

Lesson: recap

| | Objective | Solution: closed-form | Solution: via algorithm | Effect |
|--------|---|--|---|------------|
| LS | $\min_{\beta} y - X\beta _2^2$ | $\hat{\beta} = (X^T X)^{-1} X^T y$ | gradient descent | vanilla |
| Ridge | $\min_{\beta} y - X\beta _2^2 + \lambda \beta _2^2$ | $\hat{\beta} = (X^T X + \lambda I)^{-1} X^T y$ | gradient descent | shrinkage |
| LASSO | $\min_{\beta} y - X\beta _2^2 + \lambda \beta _1$ | unavailable | proximal gradient (ISTA): $\beta_{t+1} = ST_{\lambda\eta} \circ (\beta_t + \eta \cdot X^T (y - X\beta))$ | sparsity |
| Robust | $\min_{\beta} \rho(y - X\beta)$ e.g. $\rho = \cdot _1$ | unavailable | IRLS: cf. cours $D_t = \text{Diag}(\omega(y - X\beta_t))$ $\beta_{t+1} = (X^T D_t X)^{-1} X^T D_t y$ | robustness |