

Business Economics: From zero to hero.

Elasticity: $\epsilon = -\frac{dq}{dp} \cdot \frac{p}{q}$ } Lecture 1

• Marginal cost shows how much to produce, whereas average cost shows if a firm should produce at all.

• Perfect competition: $P = MC = C'(q)$
if $P > MC$, increase production and vice versa

• Monopolist's price: } Lecture 2

$$\frac{P^M - MC}{P^M} = \frac{1}{\epsilon}$$

Lerner Index

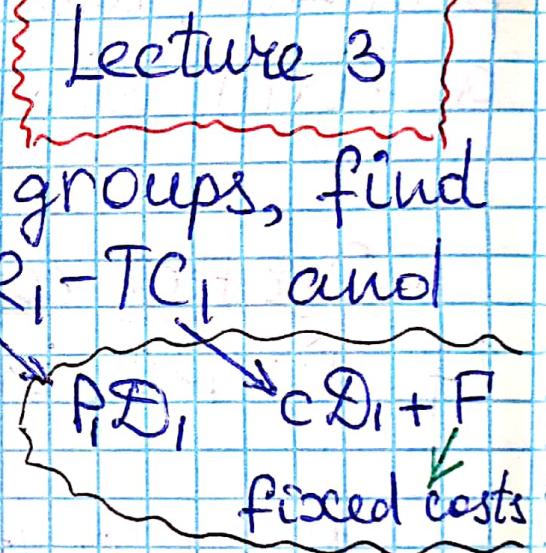
or $MR = MC$

Multi-product Monopoly:

$$\frac{P_1 - MC_1}{P_1} = \frac{1}{\epsilon_1} - \frac{(P_2 - MC_2)D_2 \epsilon_{12}}{P_1 D_1 \epsilon_1}$$

where ϵ_{12} is the cross-price elasticity of good 2 w/r respect to price 1.

- Linear pricing - if you can discriminate between groups, find P_1 and P_2 maximizing $TR_1 - TC_1$ and $TR_2 - TC_2$, respectively.



- Linear pricing where you cannot discriminate: P maximizing $TR - TC$, where you use the market (combined demand curve).

- Two-part pricing: 1) $P = MC$ and 2) $F = \text{Consumer surplus at } P = MC$.

Block pricing - find P and F

using the two-part pricing formulas.
Then, charge $P \cdot \underline{Q} + F$ for the bundle
of \underline{Q} units. (Find \underline{Q} using the price
in the demand formula.)

• Maximum F that a producer can
charge for price = x is CS when $P=x$.

• Menu pricing - two-part pricing
when the two groups are not distinguishable:

$$\Pi = \Pi_L + \Pi_H = (P_L - MC) Q_L + CS_L(P_L) + CS_H(P_H) - (CS_H(P_L) - CS_L(P_L))$$

Informational rent - surplus enjoyed by a high-demand customer when he chooses a low-demand bundle.

In the formula, $CS_H(P_H)$ is a fixed number (does not depend on P_L). So,

$$\Pi = (p_L - MC) Q_L + CS_H(p_H) + 2CS_L(p_L) - CS_H(p_L)$$

↓
CS of a high-demand customer when $p=p_L$.

Optimal pricing

① $p_H = MC$

② p_L is found using $\frac{d\Pi}{dp_L}$ and expressing $CS_L(p_L)$ and $CS_H(p_L)$ as a function of p_L

③ $F_L = CS_L(p_L)$

④ $F_H = CS_H(p_H) - (CS_H(p_L) - F_L)$

There were no formulas in - {Lecture 4}
this lecture, only long explanations
I feel lazy to copy. So, be patient, my
child, and study the lecture fully.

Bertrand (price) competition - ~~Lecture 5~~

$p_1 = p_2 = MC$, like in perfect competition

• Hotelling competition - Utility function is given by $U = \bar{s} - p_i - d_i t$ or $U = \bar{s} - p_i - d_i^2 t$ where d is the distance to a firm.

To find demand for each firm's products, solve

$$\bar{s} - p_1 - xt = \bar{s} - p_2 - (1-x)t \text{ or}$$

$$\bar{s} - p_1 - x^2 t = \bar{s} - p_2 - (1-x)^2 t \text{ depending on the } U.$$

Then, use $\frac{d\pi_1}{dp_1}$ and $\frac{d\pi_2}{dp_2}$ to find best response curves.

Cournot competition — if $P = D - q_1 - q_2$
and marginal cost is c_i : fixed costs ↑

$$\Pi_1 = TR_1 - TC_1 = q_1(D - q_1 - q_2) - q_1 c - F$$

$$\frac{d\Pi_1}{dq_1} \Rightarrow q_1 = \frac{D - q_2 - c_1}{2}$$

$$\frac{d\Pi_2}{dq_2} = q_2 = \frac{D - q_1 - c_2}{2}$$

Then, solve them simultaneously. (Substitute q_2 's formula for q_2 in the first equation.)

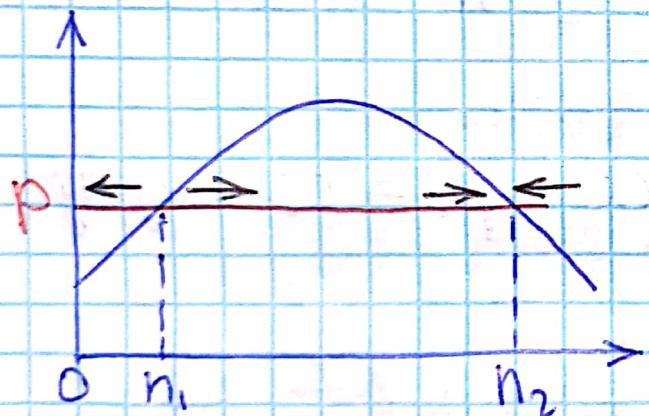
Sequential games — When 1 firm moves before the 2nd firm (e.g. Limit pricing or Capacity Leadership), find the 2nd firm's best response by $\frac{d\Pi_2}{dp_2} = 0$

or $\frac{d\Pi_2}{dq_2} = 0$. Then, use this expression

instead of p_2 or q_2 in the ϑ function.
 Finally, do $\frac{d\pi_i}{dp_i} = 0$ or $\frac{d\pi_i}{dq_i} = 0$ of the new demand function.

- Marginal user-user who is indifferent between buying and not buying. His utility $= 0$.
- Demand for a network:

$$p = a + \delta n(1-n) \text{ when } U = a + \vartheta \delta n - p$$



n_1 is called the critical mass.
 n_2 - sustainable eq'm

- When $U = \vartheta + \alpha n^e$ where $n^e = n_A + \gamma n_B$,

$$g_A = \alpha [q_A + \gamma q_B]. \text{ So,}$$

$$p_A - g_A = p_B - g_B = \hat{p}$$

$$p_i = 1 - (q_A + q_B) + g_i \Rightarrow \text{use Cournot.}$$

- When a two-sided platform Lecture 7
has users of the following type:

$$U_i = \alpha_i t + \lambda_i n_j - p_i$$

stand-alone benefit per-user benefit
↓ ↓
 # of other type of subscribers
 (for advertisers, # of consumers)

Optimal pricing

$$\frac{P_A - (\overbrace{C_A - \alpha_B n_B}^{\text{opportunity cost}})}{P_A} = \frac{1}{\varepsilon_A}$$

Socially optimal price - $p_i = c_i - \lambda_j n_j$

Duopoly in 2-sided markets

$$U'_i = \lambda_i n'_j - p'_i - \alpha t \quad \text{and}$$

$$P_A = C_A + t - \alpha_B ; P_B = C_B + t - \alpha_A$$

$$\frac{p'_i - (c_i - 2\lambda_j n_j)}{p'_i} = \frac{1}{\varepsilon'_i}$$

• A duopolist has a lower opportunity cost/lower prices than a monopolist.

• $U = \delta - \theta t - p_A$ if a

Lecture 8

customer buys from Firm A and is located in θ distance from it.

1) No firm uses data:

$$p_1 = p_2 = t \quad \& \quad \Pi_1 = \Pi_2 = \frac{t}{2}$$

2) Both firms use data:

$$p_A(\theta) = \max\{0, t(1-2\theta)\} \text{ and}$$

$$p_B(\theta) = \max\{0, t(2\theta-1)\} \text{ for old}$$

customers and $p_1 = p_2 = t$ for new customers

3) Only firm A buys info about consumers.

Firm B sets the same price p_B for all.

Firm A sets $p_A(\theta) = p_B + (1-2\theta)t$ for existing customers.

When privacy cost is low, many people will be anonymous, Firm A sets a high price in the anonymous market and Firm B will capture a bigger share of this market. A will be a monopoly in the personalized market.

When privacy cost is high, few people are anonymous. Anonymous market is less biased towards A; A sets lower standard price. B lowers its price & captures a share in both anonymous and personalized markets.

- Herfindahl-Hirschman Index - $\sum_{i=1}^N S_i^2$, where S_i is the share of firm i . HHI is between 0 (perfect competition) and 10,000 (monopoly).

This lecture is purely theoretical. I don't want to deter from reading & enjoying it yourself. Thus, the notes will be stopped here.

Lecture 10

TSM competition derivation

$$U_i' = \alpha_i n_j' - p_i' - \theta t = S_i' - \theta t$$

Indifferent customer of type i

$$S_i' - \theta t = S_i^2 - (1-\theta)t$$

$$(1-\theta)t - \theta t = S_i^2 - S_i'$$

$$-2\theta t = S_i^2 - S_i' - t$$

$$\theta^* = \frac{t - S_i^2 + S_i'}{2t}$$

$$n_i' = D_i' = \{\theta : \theta \leq \theta^*\} = \theta^* \quad D_i^2 = 1 - \theta^* = n_i^2$$

$$n_A' = \frac{t - (\alpha_A n_B^2 - p_A^2) + (\alpha_A n_B' - p_A')}{2t} =$$

$$\begin{aligned}
 &= \frac{t - \alpha_A(1-n'_B) + P_A^2 + \alpha_A n'_B - P_A'}{2t} = \\
 &= \frac{\frac{1}{2} + \frac{\alpha_A(n'_B - 1 + n'_B) - (P_A' - P_A^2)}{2t}}{2t} = \\
 &= \frac{\frac{1}{2} + \frac{\alpha_A(2n'_B - 1) - (P_A' - P_A^2)}{2t}}{2t}
 \end{aligned}$$

$$\begin{aligned}
 \Pi_1 &= D_A' P_A' - D_A' C_A' + D_B' P_B' - D_B' C_B' = \\
 &= D_A'(P_A' - C_A') + D_B'(P_B' - C_B') =
 \end{aligned}$$

~~$$= \frac{1}{2} + \frac{\alpha_A(2n'_B - 1) - (P_A' - P_A^2)}{2t}$$~~

$$n'_A = \frac{1}{2} + \frac{\alpha_A(2n'_B - 1) - (P_A' - P_A^2)}{2t}$$

$$n'_B = \frac{1}{2} + \frac{\alpha_B(2n'_A - 1) - (P_B' - P_B^2)}{2t} =$$

$$= \frac{1}{2} - \frac{(P_B' - P_B^2)}{2t} + \frac{\alpha_B}{2t} \left[1 + \frac{\alpha_A(2n'_B - 1) - (P_A' - P_A^2)}{t} \right]$$

$$= \frac{1}{2} - \frac{P'_B - P''_B}{2t} + \frac{\alpha_B}{2t} \cdot \frac{\alpha_A(2n'_B - 1) - (P'_A - P''_A)}{t}$$

$$= \frac{1}{2} - \frac{P'_B - P''_B}{2t} + \frac{\alpha_B \alpha_A \cdot n'_B}{t^2} + \frac{\alpha_B}{2t} \left[\frac{-\alpha_A - P'_A + P''_A}{t} \right]$$

$$n'_B \cdot \left(1 - \frac{\alpha_A \alpha_B}{t^2} \right) = \frac{1}{2} - \frac{P'_B - P''_B}{2t} + \frac{\alpha_B}{2t} \left[\frac{-\alpha_A - P'_A + P''_A}{t} \right]$$

$$n'_B \cdot \frac{t^2 - \alpha_A \alpha_B}{t^2} = \frac{1}{2} - \frac{P'_B - P''_B}{2t} + \frac{-\alpha_A \alpha_B - \alpha_B P'_A + \alpha_B P''_A}{2t^2}$$

$$n'_B = \frac{t^2}{2(t^2 - \alpha_A \alpha_B)} - \frac{t(P'_B - P''_B)}{2(t^2 - \alpha_A \alpha_B)} + \frac{-\alpha_A \alpha_B - \alpha_B P'_A + \alpha_B P''_A}{2(t^2 - \alpha_A \alpha_B)}$$

$$n'_B = \frac{t^2 - t(P'_B - P''_B) - \alpha_A \alpha_B - \alpha_B (P'_A - P''_A)}{2(t^2 - \alpha_A \alpha_B)}$$

$$n'_A = \frac{t^2 - t(P'_A - P''_A) - \alpha_A \alpha_B - \alpha_A (P'_B - P''_B)}{2(t^2 - \alpha_A \alpha_B)}$$

$$\Pi' = n_A' (P_A' - C_A') + n_B' (P_B' - C_B')$$

$$\frac{d\Pi'}{dP_A'} = \frac{dn_A'}{dP_A'} (P_A' - C_A') + n_A' + \frac{dn_B'}{dP_A'} (P_B' - C_B')$$

$$= \frac{-t(P_A' - C_A')}{2(t^2 - \alpha_A \alpha_B)} + \frac{t^2 - t(P_A' - P_A^2) - \alpha_A \alpha_B - \alpha_A (P_B' - P_B^2)}{2(t^2 - \alpha_A \alpha_B)}$$

$$+ \frac{-\alpha_B (P_B' - C_B')}{2(t^2 - \alpha_A \alpha_B)} = 0$$

$$\text{So, } -t(P_A' - C_A') + t^2 - t(P_A' - P_A^2) - \alpha_A \alpha_B - \alpha_A (P_B' - P_B^2) \\ - \alpha_B (P_B' - C_B') = 0$$

And using $\frac{d\Pi'}{dP_B'}$, we would have

$$-t(P_B' - C_B') + t^2 - t(P_B' - P_B^2) - \alpha_A \alpha_B - \alpha_B (P_A' - P_A^2) \\ - \alpha_A (P_A' - C_A') = 0$$

By symmetry, $P_A' = P_A^2$ and $P_B' = P_B^2$.

$$\text{So, } -t(P_A - C_A) + t^2 - \alpha_A \alpha_B - \alpha_B (P_B' - C_B') = 0$$

$$+t(P_A - C_A) = t^2 - \alpha_A \alpha_B - \alpha_B (P'_B - C'_B)$$

$$P_A - C_A = t - \frac{\alpha_B}{t} (\alpha_A + P_B - C_B)$$

$$P_A = C_A + t - \frac{\alpha_B}{t} (\alpha_A + P_B - C_B)$$

$$P_B = C_B + t - \frac{\alpha_A}{t} (\alpha_B + P_A - C_A)$$

$$P_A = C_A + t - \frac{\alpha_B}{t} (\alpha_A - C_B) - \frac{\alpha_B}{t} P_B =$$

$$= C_A + t - \frac{\alpha_B}{t} \cdot [C_B + t - \frac{\alpha_A}{t} (\alpha_B + P_A - C_A)] =$$

$$= C_A + t - \frac{\alpha_B}{t} (\alpha_A - C_B) - \frac{\alpha_B}{t} [C_B + t - \frac{\alpha_A}{t} P_A$$

$$- \frac{\alpha_A}{t} (\alpha_B - C_A)] = C_A + t - \frac{\alpha_B \alpha_A}{t} + \cancel{\frac{\alpha_B C_B}{t}}$$

$$- \cancel{\frac{\alpha_B C_B}{t}} - \frac{\alpha_B \cdot t}{t} + \frac{\alpha_B \alpha_A}{t^2} P_A + \frac{\alpha_A \alpha_B}{t^2} (\alpha_B - C_A) =$$

$$= C_A + t - \frac{\alpha_B \alpha_A}{t} - \alpha_B + \frac{\alpha_B \alpha_A}{t^2} P_A + \frac{\alpha_A \alpha_B}{t^2} (\alpha_B - C_A)$$

$$P_A \left(1 - \frac{\alpha_A \alpha_B}{t^2}\right) = C_A + t - \frac{\alpha_A \alpha_B}{t} - \alpha_B + \frac{\alpha_A \alpha_B}{t^2} (\alpha_B - C_A)$$

$$P_A = \frac{t^2}{t^2 - \alpha_A \alpha_B} \left[C_A + t - \frac{\alpha_A \alpha_B}{t} - \alpha_B + \frac{\alpha_A \alpha_B}{t^2} (\alpha_B - C_A) \right]$$

$$= \frac{t^2}{t^2 - \alpha_A \alpha_B} \left[C_A - \alpha_B - \frac{\alpha_A \alpha_B}{t^2} (C_A - \alpha_B) + \frac{t^2 \alpha_A \alpha_B}{t} \right] =$$

$$= \frac{t^2}{t^2 - \alpha_A \alpha_B} \left[(C_A - \alpha_B) \left[1 - \frac{\alpha_A \alpha_B}{t^2} \right] + \frac{t^2 \alpha_A \alpha_B}{t} \right] =$$

$$= C_A - \alpha_B + t$$

$$P_A = C_A - \alpha_B + t \quad \text{so, } P_B = C_B - \alpha_A + t$$