

## Distributions

- $X \sim \text{Bernoulli}(p)$

$$f(x; p) = p^x(1 - p)^{1-x}$$

$$E[X] = p, \text{Var}[X] = p(1 - p)$$

- $X \sim \text{Binomial}(n, p)$

$$f(x; n, p) = \binom{n}{x} p^x(1 - p)^{n-x}$$

$$E[X] = np, \text{Var}[X] = np(1 - p)$$

- $X \sim N(\mu, \sigma^2)$

$$f(x; \mu, \sigma^2) = (2\pi\sigma^2)^{-1/2} \exp\left\{-\frac{1}{2\sigma^2}(x - \mu)^2\right\}$$

- $X \sim \text{Beta}(\alpha, \beta)$

$$f(x; \alpha, \beta) = \frac{\Gamma(\alpha + \beta)}{\Gamma(\alpha)\Gamma(\beta)} x^{\alpha-1}(1 - x)^{\beta-1}$$

$$E[X] = \frac{\alpha}{\alpha + \beta}$$

- $X \sim \text{Poisson}(\lambda)$

$$f(x; \lambda) = \frac{e^{-\lambda}\lambda^x}{x!}$$

$$E[X] = \text{Var}[X] = \lambda$$

- $X \sim \text{Exponential}(\lambda)$

$$f(x; \lambda) = \lambda e^{-\lambda x}$$

$$E[X] = \frac{1}{\lambda}, \text{Var}[X] = \frac{1}{\lambda^2}$$