## 2.1 Elementary Sorts Exercises

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2.1.1 Show, in the style of the example trace with Algorithm 2.1, how selection sort sorts the array E A S Y Q U E S T I O N.

i	$\min$	0	1	2	3	4	5	6	7	8	9	10	11
		Е	A	S	Y	Q	U	Е	S	Τ	I	О	N
0	1	$\mathbf{E}$	A	$\mathbf{S}$	Y	Q	U	$\mathbf{E}$	$\mathbf{S}$	${\rm T}$	I	O	N
1	1	A	$\mathbf{E}$	$\mathbf{S}$	Y	Q	U	$\mathbf{E}$	$\mathbf{S}$	${\rm T}$	I	O	N
2	6	A	$\mathbf{E}$	$\mathbf{S}$	Y	Q	U	$\mathbf{E}$	$\mathbf{S}$	${\rm T}$	I	Ο	N
3	9	A	$\mathbf{E}$	$\mathbf{E}$	Y	Q	U	$\mathbf{S}$	$\mathbf{S}$	$\mathbf{T}$	I	Ο	N
4	11	A	$\mathbf{E}$	$\mathbf{E}$	Ι	Q	U	$\mathbf{S}$	$\mathbf{S}$	$\mathbf{T}$	Y	Ο	N
5	10	A	$\mathbf{E}$	$\mathbf{E}$	Ι	N	U	$\mathbf{S}$	$\mathbf{S}$	${ m T}$	Y	O	Q
6	11	A	$\mathbf{E}$	$\mathbf{E}$	Ι	N	Ο	$\mathbf{S}$	$\mathbf{S}$	${\rm T}$	Y	U	$\mathbf{Q}$
7	7	A	$\mathbf{E}$	$\mathbf{E}$	Ι	N	Ο	Q	$\mathbf{S}$	$\mathbf{T}$	Y	U	$\mathbf{S}$
8	11	A	$\mathbf{E}$	$\mathbf{E}$	Ι	N	Ο	Q	$\mathbf{S}$	${\rm T}$	Y	U	$\mathbf{S}$
9	11	A	$\mathbf{E}$	$\mathbf{E}$	Ι	Ν	Ο	Q	$\mathbf{S}$	$\mathbf{S}$	Y	U	$\mathbf{T}$
10	10	A	$\mathbf{E}$	$\mathbf{E}$	Ι	Ν	Ο	Q	$\mathbf{S}$	$\mathbf{S}$	$\mathbf{T}$	U	Y
		A	$\mathbf{E}$	$\mathbf{E}$	I	Ν	Ο	Q	$\mathbf{S}$	$\mathbf{S}$	$\mathbf{T}$	U	Y

2.1.2 The maximum number of exchanges involving a specific item is N exchanges. For example, take a list that is already sorted and then add to the beginning an item that is greater in value than the rest of the list. Specifically, consider the list Y A B C D.

i	$\min$	0	1	2	3	4
		Y	Α	В	С	D
0	1	Y	A	В	$\mathbf{C}$	D
1	2	A	Y	В	$\mathbf{C}$	D
2	3	A	В	Y	$\mathbf{C}$	D
3	4	A	В	$\mathbf{C}$	Y	D
4	4	A	В	$\mathbf{C}$	D	Y
		Α	В	$\mathbf{C}$	D	Y

Here, we can see Y was exchanged N times. Furthermore, because a selection sort performs one exchange for every array index, then there are at most N exchanges for an array of length N.

On the other hand, because there are N items and N exchanges then on average each item gets exchanged once. (Is this right)

2.1.3 Give an example of an array of N items that maximizes the number of times the test  $a[j] < a[\min]$  succeeds (and, therefore, min gets updated) during the operation of selection sort.

**Answer** Hypothetically, the most that a[j] < a[min] can succeed is every time it is called. In fact, a list in descending order does just that. For example, consider the list E D C B A. Before the first exchange, the following compares are made:

- (a) D < E, so min = 1
- (b) C < D, so min = 2
- (c) B < C, so min = 3
- (d) A < B, so min = 4

(Expand on this answer later)