the IOSTS for the puzzle is in Figure A.4 and the extended IOSTS is in Figure A.5.

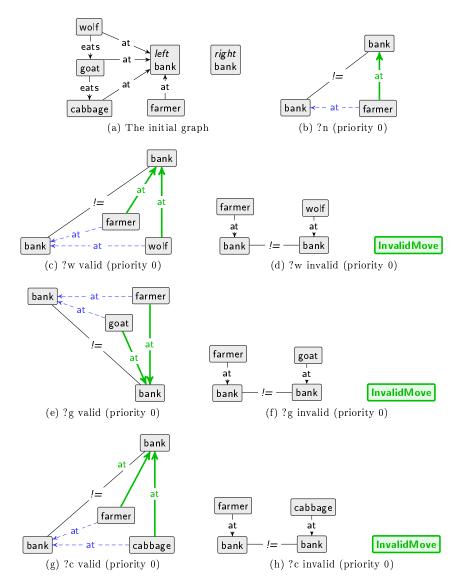


Figure A.1: The IOGG of the farmer-wolf-goat-cabbage puzzle

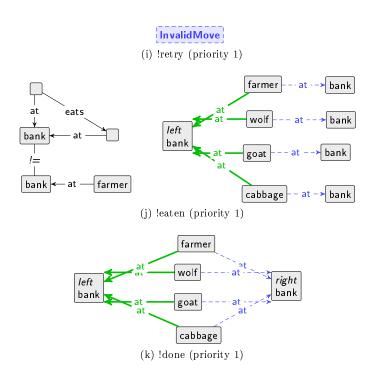


Figure A.2: The IOGG of the farmer-wolf-goat-cabbage puzzle (continued)

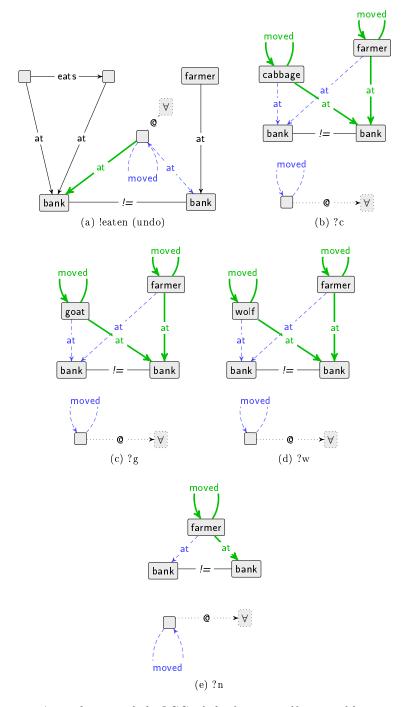


Figure A.3: The extended IOGG of the farmer-wolf-goat-cabbage puzzle

```
W
                 \{l_0, l_1\}
                 l_0
                  \{N, W, G, C\}
                  \{N \mapsto false, W \mapsto false, G \mapsto false, C \mapsto false\}
\mathcal{I}
Λ
                  \{?n,?w,?g,?c,!eaten,!done,!retry\}
                          ?n, \neg (N \neq G \land G = C) \lor (N \neq W \land W = G), \{N \mapsto \neg N\} \atop \longrightarrow l_0,
D
                 l_0
                 l_0
                 l_0
                       \xrightarrow{!retry,true,\{\}} l_0,
                 l_1
                        \underbrace{!eaten, (N \neq G \land G = C) \lor (N \neq W \land W = G), \{N \mapsto false, W \mapsto false, G \mapsto false, C \mapsto false\}}_{l_0, } \\ l_0, 
                 l_0
                        \underbrace{!done, N \land W \land G \land C, \{N \mapsto false, W \mapsto false, G \mapsto false, C \mapsto false\}}_{!done} \} \ l_0 \}
```

Figure A.4: The IOSTS of the farmer-wolf-goat-cabbage puzzle

```
W
                 \{l_0, l_1\}
                  \{N, W, G, C, Np, Wp, Gp, Cp\}
                 \{N \mapsto false, W \mapsto false, G \mapsto false, C \mapsto false, Np \mapsto false, Wp \mapsto false, Gp \mapsto false, Cp \mapsto false\}
\mathcal{I}
Λ
                 \{?n,?w,?g,?c,!eaten,!done,!retry\}
                          ?n, \neg (N \neq G \land G = C) \lor (N \neq W \land W = G), \{N \mapsto \neg N, Np \mapsto N, Wp \mapsto W, Gp \mapsto G, Cp \mapsto C\} 
D
         =
                       \overbrace{?w,N=W \land (N=G \lor G \neq C) \land (N=W \lor W \neq G),\{W \mapsto \neg W,N \mapsto \neg N,Np \mapsto N,Wp \mapsto W,Gp \mapsto G,Cp \mapsto C\}} \atop \downarrow l_0,
                       ?g,N=G \land (N=G \lor G \neq C) \land (N=W \lor W \neq G), \{G \mapsto \neg G,N \mapsto \neg N,Np \mapsto N,Wp \mapsto W,Gp \mapsto G,Cp \mapsto C\} \rbrace l_0,
                 l_0
                       ?g,N \neq G \land (N = G \lor G \neq C) \land (N = W \lor W \neq G), \{G \mapsto \neg G, N \mapsto \neg N, Np \mapsto N, Wp \mapsto W, Gp \mapsto G, Cp \mapsto C\} \} \downarrow_{1},
                       \overbrace{?c,N\neq C\land (N=G\lor G\neq C)}\land (N=W\lor W\neq G),\{C\mapsto \neg C,N\mapsto \neg N,Np\mapsto N,Wp\mapsto W,Gp\mapsto G,Cp\mapsto C\}\} l_1,
                 l_0
                 l_1
                       \underbrace{!eaten,(N \neq G \land G = C) \lor (N \neq W \land W = G),\{N \mapsto false,W \mapsto false,G \mapsto false,C \mapsto false\}}_{l_0,} \downarrow l_0,
                       \stackrel{!eaten,(N \neq G \land G = C) \lor (N \neq W \land W = G),\{N \mapsto Np,W \mapsto Wp,G \mapsto Gp,C \mapsto Cp\}}{} l_0,
                       \underbrace{!done, N \land W \land G \land C, \{N \mapsto false, W \mapsto false, G \mapsto false, C \mapsto false\}}_{!done} \mid l_0 \}
```

Figure A.5: The extended IOSTS of the farmer-wolf-goat-cabbage puzzle

## Appendix B

## Bar Tab Models

This appendix contains IOGGs and IOSTSs for the bar tab system. This system is explained in section ??. The IOGG for the system is in Figure B.1, the extended IOGG for the puzzle is in Figure B.2, the IOSTS for the puzzle is in Figure B.3 and the extended IOSTS is in Figure B.4.

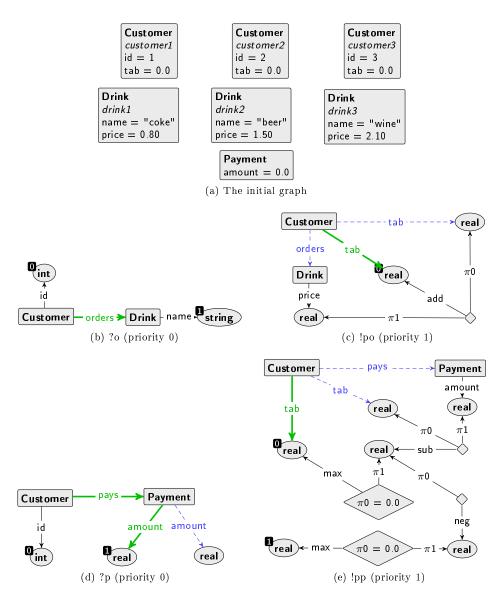


Figure B.1: The IOGG of the bar tab system

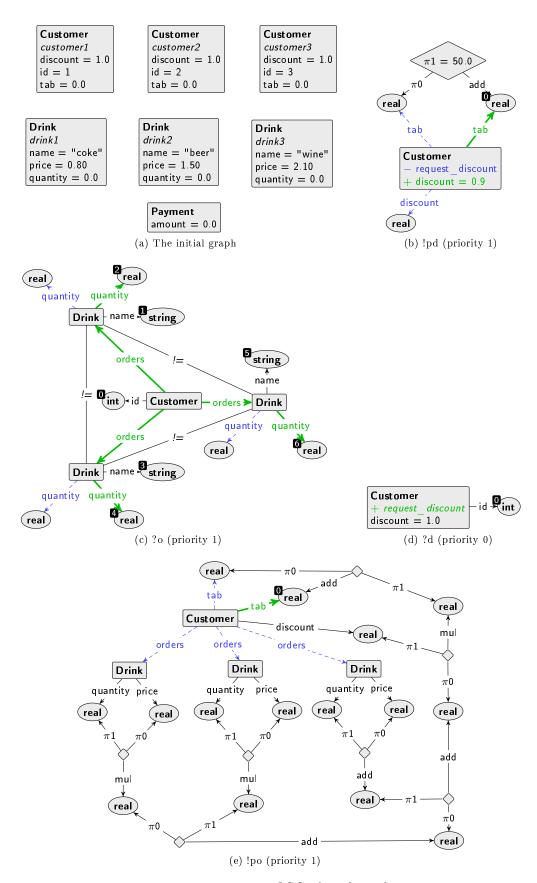


Figure B.2: The extended IOGG of the bar tab system

```
W
               \{l_0, l_1, l_2\}
         =
         = l_0
w_0
                \{I, P, T_1, T_2, T_3\}
                \{T_1 \mapsto 0, T_2 \mapsto 0, T_3 \mapsto 0\}
\mathcal{I}
                \{i,d,p,b,r\}
Λ
                 \{?o(i,d), ?p(i,p), !po(b), !pp(b,r)\}
                        D
                      ?o(i,d),d='beer' \land i \ge 1 \land i \le 3, \{I \mapsto i,P \mapsto 1.5\}} l_1,
                 l_0
                      \stackrel{!po(b),I=1 \land b=T_1+P,\{T_1 \mapsto b\}}{\longrightarrow} l_0,
                l_1
                      \xrightarrow{!po(b), I=2 \land b=T_2+P, \{T_2 \mapsto b\}} l_0,
                l_1
                      \xrightarrow{!po(b), I=3 \land b=T_3+P, \{T_3 \mapsto b\}} l_0,
                l_0
                      \stackrel{!pp(b,r)}{\underset{}{pp(b,r)}} = 1 \land b = max(T_1 - P, 0) \land r = max(-T_1 + P, 0), \{T_1 \mapsto b\} \longrightarrow l_0,
                      \stackrel{!pp(b,r)}{\longrightarrow}, I=2 \land b=max(T_2-P,0) \land r=max(-T_2+P,0), \{T_2 \mapsto b\} \longrightarrow l_0,
                      !pp(b,r),I=3 \land b=max(T_3-P,0) \land r=max(-T_3+P,0),\{T_2 \mapsto b\} \rbrace l_0 \rbrace
```

Figure B.3: The IOSTS of the bar tab system

```
W
                  \{l_0, l_1, l_2, l_3\}
                 l_0
w_0
                   \{I, P, T_1, T_2, T_3, D_1, D_2, D_3\}
\mathcal{L}
                   \{T_1 \mapsto 0, T_2 \mapsto 0, T_3 \mapsto 0, D_1 \mapsto 1.0, D_2 \mapsto 1.0, D_3 \mapsto 1.0\}
\mathcal{I}
                   \{i, d_1, d_2, d_3, q_1, q_2, q_3, p, b, r\}
Λ
                   \{?o(i,d), ?p(i,p), !po(b), !pp(b,r)\}
                           \underbrace{?o(i,d),d_1='coke'\land d_2='beer'\land d_3='wine'\land i\geq 1\land i\leq 3,\{I\mapsto i,P\mapsto 0.8*q_1+1.5*q_2+2.1*q_3\}}_{l_1} \downarrow_{l_1}
D
                        \stackrel{!po(b),I=1 \land b=T_1+P*D_1,\{T_1 \mapsto b\}}{\longrightarrow} l_0,
                   l_1
                        \xrightarrow{!po(b), I=2 \land b=T_2+P*D_2, \{T_2 \mapsto b\}} l_0,
                   l_1
                        \xrightarrow{!po(b),I=3\land b=T_3+P*D_3,\{T_3\mapsto b\}} l_0,
                   l_1
                        \underbrace{\stackrel{!pp(b,r),I=1 \wedge b=max(T_1-P,0) \wedge \widetilde{r}=max(-T_1+P,0),\{T_1 \mapsto b\}}_{l_0,}}_{l_0,} l_0,
                   l_2
                        \stackrel{!pp(b,r),I=2 \land b=max(T_2-P,0) \land r=max(-T_2+P,0),\{T_2 \mapsto b\}}{\longrightarrow} l_0,
                   l_2
                         \underbrace{!pp(b,r),I=3 \land b=max(T_3-P,0) \land r=max(-T_3+P,0),\{T_2 \mapsto b\}}_{} l_0, 
                   l_2
                   l_0
                         \stackrel{!pd(b),I=1 \land b=T_1+50.0,\{T_1 \mapsto b,D_1 \mapsto 0.9\}}{\longrightarrow} l_0, 
                         \xrightarrow{!pd(b), I=2 \land b=T_2+50.0, \{T_2 \mapsto b, D_2 \mapsto 0.9\}} l_0, 
                   l_3
                         \stackrel{!pd(b),I=3 \wedge b=T_3+50.0,\{T_3 \mapsto b,D_3 \mapsto 0.9\}}{\longrightarrow} l_0 \}
                   l_3
```

Figure B.4: The extended IOSTS of the bar tab system

### Appendix C

## SCRP Commands & Responses

This appendix gives an overview of the commands and responses in the Scanflow Cash Register Protocol. It consists of one of the chapters from the ITAB Scanflow specification document, refactored to be read as a stand-alone documentation.

### **Registration Accounts**

The SCRP protocol incorporates the concept of an account, maintained in the CR on behalf of the SFU, onto which articles can be registered. Registered articles form the basis for the amount for which the customer is charged. A registration account can be in state AS\_IDLE, AS\_OPEN, AS\_CLOSED, AS\_TRANSING or AS\_ENDING, see Figure C.1.

When the CR service is started, the account is typically initialized to AS\_IDLE. An OPEN command issued by the SFU opens the account for registration. Registration is only possible in this state. After registration is finished, the CLOSE command must be invoked. In the AS\_CLOSED state, a TRANS command initiates a (payment) transaction. This command must be re-issued until the transaction succeeds. A successful transaction causes the account to enter the AS\_ENDING. In this state, the IDLE command makes the account AS\_IDLE, i.e. available to be opened for the next session.

### General Responses

The following responses can, when appropriate, be generated as a response on any command.

500 Unknown command	In case the command is not recognized.
501 Syntax error	In case the command contains a syntax error (e.g. mandatory
	argument is missing).
502 Command failed	As a last resort, when no other appropriate response can be given.
503 Error state	In case the CR is in Error state and the requested command
	cannot be processed due to that.
504 Weighing not available	This response should be used in the case a Cash register has
	a scale configured, but no connection between the Cash register
	and the scale is established, the Cash register must go to an error
	state and send a 504 error (weighing not available).
550 Not signed on	If the CR requires to be signed on for the command involved.

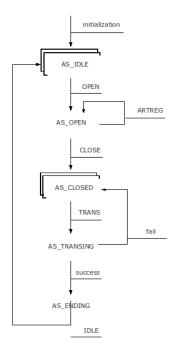


Figure C.1: Registration Account State Machine

### Commands

### Initialize SCRP Service

Command: None; a transport connection suffices.

Description: Initializes the SCRP service on the CR. The SFU must synchronize to the CR

after the connection has been established.

Responses: 220 SCRP Service ready

### Terminate SCRP Service

Command: QUIT

Description: Requests the CR to smoothly terminate the SCRP service. Although the SFU

should wait for all accounts to be AS\_IDLE before issuing this request, the CR must honour it in any state. Any non-IDLE account will be processed by the CR in an implementation defined manner. The CR remains ready to accept a (new)

SFU connection.

Responses: 221 SCRP Service terminating

### Cash Register Sign On

Command: SIGNON <SFU id>[:<password>]

Description: Requests the CR to sign on, making the actual signing state SS ON. The CR is

allowed to reject the request if the current signing state is SS HALT.

Responses: 251 Signed On

450 Signing rejected 551 Authentication failed

### Cash Register Sign Off

Command: SIGNOFF

Description: Requests the CR to sign off, making the actual signing state SS OFF or

SS\_HALT. The CR is allowed to reject the request if not all accounts are in AS\_IDLE state. Otherwise, any non-IDLE account will be processed by the CR

in an implementation defined manner.

Responses: 250 Signed Off

450 Signing rejected

#### Get CR Variable

 $Command: \quad GET < cr \quad variable >$ 

Description: Requests to get the value of a certain CR Variable. The CR must honour this

request in any state of the system. Possible variables and their values are listed

in Table 3.

Responses: 210 < cr variable > : < cr value >

510 No such variable

### Open Account

Command: OPEN [<account>|<barcode>]

Description: Opens an account for subsequent article registrations. The CR is requested to

including the state specific context.

Responses: 231 <account> Account opened

530 No such account 531 Invalid account state

### Close Current Account

Command: CLOSE

Description: Closes the current account for further registration. The CR is requested to per-

form this action before a transaction sequence is initiated. A positive response must include the total amount involved. The response may be preceded by a series of 'display responses', explaining the calculation from the previous subtotal

to the current endtotal (e.g. mix-match calculation results).

Responses: { 212 < description > [:< price > [:< amount > ]] }

230 <endtotal> Account closed

531 Invalid account state

### Request Article Identification

ARTID <br/>
<br/>
barcode> Command:

Description: Requests identification of an article, with <br/> barcode> representing its key. This

command is not a request to register the article. The CR must honor this request in any account state. A positive response must be given by means of a 211 response or a 213 response, their usage is alternative, which means that is up to the CR to use one or the other to respond to a given ARTID command. However systems using the certified weighing capability of the Cash Register must use the 213 response. Compared to the 211 response, the 213 response allows the CR to provide a full-scale specification of the attributes that characterize an article. A detailed definition of these responses including the error responses, is given hereunder. The length of the responses may never be larger than 512 characters.

Responses: 213

### Request Article Registration

Command: ARTREG [<br/>| sarcode>[:<amount>]]

Description: Requests registration of an article, with <br/> <br/> representing its key and

<amount> representing the amount of articles to register. This request is not issued before an account has been opened successfully. A positive response must consist of the following elements: <nr articles> Actual number of articles registered, <subtotal> Actual subtotal of articles registered. The response must be preceded by a series of 'display responses' with all data related to the registration of this article (e.g. linked articles, discounts, etc.). If <br/>barcode> is omitted, the command requests the complete list (as a series of 'display responses') of articles registered in the current account, which might be a recalled account. In case of a recalled account for which a partial payment was carried out on the originating (stored) account, the list of 'display responses' must include descriptive lines explaining the results of the partial payment(s) done; all in consistence with the

value and definition of subtotal. If <amount> is omitted, it will default to 1.

Responses: { 212 <description>[:<price>[:<amount>]] }

232 <nr articles>:<subtotal> Article registered

511 No such article 531 Invalid account state

### Request Account Transaction

Command: TRANS [: < amount > ]

Description: Requests transaction of the 'oldest' account from repository state AS CLOSED.

The account must be closed before the request can be honoured. For details regarding transaction methods. A negative response (failure) must include an indicator that specifies the cause of the failure. Table 8 lists an overview of possible failures for each transaction method. Both transaction method and failure indication must be represented as ASCII strings and interpreted in a case-insensitive manner. If <amount> is omitted, the actual endtotal is assumed implicitly. Otherwise, <amount> indicates the requested transaction amount. The format of the <amount> argument is identical to that of <price>. The semantics of <amount> in relation to transaction methods TM STORE and TM FLUSH is undefined; in case <amount> is specified for these transaction methods, the response must report Failure Indication FI AMOUNT (see table below). After a successful transaction, the remaining endtotal must be updated accordingly and in correspondence with the applicable exchange calculation rules that reside in the CR; this endtotal value is also returned in the (new) "240"-response. The resulting endtotal is by definition equal to 0 if the transaction was successful and the <amount> argument was omitted, even for TM\_STORE and TM\_FLUSH. Different from what is specified in the Account State Machine of Figure C.1 the account state remains AS CLOSED after a successful transaction while the resulting endtotal is unequal to 0. This allows for repeated/split TRANS requests.

Responses: 240 Transaction succeeded

531 Invalid account state

540 No such transaction method

541 Busy transacting

542 <failure ind> Transaction failed

### Print to Receipt (CR-Printing only)

 $Command: \quad PRINT < account > : < html\_text >$ 

Description: Requests the CR to print HTML-style data to the receipt of the specified account.

Responses: 260 Data printed

530 No such account531 Invalid account state560 CR-printing inactive

#### Query Receipt (SFU-Printing only)

Command: RECEIPT

Description: Queries the CR to generate a multiline response with the entire receipt of the

account currently in AS ENDING state.

Responses:  $\{ 261 < html_text > \}$ 

531 Invalid account state 561 SFU-printing inactive

#### Round-up Account

Command: **IDLE** 

Requests rounding-up of the account in AS ENDING state. A successful re-Description:

sponse makes the account state AS IDLE. In case of CR-printing, this command may cause he CR to activate the receipt cutter. With SFU-printing, this is the

acknowledge to the CR that the receipt has been correctly printed.

Responses: 233 Account idled

531 Invalid account state

### Resume Operation

Command:

Description: Requests the CR to continue operation from Error state. Once the CR is in Error

state, this command is needed to resume normal operation.

Responses: 201 Resumed operation

503 Error state

### Request Account EndTotal

Command: ENDTOT

Description: Requests to calculate the actual endtotal for the current account. The request

> is only valid in state AS OPEN. The response must be preceded by a series of 'display responses', explaining the difference between the current subtotal and the calculated endtotal. As such, the responses to this command are similar to those of the "CLOSE" command. In contrast with the "CLOSE" command,

"ENDTOT" must not affect the account state and may be issued repeatedly.

Responses: { 212 <description>[:<price>[:<amount>]] }

230 < endtotal > Account endtotal

531 Invalid account state

### Request print of Receipt Hardcopy

Command: RHCOPY [<account>|<barcode>]

Description: Requests the CR to print a hardcopy of a receipt. If <account> or <br/> <br/> <br/> code>

> is omitted, requests to print a hardcopy of the last printed receipt. This function is mandatory. A preferred implementation, however, must also support the arguments <account> or <barcode> (both may be used alternatively), in which case the command requests to print a hardcopy of the receipt associated to the specified account. The format of <br/> barcode> is syntactically the same as used by the CR to produce a store/recall ticket. It is preferred to accept this command in all/most account states recognized by the SCRP protocol. Accepting this command in account state AS IDLE is required, though. The receipt hardcopy must consist of all CR-generated print data for the designated account, as well as all

data that was PRINT-ed for that account on behalf of the SFU.

Responses: 260 Data printed

530 No such account 531 Invalid account state 560 CR-printing inactive

### Cash Register Reset

Command: RESETCR

Description: Requests the CR to execute a reset. The function will only be possible to execute

manually from within the SFU.

Responses: 202 Cash Register restored

531 Invalid account state

### Certified Weighing

 $Command: \quad GET\ CERTDATA < barcode>$ 

Description: This command requests certified weight data from the CR to be presented on the

screen for human verification. The format of <barcode> is missing the embedded weight or price information. The Command can only be issued during the state

AS\_OPEN.

Responses: 214

512 No stable weight531 Invalid account state

## Appendix D

## SCRP IOGG

This appendix gives the IOGG for the Scanflow Cash Register Protocol. The protocol is described in section ??. Each figure groups together the rules for one aspect of the protocol. The captions under each rule give the stimulus or response it represents.

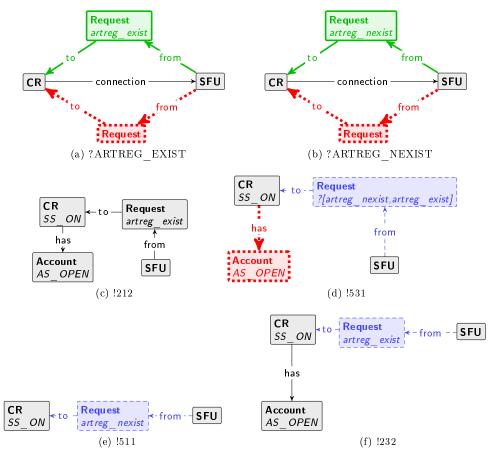


Figure D.1: Account Article Registration

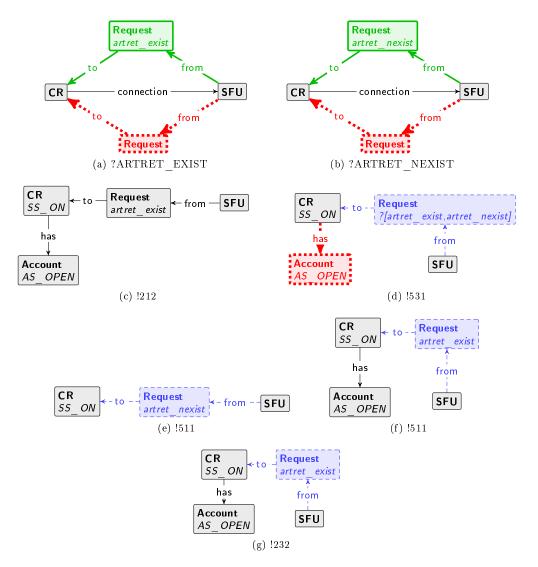


Figure D.2: Account Article Return

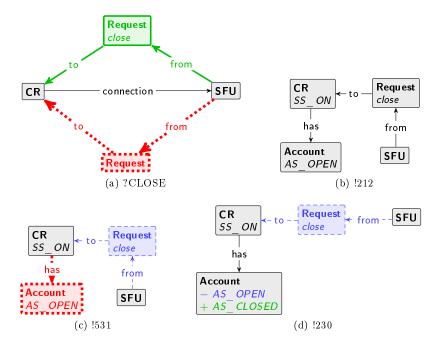


Figure D.3: Account Close

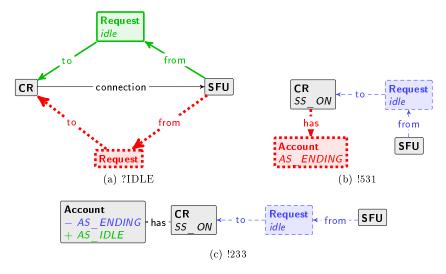


Figure D.4: Account Ending

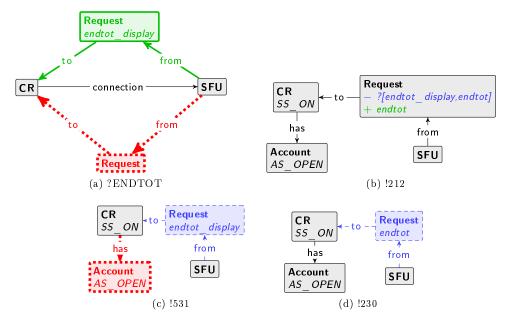


Figure D.5: Account Endtotal

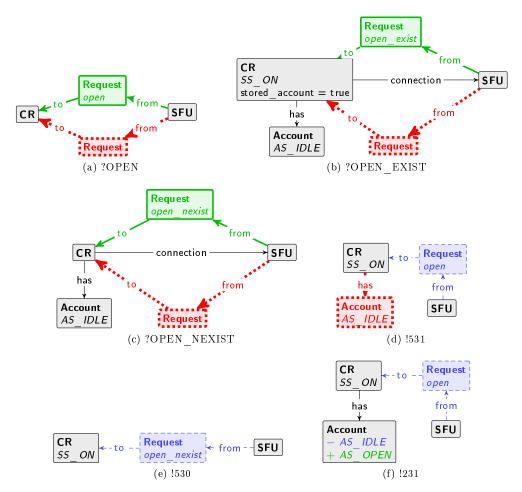


Figure D.6: Account Open

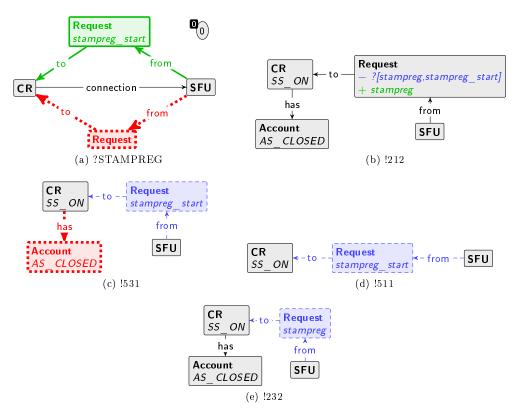


Figure D.7: Account Stamp Registration

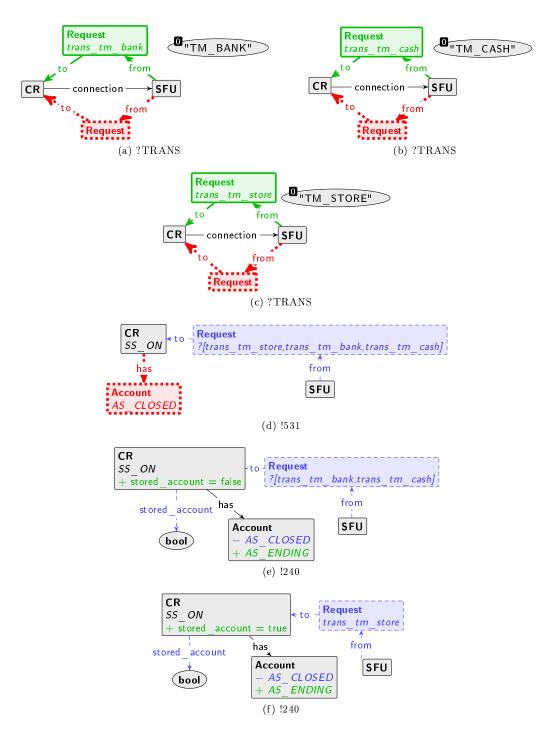


Figure D.8: Account Trans

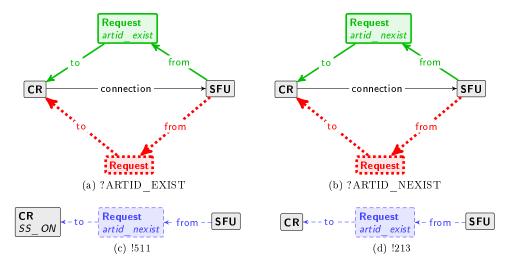


Figure D.9: Artid

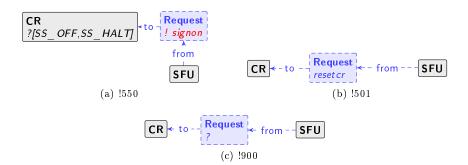


Figure D.10: General Responses

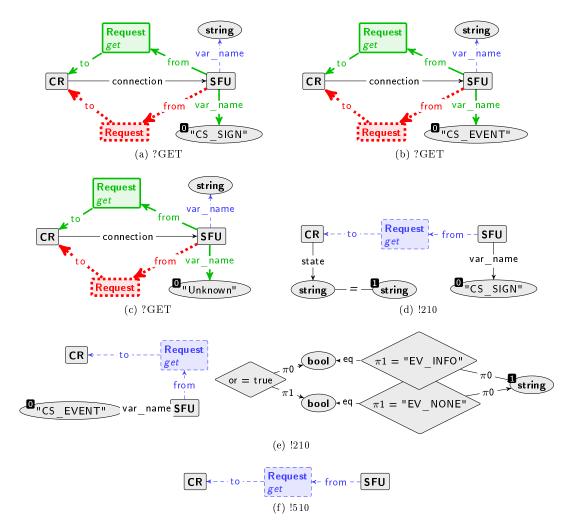


Figure D.11: Get Variable

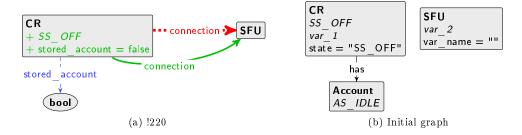


Figure D.12: Initialize

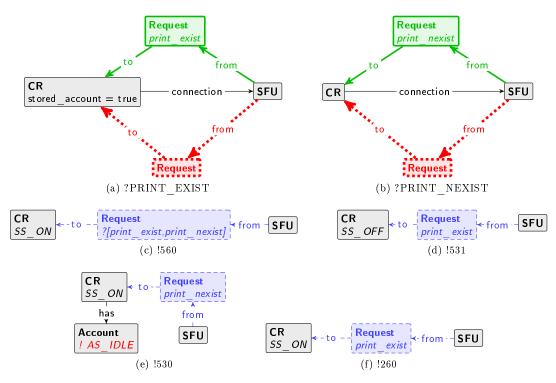


Figure D.13: Print

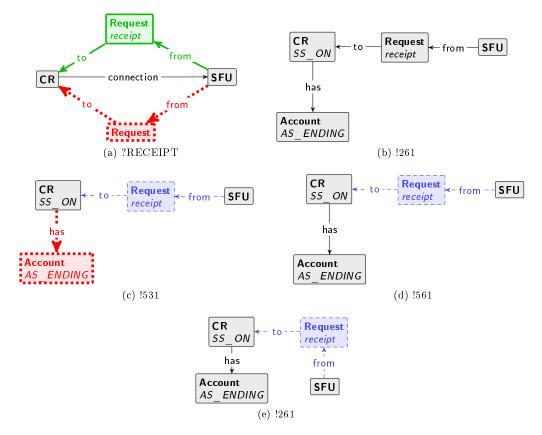


Figure D.14: Receipt

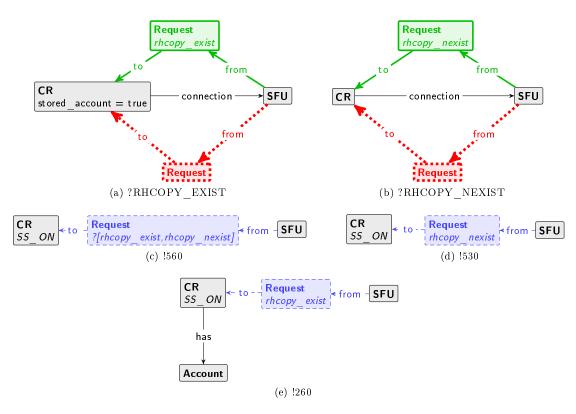


Figure D.15: Receipt Hardcopy

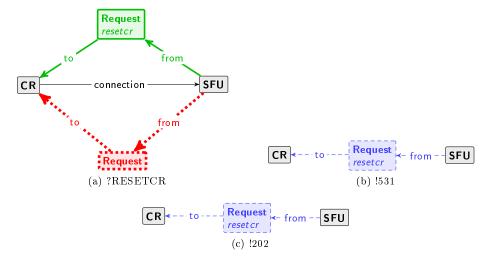


Figure D.16: Resetcr

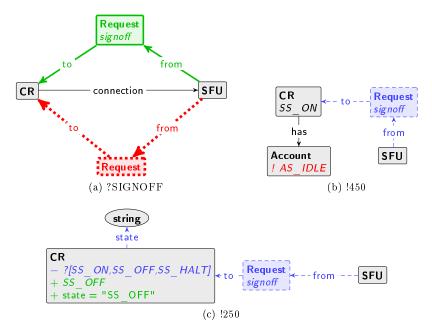


Figure D.17: Signoff

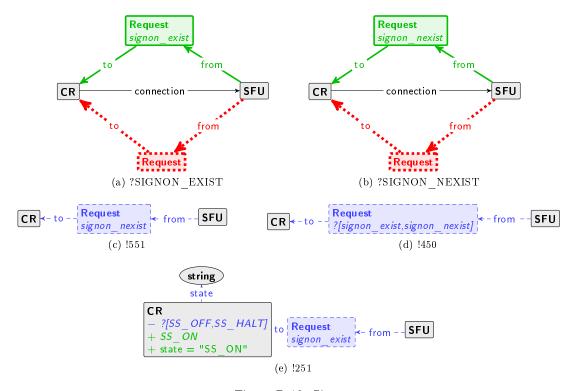


Figure D.18: Signon