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In [1]: # utils.py

from numpy.random import uniform
import matplotlib.pyplot as plt

import numpy as np
import numpy.linalg as LA

from sklearn.preprocessing import StandardScaler

def create_one_hot_label(Y,N_C):
    """
    Input
    Y: list of class labels (int)
    N_C: Number of Classes

    Returns
    List of one hot arrays with dimension N_C

    """
    y_one_hot = []
    for y in Y:
        one_hot_label = np.zeros(N_C)
        one_hot_label[y] = 1.0
        y_one_hot.append(one_hot_label)

    return y_one_hot

def subtract_mean_from_data(X,Y):
    """
    Input
    X: List of data points
    Y: list of one hot class labels

    Returns
    X and Y with mean subtracted

    """
    ss_x = StandardScaler(with_std = False)
    ss_y = StandardScaler(with_std = False)

    ss_x.fit(X)
    X = ss_x.transform(X)

    ss_y.fit(Y)
    Y = ss_y.transform(Y)

    return X,Y

def compute_covariance_matrix(X,Y):
    """
    Input
    X: List of data points
    Y: List of one hot class labels
    """
```

```
In [2]: # projection.py

from numpy.random import uniform
from numpy.random import randn
import random
import time

import matplotlib.pyplot as plt

from scipy.linalg import eig
from scipy.linalg import sqrtm
from numpy.linalg import inv
from numpy.linalg import svd

from utils import create_one_hot_label
from utils import subtract_mean_from_data
from utils import compute_covariance_matrix

import numpy as np
import numpy.linalg as LA

import sys
from numpy.linalg import svd

class Project2D():

    '''
    Class to draw projection on 2D scatter space
    '''

    def __init__(self, projection, clss_labels):

        self.proj = projection
        self.clss_labels = clss_labels

    def project_data(self, X, Y, white=None):

        '''
        Takes list of state space and class labels
        State space should be 2D
        Labels should be int
        '''

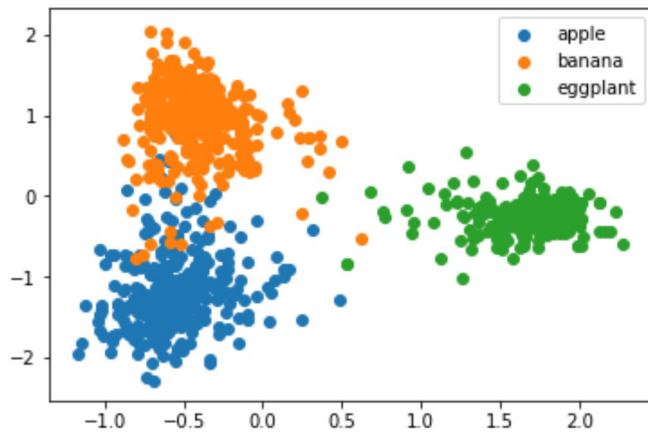
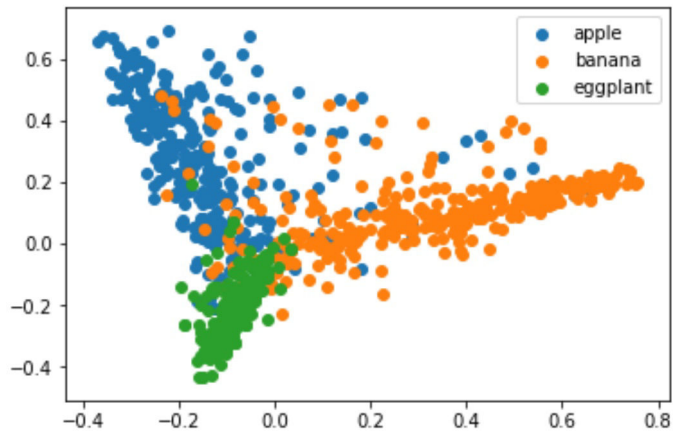
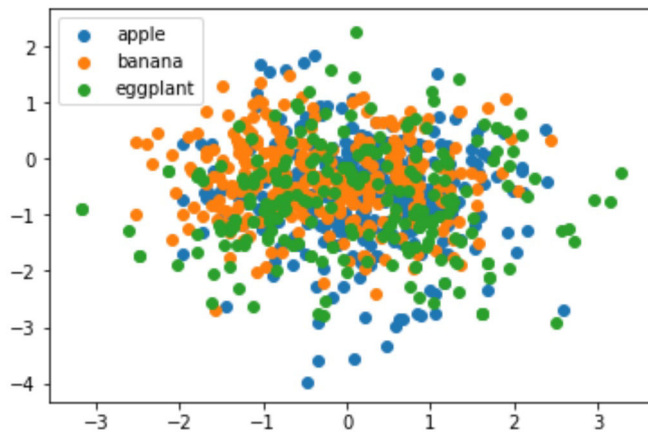
        p_a = []
        p_b = []
        p_c = []

        # Project all Data
        proj = np.matmul(self.proj, white)

        X_P = np.matmul(proj, np.array(X).T)

        for i in range(len(Y)):

            if Y[i] == 0:
                p_a.append(X_P[:, i])
            elif Y[i] == 1:
                p_b.append(X_P[:, i])
            else:
                p_c.append(X_P[:, i])
```



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In [3]: # Ridge_Model

from numpy.random import uniform
import random
import time

import numpy as np
import numpy.linalg as LA

import sys

from sklearn.linear_model import Ridge

from utils import create_one_hot_label

class Ridge_Model():

    def __init__(self, class_labels):

        ###RIDGE HYPERPARAMETER
        self.lmda = 1.0
        self.class_labels = class_labels
        self.ridge_model = Ridge(self.lmda)

    def train_model(self, X, Y):
        """
        FILL IN CODE TO TRAIN MODEL
        MAKE SURE TO ADD HYPERPARAMTER TO MODEL

        """
        X = np.array(X)
        y_one_hot = create_one_hot_label(Y, len(self.class_labels))
        self.ridge_model.fit(X, y_one_hot)

    def eval(self, x):
        """
        Fill in code to evaluate model and return a prediction
        Prediction should be an integer specifying a class
        """
        x = x.reshape(1, -1)
        y = self.ridge_model.predict(x)
        return np.argmax(y)
```

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In [ ]: # LDA

import random
import time

import glob
import os
import pickle
import matplotlib.pyplot as plt

import numpy as np
import numpy.linalg as LA

import sys
from numpy.linalg import inv
from numpy.linalg import det
from sklearn.svm import SVC
from projection import Project2, Projections

from utils import subtract_mean_from_data
from utils import compute_covariance_matrix

class LDA_Model():

    def __init__(self, class_labels):

        ###SCALE AN IDENTITY MATRIX BY THIS TERM AND ADD TO COMPUTED COVARIANCE MATRIX TO PREVENT IT BEING SINGULAR ###
        self.reg_cov = 0.001
        self.N_M_C_S_S = len(class_labels)

    def train_model(self, X, Y):
        '''
        FILL IN CODE TO TRAIN MODEL
        MAKE SURE TO ADD HYPERPARAMETER TO MODEL
        '''
        ps = [ [] for j in range(self.N_M_C_S_S) ]
        for i, y in enumerate(Y):
            ps[y].append(X[i])

        self.mean_list = []
        for lst in ps:
            self.mean_list.append( np.mean(np.array(lst), axis=0) )

        Sigma_XX = compute_covariance_matrix(X, X)
        Sigma_XX = self.reg_cov * np.identity(Sigma_XX.shape[0])
        self.Sigma_inv = inv(Sigma_XX)

    def eval(self, x):
        '''
        Fill in code to evaluate model and return a prediction
        Prediction should be an integer specifying a class
        '''
        x = x.reshape(1, -1)
        y =
        for i in range(self.N_M_C_S_S):
            x_demeaned = x - self.mean_list[i]
            f = - x_demeaned.dot(self.Sigma_inv).dot(x_demeaned.T)

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In [ ]: # QDA

import random
import time

import numpy as np
import numpy.linalg as LA

from numpy.linalg import inv
from numpy.linalg import det

from projection import Project2 , Projections

from utils import subtract_mean_from_data
from utils import compute_covariance_matrix

class DA_Model():

    def __init__(self,class_labels):

        ###SCALE AN IDENTITY MATRIX BY THIS TERM AND ADD TO COMPUTED COVARIANCE MATRIX TO PREVENT IT BEING SINGULAR ###
        self.reg_cov = 0.01
        self.N_M_C_S_S = len(class_labels)

    def train_model(self,X,Y):
        '''
        FILL IN CODE TO TRAIN MODEL
        MAKE SURE TO ADD HYPERPARAMETER TO MODEL
        '''
        ps = [ [] for j in range(self.N_M_C_S_S) ]
        for i, y in enumerate(Y):
            ps[y].append(X[i])

        self.mean_list = []
        self.Sigma_inv_list = []
        for lst in ps:
            self.mean_list.append( np.mean(np.array(lst), axis=0) )
            Sigma_XX = compute_covariance_matrix(lst, lst)
            Sigma_XX = self.reg_cov * np.identity(Sigma_XX.shape[0])

            self.Sigma_inv_list.append(inv(Sigma_XX))

    def eval(self,x):
        '''
        Fill in code to evaluate model and return a prediction
        Prediction should be an integer specifying a class
        '''
        x = x.reshape(1, -1)
        y =
        for i in range(self.N_M_C_S_S):
            x_demeaned = x - self.mean_list[i]
            f = - x_demeaned.dot(self.Sigma_inv_list[i]).dot(x_demeaned.T)

            y[i] = f.flatten()[0]
        return max(y, key=lambda x: y[x])

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In [ ]: # SVM

from numpy.random import uniform
import random
import time

import matplotlib.pyplot as plt

import numpy as np
import numpy.linalg as LA

import sys

from sklearn.svm import SVC
from projection import Project2, Projections

from utils import create_one_hot_label

class M_Model():

    def __init__(self, class_labels, projection=None):

        ### SLACK HYPERPARAMETER
        self.C = 1.0
        self.class_labels = class_labels
        self.svc_model = SVC(C=self.C)

    def train_model(self, X, Y):
        """
        FILL IN CODE TO TRAIN MODEL
        MAKE SURE TO ADD HYPERPARAMETER TO MODEL
        """
        X = np.array(X)
        self.svc_model.fit(X, Y)

    def eval(self, x):
        """
        Fill in code to evaluate model and return a prediction
        Prediction should be an integer specifying a class
        """
        x = x.reshape(1, -1)
        y = self.svc_model.predict(x)
        return y[0]
```

```
In [17]: # confusion_mat.py

from sklearn.metrics import confusion_matrix
import matplotlib.pyplot as plt
import random
import IPython

def main():
    """
    Result
    Plot RANDOM confusion matrix (true labels vs. predicted labels)
    """
    true_labels = [random.randint(1, 10) for i in range(100)]
    predicted_labels = [random.randint(1, 10) for i in range(100)]

    # Plot confusion matrix (true labels vs. predicted labels)
    plot = getConfusionMatrixPlot(true_labels, predicted_labels)
    plot.show()

def getConfusionMatrix(true_labels, predicted_labels):
    """
    Input
    true_labels: actual labels
    predicted_labels: model's predicted labels

    Output
    cm: confusion matrix (true labels vs. predicted labels)
    """

    # Generate confusion matrix using sklearn.metrics
    cm = confusion_matrix(true_labels, predicted_labels)
    return cm

def plotConfusionMatrix(cm, alphabet):
    """
    Input
    cm: confusion matrix (true labels vs. predicted labels)
    alphabet: names of class labels

    Output
    Plot confusion matrix (true labels vs. predicted labels)
    """

    fig = plt.figure()
    plt.clf() # Clear plot
    ax = fig.add_subplot(111) # Add 1x1 grid, first subplot
    ax.set_aspect(1)
    res = ax.imshow(cm, cmap=plt.cm.binary,
                    interpolation='nearest', vmin=0, vmax=80)

    plt.colorbar(res) # Add color bar

    width = len(cm) # Width of confusion matrix
    height = len(cm[0]) # Height of confusion matrix

    # Annotate confusion entry with numeric value
    for x in range(width):
        for y in range(height):
            ax.annotate(str(cm[x][y]), xy=(y, x), horizontalalignment='center',
                        verticalalignment='center', color=getFontColor(cm[x][y]))
```



```

In [7]: # linear_classification.py

from numpy.random import uniform
import random
import time

import matplotlib.pyplot as plt

import numpy as np
import numpy.linalg as LA

import sys

from projection import Project2D, Projections
from confusion_mat import getConfusionMatrixPlot

from ridge_model import Ridge_Model
from da_model import DA_Model
from lda_model import LDA_Model
from svm_model import SVM_Model

CLASS_LABELS = ['apple', 'banana', 'eggplant']

class Model():
    """ Generic wrapper for specific model instance. """

    def __init__(self, model):
        """ Store specific pre-initialized model instance. """

        self.model = model

    def train_model(self, X, Y):
        """ Train using specific model's training function. """

        self.model.train_model(X, Y)

    def test_model(self, X, Y):
        """ Test using specific model's eval function. """

        labels = [] # List of actual labels
        p_labels = [] # List of model's predictions
        success = 0 # Number of correct predictions
        total_count = 0 # Number of images

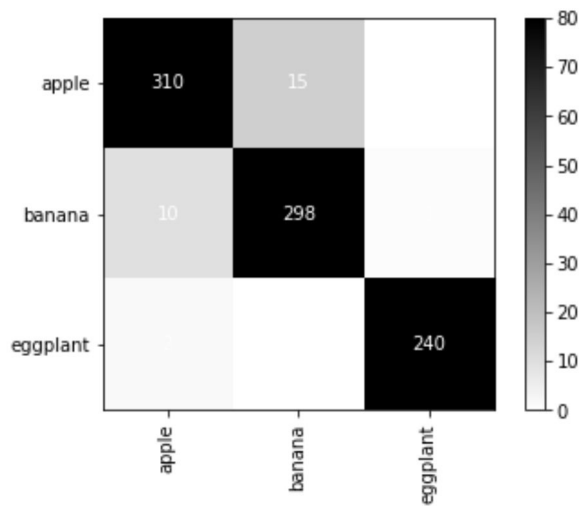
        for i in range(len(X)):

            x = X[i] # Test input
            y = Y[i] # Actual label

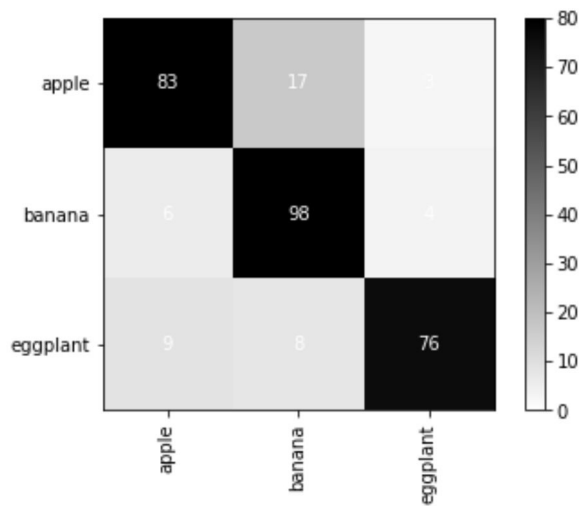
            y_ = self.model.eval(x) # Model's prediction
            labels.append(y)
            p_labels.append(y_)

```

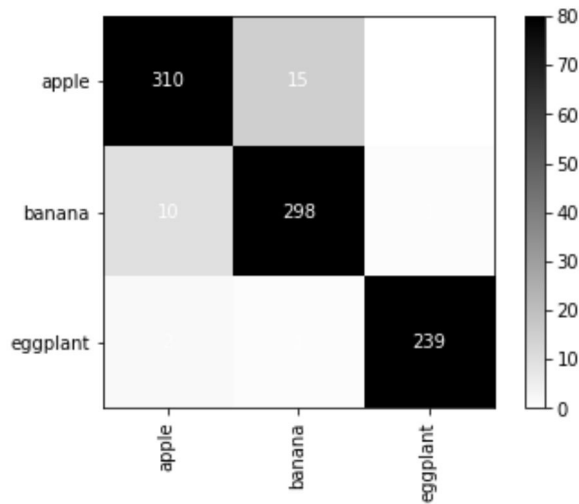
```
[[310 15 0]
 [ 10 2 8 1]
 [ 2 0 240]]
```



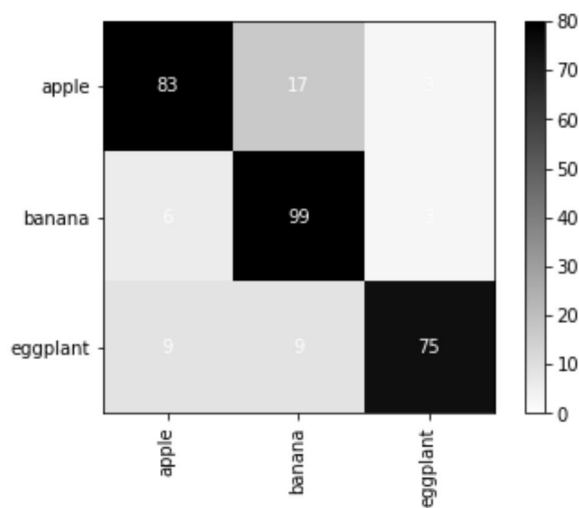
```
[[83 17 3]
 [ 6 8 4]
 [ 8 76]]
```



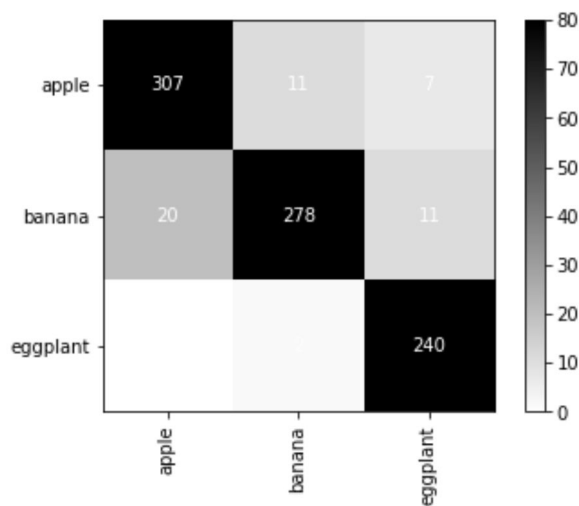
```
[[310 15 0]
 [ 10 2 8 1]
 [ 2 1 23 ]]
```



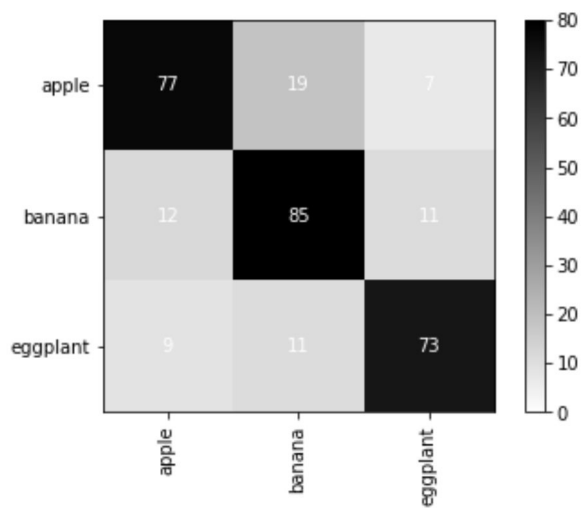
```
[[83 17  3]
 [ 6  3]
 [    75]]
```



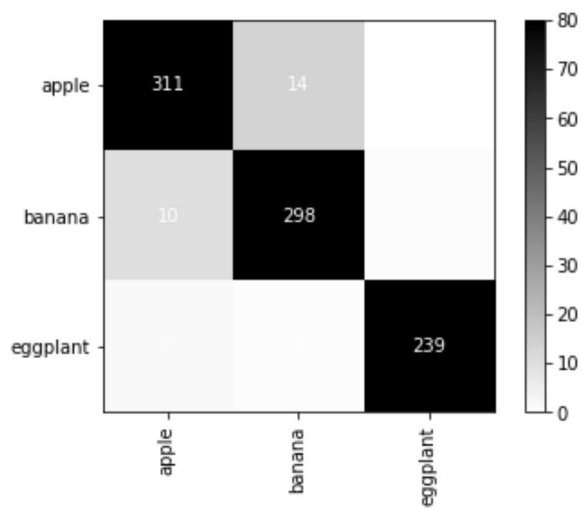
```
[[307 11  7]
 [ 20 278 11]
 [  0  2 240]]
```



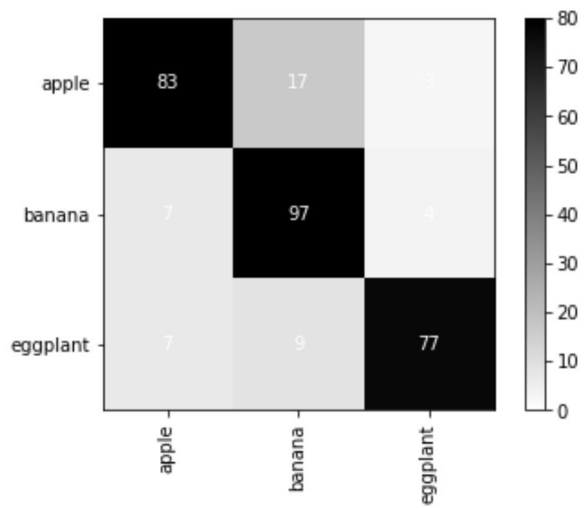
```
[[77 1  7]  
 [12 85 11]  
 [  11 73]]
```



```
[[311 14  0]  
 [ 10 2  8  1]  
 [  2  1 23 ]]
```



```
[[83 17  3]  
 [ 7  7  4]  
 [ 7  77]]
```



```
In [8]: # hyper_search.py

import IPython
from numpy.random import uniform
import random
import time

import glob
import os
import pickle
import matplotlib.pyplot as plt

import numpy as np
import numpy.linalg as LA

import sys

from projection import Project2D, Projections

from confusion_mat import getConfusionMatrix
from confusion_mat import plotConfusionMatrix

from ridge_model import Ridge_Model
from qda_model import QDA_Model
from lda_model import LDA_Model
from svm_model import SVM_Model

CLASS_LABELS = ['apple', 'banana', 'nectarine', 'plum', 'peach', 'watermelon', 'pear',
                'mango', 'grape', 'orange', 'strawberry', 'pineapple',
                'radish', 'carrot', 'potato', 'tomato', 'bellpepper', 'broccoli', 'cabbage', 'c
auliflower', 'celery', 'eggplant', 'garlic', 'spinach', 'ginger']

def eval_model(X, Y, k, model_key, proj):
    # PROJECT DATA
    cca_proj, white_cov = proj.cca_projection(X, Y, k=k)

    X_p = proj.project(cca_proj, white_cov, X)
    X_val_p = proj.project(cca_proj, white_cov, X_val)

    # TRAIN MODEL
    model = models[model_key]

    model.train_model(X_p, Y)
    acc, cm = model.test_model(X_val_p, Y_val)

    return acc, cm

class Model():
    """ Generic wrapper for specific model instance. """

    def __init__(self, model):
        """ Store specific pre-initialized model instance. """

        self.model = model

    def train_model(self, X, Y):
```

