

Review

1. LS : $Y = AX$

$$A'Y = A'AX$$

$$(A'A)^{-1}A'Y = X$$

2. Ridge

$$A'Y = (A'A + \delta I)X$$

$$(A'A + \delta I)^{-1}A'Y = X$$

3. Features

$A \rightarrow$ polynomials

4. Cross-validation

train	val	test
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parameter	hyper-param.	method
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1.) ~~Additive white noise~~ Data Generated w/ Additive White Noise

additive : $Y = f(x) + N(x)$

random var. : $N(x) \sim p(n(x))$

zeromean : $E[N(x)] = 0, \forall x$

independent & identical distributed : $p(n(x)) = p(n), \forall x$

2) Univariate Gaussian Distribution

Random variable : $X \sim p(x)$

Probability : $p(x) = \frac{1}{\sqrt{2\pi}\sigma} e^{-(x-\mu)^2/(2\sigma^2)}$

Mean : $E[X] = \int_{-\infty}^{\infty} x p(x) dx = \mu$

Variable : $V[X] = E[(X-\mu)^2] = \int_{-\infty}^{\infty} (x-\mu)^2 p(x) dx = \sigma^2$

Parameter : $x \sim N(\mu, \sigma^2)$

Log-likelihood : $\log p(x) = -\frac{(x-\mu)^2}{2\sigma^2} - \log(\sqrt{2\pi}\sigma)$

Linear Combination : $E(aX + bY) = a\mu_x + b\mu_y$

X, Y independent : $V[aX + bY] = a^2\mu_x + b^2\mu_y$

Review

1. LS

$$Y = AX$$

$$Y'A' = A'A$$

$$X = Y'A'^{-1}(A'A)$$

2. Ridge

$$X(II + A'A) = Y'A'$$

$$X = Y'A'^{-1}(II + A'A)$$

3. Features

$A \rightarrow$ polynomials

4. Cross-validation

train / val / test

parameter hyper-param. method

1. Additive noise data generated w/ Additive White Noise

$$\text{additive: } Y = f(x) + n(x)$$

$$\text{random var: } n(x) \sim p(n(x))$$

$$\text{assumes: } E[n(x)] = 0, \dots$$

$$\text{independent \& identical distributed: } p(n(x)) = p(n), \forall x$$

2) Univariate Gaussian Distribution

$$\text{Random variable: } x \sim p(x)$$

$$\text{Probability: } p(x) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$

$$\text{Mean: } E[x] = \int_{-\infty}^{\infty} x p(x) dx = \mu$$

$$\text{Variance: } V(x) = E[(x-\mu)^2] = \int_{-\infty}^{\infty} (x-\mu)^2 p(x) dx = \sigma^2$$

$$\text{Parameter: } x \sim N(\mu, \sigma^2)$$

$$\text{log-likelihood: } \log p(x) = -\frac{(x-\mu)^2}{2\sigma^2} - \log(\sqrt{2\pi}\sigma)$$