

Newton's second law of motion:

$$\begin{aligned}\vec{F} &= \begin{pmatrix} F_x \\ F_y \\ F_z \end{pmatrix} = \frac{d\vec{p}}{dt} \\ &= \frac{d}{dt}(m\vec{v}) \\ &= \frac{dm}{dt}\vec{v} + m\frac{d\vec{v}}{dt} \\ &= m\vec{a}\end{aligned}$$

Nabla operator:

$$\nabla := \begin{pmatrix} \partial_x \\ \partial_y \\ \partial_z \end{pmatrix} = \begin{pmatrix} \frac{\partial}{\partial x} \\ \frac{\partial}{\partial y} \\ \frac{\partial}{\partial z} \end{pmatrix}$$

Navier-Stokes equations:

$$\begin{aligned}\frac{\vec{F}}{V} &= \frac{m}{V}\vec{a} \\ &= \rho\vec{a} \\ &= \rho\frac{D}{Dt}\vec{v} \\ &= \rho\left(\frac{\partial}{\partial t} + \vec{\nabla}\right)\vec{v} \\ &= -\nabla p + \mu\Delta\vec{v} + \rho\vec{F}\end{aligned}$$

Conservation of mass:

$$\nabla\vec{v} = 0$$