

**True/False** - No explanation needed. (1pt for correct, 0pt - no answer, -1pt - incorrect)

1. If two samples that were treated identically show a difference that is statistically significant, it is a Type II error. True/False  
False. It's Type I error.
2. The independent-samples t-test cannot be used when samples differ in size. True/False  
False. Just truncate the bigger sample.

**Problems** - Need justification. No justification means **zero**!

1. (10pts) We toss two coins 100 times and record the outcomes: 30 times of two H's, 40 times of one H one T, 30 times of two T's.  
(a) Calculate the expected frequencies, given the null hypothesis  $H_0$  that both coins are fair.

The expected frequencies for HH's, one H one T's, TT's are, respectively: 25, 50, 25

(b) Take the significance level  $\alpha = 0.1$ , perform the  $\chi^2$  test and draw a conclusion.

$H_0$ : both coins are fair vs  $H_1$ : not fair

$$\chi^2 = \frac{(30 - 25)^2}{25} + \frac{(40 - 50)^2}{50} + \frac{(30 - 25)^2}{25} = 4$$

$$\text{DOF} = 3 - 1 = 2$$

Critical  $\chi^2$  corresponding to  $\alpha = 0.1$  and  $\text{DOF} = 2$  is 4.61.

$4 < 4.61$ . Thus, fails to reject  $H_0$