

# Achieving results with untrained neural networks using Supermasks

## Independent Study Proposal

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## 1 Introduction

Interest in decreasing the size of neural networks that are used to solve certain problems has existed since at least the year 1990 [1]. Different methods have been proposed that can be used to achieve a decrease in network size of up to 90% while retaining performance [1] [4] [5] [7].

This has multiple advantages, which can be classified according to the type of pruning that is applied. If the network is pruned after training while otherwise keeping the trained weights constant, this may result in reduced storage size, less energy consumption and faster computation during the application phase [3]. If it is possible to retrain the smaller network from scratch, this may result in less overfitting because the number of parameters has decreased [4]. And if a smaller but still effective network topology can be chosen before training, this can reduce the training time, because less parameters have to be optimized.

However, conventional pruning techniques have the problem that, when retraining from scratch on the smaller topology, the performance gets considerably worse [3]. These pruning techniques are only amenable for pruning the weights computed by an inital training run, and do not work well if the aim is to retrain once again on the smaller topology. Therefore, they cannot be used to choose a good topology before the training starts, because the correct parameters for the smaller network can only be discovered by training the larger network.

In contrast to this negative state of affairs, in their paper "The Lottery Ticket Hypothesis: Finding Sparse, Trainable Neural Networks" [3], the authors present a hypothesis that essentially claims that pre-training pruning nonetheless has a lot of potential:

The Lottery Ticket Hypothesis [3]. A randomly-initialized, dense neural network contains a subnetwork that is initialized such that – when trained in isolation – it can match the test accuracy of the original network after training for at most the same number of iterations.

The authors further show that the subnetwork mentioned in the hypothesis can be uncovered by training the dense network and then setting a percentage p% of the parameters with smallest magnitude to zero (and freezing them, so that they are not trained anymore). If the remaining parameters are then set to their inital values (the random values they had before the training started), and one retrains the smaller network starting with these initial values, then the training time will usually be less and the test performance better compared to the original, dense, trained network [3].

It is imperative here that the non-frozen parameters are reset to their *initial*, random values, not newly chosen random values. If the latter is chosen, the performance is much worse and the "Lottery Ticket" has not been uncovered [3]. In other words, we should not only search for efficient network topologies, but also for good initial values.

This curious fact has been further investigated by Zhou et al. [9]. They realized that the subnetworks obtained through pruning show a performance that is

already significantly higher than chance before they are trained. More specifically, a randomly-initialized, dense network is first trained. The trained parameters are then ranked by a value given by

$$sign(w_{initial}) \cdot w_{trained}$$

so that parameters with large magnitude that retained their sign are ranked high. A percentage p% of the lowest-ranking parameters is set to zero and frozen, the rest is reset to a constant with the same sign as their initial value. The resulting network is **not** trained again, rather it is being evaluated directly. Note that the values of the parameters at that point come directly from the initial random initialization, the only training information comes from deciding which of these random values to set to zero. Nonetheless, this technique achieves a remarkable 86% accuracy on MNIST, and 41% on CIFAR-10. The authors call the corresponding 0-1-masks "Supermasks".

In this paper, we provide the following contributions to the new theory of Lottery Ticket pruning:

- We describe a complete methodology for applying Lottery Ticket pruning to a trained neural network. The methodology crucially uses the Supermask idea for finding the pruning treshold.
- We show that the methodology applied on MNIST outperforms hyperoptimization of the network layer sizes: Our method can yield a significantly smaller size while retaining the same accuracy and training speed.
- As part of this, we reproduce the main results regarding Lottery Tickets [3] and Supermasks [9] on MNIST: Supermasks do indeed yield untrained networks with higher-than-random accuracy, which can be trained to achieve faster training and higher accuracy with less parameters, compared to the unpruned networks.

## 2 Approach

In this section we describe a complete methodology for applying Lottery Ticket pruning to a trained neural network. We assume that we have a fully connected multilayer perceptron which has already been trained to satisfaction and should be pruned now. Importantly, we also assume that the weights with which the network had been initialized before training have been saved.

#### 2.1 Main idea

Following the Lottery ticket approach, we want to take our initial network parameters, set some of them to zero and freeze them there, and then train the resulting network. The result will effectively have a (much) smaller size. There are different methods for choosing which of the initial parameters to prune: In the original Lottery ticket paper [3], this is done by setting all parameters to zero which had a small magnitude after training. How many parameters are set to zero depends on

the specific threshold – a higher treshold corresponds to more aggressive pruning. For example, suppose the initial parameters are 0.1, 0.2, 0.3 and the parameters after training are -0.2, 0.05, 0.3. If we prune with a treshold of t = 0.1, we would get the parameters 0.1, 0, 0.3. Starting with these values, we would then train the network, but the second value would be frozen at 0.

In [9], the authors show that instead of setting those parameters to zero whose magnitude after training is minimal ( $|w_{trained}|$  is minimal), one gets better results by setting those parameters to zero for which the value

$$sign(w_{initial}) \cdot w_{trained}$$

is minimal. In other words, we keep those values which both have a large magnitude after training and retain their sign, and set the other parameters to zero. Following the example above, if the initial parameters are 0.1, 0.2, 0.3 and the parameters after training are -0.2, 0.05, 0.3, then pruning with a treshold t = 0.1 yields 0, 0, 0.3 – in this case, the first value is pruned as well, because it changed signs.

## 2.2 Choosing the treshold

In [9], the authors provide a second, and most crucial, insight, which will help us choose a good pruning treshold. When choosing the parameters as outlined above, the result is just a version of the initial, random parameters with some set to zero. However, without further training, the resulting networks nonetheless already show a suprisingly good performance when evaluated. This is where the term Supermask comes from: We take the initial, random parameters and multiply them with a mask of zeros and ones, and suddenly we get suprisingly great performance. For example, in [9], the authors report an accuracy of 86% on MNIST.

This leads us to a straightforward way of choosing a treshold: We simply compute the masked networks for different tresholds, and then (without training!) check their performance on the validation set. We then choose the treshold that yielded the highest performance. More to the point, we choose the masked network corresponding to that treshold, and train it to yield our pruned network.

This is especially useful since both the computation of the masked networks and the evaluation of them are computationally cheap, since no training is required.

## 2.3 Summary of steps

The complete recipe for applying Lottery Ticket pruning looks like this:

- 1. Take a fully connected multilayer perceptron, initialize it with random values and save these initial values.
- 2. Train the network to satisfaction.
- 3. For many different tresholds t, compute the parameters for a masked network  $M_t$  using the formula

$$w_i^{\text{new}} := \begin{cases} w_i^{\text{initial}} & \text{if sign} \left( w_i^{\text{initial}} \right) \cdot w_i^{\text{trained}} \ge t, \\ 0 & \text{otherwise.} \end{cases}$$

- 4. Evaluate all the networks  $M_t$  on a validation set and choose the best performing network  $M_*$ .
- 5. Freeze all the parameters of  $M_*$  which are exactly zero, so that they don't change during training.
- 6. Train  $M_*$  to satisfaction.

## 3 Evaluation

In order to evaluate the outlined methodology, we will apply it to a standard dataset ten times using ten different random seeds. For each of these runs, we also perform a standard hyperoptimization approach for layer size reduction as a comparison. As part of this evaluation, we reproduce the main results regarding Lottery Tickets [3] and Supermasks [9].

#### 3.1 Dataset

All experiments are done with the well-established MNIST dataset [2]. It contains a collection of grayscale images of size  $28 \times 28$ , which each correspond to exactly one of ten possible digits 0 to 9. The dataset has already been split into a training and a testing part; it contains 60.000 training examples and 10.000 testing examples. We are using the training examples for training the network, and the testing examples for validation of the network performance during training.

#### 3.2 Baseline neural network

In order to apply the pruning techniques and supermasks, we need a baseline neural network. As in [9], we chose a fully connected neural network with three layers. The input size is  $28 \times 28 = 784$ , the first layer has size 200, the second has size 30 and the output layer has size 10, since there are ten classes in the dataset. Compared to [9] we chose smaller values for the first and second layer size: In that paper, the sizes are 300 and 100 respectively. This was done because early experimentation with simple hyperoptimization showed that we could achieve the same performance with our smaller architecture during training. Since we are testing pruning capabilities, it is good to start with a network size that cannot be reduced trivially.

## 3.3 Training and early stopping

Since we need a meaningful trained baseline that does not overfit, we use the same early stopping criterion as in [9]. After saving the initial, random parameters, the neural network is first trained for 20.000 iterations, using the Adam optimizer [6] with learning rate 0.0012 (as in [9]) and the PyTorch cross entropy loss [8]. Each iteration corresponds to the processing of one batch of training data; one batch

contains 60 training examples. This initial training certainly leads to overfitting, which can be seen by plotting the validation loss (Figure 1).

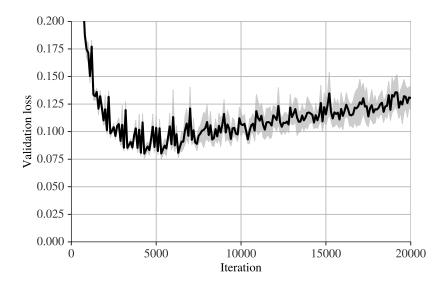


Figure 1: The validation loss during the initial training run, evaluated every 100 iterations across all ten random seeds. The indicated intervals show the standard deviation. Overfitting is clearly apparent: After about iteration 5000, the validation starts increasing again.

Because of this, we record at which iteration the minimal validation loss was achieved, and retrain the network from scratch – starting from the saved, initial parameters – for that many iterations. For all random seeds, the minimal validation loss is always achieved around iteration 5000. While the training will never go exactly the same the second time around due to randomness, this seems to work well in practice both in our experiments and in [9], yielding a trained, non-overfit baseline network. The validation loss during the second training run is visualized in Figure 2.

Across random seeds, the validation accuracy is  $0.101 \pm 0.016$  before training and  $0.977 \pm 0.001$  after training.

## 3.4 Training and early stopping

The next step of our methodology is the application of the supermasks. To that end, we apply the following procedure taken from [9]. First, we reset the baseline network to its initial parameters, which were randomly initialized, but saved before the training started. Next, we choose a treshold t and iterate through the parameters  $w_1, \ldots, w_n$  of the network. We set a new value for each parameter according to the formula

$$w_i^{\text{new}} := \begin{cases} w_i^{\text{initial}} & \text{if sign} \left(w_i^{\text{initial}}\right) \cdot w_i^{\text{trained}} \ge t \\ 0 & \text{otherwise.} \end{cases}$$

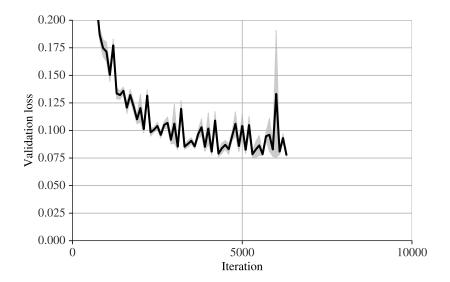


Figure 2: The validation loss during the second training run with early stopping, evaluated every 100 iterations across all ten random seeds. The indicated intervals show the standard deviation. For each seed, the training was stopped at the iteration that achieved the minimal validation loss during the initial training run. We can see that this approach results in a non-overfit, small validation loss when the training finishes.

In effect, we keep parameters the same which had a large magnitude after training, and still had the same sign as the initial value. The other parameters are set to zero. The resulting neural network is identical to the initial, randomly initialized network, with some parameters set to zero. Effectively, a zero-one mask was applied to the initial, untrained network – the so-called Supermask.

We then evaluate the accuracy of this masked network on the validation set. Of course, the performance depends on the threshold: For very large thresholds, all parameters are set to zero, so the accuracy will be close to 0.1. For very small (negative) thresholds, all parameters are kept at their initial value, which was randomly chosen at the beginning, so we still expect an accuracy close to 0.1. For intermediate tresholds, something remarkable happens: The masked network achieves a validation accuracy that is significantly better than 0.1, even though all the parameter values come from a random distribution, and the only training information lies in the decision which parameters to set to zero. The performance for different tresholds of the masked networks across all ten random seeds are shown in XXX.

## 3.5 Lottery tickets

The next step is to apply the knowledge we have about the performance of the masked networks. We wish to find a "Lottery Ticket" – this is essentially a masked network which has been trained, where the parameters that are zero are frozen

during training. When trying to prune a network using lottery tickets, one is faced with the one question that always arises during pruning: How small should the resulting network be? Here, we use the validation results of the supermasks as a guideline: Out of all the masked networks resulting from different tresholds, we choose the masked network that has the highest validation accuracy before training. We then train this masked network for 5000 iterations and observe the validation loss.

## 3.6 Hyperoptimization

In order to have a comparization for the quality of the pruning produced by the lottery ticket approach, we employ a simple hyperoptimization scheme to optimize the network size. Whereas the initial sizes for layers 1 and 2 were 200 and 30 respectively, for the hyperoptimization we allow all combinations of 50, 100, 150 and 5, 15, 25 respectively. For each of these size combinations, we take a randomly initialized network of that size, and train it for 5000 ietrations, observing the validation loss.

## 4 Conclusion

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