

# Generative Interpretable Visual Design: Using Disentanglement for Visual Conjoint Analysis

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## Abstract

This article develops a method to automatically discover and quantify human-interpretable visual characteristics directly from product image data. The method is generative, and can create new visual designs spanning the space of visual characteristics. It builds on disentanglement methods in deep learning using variational autoencoders, which aim to discover underlying statistically independent and interpretable visual characteristics of an object. The impossibility theorem in the deep learning literature indicates that supervision with ground truth characteristics would be required to obtain unique disentangled representations. However, these are typically unknown in real world applications, and are in fact exactly the characteristics we want to discover. Extant machine learning methods require ground truth labels for each visual characteristic, resulting in a task requiring human evaluation and judgment to both design and operationalize. In contrast, this method postulates the use of readily available product characteristics (such as brand and price) as proxy supervisory signals to enable disentanglement. This method discovers and quantifies human-interpretable and statistically independent characteristics without any specific domain knowledge on the product category. It is applied to a dataset of watches to automatically discover interpretable visual product characteristics, obtain consumer preferences over visual designs, and generate new ideal point designs targeted to specific consumer segments.

**Keywords:** Visual Characteristics; Generative Product Design; Disentanglement; Deep Learning

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## ***INTRODUCTION***

*Visual product characteristics* including shape, size and color are known to be a significant driver of consumer purchase across a wide range of product categories, including automobiles, apparel, furniture, consumer technology products, and even houses (Simonson and Schmitt 1997; Bloch 1995; Heitmann et al. 2020). A recent study by Bloomberg evaluated the economic impact of visual design elements of watches based on the prices paid (Hoffman 2024). Manufacturers like Rolex create different versions of watches that vary along visual design (e.g. color), while retaining the exact same product specifications on all other characteristics. The study found that essentially, a minor change in the bezel color was found to double the price in the secondary market.

The above findings speak to the need to include visual design in quantitative marketing models for accurate forecasts of market demand, as well as segmentation and targeting for new product design. Demand has been traditionally modeled in marketing and economics as being based on underlying product characteristics (Lancaster 1966), but identifying and quantifying visual design characteristics remains a significant challenge. In contrast, structured product characteristics are readily characterized and quantified, e.g., in the automobile market, this may include horsepower and fuel efficiency; in housing, square footage and number of bedrooms; in apparel, size and material.<sup>1</sup>

We develop a method with the following aims related to visual design: a) identifying (discovering) and quantifying human-interpretable visual characteristics from product images, b) obtaining consumer preferences across a range of generated visual designs (visual conjoint), and c) generating novel “ideal point” visual designs targeted to specific consumer segments. Our method of obtaining interpretable visual characteristics could then be used in quantifying consumer preferences, demand responses, and firms’ strategic choices in the visual domain. Discovery and quantification of visual characteristics is a first step in enabling these analyses. Practitioners can also use our method to generate visual designs for prototyping, visually differentiate their products

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<sup>1</sup>We use the terminology since they can be represented in structured data.

from market offerings, and generate new visual designs targeted to consumer segments.

Articulating *why* a product looks appealing and what aspects contribute to such appeal is challenging for consumers, practitioners, and researchers alike (Berlyne 1973). Methods for modeling the visual characteristics of products require significant product knowledge, expertise, and judgment. The expert must *manually* identify and define which visual characteristics adequately represent a product’s visual form (Bloch 1995). Even after defining visual characteristics in this manner, the question remains of how to *quantify* these characteristics. To our knowledge, there is no extant research in marketing that automatically characterizes and quantifies different aspects of visual design in a human-interpretable manner.<sup>2</sup>

**Generative Design for Visual Conjoint:** We demonstrate how to use these quantified visual characteristics in an application of *visual conjoint analysis*. The generative aspect of our method is critically important in obtaining consumer preferences across visual characteristics, since it allows us to automatically generate images that vary the visual design separately along each of the discovered characteristics. We obtain consumer preferences over these discovered visual characteristics using a Hierarchical Bayesian (HB) model, accounting for consumer heterogeneity over observed demographic and psychographic variables. We then show how our method can be used to automatically generate novel and targeted product designs for consumer segments. Specifically, we identify two segments of consumers, and obtain segment-level “ideal points” using their estimated preferences over the disentangled visual characteristics. We then use the generative capability of the method to generate novel designs corresponding to each segment’s most preferred watch design. We qualitatively show these “ideal point” visual designs are differentiated, and quantitatively show they draw choice share away from existing product offerings.

**Methodological Basis:** We build upon the disentanglement stream of literature in representation learning, an area of deep learning, with our primary goal of obtaining interpretable representations

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<sup>2</sup>Our focus here is not on discovering *outlier* characteristics that are particularly *surprising* to humans, especially experts. Rather, it is to identify *and quantify* aspects directly from visual product images and show their use in generative design, all in an automated manner.

from image data. According to Locatello et al. (2019), “the key idea behind this [disentanglement learning] model is that the high-dimensional data [e.g., raw images] can be explained by the substantially lower dimensional and semantically meaningful [to humans] latent variables.” ([]) indicate our additions for clarity).

Disentanglement learning is a form of representation learning (Bengio, Courville, and Vincent 2013), and commonly builds upon variational autoencoders (VAE) (Kingma and Welling 2014). VAEs are comprised of an encoder neural net and decoder neural net, both of which are parameterized by highly nonlinear deep neural networks. The encoder neural net takes high-dimensional unstructured data (images) as input and outputs a latent low-dimensional vector of distributions (embedding of visual characteristics). The VAE uses variational inference, an approximate Bayesian approach, resulting in each of the latent (visual) characteristics represented as distributions rather than “point estimates.” In contrast to (typical) deterministic neural networks such as autoencoders, this stochastic approach helps model uncertainty over visual characteristics via a smooth, continuous, compact, and flexible latent embedding distribution. This modeling is important to obtain a consistent (and interpretable) representation to estimate consumer preferences, as well as smooth and controllable generation of novel visual designs through sampling of different points in the distribution. The decoder neural net takes as input the low-dimensional vector and attempts to reconstruct the original data as output. The idea underlying representation learning is that the “true” dimension of images in the data belonging to a category (e.g., a set of images of watches) is much lower than the dimensionality of the raw images.<sup>3</sup>

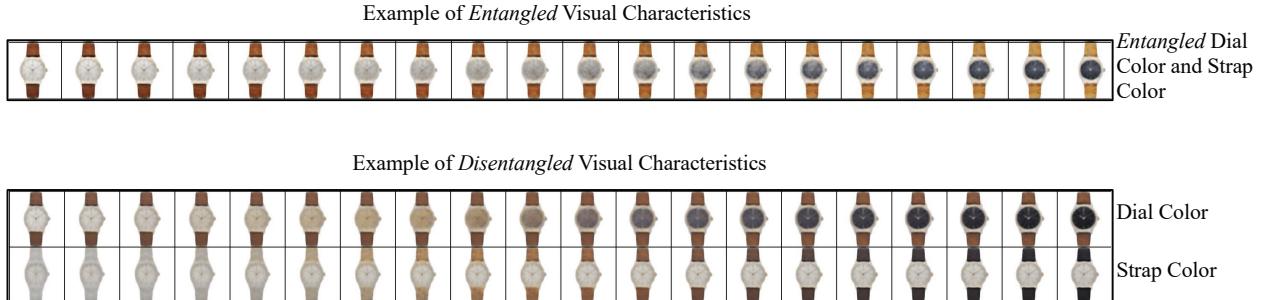
Disentanglement aims to identify a multi-dimensional latent representation in the image data, where each dimension maps one-to-one with a human-interpretable characteristic (Bengio, Courville, and Vincent 2013; Locatello et al. 2019). With a disentangled representation, a change in one latent dimension would result in a change to only one human-interpretable visual characteristic, whereas

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<sup>3</sup>Images are high-dimensional data since even a modest-sized image of  $1,000 \times 1,000$  pixels exists in a  $1,000,000$ -dimensional space. Random images typically cannot be reduced in dimension, but images that belong to a category can typically be represented in much lower dimension. Suppose we know that each of the images represents a black circle on a white background; each image can then be completely represented by the location of the center  $(x, y)$  and radius  $r$  of the circle, essentially making the data three-dimensional.

with an entangled representation, a change in the level across one discovered latent dimension would impact *multiple* human-interpretable characteristics. Figure 1 illustrates the difference between disentangled and entangled representations.

**Figure 1:** (Color Online) Entangled and Disentangled Visual Characteristics



Visual characteristics correspond to dimensions in latent space. Here, we see that the entangled visual characteristic changes both the dial color and strap color as its value is changed. Disentangled characteristics correspond to two independent characteristics for dial color and strap color, so a change in value corresponds to a change in only one visual characteristic.

Disentanglement learning using only images with unsupervised learning has significant limitations, due to a well-known result called the impossibility theorem (Locatello et al. 2019). Recent research recommends using supervised learning with “ground truth” visual characteristics for each data point (i.e., product image) as a supervisory signal (Locatello et al. 2020).<sup>4</sup> However, in our case, and in many practical marketing and business applications, these “ground truth” visual characteristics *are unknown and exactly what we seek to learn*. Our research thus aims to extend recent machine learning developments in disentanglement methods.

**Contribution:** The goal of our method is to *automatically* identify and obtain a disentangled representation of *interpretable* visual characteristics in order to *generate* counterfactual visual designs targeted to consumer preferences. Our method works even in the presence of correlation between these visual characteristics in the original data. Current machine learning approaches use

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<sup>4</sup>Specifically, the prediction problem is to predict the ground truth visual characteristics using the discovered characteristics in the latent representation. For real-world data, researchers first decide on a set of visual characteristics to obtain annotations for, and then ask human coders to quantify the “ground truth” labels corresponding to the chosen set of visual characteristics. For example, in a dataset of celebrity faces, human annotations were created for a wide variety of visual characteristics including eyeglasses, shape of face, wavy hair, mustache, etc. (Liu et al. 2015). Broadly, this manual approach requires identifying the visual characteristics (by researcher), obtaining annotations from multiple human coders, and reconciling these noisy measures to create “ground truth” labels.

ground truth signals separately for each visual characteristic, which are assumed to completely and accurately capture the true underlying data generating process for images. However, the critical challenge is that ground truth is not available in typical applications, and designers expend lots of effort and resources in determining the visual characteristics for products. Our methodology aims to overcome this issue by showing that supervised disentanglement, with structured product characteristics as signals (labels), which are readily-available in typical marketing datasets, can both address known theoretical limitations and improve disentanglement performance to obtain human-interpretable visual characteristics. We evaluate different combinations of signals and find that using multiple signals can be beneficial for disentanglement. We also caution that the choice of supervisory signal(s) is important, with some choices leading to worse disentanglement. Finally, we also compare our method to other approaches for obtaining a low-dimensional representation in the literature, including standard and variational autoencoders in Web Appendix A, and find that none of the compared methods produce human-interpretable characteristics.

Our approach has a number of practical advantages. First, the method is designed to work with unstructured *image data* that would be practically obtainable in real market settings. It does not require labeled data on visual characteristics, and is designed to leverage typically available structured characteristics. Second, the analyst does not define the (unknown) visual characteristics in advance, and does not even need to specify the number of such characteristics that must be discovered. Third, our method is also flexible with regard to image quality, and works with very low resolution images (like 128x128 pixels). Finally, our approach is not very computationally burdensome, and can be applied in a scalable manner across different product categories.

**Application and Results:** We apply our proposed method on two product categories where visual design is known to be relevant. We use watches as the primary product category, and also test the method using sneakers as a second unrelated product category. The disentanglement method on the watch dataset (both images and structured product characteristics) automatically discovers and quantifies six *interpretable* visual characteristics of the watches. These discovered character-

istics correspond to “dial size,” “dial color,” “strap color,” “rim (bezel) color,” “dial shape,”, and “knob (crown) size.”<sup>5</sup> We then evaluate disentanglment performance and human interpretability of the automatically discovered and quantified visual characteristics. These visual characteristics are later used for quantifying consumer preferences and generating targeted “ideal point” product designs.

**Evaluation:** We evaluate our disentanglement method relative to benchmark alternatives in four different ways. First, we use a metric called Unsupervised Disentanglement Ranking (UDR) from the machine learning literature (Duan et al. 2020). We compare the UDR of supervised and unsupervised disentanglement, and find that across product categories, having access to these supervisory signals based on product characteristics improves disentanglement. Second, we examine human interpretability of the discovered visual characteristics by surveying users from the United States using Prolific. We generate visual designs of watches by varying one dimension of the latent representation at a time, corresponding to one visual characteristic. When respondents are asked to determine whether these *changes* are human-interpretable and what the change represents, we find that on average, 86% of respondents agree on the corresponding visual characteristic, indicating that disentanglement helps lead to human-interpretable visual characteristics. Third, we examine whether the quantified level of the visual characteristic is human-interpretable, and find that human respondents and our disentanglement algorithm highly agree (85%). Fourth, we obtain consumer preferences over visual characteristics using visual conjoint analysis by separately varying each visual characteristic. We then use these estimated preferences to predict consumer choices between pairs of watch designs on a holdout sample. We find that our method’s representation with only six visual characteristics obtains higher predictive accuracy than representations learned from more complex machine learning models, such as pretrained deep neural nets that have been trained on millions of images. Fifth, we generate new “ideal point” product designs for two consumer segments defined using estimated preferences. We show these new products align with segment

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<sup>5</sup>The visual depiction and description of the parts of a watch are available at the website: <https://bespokeunit.com/watches/watch-parts-guide/>.

visual preferences, and steal choice share from existing products. Finally, we test the generality of the approach by using the same model architecture in a separate and completely unrelated product category of sneakers. We find that a supervised approach achieves significantly higher disentanglement performance (UDR) than the unsupervised approach. However, a different combination of supervisory signals proves to be better in the sneakers application.

## LITERATURE REVIEW

Visual design is instrumental in shaping consumer preferences, perceptions of value, and experiences across a range of categories. As noted in [Bloch, Brunel, and Arnold \(2003\)](#), “Vegetable peelers, wireless phones, car-washing buckets, and lawn tractors are all being designed with attention to the aesthetic value of their appearance.” Brands follow a process of incorporating visual design including identifying and selecting visual elements and implementing them to impact consumer experiences ([Simonson and Schmitt 1997](#)). Other research has found a positive relationship between aesthetic appeal and usability ([Tractinsky, Katz, and Ikar 2000](#)).

While important, it is currently challenging to characterize and study visual design from a quantitative perspective. As [Orsborn, Cagan, and Boatwright \(2009\)](#) summarize, “... possibly even more challenging, user feedback requires objective measurement and quantification of aesthetics and aesthetic preference.” This work used *7 researcher-defined* visual design characteristics for automobiles and then quantified these characteristics using distances between components in the automobile’s physical design specifications. Likewise, [Landwehr, Labroo, and Herrmann \(2011\)](#) and [Kang et al. \(2019\)](#) both morph visual style of automobiles by identifying feature points representing key design components, while ([Liu et al. 2017](#)) also used this approach to study the impact of product appearance on demand. Recently, [Dew, Ansari, and Toubia \(2022\)](#) and [Burnap, Hauser, and Timoshenko \(2023\)](#) use generative deep models for visual morphing over visual characteristics of logos and automobiles, respectively; however, both works still required definition and quantification over interpretable visual characteristics for use by logo or automobile designers. Broadly, current approaches require human experts to both identify and quantify visual characteristics.

In conceptual contrast, there is a rich literature on methods that aim at automatic, but not interpretable, summarization of data (e.g., MDS, PCA). These methods have been extensively used in marketing (DeSarbo, Ramaswamy, and Cohen 1995). We refer readers to Web Appendix B for a detailed overview of connections with existing marketing methods. Our disentanglement approach aims at *both* automatic and interpretable discovery, and quantification of visual characteristics. This enables their use in common marketing tasks, which in our case involves visual conjoint analysis for generating novel counterfactual “ideal point” visual designs targeted to consumer segments.

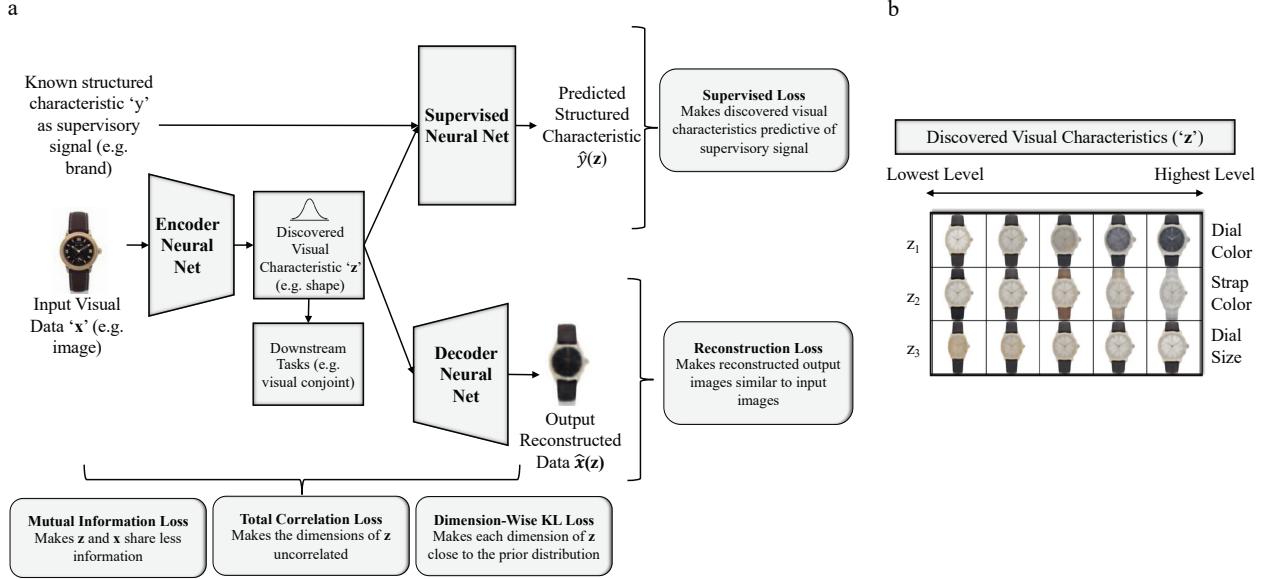
**Representation Learning and Disentanglement** Representation learning is a sub-field of machine learning that posits that the data generating process for real-world high-dimensional data arises from low-dimensional factors. According to Bengio, Courville, and Vincent (2013), representation learning means “learning representations of the data that make it easier to extract useful information when building classifiers or other predictors.” The literature has focused on the properties and the value of different representations for different feature extraction and prediction applications. Representation learning has found success in a wide variety of applications such as natural language processing (Liu, Lin, and Sun 2020), speech recognition (Conneau et al. 2020), causal learning (Schölkopf et al. 2021), and even in the data-driven design of logos, exploring their influence on brand personality (Dew, Ansari, and Toubia 2022).

## ***METHODOLOGY***

Our proposed approach builds on a stream of literature in representation learning known as *disentangled* representation learning, which aims to separate distinct informative factors of variation in the data (Bengio, Courville, and Vincent 2013). An example of disentanglement with simple geometric shapes is provided in Web Appendix C. Disentanglement methods typically build on deep generative models such as variational autoencoders (VAE) (Kingma and Welling 2014) and generative adversarial networks (GAN) (Goodfellow et al. 2020).

The methodology developed here builds upon a VAE designed for disentanglement represen-

**Figure 2:** (Color Online) Schematic of Proposed Disentanglement Approach



*Notes:* **a:** The encoder neural net maps an input image into low-dimensional visual characteristics, which are then used by both the decoder neural net to reconstruct the original image and by the supervised neural net to predict a supervisory signal corresponding to the image. **b:** Varying the levels of discovered characteristics to visualise the semantic meaning encoded by single disentangled visual characteristic of a trained model. In each row the level of a single visual characteristic is varied while the other characteristics are fixed. The resulting effect on the reconstruction is visualised. Note that (1) we show three discovered visual characteristics here for illustration purposes, and (2) this figure only shows disentanglement, not its later use in visual conjoint and generative visual design.

tation learning. Disentanglement refers to the process of decomposing complex data into independent, interpretable factors in order to better capture the true underlying relationships.<sup>6</sup> The method is illustrated in the schematic depicted in Figure 2, and contains an encoder and decoder neural net. The encoder *encodes* visual data to discover a low-dimensional latent space of visual characteristics that are independent and human-interpretable. The discovered visual characteristics are then *decoded* to reconstruct visual representation of the input images using the generative model. The supervised version of the model also *predicts* a supervisory signal (e.g., brand) from the discovered visual characteristics. The model minimizes the weighted sum of 5 different type of losses — reconstruction loss, mutual information loss, total correlation loss, dimension-wise

<sup>6</sup>Burgess et al. (2018) describes this in more detail: “A disentangled representation can be defined as one where single latent units are sensitive to changes in single generative factors, while being relatively invariant to changes in other factors (Bengio, Courville, and Vincent 2013). For example, a model trained on a dataset of 3D objects might learn independent latent units sensitive to single independent data generative factors, such as object identity, position, scale, lighting or colour, similar to an inverse graphics model (Kulkarni et al. 2015). A disentangled representation is therefore factorised and often interpretable, whereby different independent latent units learn to encode different independent ground-truth generative factors of variation in the data.”

Kullbeck-Leibler (KL) loss and supervised loss. Note that the supervisory signal can be just one product characteristic or a combination of product characteristics. We detail the notation used here in Table 1.

### ***Model: Supervised Variational Autoencoder with Disentanglement Losses***

We first describe a variational autoencoder (VAE), the backbone model of our approach, its extension with disentanglement constraints and supervision. We denote the observed dataset  $\mathcal{D} = \{\mathbf{X}, \mathbf{Y}\} = \{(\mathbf{x}_1, \mathbf{y}_1), \dots, (\mathbf{x}_N, \mathbf{y}_N)\}$  where the  $i$ -th observation is a high-dimensional product image  $\mathbf{x}_i$  and its corresponding vector of data that can be used as supervisory signals, denoted  $\mathbf{y}_i$ .

The VAE uses a two-step data generating process  $p(\mathbf{x}, \mathbf{z})$  (Kingma and Welling 2014). The first step samples the visual discovered characteristics denoted by  $\mathbf{z}_i \in \mathbb{R}^J$ , where  $J$  is the number of characteristics to be discovered (or the size of the latent space). In the second step, the original product image  $\mathbf{x}_i$  is reconstructed as  $\hat{\mathbf{x}}_i$  using the conditional distribution  $p_\theta(\mathbf{x}|\mathbf{z})$ . The distribution  $p_\theta$  is specified as a multivariate Gaussian distribution whose probabilities are formed by nonlinear transformation of the characteristics,  $\mathbf{z}$ , using a neural network with parameters  $\theta$ . We add a supervised signal  $\mathbf{y}_i$  that is predicted from the conditional distribution  $p_w(\mathbf{y}|\mathbf{z})$ , which is a function formed by non-linear transformation, with parameters  $w$ , of latent (visual) characteristics  $\mathbf{z}$ .

In practice, neural networks are estimated using optimization methods that result in point estimates of model parameters (Bengio, Courville, and Vincent 2013); in other words, they do not model uncertainty of the conditional distributions described above. Modeling the distribution of the visual characteristics  $\mathbf{z}$  directly allows the characterization of distributional uncertainty over the space of possible neural networks (Blei, Kucukelbir, and McAuliffe 2017). The disentanglement approach uses the distributional aspect of modeling visual characteristics by setting distribution-level penalizations to encourage disentanglement (Kingma and Welling 2014; Chen et al. 2018). Importantly, for this paper, the modeling of distributions is critical to smooth generation of novel counterfactual images, since we are not restricted only to points that are observed in the data.

**Table 1:** Table of Notation for Disentanglement Model

Symbol	Category	Meaning
$\mathbf{x}$	Input Data	Product image
$\mathbf{y}$	Input Data	Supervisory signal(s)
$\hat{\mathbf{x}}$	Output Data	Reconstructed image
$\hat{\mathbf{y}}$	Output Data	Predicted Supervisory Signal(s)
$\mathbf{z}$	Latent Space	Visual characteristic vector
$\mathbf{z}_{\text{inf}}$	Subset of Latent Space	Informative visual characteristic vector
$\mathbf{Z}(\mathbf{i})$	Latent Space	Set of Latent Characteristics for model $i$
$p(\mathbf{z})$	Model	Prior distribution
$p_{\theta}(\mathbf{x} \mathbf{z})$	Decoder Neural Net	Conditional Probability of Generating Image Data given Latent Space
$q_{\phi}(\mathbf{z} \mathbf{x})$	Encoder Neural Net	Conditional Probability of Latent Space given Image Data
$p_w(\mathbf{y} \mathbf{z})$	Supervisory Neural Net	Conditional Probability of Supervisory Signal given Latent Space
$\theta$	Weights of Neural Net	Decoder's parameters
$\phi$	Weights of Neural Net	Encoder's parameters
$w$	Weights of Neural Net	Supervisory Net's parameters
$\mathbf{E}_{q_{\phi}(\mathbf{z} \mathbf{x})} [\log p_{\theta}(\mathbf{x} \mathbf{z})]$	Loss Function	Reconstruction Loss
$I_q(\mathbf{z}, \mathbf{x})$	Loss Function	Mutual Information Loss
$KL \left[ q(\mathbf{z})    \prod_{j=1}^J q(z_j) \right]$	Loss Function	Total Correlation Loss
$\sum_{j=1}^J KL [q(z_j)    p(z_j)]$	Loss Function	Dimension KL Divergence Loss
$P(\hat{\mathbf{y}}(\mathbf{z}), y)$	Loss Function	Supervised Loss
$\mathcal{L}(\theta, \phi, \beta; \mathbf{x}, \mathbf{z})$	Loss Function	Total Loss
$J$	Hyperparameter	Dimensionality of latent space
$\alpha$	Hyperparameter	Weight on Mutual Information Loss
$\beta$	Hyperparameter	Weight on Total Correlation Loss
$\gamma$	Hyperparameter	Weight on Dimension KL Divergence Loss
$\delta$	Hyperparameter	Weight on Supervised Loss

The VAE specifically builds on the variational Bayesian inference literature to incorporate neural networks within an approximate Bayesian framework (Blei, Kucukelbir, and McAuliffe 2017). In short, while the neural networks parameterizing the distributions of interest are estimated using point estimates of their parameters  $(\theta, \phi, \mathbf{w})$ , we learn full distributions over the visual characteristics  $\mathbf{z}$ . We refer to  $p_\theta(\mathbf{x}|\mathbf{z})$  as the decoder neural net,  $q_\phi(\mathbf{z}|\mathbf{x})$  as the encoder neural net, and  $p_{\mathbf{w}}(\mathbf{y}|\mathbf{z})$  as the supervised neural net. Given that the “true” unknown posterior  $p(\mathbf{z}|\mathbf{x})$  is intractable, the variational Bayesian framework approximates this posterior to maximize a lower bound to, rather than, the likelihood of the posterior (and thus DGP) itself (Blei, Kucukelbir, and McAuliffe 2017). We adopt the conventional VAE assumption by parametrizing this approximate posterior with a multivariate Gaussian with diagonal covariance matrix specified as  $\log q_\phi(\mathbf{z}|\mathbf{x}) = \log \mathcal{N}(\mathbf{z}; \boldsymbol{\mu}, \boldsymbol{\sigma}^2 \mathbf{I})$ , where  $\boldsymbol{\mu}$  and  $\boldsymbol{\sigma}$  are the mean and the standard deviation of the approximate posterior (Kingma and Welling 2014).

We simultaneously train the encoder neural net, the decoder neural net and the supervised neural net by minimizing a variational bound of the negative log-likelihood. In practice, this is specified as a loss minimization problem to find point estimates of the neural network parameters,  $(\theta, \phi, \mathbf{w})$ , while inferring a full distribution over the discovered characteristics,  $\mathbf{z}_i \in \mathbb{R}^J$ . The parameter space of the deep neural networks in our intended applications are typically in the range of hundreds of thousands to hundreds of millions depending on architectural choices (e.g., our specific architecture has 1,216,390 parameters).

The overall loss is composed of several loss terms corresponding to a VAE extended with supervision and disentanglement terms. We detail these losses starting with the loss of the original VAE in Equation (1), and refer readers to Kingma and Welling (2014) for its detailed derivation. The reconstruction loss captures the differences between the reconstructed images generated by the decoder and the original inputs. Minimizing only this term would obtain a deep net that is able to generate images that match the input with high fidelity. The regularizer term ensures that the aggregate distribution of the latent variables does not deviate too much from the prior. This ensures that the latent space becomes structured and shares the properties of the prior distribution, such as

compactness, smoothness and continuity.

$$\underbrace{\mathcal{L}(\theta, \phi, \mathbf{w}; \mathbf{x}, \mathbf{z})}_{\text{Total Loss}} = \underbrace{-\mathbf{E}_{q_\phi(\mathbf{z}|\mathbf{x})} [\log p_\theta(\mathbf{x}|\mathbf{z})]}_{\text{Reconstruction Loss}} + \underbrace{KL [q_\phi(\mathbf{z}|\mathbf{x})||p(\mathbf{z})]}_{\text{Regularizer Term}} \quad (1)$$

To learn disentangled representations, the  $\beta$ -VAE model (Higgins et al. 2017) extends Equation (1) by imposing a heavier penalty on the regularizer term using an adjustable hyperparameter  $\beta > 1$ . The idea is that disentangled representations are likely to be less complex and lower dimensional than entangled representations that also demonstrate statistical independence. The regularizer, which penalizes information capacity of the latent variables, therefore promotes disentanglement (Burgess et al. 2018).

Higgins et al. (2017) derive the  $\beta$ -VAE loss function as a constrained optimization problem. Specifically, the goal is to minimize the reconstruction inaccuracy subject to the inferred visual characteristics being matched to a prior isotropic unit Gaussian distribution. This can be seen in Equation (2) where  $\epsilon$  specifies the strength of the applied constraint.

$$\min_{\theta, \phi} -\mathbf{E}_{q_\phi(\mathbf{z}|\mathbf{x})} [\log p_\theta(\mathbf{x}|\mathbf{z})] \text{ subject to } KL [q_\phi(\mathbf{z}|\mathbf{x})||p(\mathbf{z})] < \epsilon \quad (2)$$

We can re-write Equation (2) as a Lagrangian under the KKT conditions (Karush 1939), where the KKT multiplier  $\beta$  is a regularization coefficient. This coefficient  $\beta$  is used as a hyperparameter to flexibly promote disentanglement, and results in the  $\beta$ -VAE formulation in Equation (3).

$$\min_{\theta, \phi} -\mathbf{E}_{q_\phi(\mathbf{z}|\mathbf{x})} [\log p_\theta(\mathbf{x}|\mathbf{z})] + \beta KL [q_\phi(\mathbf{z}|\mathbf{x})||p(\mathbf{z})] \quad (3)$$

Intuitively,  $\beta$ -VAE uses the hyperparameter  $\beta$  to sacrifice reconstruction accuracy in order to learn more disentangled representations. This framework is adapted and further extended by decomposing the regularizer term in Equation (1) into three terms (Chen et al. 2018; Hoffman and Johnson 2016; Kim and Mnih 2018). These three terms enable us to directly and separately control disentanglement constraints of the model as follows in Equation (4).

$$\underbrace{KL [q_\phi(\mathbf{z}|\mathbf{x})||p(\mathbf{z})]}_{\text{Regularizer Term of Total Loss}} = \underbrace{I_q(\mathbf{z}, \mathbf{x})}_{\text{Mutual Information Loss}} + \underbrace{KL \left[ q(\mathbf{z}) || \prod_{j=1}^J q(z_j) \right]}_{\text{Total Correlation Loss}} + \underbrace{\sum_{j=1}^J KL [q(z_j)||p(z_j)]}_{\text{Dimension-Wise KL Divergence Loss}} \quad (4)$$

Finally, we add a supervised loss term to enforce the discovered characteristics to help predict the supervisory signal(s)  $\mathbf{y}$  in Equation (5). This enables us to study whether using typical structured data (e.g., ‘brand’) with a supervised model helps improve disentanglement, and to compare supervised versus unsupervised disentanglement.

$$\underbrace{\mathcal{L}(\theta, \phi, \mathbf{w}); \mathbf{x}, \mathbf{z}}_{\text{Total Loss}} = \underbrace{-\mathbf{E}_{q_\phi(\mathbf{z}|\mathbf{x})} [\log p_\theta(\mathbf{x}|\mathbf{z})]}_{\text{Reconstruction Loss}} + \alpha \underbrace{I_q(\mathbf{z}, \mathbf{x})}_{\text{Mutual Information Loss}} + \beta \underbrace{KL \left[ q(\mathbf{z}) || \prod_{j=1}^J q(z_j) \right]}_{\text{Total Correlation Loss}} + \gamma \underbrace{\sum_{j=1}^J KL [q(z_j)||p(z_j)]}_{\text{Dimension-Wise KL Divergence Loss}} + \delta \underbrace{P(\hat{\mathbf{y}}(\mathbf{z}), \mathbf{y})}_{\text{Supervised Loss}} \quad (5)$$

The total loss is comprised of five terms weighted using hyperparameters,  $(\alpha, \beta, \gamma, \delta)$ . Adjusting these hyperparameters impacts the relative weight of each loss term and directly affects disentanglement performance. We detail the intuition for these loss terms below.<sup>7</sup>

*Reconstruction Loss:* Penalizing the reconstruction loss encourages the reconstructed output  $\hat{\mathbf{x}}(\mathbf{z})$  to be as close as possible to the input data  $\mathbf{x}$ . This ensures that the discovered characteristics possess the necessary information to be able to reconstruct the product image with high fidelity. We use L1 Loss (Absolute Error Loss) because unlike an L2 Loss (Squared Error Loss), it is more robust to outliers. Moreover, L1 loss introduces sparsity and thus, allows the model to focus on fewer important characteristics for reconstruction.

*Mutual Information Loss:*  $I_q(\mathbf{z}, \mathbf{x}) = \mathbf{E}_{q(x,z)} \log \left( \frac{q(x,z)}{q(x)q(z)} \right)$  is the mutual information between

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<sup>7</sup>Note that adjusting these hyperparameters also leads to different models as special cases. In the original VAE,  $\alpha = \beta = \gamma = 1$  and  $\delta = 0$ . In the  $\beta$ -VAE,  $\alpha = \beta = \gamma > 1$  and  $\delta = 0$ , meaning that a heavier penalty is imposed on all three terms of the decomposed regulariser term in Equation (4). Finally, in  $\beta$ -TCVAE,  $\alpha = \gamma = 1$ ,  $\beta > 1$  and  $\delta = 0$  and thus there is a heavier penalty only on the total correlation loss term. In our proposed supervised approach, we impose  $\alpha = \gamma = 1$  and find levels of the hyperparameter set  $\Omega = \{\beta, \delta\}$ . We compare it with an unsupervised approach in which we impose  $\alpha = \gamma = 1, \delta = 0$  and find the levels of the hyperparameter set  $\Omega = \{\beta\}$ .

the discovered visual characteristic  $\mathbf{z}$  and the product image  $\mathbf{x}$ . From an information-theoretic perspective (Achille and Soatto 2018), penalizing this term reduces the amount of information about  $\mathbf{x}$  stored in  $\mathbf{z}$ . The information needs to be sufficient to reconstruct the data while avoiding storing nuisance information, minimizing copying of the input data. A low  $\alpha$  would result in  $\mathbf{z}$  storing nuisance information, whereas a high  $\alpha$  could result in the loss of sufficient information needed for reconstruction.

*Total Correlation Loss:* The total correlation loss,  $KL \left[ q(\mathbf{z}) \parallel \prod_{j=1}^J q(z_j) \right]$ , represents a measure of dependence of multiple random variables in information theory (Watanabe 1960). If the discovered latent variables  $\mathbf{z}$  are independent, then the KL divergence is zero. More generally, a high penalty for the total correlation term forces the model to find statistically independent visual characteristics. A high  $\beta$  results in a more disentangled representation but with potentially worse reconstruction quality (and other loss terms).

*Dimension-Wise KL Loss:* The dimension-wise KL loss term,  $\sum_{j=1}^J KL [q(z_j) \parallel p(z_j)]$ , penalizes the objective to push  $q(z_j)$  closer to the prior  $p(z_j)$ , encouraging the distribution of each latent dimension to not deviate from the prior (e.g., Gaussian) of each dimension. A high weight on this term reduces the number of discovered visual characteristics, and sets a higher bar for allowing an additional informative dimension. It ensures that each learned representations in the latent space has the desired properties of the prior distribution, such as compactness, smoothness, and continuity (Hoffman and Johnson 2016).

*Supervised Loss:* Penalizing the supervised loss  $P(\hat{\mathbf{y}}(\mathbf{z}), \mathbf{y})$ , where  $\hat{\mathbf{y}}(\mathbf{z}) \sim p_{\mathbf{w}}(\mathbf{y}|\mathbf{z})$  prioritizes the discovered visual characteristics  $\mathbf{z}$  to obtain high accuracy in predicting  $\mathbf{y}$ . We set the level of the hyperparameter  $\delta$  by model selection, and note that  $\delta = 0$  for the *unsupervised* disentanglement approach. Since our signals are discrete (e.g. brand), we use cross-entropy loss for the multiclass classification prediction task. Continuous signals like price are discretized using a quantile split to obtain discrete classes.

## ***Supervised and Unsupervised Disentanglement***

A key issue we examine in this research is whether structured product characteristics typically found in marketing contexts (e.g., brand, price etc.) can be used as supervisory signals to improve disentanglement, and also our ability to discover human-interpretable visual characteristics. Locatello et al. (2019), in a well-known impossibility theorem, showed that in the absence of a supervisory signal, disentangled representations are probabilistically equivalent to (an infinite set of) entangled representations. This finding implies that it is not possible to obtain a unique disentangled representation of the visual characteristics using an unsupervised approach. Locatello et al. (2020) further experimentally demonstrated that this challenge could be resolved by using *supervision with ground truth visual characteristics*, in which lower supervised loss is connected to better disentanglement performance.

However, their approach of knowing ground truth for each of the visual characteristics across multiple products cannot be used for our goal of *automatic* discovery and quantification of visual characteristics. The ground truth labels corresponding to visual characteristics *are precisely what we are aiming to discover*. Moreover, we would need a researcher to apply their judgment and define visual characteristics in advance for the product category, as well as quantify each of them for the products in the dataset, implying the approach would not be automated. Our method instead posits that structured product characteristics and price might have information that correlates with visual characteristics, and using them as supervisory signals can be helpful in achieving disentanglement. Therefore, our method has a major advantage that it does not require access to ground truth characteristics.

**Why might structured characteristics serve as good supervisory signals?** Typical structured product characteristics commonly available in marketing data include brand, material, performance characteristics and price. Material more broadly is known to significantly affect visual appearance and consumer perceptions (Fleming 2014), e.g. being made of metal (like silver) provides a certain visual look. Similarly, brand can have a strong impact on the visual look. Consider, for instance

the distinct look of a Mercedes-Benz car or a Louis Vuitton handbag. “Brand signature” is often perceptible in visual design, especially for product categories with conspicuous consumption (Simonsen and Schmitt 1997) and for luxury brands (Lee, Hur, and Watkins 2018). Research has shown that brands have different personalities (Aaker 1997) that can be expressed through their product-related characteristics, product category associations, brand name, symbol or logo, advertising style, price, distribution channel and user imagery (Batra, Lehmann, and Singh 1993; Liu, Dzyabura, and Mizik 2020). Consumers also recognize unique visual styles of brands (Ward et al. 2020). Next, consider the role of price. Many brands, especially luxury brands, maintain carefully curated pricing tiers with strong consumer associations, and in many categories, high-priced products are viewed as having a “premium look” (Cho, Lee, and Saini 2022).

**Evaluating Disentanglement Performance:** To evaluate disentanglement performance, we need a metric that is applicable even when ground truth is not available, and therefore works for both supervised and unsupervised disentanglement. We evaluate disentanglement performance using a metric called Unsupervised Disentanglement Ranking (UDR), which satisfies the above requirements. UDR is a metric ranging from 0 to 1, with higher values representing more disentangled representations. UDR crucially allows for an automated way to select a model *when ground truth is not available* (Duan et al. 2020).<sup>8</sup>

The UDR metric is based on the assumption that representations obtained from models that are more disentangled would be more similar to each other than those from models that do not disentangle as well. This implies that given a dataset and a model, the visual characteristics learned using different random seeds (or different initial conditions) with a disentangled model should be similar, whereas every entangled representation is different in its own way and there are several ways to obtain entangled representations, since the set of entangled representations is very large and potentially infinite. We note that while the model defines all the hyperparameter levels, the random seed levels only determine the initial levels of the parameters for the neural net and any

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<sup>8</sup>Most existing metrics in the machine learning literature such as  $\beta$ -VAE metric (Higgins et al. 2017), the FactorVAE metric (Kim and Mnih 2018), Mutual Information Gap (MIG) (Chen et al. 2018), and DCI Disentanglement scores (Eastwood and Williams 2018) require access to the ground truth data generating process and are therefore not suitable for our empirical setting.

sampling within the algorithm (e.g., dataset splitting or batch-level data sampling during training). If the disentanglement model is discovering the ground truth representation, then the initial parameters should not matter as much.

**Defining UDR:** Unsupervised Disentanglement Ranking (UDR) is defined for a pair of models  $i$  and  $j$  using Equation 6. For any pair of models  $i$  and  $j$ ,  $UDR_{ij}$  is defined as a pairwise metric.

$$UDR_{ij} = \frac{1}{d_i + d_j} \left[ \sum_{b \in \mathbf{Z}(j)} \frac{r_b^2}{\sum_{a \in \mathbf{Z}(i)} R(a, b)} I_{KL}(b) + \sum_{a \in \mathbf{Z}(i)} \frac{r_a^2}{\sum_{b \in \mathbf{Z}(j)} R(a, b)} I_{KL}(a) \right] \quad (6)$$

In the above equation,  $R(a, b)$  is the correlation between the visual characteristic  $a$  that belongs to model  $i$  and the visual characteristic  $b$  that belongs to model  $j$ . We show the definition in Equation 7.

$$R(a, b) = \text{cor}(z_i(a), z_j(b)) \quad (7)$$

The term  $r_a$  is the correlation of the visual characteristic in model  $j$  that is most similar to the visual characteristic  $a$  in model  $i$ . In other words,  $r_a$  can be defined using Equation 8.

$$r_a = \max_{b \in \mathbf{Z}(j)} \text{cor}R(a, b) \quad (8)$$

The right hand side of Equation 6 has two terms inside the square bracket. The first term  $\frac{r_b^2}{\sum_{a \in \mathbf{Z}(i)} R(a, b)}$  represents the ratio of the (squared) correlation of the visual characteristic  $a$  in model  $i$  that is most similar to visual characteristic  $b$  in model  $j$ , to the sum of the correlations across *all the visual characteristics* in model  $i$ . The squaring ensures that corner solutions or one-to-one mappings lead to higher UDR values, which is consistent with the idea of disentanglement. This term will be higher if there is a one-to-one mapping between one visual characteristic in model  $i$  and another in model  $j$ , and the characteristics are statistically uncorrelated. The first term is then added across all the informative visual characteristics  $b$  of model  $j$ , which are represented by  $I_{KL}(b)$  using a threshold for KL divergence between the characteristic's posterior and the prior. The second term represents the counterpart by considering one visual characteristic  $a$  that belongs

to model  $i$  and then going through the corresponding process described above. Finally, we sum across all the informative visual characteristics  $a$  of model  $i$ , i.e.,  $I_{KL}(a)$ .

We normalize this sum above by the total number of informative visual characteristics from model  $i$  and model  $j$ , denoted  $(d_a + d_b)$ . This is done to ensure that just having more informative characteristics does not mechanically lead to a higher UDR. Therefore,  $UDR_{ij}$  can be considered as the average correspondence in informative visual characteristics between two models  $i$  and  $j$ , and with a perfect and complete one-to-one correspondence, we will have  $UDR_{ij} = 1$ . We calculate the final UDR score for a particular hyperparameter configuration by averaging the UDR across all pairs of random seeds.

**What Does UDR Capture?** UDR captures the idea of similarity of two visual representations, which in turn are comprised of multiple visual characteristics. A pair of visual characteristics  $a$  and  $b$  from models  $i$  and  $j$  respectively, denoted  $z_{i,a}$  and  $z_{j,b}$  would be scored as highly similar if they are axis-aligned with each other (i.e., correlate) up to *permutation* and *sign inverse*. By permutation, we mean that the same ground truth factor  $c_k$  may be encoded by different visual characteristics within the two models  $z_{i,a}$  and  $z_{j,b}$  where  $a \neq b$ . By sign inverse, we mean that the two models may learn to encode the levels of the generative factor in the opposite order to each other,  $z_{i,a} = -z_{j,b}$ . Models that are identical except for sign inverse and permutation are isomorphic and equivalent from a representation learning viewpoint.

We additionally note that the UDR metric in Equation 6 is flexible enough to account for *subsetting*, i.e., non-overlapping subsets of visual characteristics that another model has learned. While we did not observe this case in our empirical results, we found that changing the supervisory signal led to the discovery of different subsets of visual characteristics (see Web Appendix D). We note that differing hyperparameter settings resulted in models with different numbers of latent dimensions to be “switched off.”

**Operationalizing UDR:** For each trained model, i.e. with  $N_{seed} = 10$  random seeds, each of the representations obtained is compared pairwise with the others. Thus, we perform  $\kappa =$

$\binom{N_{seed}}{2} = 45$  pairwise comparisons with all other models trained with the same hyperparameters ( $\beta$ ,  $\delta$ ), and the same vector of supervisory signals but with different seed levels. From these pairwise comparisons, we obtain  $UDR_{ij}$ , where  $i$  and  $j$  index the two models. UDR is then averaged across all combinations of  $i$  and  $j$ .

We next select informative visual characteristics and ignore uninformative visual characteristics. To implement this, we obtain the  $KL[q_\phi(\mathbf{z}|\mathbf{x})||p(\mathbf{z})]$  for each visual characteristic and then select characteristics with KL divergence above a threshold. Variation across an uninformative characteristic would produce little to zero visual change in the image. [Rolinek, Zietlow, and Martius \(2019\)](#) showed that during training, models based on VAEs enter a *polarized regime* such that some latent variables (in our case, visual characteristics) switch off by being reduced to the prior  $q_\phi(z_j) = p(z_j)$ . This is due to the choice of a diagonal posterior. Typically, the dimensionality of the latent space is set higher than the expected true set of visual characteristics. This results in some of the characteristics being “switched off” or being very close to the prior distribution. These switched off characteristics are referred to as uninformative characteristics. [Duan et al. \(2020\)](#) showed that models with some uninformative characteristics tend to disentangle better and their unstructured (visual) characteristics are easier to semantically interpret.

### ***Model Training, Selection, and Evaluation***

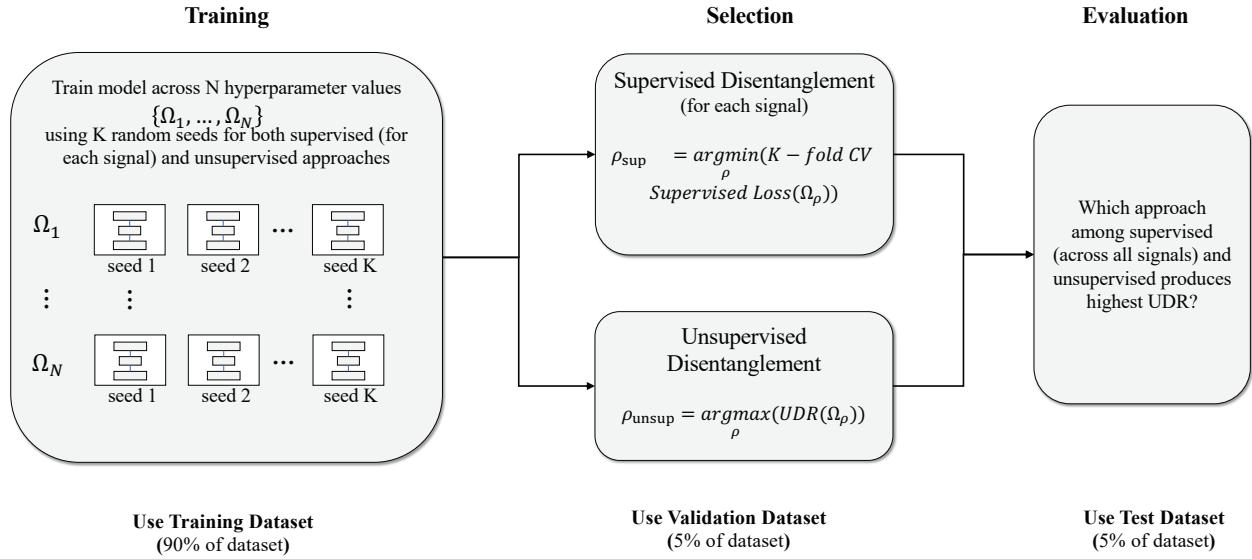
Both the supervised and unsupervised disentanglement approaches require model training (i.e., learning model parameters), model selection (i.e., choosing hyperparameters), and model evaluation (i.e., UDR disentanglement performance). However supervised and unsupervised approaches require different model training and selection steps, while the same evaluation step can be used, so we can compare them appropriately.

**Model Training and Selection:** We divide the dataset into (a) a training dataset for learning disentangled representations, (b) a validation dataset for model selection, and (c) a test dataset in the ratio 90 : 5 : 5. To avoid data leakage, we ensure that each product is present only in one of the above subsets. Figure 3 provides a schematic diagram for the model training and selection for the

supervised and the unsupervised approaches. The training process takes in the unstructured data (watch images) as input, and uses a subset of structured watch characteristics (e.g., brand) as the supervisory signal to the model.

We fix the hyperparameters based on suggestions in the literature (Locatello et al. 2020; Chen et al. 2018). The number of latent codes  $J$  represents the number of characteristics that our model aims to find. A very low  $J$  might miss important characteristics, whereas a high value of  $J$  might lead to more uninformative characteristics. We choose  $J = 20$  to balance these considerations, based on our empirical setting. We find that higher values of  $J$  do not result in any meaningful change in the discovered visual characteristics. We need to tune other hyperparameters including learning rate, batch size and number of training steps or epochs.<sup>9</sup>

**Figure 3:** Model Training, Selection, & Evaluation



*Notes:* We train  $N$  different hyperparameter ( $\Omega$ ) levels for both supervised and unsupervised approaches. For supervised approaches, we choose the hyperparameter level that minimize the supervised loss  $P(\hat{y}(\mathbf{z}), y)$  on the validation dataset. For the unsupervised approach, we choose the hyperparameter level that maximise the UDR. We evaluate different sets of visual characteristics learned by various approaches using the UDR metric.

<sup>9</sup>The considerations for tuning hyperparameters detailed below are common to all deep learning models. A very low learning rate can lead the model to get stuck on a local minima or converge very slowly and a very high learning rate can lead the model to overshoot the minima. A low batch size increases the time required to train the model till convergence while a large batch size significantly degrades the quality of the model so that it is not generalizable beyond the training dataset. Training for low number of epochs may result in the model not converging, whereas training for a very high number of epochs may result in the model overfitting on the train dataset. Specifically, we choose the number of random seeds used as 1 to 10; Adam optimizer with learning rate 5e-4 and parameters  $b_1 = 0.9$  and  $b_2 = 0.999$ ; batch size as 64; number of epoch as 100.

In order to select the model with appropriate hyperparameters, we sweep over levels of hyperparameters corresponding to  $\beta$  (weight on the total correlation loss term) and  $\delta$  (weight on the prediction loss term).<sup>10</sup> In the unsupervised approach  $\delta = 0$  by definition.<sup>11</sup> Finally, we retrain the model on the entire training dataset with the selected hyperparameters, and then use the trained model to extract discovered visual characteristics on the test dataset. For model evaluation, we compare all models using the UDR metric.

**Model Architecture:** We modify the architecture used in [Burgess et al. \(2018\)](#) in order to use images with a resolution of  $128 \times 128$  pixels as well as to incorporate a supervised neural net. We use Convolutional Neural Net (CNNs) to construct the encoder neural net, where we stack a sequence of CNN layers to learn high-level concepts for images. Finally, we introduce 2 fully-connected (FC) layers to first flatten the output of the sequence of CNN layers and then reduce the number of dimensions in order to learn  $J$  visual characteristics. The decoder neural net is the transpose of the encoder neural net, and is designed to reconstruct the image from the  $J$ -dimensional latent visual characteristics. Finally, we include fully connected layers to the discovered visual characteristics to create the supervised neural net that predicts the signals (structured product characteristics). Further details of the architecture are provided in [Web Appendix E](#).

**Generating New Visual Designs:** We exploit the generative nature of the disentanglement learning model to controllably generate produce images. We feed the decoder of the disentanglement model a vector whose each dimension corresponds to a latent representation,  $\mathbf{z}$ . Recall that if the model achieves disentanglement, then  $\mathbf{z}$  should be human-interpretable. More specifically, each element of the vector  $\mathbf{z} = (z_1, z_2, \dots, z_{J_{inf}})$  corresponds to a specific visual characteristic, e.g. dial color. Note that  $J_{inf}$  corresponds to the number of informative visual characteristics discovered by the model. Thus, when we choose values of the vector  $\mathbf{z}$ , the model is able to generate a visual design. We can thus controllably generate a wide range of visual designs corresponding to

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<sup>10</sup>For each  $\beta$  and  $\delta$  level, following [Locatello et al. \(2020\)](#), we select the hyperparameter setting corresponding to the lowest 10-fold cross-validated supervised loss for supervised model selection.

<sup>11</sup>We use Unsupervised Disentanglement Ranking (UDR) for unsupervised model selection.

any specified vector  $\mathbf{z}$ . Since the decoder can take input at any point in the latent space, the model can generate novel visual designs not present in the original product image data. We show how these generated visual designs can be used for conducting visual conjoint analysis.

## ***EMPIRICAL APPLICATION***

We use our disentanglement method with an application to a dataset of watches. This dataset satisfies several desiderata detailed below. First, we would like a product category where visual and design aspects captured in the images are likely to play an important role in consumer valuation and choice behavior ([Kotler and Rath 1984](#)). Second, we would like a market with a large number of products in order to train the deep learning algorithm. Third, as with typical marketing data, we need to have a set of structured characteristics appropriately matched up with the images. Finally, for our validation exercise, human respondents need to be familiar with the product category in order to evaluate the interpretability of the discovered visual characteristics.

### ***Data***

Our data includes 6,187 watches corresponding to 2,963 unique brand-models auctioned, spanning the years 2010 – 2020. The data on watches is particularly appropriate for the reasons above. For each auctioned watch in the dataset, we have its image, structured product characteristics, and the hammer price paid at the auction. Structured characteristics include the brand of the watch, model of the watch, year of manufacture or *circa*, type of movement associated with the watch, dimensions of the watch and materials used in the watch. Figure 4 shows a sample of watch images in our dataset. The hammer price (in \$1000s) are in inflation-adjusted year 2000 dollars.

A total of 199 unique brands are present in the data. Audemar’s Piguet, Cartier, Patek Philippe and Rolex are the four brands with the largest share of observations, while the remaining brands are coded as Others. Circa is coded as Pre-1950, 1950s, 1960s, 1970s, 1980s, 1990s, 2000s and 2010s. Movement of a watch is classified as either mechanical, automatic or quartz. Dimensions of the watch refers to the watch diameter in case of a circular dial or the length of the longest edge

**Figure 4:** (Color Online) Sample of Watches



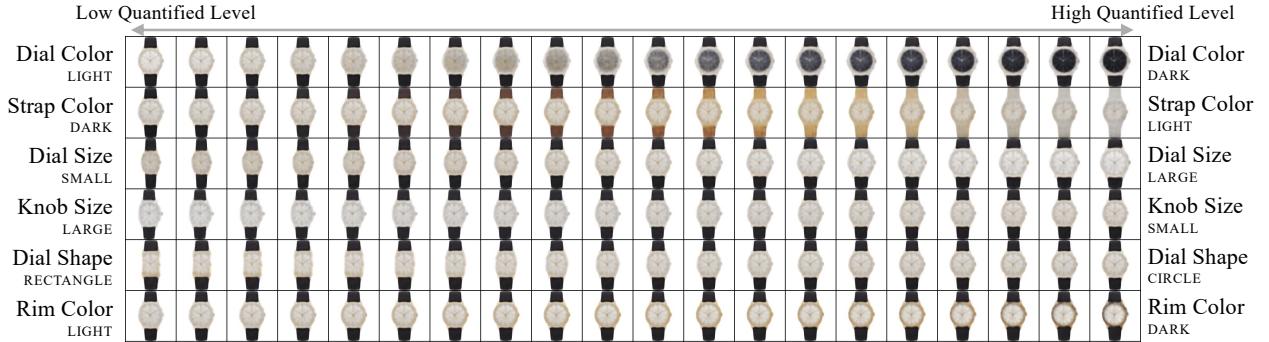
in case of a rectangular dial (in millimeters). Material is coded as gold, steel, a combination of gold and steel or other materials. Summary statistics of the data are provided in Web Appendix F.

### Results: Discovered Visual Characteristics

Figure 5 illustrates the output of the disentanglement model with supervisory signals “Brand + Circa + Movement,” showing discovered visual characteristics corresponding to the signals with the highest UDR. Each row of the figure demonstrates how the watch design changes based on changes in levels of *one specific* discovered visual characteristic, while keeping all the other characteristics fixed. We only show 6 visual characteristics as the others were found to be uninformative. By uninformative, we mean that traversing along those dimensions leads to no visual changes, and the posterior distribution of the discovered latent variable is almost identical to pure Gaussian noise. From ex-post human inspection (by researchers), we observe six distinct visual characteristics that are independent as well as human-interpretable. These are labeled ‘dial color’, ‘strap color’, ‘dial size’, ‘knob (crown) size’, ‘dial shape’, and ‘rim (bezel) color’.

Figure 6 shows the density plot of these discovered visual characteristics. All visual characteristics are initially modeled by a standard normal prior distribution. In the training process, each visual characteristic is encoded in the representation as a continuous distribution. If the algorithm finds a lot of variation along the visual characteristic in the image data, then we would observe the variance of that characteristic to increase. In contrast, if the algorithm finds little variation on some visual characteristic, e.g., if all watches have circular dials, the posterior distribution for this dimension would have a low variance. It is important to note that we do not artificially constrain the scale of the visual characteristics, and allow the model to discover it from the data. Summary

**Figure 5:** (Color Online) Discovered Visual characteristics



*Notes:* Latent traversals along a *focal watch* used to visualise the semantic meaning encoded by single visual characteristic learnt by a trained model. In each row, the quantitative level of a single characteristic is varied keeping the other characteristics fixed. The resulting reconstruction is visualized. Discovered visual characteristics are learned by supervising the characteristics to predict both the brand, circa and movement simultaneously.

statistics of the visual characteristics are provided in Web Appendix G.

The sign (negative or positive) is arbitrary. For example, with dial size, negative might imply large dials, whereas positive might imply smaller dials. The sign might also be reversed, and both representation would be equally valid (in fact, isomorphic). As the literature on disentanglement has pointed out, representations with different permutations (of latent dimensions) and signs are equivalent (Duan et al. 2020). Thus, the numbers corresponding to the latent dimension do represent “size” in the image in a monotonic sense. Thus, knowing the latent visual characteristic can permit the model to generate a product image with a specific size, or the inverse.

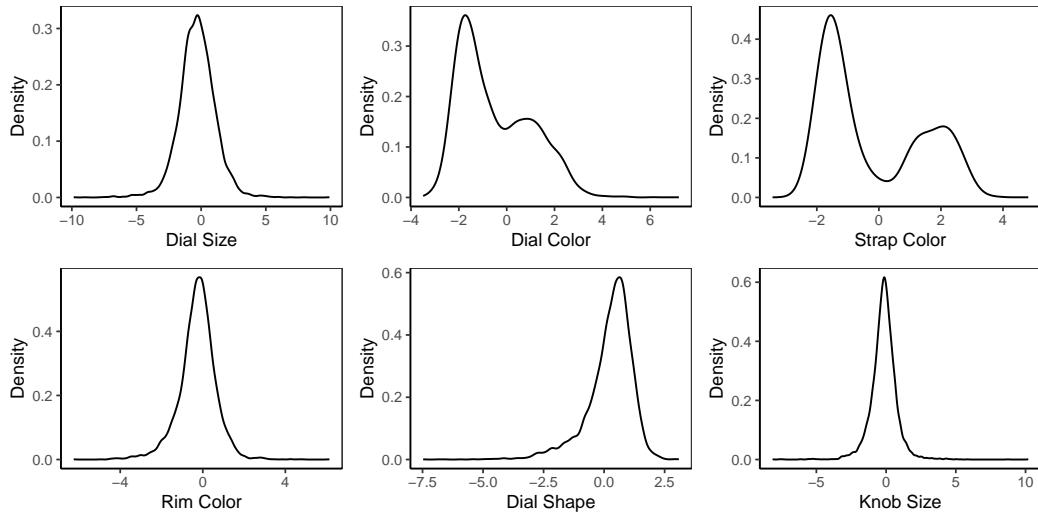
Finally, we show that the discovered visual characteristics are not highly correlated (Table 2), consistent with the goal of maintaining statistical independence across the latent dimensions. In contrast, an autoencoder is not able to find any disentangled visual characteristic and a plain-vanilla variational autoencoder finds entangled visual characteristics. Please refer to the Web Appendix A for these results.

**Evaluating Models with UDR:** The model evaluation step compares the set of supervised models and the unsupervised model to evaluate the model with the best disentanglement, or the highest UDR metric. The results of the comparison of different supervisory signals for disentanglement learning are detailed in the Web Appendix H.

**Table 2:** Correlations Between Visual Characteristics

	Dial Size	Dial Color	Strap Color	Rim (Bezel) Color	Dial Shape	Knob (Crown) Size
Dial Size	1.00	0.17	-0.09	0.04	0.02	0.00
Dial Color	0.17	1.00	0.06	0.01	0.03	0.01
Strap Color	-0.09	0.06	1.00	0.10	0.03	-0.06
Rim (Bezel) Color	0.04	0.01	0.10	1.00	0.07	0.04
Dial Shape	0.02	0.03	0.03	0.07	1.00	0.01
Knob (Crown) Size	0.00	0.01	-0.06	0.04	0.01	1.00

**Figure 6:** Density of Discovered Visual characteristics (from ‘Brand+Circa+Movement’ Signal)



*Notes:* The distribution of the visual characteristics corresponding to dial size, rim (bezel) color, dial shape and knob (crown) size is close to a standard normal distribution. However, the distribution of dial color and strap color is not similar to any standard distribution.

We find that including a combination of signals, i.e. brand, circa, and movement, was substantially better ( $UDR = 0.414$ ) than the unsupervised approach ( $UDR = 0.131$ ). We also note that additional supervision might not always help, because the classification problem of predicting a combination of *all* signals correctly can become more challenging. We show the discovered visual characteristics from the unsupervised as well as supervised approaches in the Web Appendix A. We find that supervision using structured product characteristics can help even in the absence of ground truth on visual characteristics. However, the specific combinations of signal(s) that would work better is likely to depend to a significant degree on the details of the empirical setting, including the product category and potentially even the resolution of the product images.

## *Effectiveness of Supervisory Signals in Disentanglement*

We next aim to develop an understanding of why some signals might be good for supervision. Consider what is required for a signal to work well for disentanglement. Let's start with why ground truth works, when the data images have been generated perfectly from different values of this ground truth factor. The supervised loss term in the objective uses the visual image to predict the signal, when there is only a single visual dimension that is varying in the data (image) generating process. The objective is to minimize prediction loss (e.g., MSE). If we use ground truth on a specific visual characteristic (e.g., dial color), the disentanglement algorithm is incentivized to find that visual characteristic as a discovered latent dimension, since doing so would allow it to reduce the supervised loss, all else equal.

A similar logic holds when we have a “good signal” that is correlated with the ground truth. The presence of the supervisory signal incentivizes the algorithm to find the specific latent dimension corresponding to the visual characteristic. By penalizing total correlation, the algorithm is unlikely to entangle it with other factors since there is an incentive to find orthogonal (or statistically uncorrelated) latent dimensions. A higher quality (or stronger) signal would improve the incentive to find the visual characteristic that predicts the signal as a separate dimension, and also improve disentanglement by the above logic ([Khemakhem et al. 2020](#)).

With ground truth, there is a one-to-one mapping between each ground truth signal and a specific latent dimension or discovered visual characteristic. However, with imperfect signals, there is a many-to-many mapping between these signals and the true visual characteristics. Thus, while the above logic holds, there are some additional tradeoffs. For instance, if one supervisory signal impacts multiple true visual characteristics, then the algorithm would have to trade off the improvements in predictive accuracy across multiple dimensions. If there are multiple such signals that are predictive of one visual characteristic, the model would also have to weigh improvements across each of them in terms of predictive accuracy.

Broadly speaking, signals that are more strongly correlated with the visual look of the product would prove to be better signals. Signals that are more likely to strongly predict one of the visual

characteristics are likely to perform well, even if they do not predict all of the visual characteristics. In contrast, signals that weakly predict multiple visual characteristics are less likely to work well. Also, a set of signals would work better when they encode different information, i.e., each signal in the set would be strongly correlated with one separate dimension of visual characteristics, but not other dimensions. Beyond this broad logic, it is an empirical question as to which signals work better. For some product categories, brand – for instance – might work well if brand influences the look. However, in other categories, where a brand might include several different products without a common look, then brand might not be a good signal.

To evaluate whether a signal is effective, we quantify the degree to which the representation obtained separates out the visual characteristics when conditioned by different values of the signal. To implement this concept, we first select the most disentangled representation using UDR across all possible supervisory signal combinations. We then compare the distribution of these visual characteristics across different values of the signal, operationalized by the Jensen-Shannon (JS) distance.<sup>12</sup>

Let  $\mathbf{z}_{\text{inf}}$  be the set of informative latent variables. Denote the set of values taken by a supervisory signal  $i$  as  $y_i \in \mathcal{Y}_i = \{1, 2, \dots, Y_i\}$ . For example, say signal  $i = 1$  is brand, and the values it can take include *Patek Philippe* and *Rolex* and *Cartier*, etc. Signal  $i = 2$  say is price with values *High* and *Low*. We define the *signal effectiveness*  $\mathcal{S}_i$  of a supervisory signal  $i$  as:

$$\mathcal{S}_i = \frac{1}{2J_{\text{inf}}|Y_i|(|Y_i|-1)} \sum_{k \in \mathbf{z}_{\text{inf}}} \sum_{l \in \mathcal{Y}_i} \sum_{m \in \mathcal{Y}_i: m \neq l} JS(p(z_k|y_i = l), p(z_k|y_i = m)) \quad (9)$$

The intuition is that better or *more informative signals will generate more separation* in latent visual characteristics. Consistent with this intuition, we find that Brand obtains a signal effectiveness of 0.24, whereas Price has a lower signal effectiveness of 0.13. This implies that the difference in

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<sup>12</sup>The Jensen-Shannon distance (JS distance) is a symmetric and smoothed version of the Kullback-Leibler divergence (KL divergence). It measures the similarity between two probability distributions. Given two probability distributions  $P$  and  $Q$ , the JS distance is defined as:  $JS(P, Q) = \left( \frac{1}{2} \text{KL}(P||M) + \frac{1}{2} \text{KL}(Q||M) \right)^{\frac{1}{2}}$ , where  $\text{KL}(X||Y)$  is the Kullback-Leibler divergence of  $X$  from  $Y$ , and  $M = \frac{1}{2}(P + Q)$ . Note that JS distance is always bounded between 0 and  $\sqrt{\log 2}$ .

the distribution of visual characteristics across watches corresponding to different brands is greater than the difference in the distribution of visual characteristics across low and high prices.

*Price as a Signal:* Price could well be an effective signal in other empirical settings. In our case of luxury watches, the price has some unique properties that might reduce its effectiveness.<sup>13</sup> In other empirical settings without these specific considerations, price could well serve as one of the better signals. We show results for a separate product category, sneakers, in which price is a better signal for disentanglement in Web Appendix D.

### ***Validation of Discovered Visual Characteristics***

We would like to evaluate whether the visual characteristics discovered by the disentanglement model are human-interpretable, both qualitatively and quantitatively. We conducted two surveys to validate that humans (a) identify the distinct characteristics and (b) are consistent with our model in their quantitative evaluation.<sup>14</sup> In the first survey, we evaluate the interpretability of the discovered characteristics from visual data. We show respondents an image illustrating different parts of the watch before the survey to help them understand the visual elements of the product.<sup>15</sup>

Next, we generated counterfactual images that vary along only one visual characteristic. For example, each watch image (see Figure 7) is generated by fixing all except one focal visual characteristic, and *only changing the level of the focal visual characteristic*. We ask 99 respondents to identify *which part* of the watch is changing as they scan the images from left to right, and *how* that part was changing. We find that the average agreement among respondents was 86%, with a range from 73%–96%, despite the low image resolution. In the second column of the Table 3, we report the percentage of respondents in the survey who agree with each other on which part of the watch is changing.

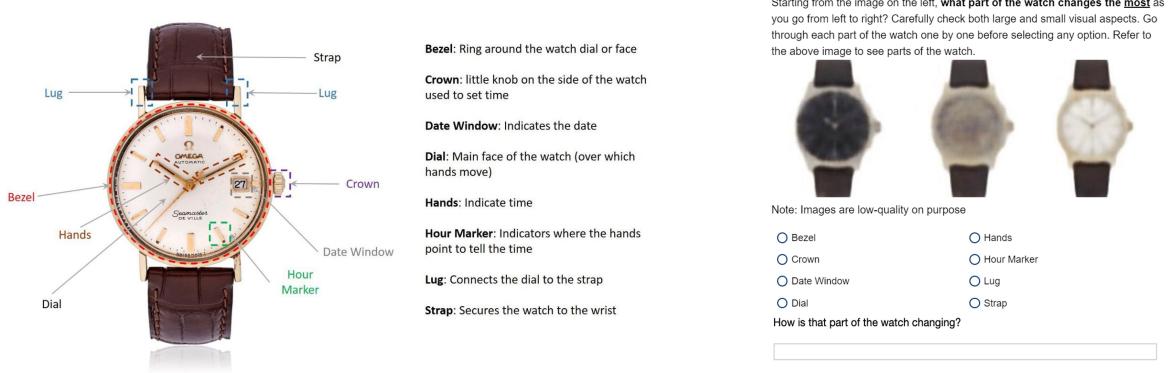
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<sup>13</sup>First, luxury watches are expensive products, and no low cost watches were included in our dataset. Second, hammer prices are based on auction outcomes and hence can be driven by a small number of bidders. These buyers may not be price sensitive, and hence price might not be an informative signal. Third, the same model of a watch can be auctioned multiple times, leading to variation in prices within the model, and therefore a noisier price signal.

<sup>14</sup>We choose respondents based in the US who are fluent in English. For both surveys, we employ an attention check.

<sup>15</sup>We obtained the parts of the watch from the URL: <https://bespokeunit.com/watches/watch-parts-guide/>. This was shown in all survey screens.

**Figure 7:** (Color Online) Survey Question to Validate Interpretability



We next examine in a second survey (Figure 8) whether the quantification of the characteristics automatically determined by the method was consistent with human interpretation. We generated several pairs of watch images that differed only along one visual characteristic. We ask 300 respondents to select the pair of watches that are more similar, which represents an ordinal evaluation. We evaluate whether the responses matched with our algorithm’s quantification. We find that a strong majority (average of 85%) agree with the algorithm’s quantification scale for the visual characteristics, as detailed in the third column of Table 3.

**Figure 8:** (Color Online) Survey Question to Validate Quantification

Which pair of watches in your judgment are more similar in terms of dial color than the other pair? (ignore all the other features of the watches)



**Table 3:** Human Interpretation of Visual Characteristics and Quantification

Visual characteristic	Interpretability Survey	Quantification Survey
Dial Size	76%	83%
Dial Color	80%	92%
Strap Color	88%	92%
Rim (Bezel) Color	79%	88%
Dial Shape	87%	68%
Knob (Crown) Size	70%	85%

In addition to comparing the supervised and unsupervised disentanglement models using UDR, we compare the interpretability of the visual characteristics produced by them. Table A.1 in the Web Appendix A shows that supervised disentanglement models produce more human-interpretable visual characteristics.

### ***Robustness***

We examine the robustness of the model and findings as detailed below.

**Different Product Category:** We evaluate the disentanglement performance of our method with an unrelated product category of sneakers. We obtain data for over 2000 sneakers from a fashion e-commerce firm, along with the structured product characteristics of price and brand. We find that our method, without any changes in architecture, is able to disentangle three human-interpretable visual characteristics: upper color, sole color and topline shape. These results are in the Web Appendix D. We find that for sneakers, price serves as a relatively good supervisory signal for disentanglement.

**Alternative Approach:** We evaluate an alternative approach of using SHAP-learned features as an input to the disentanglement model (Lundberg and Lee 2017). The idea behind SHAP is to determine the pixels in the image that are most influential in the classification of a data point. We find that the SHAP-based approach produces fewer number of visual characteristics than our existing approach of feeding the raw image data to the disentanglement learning model. These results are in the Web Appendix I.

## ***VISUAL CONJOINT ANALYSIS TO GENERATE “IDEAL POINT” PRODUCTS***

Next, we develop and implement conjoint analysis to obtain consumer preferences over six disentangled visual characteristics. We then generate novel “ideal point” visual designs for different segments. Table 4 provides a seven-step summary.

## **Conjoint Survey Design**

We developed a choice-based conjoint (CBC) survey to elicit consumer preferences over a set of generated watches. Generated watch designs were created by sampling three levels – low, medium, and high – of the posterior distributions of the six discovered visual characteristics, resulting in  $3^6 = 729$  visual designs.<sup>16</sup>

**Table 4:** Steps in Visual Conjoint Analysis and Generative “Ideal Point” Design

Step	Description
1	Conduct a visual conjoint analysis to elicit consumer choices over 729 generated visual designs across 6 visual characteristics.
2	Estimate consumers’ visual preferences using a three-tiered hierarchical Bayesian model trained on conjoint analysis data.
3	Segment consumers into two segments using the estimated consumer preference relationship between consumer covariates (demographics) and visual characteristic.
4	Define the “existing market” as the Top-10 products by utility in the overall set of 729 existing products used in the conjoint survey.
5	Define segment-level “ideal points” in visual characteristics space for the two segments. The “ideal point” for each segment is defined as the norm-scaled average preference vector of the segment. <sup>17</sup>
6	Generate new “ideal point” designs corresponding to above visual characteristics.
7	Evaluate model predictions of consumer preference for generated “ideal point” designs by inferring how choice shares change for each segment in the counterfactual market of “existing + ideal point” products.

We obtained CBC survey responses from 400 individuals through the Prolific platform, filtered to obtain a set of 253 respondents.<sup>18</sup> Each respondent evaluated 15 pairs of watches. The data includes binary responses for 15 CBC questions, as well as respondents’ covariates; namely,

<sup>16</sup>Our method is flexible enough to accommodate and characterize nonlinear and non-monotonic consumer preferences in visual characteristics. However, there are two requirements in order for such discovery to be feasible. First, the functional form in the consumer utility model must be specified to be able to discover these nonlinear preferences. If the functional form is specified as linear, then the results obtained would be a linear approximation of the true utility specification. Second, we need to have a sufficient number of levels for each visual characteristic to be able to discover the nonlinearity. If we only have two levels, for instance, it would be impossible to identify non-linear preferences even with a flexible utility model. Thus, a minimum of three levels for visual characteristics are required along with a corresponding utility specification for nonlinear preferences. Adding more levels helps to better approximate the utility functions over visual characteristics, but the flip side is that the number of conjoint respondents increases greatly. The practitioner thus faces a tradeoff between flexibility in characterizing consumer preferences and the practical feasibility of conjoint implementation.

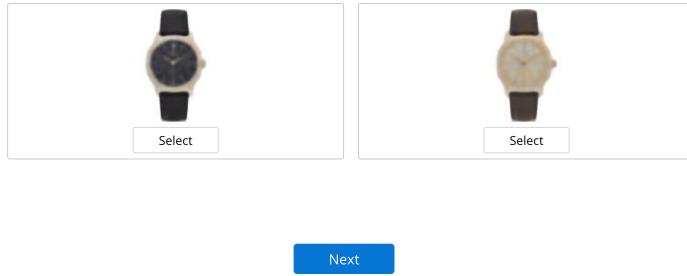
<sup>18</sup>Respondents were filtered post-hoc for a number of reasons: (a) they did not pass the Instructional Manipulation Check (IMC) attention check (Oppenheimer, Meyvis, and Davidenko 2009), (b) they gave inconsistent responses to repeated questions, (c) they did not wear a watch, or (d) they answered “Prefer not to say” for any of the demographic questions.

demographics and psychographics.

The conjoint survey was designed with seven survey stages. The conjoint survey stages are summarized along with their purpose in the Web Appendix J. Each CBC question consisted of a binary choice between two watch designs as shown in Figure 9. The CBC design ensured all unique product designs were enumerated, while also sampling pairs of product images that spanned the visual attribute space for statistical efficiency, i.e., D-optimality (McCullough 2002).

**Figure 9:** (Color Online) Example choice-based conjoint (CBC) question in conjoint survey.

Consider the two watches below that vary only on visual style. Of these two, which watch would you prefer more (for yourself)?



### Conjoint Model Specification, Estimation, and Evaluation

**Model Specification:** We specify in Table 5 a three-level Hierarchical Bayesian (HB) model (Lenk et al. 1996) to estimate and infer individual-level preferences elicited from the conjoint survey over the 6 discovered visual characteristics denoted  $\mathbf{z}$  (“Dial Color,” “Dial Shape,” “Strap Color,” “Dial Size,” “Knob (Crown) Size,” “Rim (Bezel) Color”). We additionally include seven respondent covariates denoted  $\mathbf{r}$  (“Constant Intercept,” “Gender - Male,” “Gender - Female,” “Age,” “Income,” “Education,” and “Aesthetic Importance”).<sup>19</sup>

Note that in Table 5,  $LKJ(\eta)$  is a Cholesky factorization of the correlation matrix  $\Omega_\beta$  of the individual “part-worth” preference vector over visual characteristics (Lewandowski, Kurowicka, and Joe 2009).  $D(\cdot)$  denotes a diagonal matrix,  $\mathbf{r}_i$  are consumer covariates,  $u_i^j$  is the utility customer  $i$  gets from watch design  $j$ , and  $\epsilon_{ij}$  is a Gumbel random variable. The Bernoulli probability

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<sup>19</sup>These covariates were selected from the full set of covariates for model parsimony via initial correlation analysis. Gender covariates were one-hot encoded, while the remaining four covariates were re-coded as real values normalized in the range [-1, 1].

**Table 5:** Mathematical Representation of HB Conjoint Model for Visual Characteristics

Model Element	Mathematical Representation
Impact of Consumer Characteristics on Preferences	$\text{vec}(\Theta) \sim N(\mu_\theta, \Lambda_\theta)$
Correlation of Preferences over Visual Characteristics	$\Omega_\beta \sim \text{LKJ}(\eta)$
Preference Parameters	$\beta_i \sim \mathcal{N}(\Theta^T \mathbf{r}_i, \mathbf{D}(\sigma_\beta) \Omega_\beta \mathbf{D}(\sigma_\beta))$
Utility Function	$u_i^j = \beta_i^T \mathbf{z}_j + \epsilon_{ij}$
Probability of choice $j$	$\psi_i(j, j') = \frac{\exp(u_i^j)}{\exp(u_i^j) + \exp(u_i^{j'})}$

parameter  $\psi_i(j, j')$  is specified by the logit function, and  $\{j, j'\}_i$  denotes the set of all pairwise choice comparisons for watches  $j, j' \in J$  that customer  $i$  chose over in the conjoint survey. Note that  $\sigma_\Theta^2, \Lambda_\Theta, \eta$  are researcher-defined hyperparameters chosen via model selection using prediction accuracy on the validation data split as the evaluation metric.

We tested a variety of parametric HB model specifications including Gaussian mixture priors before settling on a variant of the conventional HB model specification, namely, a unimodal population-level prior,  $\beta$ , over individual-level “part-worth” coefficient vectors,  $\beta_i$ . The mean of the consumer preference “part-worth” vector was accordingly modeled as the inner product between respondents’ covariates and an upper-level model parameter matrix,  $\Theta$ , plus an intercept term.<sup>20</sup> We specified the full covariance matrix over the visual attributes, with the prior drawn from a Cholesky factorization of the covariance matrix to impose positive semi-definiteness for numerical stability using sampling (Lewandowski, Kurowicka, and Joe 2009). We estimated this hierarchical model using MCMC sampling based on observed consumer choices and demographics. For details, see Web Appendix J.

<sup>20</sup>We include the intercept implicitly by appending a vector of 1’s to the consumer covariates matrix  $\mathbf{Z}$  and expanding the dimensionality of  $\Theta$  by one.

**Table 6:** Population-level posterior distributions of visual preference parameters  $\beta$

Visual Characteristic	Mean Preference	Heterogeneity Interval (95%)
Dial Color	0.40	[0.22, 0.56]
Dial Shape	0.003	[-0.17, 0.16]
Strap Color	-1.6	[-1.8, -1.3]
Dial Size	0.41	[-0.13, 0.66]
Knob (Crown) Size	-0.30	[-0.46, -0.14]
Rim (Bezel) Color	-0.57	[-0.72, -0.39]

Table 6 shows population-averaged preference parameters  $\beta$  as well as the heterogeneity across individuals.<sup>21</sup> For robustness, we compared the mean of these posteriors to a homogeneous logit model and found qualitatively similar results, noting that the magnitudes are different due to modeling heterogeneity as well as the (implicit) assumption of the scale parameter being unity in logit estimation (Hauser, Eggers, and Selove 2019).

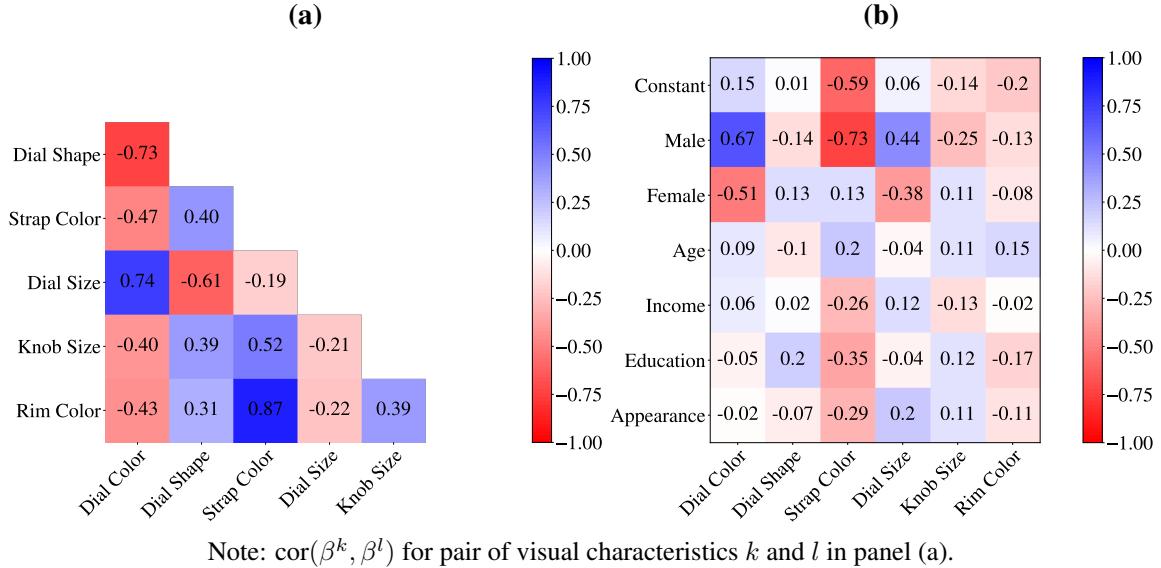
Figure 10(a) shows the correlation matrix of consumer preferences as a heatmap (i.e., normalized mean and standard deviation) over the six visual characteristics. We find that the strongest correlation (0.87) in consumer preferences is between “strap color” and “rim color.” Thus, dark “strap color” and dark “rim color” are preferred together. The second highest correlation (0.74) is between “dial size” and “dial color.” This implies consumers prefer larger “dial size” with dark “dial color.” Similarly, the third highest correlation (-0.73) is between “dial shape” and “dial color.”

We next analyze the relationship between respondents’ covariates and their preferences over visual characteristics. Figure 10(b) shows a heatmap of the estimate of  $\Theta$ . We can then see how demographic variables like “gender” correlate with visual characteristics like “strap color.” For example, respondents who indicated they are male, on average, preferred watches with a dark “dial color,” dark “strap color,” and large “dial size”; respondents who indicated they are female, on average, preferred watches with a light “dial color,” and small “dial size”; and respondents who indicated appearance is important for them prefer dark “strap color.”

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<sup>21</sup>Note that these are the estimated distributions of preference coefficients, not distributions of visual product characteristics.

**Figure 10:** Consumer Preferences. (a) Correlation Matrix of Pairs of Visual Characteristics (b) Interaction between Visual Preferences and Consumer Demographics  $\Theta$



**Model Evaluation:** We compare the predictive accuracy of our representation used along with the HB model against several benchmarks, and evaluated the models on hit rates for respondents’ binary choices among watch visual designs. The first benchmark was a homogenous logit model without respondent covariate variables. The second benchmark was a pretrained deep learning model that included covariate variables to model respondent heterogeneity. We chose the ResNet50 architecture (He et al. 2016) after pre-testing a variety of pretrained network architectures (e.g., DenseNets, VGG) and their performance on the *prediction accuracy metric*.<sup>22</sup> Transfer learning to our conjoint choice task was achieved by “freezing” parameters in the “bottom” layers of the neural network, removing the “top” classification layer, and adding new layers on top to train for conjoint choice prediction. These new layers consisted of two nonlinear layers of size 64 before input into a final logit layer for classification. Lastly, we benchmarked three nonlinear machine learning models as well as an HB model with pairwise interaction terms in an effort to assess how interactions between the visual characteristics influence consumer choice.

Table 7 reports out-of-sample hit rates. Out-of-sample splits were defined by holding out CBC

<sup>22</sup>ResNet50 consists of 50 layers consisting of 48 convolutional layers, each with batch normalization, rectified linear, and residual connection between layers. We used pretrained parameters originally estimated on the ImageNet benchmark dataset.

**Table 7:** Conjoint Model Accuracy

Model	Out-of-Sample Hit Rate (SD)
Disentangled Embedding + Logit Model (Homogeneity)	62.97% (2.90%)
Disentangled Embedding + Neural Net (Homogeneity)	65.81% (2.22%)
Pretrained Deep Learning Model Embedding (Observable Heterogeneity)	68.31% (1.54%)
Disentangled Embedding + Neural Net (Observable Heterogeneity)	67.52% (0.92%)
Disentangled Embedding + Random Forest (Observable Heterogeneity)	68.77% (0.90%)
Disentangled Embedding + XGBoost (Observable Heterogeneity)	69.10% (0.41%)
<b>Disentangled Embedding + HB Model (+ Unobserved Heterogeneity)</b>	<b>71.61% (1.69%)</b>
Disentangled Embedding + HB Model w/ Interactions (+ Unobserved Heterogeneity)	70.82% (1.50%)

Note: In the above table, heterogeneity refers to *consumer-level* heterogeneity.

conjoint tasks for each respondent (stratified splitting), as is convention in the conjoint analysis literature (Gustafsson, Herrmann, and Huber 2013), and preference learning in the machine learning literature (Fürnkranz and Hüllermeier 2010). We find the homogenous logit model achieves the lowest prediction accuracy, perhaps unsurprising given that out of all benchmarked models, it makes the strongest (implicit) assumptions on the data and does not account for heterogeneity. The nonlinear machine learning models achieved relatively high hit rates, with random forests and XGBoost outperforming the two neural networks: namely a feedforward neural net on the visual characteristics and the ResNet50 pretrained deep learning model on the generated images.

The HB model with a linear utility specification achieved the highest prediction accuracy, reflecting the value of modeling both observed and unobserved consumer heterogeneity.<sup>23</sup> The HB MNL with interactions did not obtain a higher accuracy than the HB MNL model without the (explicit in likelihood) interaction terms. We believe this is likely due to two reasons. First, the HB model without interactions models correlations in consumer preferences across characteristics, as we are estimating a full covariance matrix (i.e., not isotropic or diagonal). Second, we observed lack of convergence likely from model overparameterization. Our parameterization of the HB MNL model with interactions required us to model the (explicit) interaction parameters as being homogeneous (not conditional on covariates). Without this simplification, the number of

<sup>23</sup>We note that the conjoint survey design measured consumer responses over three levels of each of the discovered visual characteristics, which is likely to favor linear utility models over more nonlinear specifications.

parameters would increase substantially.<sup>24</sup> In short, we believe explicit modeling of interactions, specifically for this dataset, resulted in a less parsimonious model than the HB MNL model, resulting in worse out-of-sample performance. While this finding is in line with recent marketing research (Smith, Seiler, and Aggarwal 2023), this suggests more research into when conventional methods outperform machine learning methods is needed.

### ***Generating New “Ideal Point” Product Designs for Customer Segments***

Developing new products and their product positioning is critical to firms (Rao et al. 2014). “Ideal points” refer to the optimal positioning of a new product in characteristic space based on preferences, often of a targeted consumer segment (DeSarbo, Ramaswamy, and Cohen 1995; Wedel and Kamakura 2000; Lee, Sudhir, and Steckel 2002). Identification of such ideal points has been extensively studied in marketing research and practice for over 50 years (Johnson 1971; Hauser and Urban 1977). The general approach involves the following steps: (a) obtain data on a consumer or segment stated or revealed preferences over a set of existing products that are represented by product characteristics, (b) estimate a predictive model of preferences over these characteristics, and (c) identify new points in product characteristic space corresponding to the position of the maximally preferred product of the customer or segment.

We build upon this work by *generating* “ideal point” visual designs, in our case, maximally preferred watch designs for two chosen customer segments. Recent work in marketing has likewise used generative modeling to obtain preferred product designs (Dew, Ansari, and Toubia 2022; Cheng, Lee, and Tambe 2022; Burnap, Hauser, and Timoshenko 2023). The difference is that our method is based on interpretable visual characteristics *that were unknown a priori and discovered by our model without human input*. Moreover, and critically for generative design, we can vary any subset of them separately to create designs that span the space of visual characteristics. Interpretability is highly desirable and often required by practitioners for implementing these systems (Bloch 1995; Norman 2004).

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<sup>24</sup>Specifically, we would have to model the likelihood using explicit terms for the 6 main effect + 15 interaction effects, in addition to their covariance matrix, which would be of size  $(6 + 15) \times (6 + 15)$ .

We identify two customer segments to design “ideal point” products from customer preferences estimated using the HB model on the conjoint survey data. Segment 1 corresponds to “affluent women” who self-reported they were female and made more than \$100,000, and Segment 2 corresponds to “less affluent men” who self-reported they were male and made less than \$50,000. The variables and thresholds that used segmentation were chosen via the HB estimated  $\Theta$  matrix connecting customer covariates and visual characteristics, as shown in Figure 10.

**Figure 11:** (Color Online) Generated “Ideal Point” Watches for Two Segments

(a) Segment 1 (b) Segment 2



We next generate new visual designs for watches corresponding to the “ideal point” product (i.e., optimal visual characteristics) for each segment, and plot them in Figure 11. The “ideal point” refers to a point in the visual characteristic space corresponding to the maximal expected utility of consumers in a given segment, constrained to lie in a feasible portion of the visual characteristic space (DeSarbo, Ramaswamy, and Cohen 1995). “Feasible” must be defined given our (conventional) assumption of utility as an inner product between consumer preferences and (visual) product characteristics (i.e., “more is better”). We defined the “ideal point” product  $\mathbf{z}_s$  for segment  $s$  as the segment’s preference coefficients scaled to the average Euclidean norm  $\rho_c$  of the set of  $C$  “existing products” in the market.<sup>25</sup> Alternative models that instead *search* the characteristic space via optimization methods could also be used (Michalek, Feinberg, and Papalambros 2005; Belloni et al. 2008). The ideal point  $\mathbf{z}_s$  is specified as:

$$\mathbf{z}_s = \frac{\rho_s}{\rho_c} \bar{\beta}, \quad \rho_s = \|\bar{\beta}\|_2, \quad \rho_c = \frac{1}{C} \sum_{j=1}^C \|\mathbf{z}_j\|_2 \quad (10)$$

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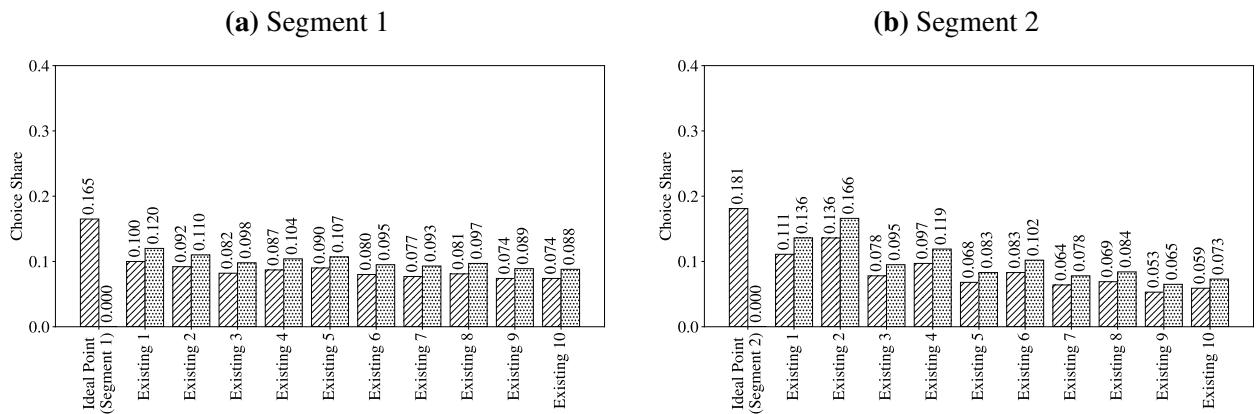
<sup>25</sup>This norm scaling  $\frac{\rho_s}{\rho_c}$  is an assumption required for us to define an “ideal point,” given that we have assumed the conventional inner-product-based utility model between consumer preference and product (visual) characteristics. Without this assumption (or a similar bound), the “ideal point” would be at infinity (Kaul and Rao 1995). Intuitively, this assumption and our definition of  $\mathbf{z}_s$  is analogous to “ideal point” methods in that we are finding the location on a hypersphere in which inverse-distance from that point results in maximum utility for the segment (DeSarbo, Ramaswamy, and Cohen 1995; Hauser and Simmie 1981).

where  $\|\cdot\|_2$  denotes the Euclidean norm.

Lastly, we calculate the expected choice share of adding the ideal point product for each segment to the market. For each segment, we assume  $C = 10$  such that the segment's consideration set consists of the Top-10 products by utility in the overall set of existing products (729 existing watches used in the conjoint survey). Since we have heterogeneity at the individual-level  $\beta_i$ , not every customer will have the same Top-10, so we defined the segment's Top-10 as the 10 watches that appeared most frequently when aggregated across individual customers. We note that with the given definition of ideal point, we may not always see the ideal point visual design having the highest choice share, so it can be viewed as a conservative interpretation.

Figure 12 shows the change in expected choice shares for each segment’s “ideal point” and the Top-10 existing products for the segment. We find 16.5% choice share for Segment 1’s ideal point and 18.1% choice share for Segment 2’s ideal point visual design, indicating that the new ideal point product did indeed align with segment-level preferences. Thus, the “ideal point” generated product obtained substantial choice share from existing products for each segment. We note this analysis did not elicit (and subsequently estimate) individual consumer preferences for an “outside option,” and is therefore limited to choice shares rather than market shares.

**Figure 12:** Segment-Level Choice Shares With and Without Ideal Point Product



## ***DISCUSSION AND CONCLUSION***

Despite the importance of visual characteristics, the automatic identification and quantification of visual characteristics that represent visual design (and corresponding consumer response) has remained an open challenge. This is important as consumers have preferences over visual design across a wide range of product characteristics (Bloch 1995). Marketing research has a long history of studying visual design, but only recently has had access to representations of visual characteristics that are realistic (e.g., images) while also being human-interpretable.

Our research develops a methodology to automatically discover and quantify visual design characteristics using a combination of unstructured product image data, in conjunction with structured product characteristics and price. In contrast to ML methods which require ground truth, we use structured characteristics to supervise the disentanglement model to enhance its performance. The discovered characteristics are disentangled, and interpretable by humans. Moreover, we can generate novel counterfactual designs by varying the levels of the discovered characteristics one at a time. We use this flexibility to conduct visual conjoint design and obtain consumer preferences over visual characteristics, which are then used to generate targeted “ideal point” visual designs.

Our approach has specific limitations worth noting and addressing in future research. First, it requires structured data to be matched to corresponding unstructured data; our application used watch images matched to structured characteristics, but other applications may not have structured data as readily accessible. Second, although the model does not require human intervention, the data is preprocessed to ensure centering, similar size, background color, and orientation. Third, no algorithm can *guarantee* semantic interpretability of discovered visual characteristics, because that is a uniquely human ability (Locatello et al. 2019; Higgins et al. 2021). However, we validate our proposed method and find that it performs well quantitatively both with disentanglement metrics (UDR) as well as in human interpretability. Fourth, the performance of our (basic) model architecture likely varies with quality and resolution of images; richer characteristics in higher-resolution images may necessitate adjustments. Lastly, though literature heavily suggests the importance of

visual stimuli in conjoint analysis (Dahan and Srinivasan 2000; Dotson et al. 2019; Sylcott, Orsborn, and Cagan 2016), future work could provide more direct comparisons between visual and traditional text descriptors.

There are several questions worthy of note for future research. First, it is important to understand the underlying reason why a particular product characteristic serves as a good supervisory signal in any specific product category. Second, it would be useful to understand what combinations of product characteristics typically improve disentanglement the most *across* product categories, and the underlying reason. Likewise, developing neural network architectures with inductive biases for disentanglement would be valuable. Third, examining the performance of this or similar methods in other modalities like text or audio would help answer questions around practical usage for other marketing tasks. Since consumer decision making is likely to depend on multiple sources of information and persuasion, it would be interesting to examine whether having one modality helps to improve the impact of another, e.g. the presence of text might help disentangle images better. Fourth, this paper raises interesting questions on when can a low-dimensional interpretable representation combined with conventional methods such as hierarchical bayesian outperform complex machine learning methods pretrained on a much broader set of image data (i.e. millions of images). Finally, it would be interesting to examine how visual characteristics may be incorporated into models of demand and supply, so that we can understand both consumer preferences and firm’s strategic choices involving visual design.

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# Generative Interpretable Visual Design: Using Disentanglement for Visual Conjoint Analysis

## (Web Appendix)

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2024

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## A Discovery of Visual Characteristics across Models

We compare the visual characteristics discovered by our disentanglement approach with benchmark models like Autoencoders, Variational Autoencoders and Unsupervised Disentanglement.

**Comparison among Disentanglement Models:** Figure A.1 show the discovered visual characteristics learned by the supervised approaches corresponding to three cases: supervised with high UDR, supervised with low UDR and the unsupervised approach. We compare the human interpretability of the visual characteristics obtained from the supervised disentanglement approach with the ones obtained from the unsupervised approach using consumer surveys. In these surveys, we ask consumers whether they are able to interpret the discovered visual characteristics. From Table A.1, we can see that on average consumers are better able to interpret the visual characteristics from the supervised approach as compared with the unsupervised approach. Thus, the results of these survey validate that supervision helps us obtain more disentangled visual characteristics in addition to just using the UDR metric.<sup>1</sup>

**Table A.1:** Human Interpretation of Visual Characteristics

Visual Characteristic	Mean [95% CI]		% Improvement
	Supervised	Unsupervised	
Dial Color	0.80 [0.70, 0.89]	0.81 [0.72, 0.90]	– <sup>†</sup>
Dial Size	0.76 [0.66, 0.86]	0.78 [0.69, 0.88]	– <sup>†</sup>
Strap Color	0.88 [0.80, 0.96]	0.90 [0.83, 0.97]	– <sup>†</sup>
Rim Color	0.79 [0.69, 0.88]	0.42 [0.30, 0.54]	88.1%
Dial Shape	0.87 [0.79, 0.95]	0.49 [0.37, 0.61]	90.5%
Knob Size	0.70 [0.59, 0.80]	0.56 [0.44, 0.68]	25.0%
Across All 6 Char	0.80 [0.76, 0.84]	0.67 [0.62, 0.71]	21.2%

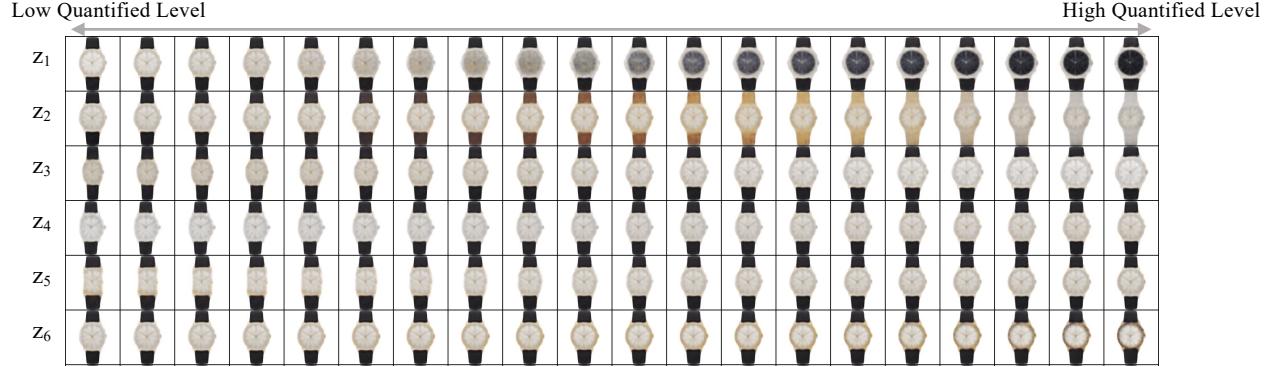
<sup>†</sup> The mean interpretability of the visual characteristic in the supervised approach overlaps with the 95% CI of the interpretability of the unsupervised.

We note that although we find supervision helps disentanglement, and that supervision is required for overcoming the “impossibility theorem” discussed in Locatello et al. (2019), unsupervised disentanglement has a known ability to discover some visual characteristics. This observation helped spur the drive towards more control over the VAE objective by decomposing it into

<sup>1</sup>To assess the variability and reliability of our sample estimates, we employed a bootstrap resampling method.

**Figure A.1:** Discovered Visual characteristics from Multiple Supervisory Signals

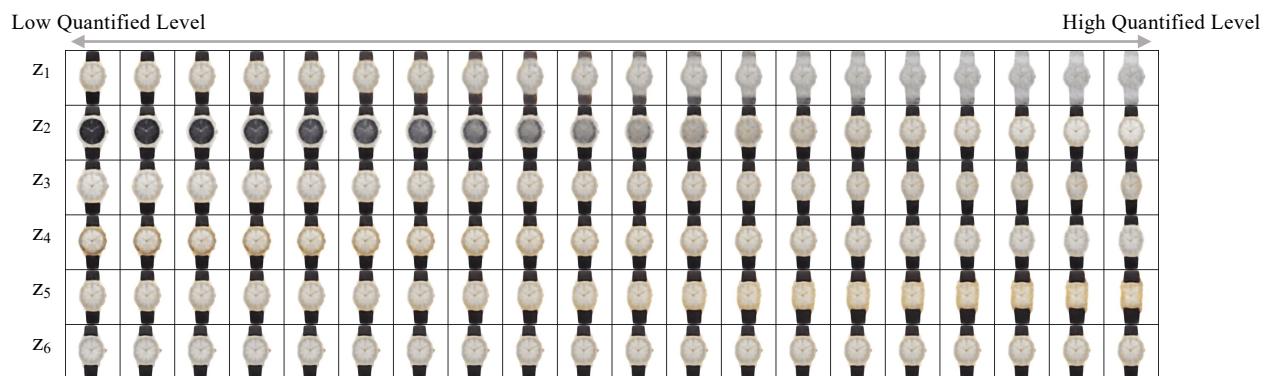
(a) High UDR: ‘Brand’, ‘Circa’ & ‘Movement’ Supervisory Signal



(b) Low UDR: ‘Circa’ Supervisory Signal



(c) Unsupervised Approach



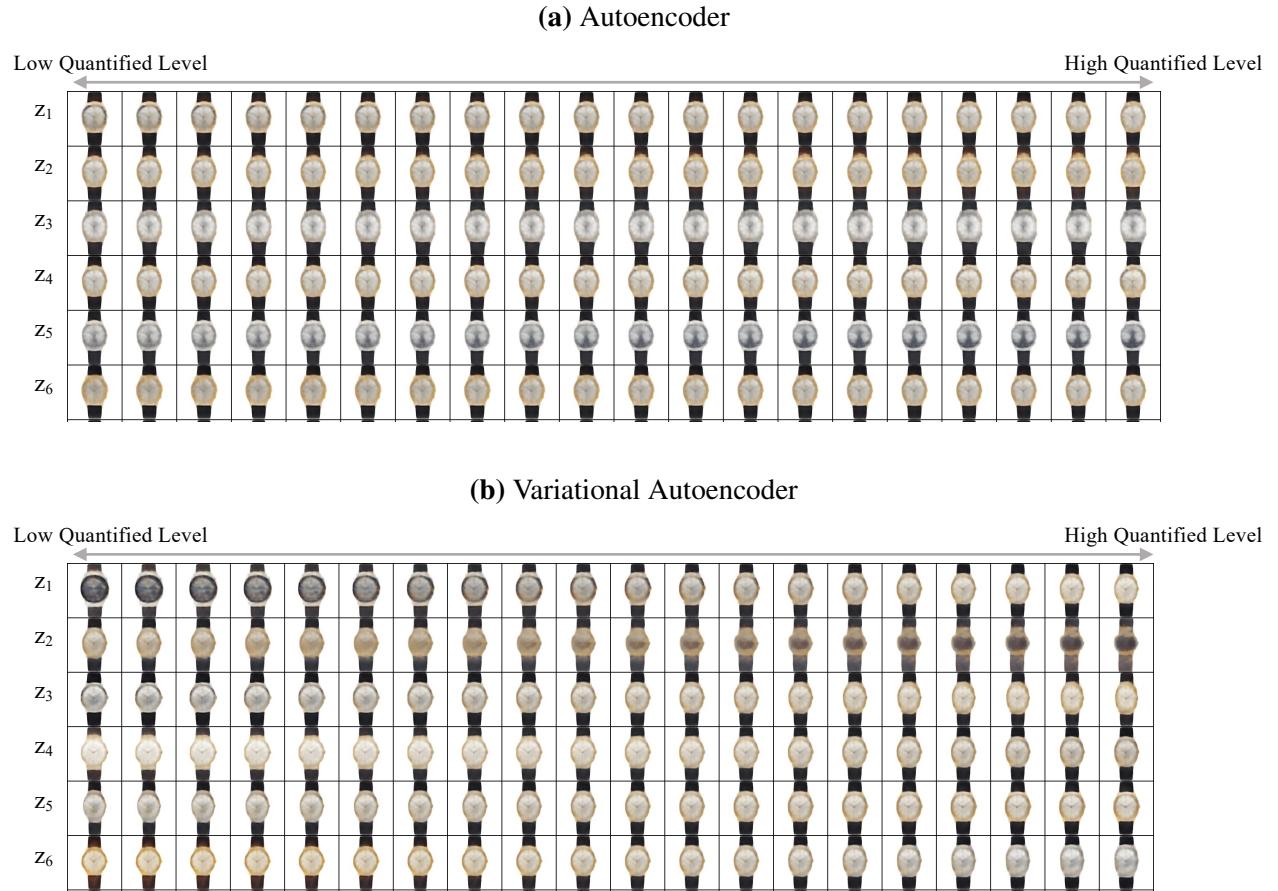
*Notes:* Latent traversals along a *focal watch* used to visualise the semantic meaning encoded by single visual characteristic learnt by a trained model. In each row, the quantitative level of a single characteristic is varied keeping the other characteristics fixed. The resulting reconstruction is visualized. **a:** Discovered visual characteristics learned by supervising the characteristics to predict the brand, circa, and movement simultaneously. **b:** Discovered visual characteristics learned by supervising the characteristics to predict the circa simultaneously. **c:** Discovered visual characteristics learned by the unsupervised approach.

terms that explicitly control disentanglement (Chen et al. 2018; Hoffman and Johnson 2016). In short, several factors may be at play, including (1) the common prior assumption of isotropic Gaussian has no off-diagonal covariance terms, promoting uncorrelatedness of the embedding; and (2) VAEs pursue PCA direction (locally) (Rolinek, Zietlow, and Martius 2019). Further intuition for why unsupervised disentanglement can work in practice at all is well-discussed in Mathieu et al. (2019).

**Comparison with Benchmark Models:** We obtain the visual characteristics discovered by an autoencoder (AE) and a variational autoencoder (VAE) to serve as reference to the disentanglement model. Figure A.2 gives the output of discovered visual characteristics from an autoencoder and a variational autoencoder. We show the top six visual characteristics based on the KL divergence value of the difference between the posterior and the Gaussian prior.

We cannot interpret any of the visual characteristics discovered by the AE. Note that these characteristics are not uninformative because their KL divergence is not close to 0. We find that the VAE leads to entanglement. By entangled, we mean that when any one entangled characteristic is changed while others are fixed, the watch image changes in more than one interpretable visual characteristic. This is unlike a disentangled model in which there is a one-to-one mapping between visual characteristics and latent factors of variation.

**Figure A.2:** Discovered Visual characteristics from Different Methods



*Notes:* Latent traversals along a *focal watch* used to visualise the semantic meaning encoded by single visual characteristic learnt by a trained model. In each row, the quantitative level of a single characteristic is varied keeping the other characteristics fixed. The resulting reconstruction is visualized. **a:** Discovered visual characteristics learned by Autoencoder. **b:** Discovered visual characteristics learned by Variational Autoencoder.

## B Connections with Existing Marketing Methods

We include a high-level comparison of the methods in Table B.1.

**Table B.1:** Comparison of Methods

Method	PCA	MDS	AE	VAE	Disentanglement
Dimensionality Reduction	Yes	Yes	Yes	Yes	Yes
Reconstruction of Existing Examples	Yes	Yes	Yes	Yes	Yes
Generation of New Examples	No	No	No	Yes	Yes
Use with Unstructured Data	Yes	Yes	Yes	Yes	Yes
Interpretability using Unstructured Data	No	No	No	No	Yes
Stochastic (S) or Deterministic (D)	D	D	D	S	S
Non-Linear Transformations	No	No	Yes	Yes	Yes

Several methods used in marketing can be used to compress high-dimensional data into a lower-dimensional representation as shown in Table B.1. The simplest and perhaps most well-known is principle component analysis (PCA). PCA assumes that the data lie on a linear subspace and captures the global linear structure in the data. PCA has been used in marketing for dimensionality reduction (Liu, Singh, and Srinivasan 2016; Kappe and Stremersch 2016) in order to make solving the models tractable. Multi-dimensional scaling (MDS) is a method that aims to minimize dissimilarity between distances in the high-dimensional data and distances in the lower-dimensional representation. MDS is a general method as “distance” can be nonlinear and even non-metric; however, conventionally researchers assume Euclidean distances which makes it equivalent to PCA (Williams 2000). While PCA and MDS have been widely-used in marketing to reduce data dimensionality for managerial interpretation (Lee and Bradlow 2011), these methods are not well suited to capturing complex nonlinear relationships in unstructured data (Linting et al. 2007). Consequently, they are likewise not well suited for our goal of discovering interpretable visual characteristics directly from unstructured image data.

An autoencoder (AE) (Baldi and Hornik 1989; Rumelhart, Hinton, and Williams 1986) is a nonlinear method that focuses on reconstructing the original high-dimensional data

(typically unstructured data such as images), while compressing the original data into a lower-dimensional representation. Autoencoders can capture complex nonlinear relationships, especially those prevalent in visual data, and thus typically outperform linear methods like PCA in terms of reconstruction accuracy (Mika et al. 1998). An AE is equivalent to PCA if it is restricted to only linear transformations (Roweis and Ghahramani 1999; Bengio, Courville, and Vincent 2012). While the AE can reconstruct the original data with medium-to-high fidelity, it cannot generate new out-of-sample data that it has never seen. Thus, similar to the case of PCA and MDS, we cannot term it as a generative model.

In contrast, a variational autoencoder (VAE) is a probabilistic generative model that similarly represents high-dimensional data using lower-dimensional latent variables (Kingma and Welling 2014). The VAE takes a Bayesian approach by learning the latent variable distributions using variational inference. While architecturally similar to the (non-generative) AE, the VAE is able to *generate new data that are similar to the input data* by sampling from its probabilistic generative model by conditioning on the latent variables. Lastly,  $\beta$ -TCVAE (Chen et al. 2018) builds upon VAE by: (a) promoting statistical independence in the latent space; (b) discourages data copying by minimizing mutual information between the input data and the latent space; (c) minimizes the number of truly informative dimensions. The above objectives are often conflicting, and the model uses hyperparameters that decide the weights associated with these terms.

**Comparison of Generative Methods:** The two broad classes of generative models are based on variational autoencoders (VAEs) (Kingma and Welling 2014) and generative adversarial networks (GAN)<sup>2</sup> (Goodfellow et al. 2020). Most state-of-the-art disentangled *representation learning* methods are based on VAEs. VAEs are comprised of two models – the encoder neural net and the decoder neural net. The encoder neural net compresses high-dimensional input data to a lower-dimensional latent vector (latent characteristics), followed by inputting the latent vector to the decoder neural net

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<sup>2</sup>In a GAN, two neural networks compete with each other in a zero-sum game to become more accurate.

which outputs a reconstruction of the original input data. VAEs balance having both a low reconstruction error between the input and output data (e.g., images, text), as well as a KL-divergence of the latent space distribution (latent characteristics) from a researcher-defined prior distribution (e.g., Gaussian). The KL-divergence term acts as a regularizer on the latent space, such that it has desired structure (smoothness, compactness). VAEs are parameterized in both the encoder neural net and decoder neural net using neural networks whose parameters are learned jointly.

**Table B.2:** Comparison between VAE and GAN based methods

#	Topic	VAE	GAN	Source
1	Disentanglement Performance	High	Low	(Lee et al. 2020)
2	Quality of generated image	Low	High	(Lee et al. 2020)
3	Training instability	Low	High	(Lee et al. 2020)
4	Local v Global Concepts	Global	Local	(Gabbay, Cohen, and Hoshen 2021)
5	Data requirement	Low	High	(Karras et al. 2020)
6	Ability to work on small or detailed objects	No	Yes	(Locatello et al. 2020)

*Notes:* **1,2,3** According to Lee et al. (2020): “VAE-based approaches are effective in learning useful disentangled representations in various tasks, but their generation quality is generally worse than the state-of-the-arts, which limits its applicability to the task of realistic synthesis. On the other hand, GAN based approaches can achieve the high-quality synthesis with a more expressive decoder and without explicit likelihood estimation. However, they tend to learn comparably more entangled representations than the VAE counterparts and are notoriously difficult to train, even with recent techniques to stabilize the training.” **4:** According to Gabbay, Cohen, and Hoshen (2021): “Such methods that rely on a pretrained unconditional StyleGAN generator are mostly successful in manipulating highly-localized visual concepts (e.g. hair color), while the control of global concepts (e.g. age) seems to be coupled with the face identity.” **5:** According to Karras et al. (2020): “Acquiring, processing, and distributing the  $10^5$  —  $10^6$  images required to train a modern high-quality, high-resolution GAN is a costly undertaking. The key problem with small datasets is that the discriminator overfits to the training examples; its feedback to the generator becomes meaningless and training starts to diverge.” **6** According to Locatello et al. (2020): “It is however interesting to notice how the GAN based methods perform especially well on the data sets SmallNORB and MPI3D where VAE based approaches struggle with reconstruction as the objects are either too detailed or too small.”

Several methods based on GANs have also been used for disentanglement. InfoGAN was one of the first scalable unsupervised methods for learning disentangled representations (Chen et al. 2016). While GANs are typically less suited relative to VAEs

for representation learning, as GANs traditionally do not infer a representation<sup>3</sup>, InfoGAN explicitly constrains a small subset of the ‘noise’ variables to have high mutual information with generated data. Several VAE-based methods have proven to be superior (Kim and Mnih 2018; Chen et al. 2018) than InfoGAN. Recent methods based on StyleGAN (Karras, Laine, and Aila 2019) such as Info-StyleGAN (Nie et al. 2020) are able to perform disentanglement at a much higher resolution ( $1024 \times 1024$ ) unlike the VAE-based methods. However, unlike InfoGAN, Info-StyleGAN suffers from the need for human labels or pretrained models, which can be expensive to obtain (Voynov and Babenko 2020).

We choose a VAE-based approach over a GAN-based approach for several reasons. First, our goal is to propose an easy-to-train method that can be used by researchers as well as practitioners (Lee et al. 2020). Second, our goal of discovering unique (visual) characteristics that are human interpretable and independent of each other requires high disentanglement performance, but reconstruction accuracy is not our primary goal (Lee et al. 2020). GANs suffer from lower disentanglement performance because they focus on localized concepts but not global concepts of the image (Gababay, Cohen, and Hoshen 2021). On the other hand, discovered characteristics from VAEs are much more globally distributed as compared with GANs. This allows the VAE-based methods to discover few important and human interpretable unstructured (visual) characteristics that can represent the input raw data. Third, one of the benefits of our approach is that we are able to not just discover disentangled characteristics, but infer the levels of these characteristics for all datum in the data. This enables use in downstream marketing tasks that require characteristic levels, for example, visual conjoint analysis to understand consumer preferences. GANs do not conventionally infer a representation of the data, and hence do not have this benefit. Finally, VAEs often require less data to train in comparison with GANs (Karras, Laine, and Aila 2019). Thus, even though GANs can provide much better reconstruction and work better for small and detailed objects (Locatello et al. 2020), we choose a VAE-based approach

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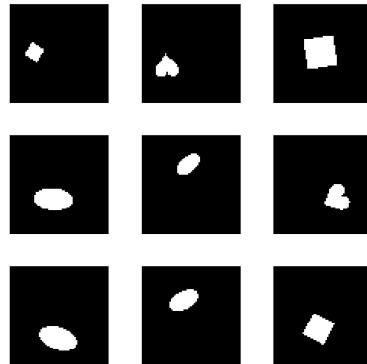
<sup>3</sup>Moreover, GANs tend to suffer from training instability. Common failure modes are vanishing gradients, mode collapse, and failure to converge.

because of its suitability to our research question.

## C Disentanglement with a Simple Geometric Shape

Consider the dataset of 2D objects dSprites (Higgins et al. 2017). Each image in this data (see Figure C.1) shows an object of a specific shape, size and color at a specific location in the image. Across images, we can see different possible combinations of these visual characteristics. The objective of disentanglement is to separate out these independent factors of variation to obtain object shape, position, size, and color as the 4 latent dimensions discovered by the disentanglement model. The advantage of disentanglement is that, even when the dimensionality of the latent space is increased to a large number, it will only discover these true factors of variation (shape, size, color and position).

**Figure C.1:** Sample of dSprites Images



## D Disentanglement in a Different Product Category – Sneakers

Our data includes sneakers sold at a fashion e-commerce firm. For each sneaker in the dataset, we have its image, brand, and price. Figure D.1 shows a sample of sneaker images in our dataset. We obtained the dataset of sneakers sold on a fashion e-commerce firm in March 2023. These shoes were classified as sneakers by the retailer. Overall, our dataset includes 2,227 unique sneaker models with an average of 2.5 images per sneaker model. The size of the overall dataset includes 5,575 images. We only included the side view of sneakers in order to focus on the variation in the shape of the sneakers. Finally, we specifically used grayscale images because each sneaker model with the same shape comes in multiple colors. We preprocessed each image to have the size of 128x128 dimensions to keep the images consistent with the watch category. A total of 247 unique brands are present in the data. Skechers, Vans, New Balance, adidas and ASICS are the five brands with the largest share of observations. Table D.1 provides summary statistics of the sneakers.

We use the same deep learning model architecture as well as the same hyperparameters (except the disentanglement hyperparameters  $\beta$  and  $\delta$ ) as the one used for learning visual characteristics of watches. We follow the same method for training the model, selecting the hyperparameters  $\beta$  and  $\delta$  based on lowest supervised loss on a held-out dataset and then evaluating different supervisory signals for the sneakers category using Unsupervised Disentanglement Ranking (UDR).

**Figure D.1:** Sample of Sneakers



From Table D.2, we show that price serves as the most effective supervisory signal for learning human-interpretable visual characteristics for sneakers. To understand why price is the most effective supervisory signal, we calculate the Signal Effectiveness score that relies on the intuition that better or more informative signals will generate more separation in latent visual characteristics. Consistent with this intuition, in sneakers, the Signal Effectiveness Score for brands is 0.26

**Table D.1:** Summary Statistics of Structured characteristics of Sneakers

Statistic	Mean	SD	Min	Max
Brand (Skechers)	0.09	0.29	0	1
Brand (Vans)	0.08	0.28	0	1
Brand (New Balance)	0.07	0.26	0	1
Brand (adidas)	0.06	0.24	0	1
Brand (ASICS)	0.05	0.22	0	1
...				
Brand (Others)	0.14	0.34	0	1
Price (in \$s)	112.30	46.45	30.00	650.00

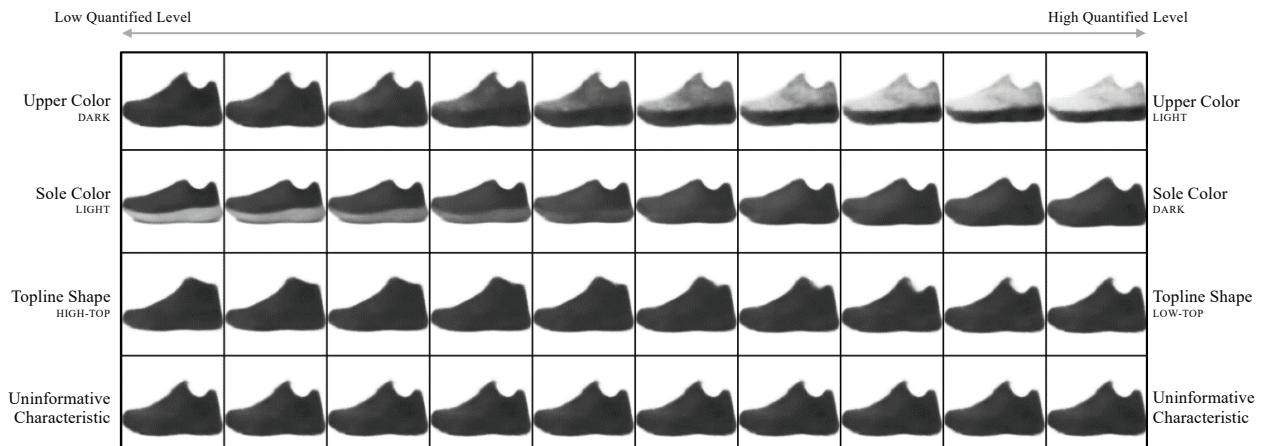
compared with 0.32 for discrete prices.

**Table D.2:** Comparison of Different Supervisory Approaches

Number of Signals	Supervisory Signals	UDR
0	Unsupervised	0.126
1	Brand	0.093
1	Price (5 Discrete Classes)	0.267

Figure D.2 gives an output of discovered visual characteristics corresponding to the supervisory signals ‘price’. In each row of the figure, we show how the sneaker image changes based on changes in levels of one visual characteristic, while keeping all the other characteristics fixed. We only show three visual characteristics as rest of the characteristics are found to be uninformative i.e. the KL divergence of the posterior was not much different from the Gaussian prior. Traversing along an uninformative characteristic leads to no visual change, and we show one uninformative characteristic for reference.

**Figure D.2:** Discovered Visual Characteristics of Sneakers



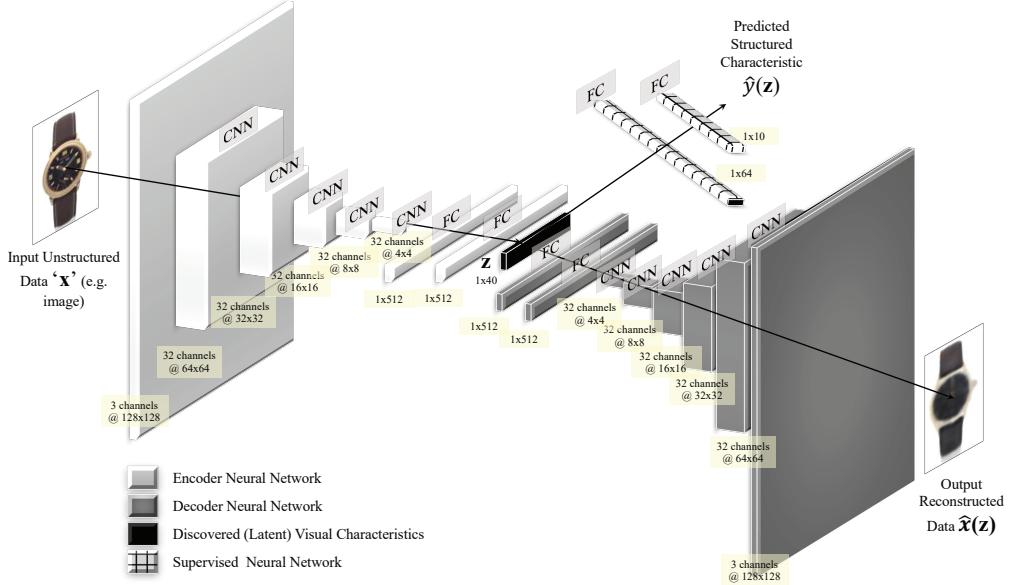
*Notes:* Latent traversals along a *focal sneaker* used to visualise the semantic meaning encoded by single visual

characteristic learnt by a trained model. In each row, the quantitative level of a single characteristic is varied keeping the other characteristics fixed. The resulting reconstruction is visualized. Discovered visual characteristics learned by supervising the characteristics to predict the price simultaneously.

## E Model Architecture

The model architecture is detailed in Figure E.1. The encoder neural net for the VAEs consisted of 5 convolutional layers, each with 32 channels,  $4 \times 4$  kernels, and a stride of 2. This was followed by 2 fully connected layers, each of 512 units. The latent distribution consisted of one fully connected layer of 40 units parameterizing the mean and log standard deviation of 20 Gaussian random variables. The decoder neural net architecture was the transpose of the encoder neural net but with the output parameterizing Bernoulli distributions over the pixels. Leaky ReLU activations were used throughout. We used the Adam optimizer with the learning rate 5e-4 and parameters  $b_1 = 0.9$  and  $b_2 = 0.999$ . We set batch size equal to 64. We train the model for 100 epochs. Portions of our codebase were built on elements sourced from the disentangling-vae open source project (Dubois et al. 2019).

**Figure E.1:** Model Architecture



## F Summary Statistics of Structured Characteristics of Auctioned Watches

Table F.1 provides summary statistics of the auctioned watches.

**Table F.1:** Summary Statistics of Structured Characteristics of Auctioned Watches

Statistic	Mean	SD	Min	Max
Brand (Audemar's Piguet)	0.06	0.24	0	1
Brand (Cartier)	0.07	0.25	0	1
Brand (Patek Philippe)	0.20	0.40	0	1
Brand (Rolex)	0.18	0.38	0	1
Brand (Others)	0.49	0.50	0	1
Circa (Pre-1950s)	0.05	0.21	0	1
Circa (1950s)	0.05	0.22	0	1
Circa (1960s)	0.07	0.26	0	1
Circa (1970s)	0.10	0.30	0	1
Circa (1980s)	0.08	0.26	0	1
Circa (1990s)	0.19	0.39	0	1
Circa (2000s)	0.33	0.47	0	1
Circa (2010s)	0.14	0.35	0	1
Movement (Automatic)	0.54	0.50	0	1
Movement (Mechanical)	0.36	0.48	0	1
Movement (Quartz)	0.11	0.31	0	1
Watch Dimensions (in mm)	36.21	6.83	9	62
Material (Gold)	0.60	0.49	0	1
Material (Gold and Steel)	0.05	0.22	0	1
Material (Steel)	0.28	0.45	0	1
Material (Others)	0.07	0.25	0	1
Hammer Price (in \$000s)	23.25	55.18	1.00	950.20

*Notes:* The unit of analysis for each auction is a single watch.

## G Summary Statistics of Visual Characteristics of Auctioned Watches

Table G.1 details the summary statistics of the visual characteristic levels learned.

**Table G.1:** Summary Statistics of Discovered Visual Characteristics

Visual characteristic	Mean	SD	Min	Max
Dial Size	-0.32	1.42	-9.86	9.92
Dial Color	-0.50	1.52	-3.49	7.20
Strap Color	-0.24	1.67	-3.43	4.82
Rim (Bezel) Color	-0.26	0.90	-6.26	6.14
Dial Shape	0.24	0.95	-7.48	3.09
Knob (Crown) Size	-0.17	0.95	-8.14	10.20

## H Watches: UDR and Hyperparameters for Different Supervisory Signals

Table H.1 lists the UDR corresponding to each combination of supervisory signals. Table H.2 lists the hyperparameters obtained for each combination of supervisory signals.

**Table H.1:** Comparison of Different Supervisory Approaches (at Optimal Hyperparameter Weights for Each Signal)

Number of Signals	Supervisory Signals	UDR
0	Unsupervised	0.131
1	Brand	0.316
1	Circa	0.111
1	Material	0.130
1	Movement	0.122
1	Price (2 Discrete Classes)	0.122
2	Brand & Circa	0.382
2	Brand & Material	0.349
2	Brand & Movement	0.123
2	Brand & Price	0.120
2	Circa & Material	0.209
2	Circa & Movement	0.338
2	Circa & Price	0.103
2	Material & Movement	0.119
2	Material & Price	0.108
2	Movement & Price	0.140
3	Brand, Circa & Material	0.260
<b>3</b>	<b>Brand, Circa &amp; Movement</b>	<b>0.414</b>
3	Brand, Circa & Price	0.342
3	Brand, Material & Movement	0.206
3	Brand, Material & Price	0.299
3	Brand, Movement & Price	0.273
3	Circa, Material & Movement	0.364
3	Circa, Material & Price	0.230
3	Circa, Movement & Price	0.224
3	Material, Movement & Price	0.080
4	Brand, Circa, Material & Movement	0.242
4	Brand, Circa, Material & Price	0.293
4	Brand, Circa, Movement & Price	0.279
4	Brand, Material, Movement & Price	0.262
4	Circa, Material, Movement & Price	0.322
5	Brand, Circa, Material, Movement & Price	0.321

**Table H.2:** Optimal Hyperparameters Obtained by Model Selection Criteria

Approach	Signal	# Signals	$\beta$	$\delta$
Unsupervised	—	0	18	0
Supervised	Brand	1	18	50
Supervised	Circa	1	4	35
Supervised	Material	1	6	25
Supervised	Movement	1	4	20
Supervised	Price	1	1	16
Supervised	Price (with 2 classes)	1	22	45
Supervised	Brand and Circa	2	48	5
Supervised	Brand and Material	2	50	1
Supervised	Brand and Movement	2	6	20
Supervised	Brand and Price	2	6	25
Supervised	Circa and Material	2	36	1
Supervised	Circa and Movement	2	50	5
Supervised	Circa and Price	2	4	18
Supervised	Material and Movement	2	6	10
Supervised	Material and Price	2	4	20
Supervised	Movement and Price	2	12	20
Supervised	Brand, Circa and Material	3	48	1
Supervised	Brand, Circa and Movement	3	50	1
Supervised	Brand, Circa and Price	3	50	1
Supervised	Brand, Material and Movement	3	40	1
Supervised	Brand, Material and Price	3	50	1
Supervised	Brand, Movement and Price	3	48	1
Supervised	Circa, Material and Movement	3	48	1
Supervised	Circa, Material and Price	3	46	1
Supervised	Circa, Movement and Price	3	42	1
Supervised	Material, Movement and Price	3	1	1
Supervised	Brand, Circa, Material and Movement	4	44	1
Supervised	Brand, Circa, Material and Price	4	50	1
Supervised	Brand, Circa, Movement and Price	4	50	1
Supervised	Brand, Material, Movement and Price	4	44	1
Supervised	Circa, Material, Movement and Price	4	44	1
Supervised	Brand, Circa, Material, Movement and Price	5	44	1

## I Using Shapley Values (SHAP) for Disentanglement

In this section, we use an alternative approach to discover visual characteristics. The idea behind this approach is to identify select elements (pixels) of each input image that are predictive of a supervisory signal, and then use those elements as an input to the disentanglement model.

In this approach, we first train a deep learning model to predict the supervisory signal (e.g. brand) from images. Next, we calculate SHAP values to identify which features of the deep learning model drive the model’s results ([Lundberg and Lee 2017](#)). The SHapley Additive exPlanations (SHAP) technique utilizes game theory to interpret the results of machine learning models. It connects optimal credit allocation with local explanations using the classic Shapley values from game theory and their related extensions ([Shapley 1997](#)). SHAP values of each feature captures the contribution of each feature to overall model predictions. It is calculated by estimating differences between models with subsets of the feature space and then averaging across samples.

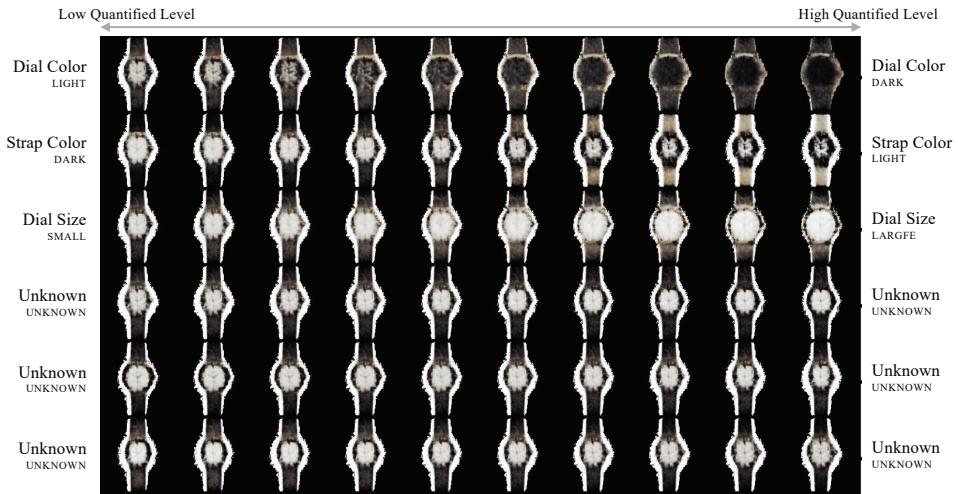
We calculate SHAP values to rank the features based on their contribution to the model’s output. The higher the SHAP value for a feature, the more significant its contribution. We then sort the SHAP values in descending order to select the pixels corresponding to the top features using the SHAP values as a mask. These image subsamples are used as an input to the disentanglement-based VAE model. Figure I.1 shows a sample of images fed to the disentanglement-based VAE model using this approach.

Figure I.2 gives example output of discovered visual characteristics from this approach. In each row of the figure, we show how the watch image changes based on changes in levels of one selected visual characteristic, while keeping all the other characteristics fixed. We show the top six visual characteristics based on the KL divergence value of the difference between the posterior and the Gaussian prior. We can only interpret the first three visual characteristics. The next three visual characteristics appear to be entangled. By entangled, we mean that when any one entangled characteristic is kept fixed and other characteristics are changed, the watch image changes in more than one interpretable way. Note that these characteristics are not uninformative because their KL divergence is not close to 0.

**Figure I.1:** Sample of images from SHAP-based approach



**Figure I.2:** Discovered Visual Characteristics using SHAP-based approach



*Notes:* Latent traversals along a *focal watch* used to visualise the semantic meaning encoded by single visual characteristic learnt by a trained model. In each row, the quantitative level of a single characteristic is varied keeping the other characteristics fixed. The resulting reconstruction is visualized.

## J Conjoint Analysis: Survey Design and Model Estimation

**Conjoint Survey Stages** The conjoint survey stages are summarized along with their purpose in Table J.1.

**Table J.1:** Conjoint Survey Design Elements

Stage	Name	Purpose
1	Introduction	Explain purpose of study and obtain consent. <sup>1</sup>
2	Category Identification	Open-ended questions to determine whether respondents were able to identify what category (e.g. shoes) a blurry image belonged to. <sup>2</sup>
3	Instructional Manipulation Check (IMC)	Attention check “trap question” for post-hoc respondent filtering.
4	Choice-Based Conjoint (CBC) Instructions	Explain upcoming conjoint choice question tasks with instructions to choose based only on visual style. <sup>4</sup>
5	“Warm Up” CBC Practice	Help respondents understand the range of watch designs before making real choices.
6	15 CBC questions	Elicit respondent choice of preferred watch design
7	Respondent Information	Obtain demographic and psychographic variables <sup>7</sup>

<sup>1</sup> Respondents were also instructed to be as “consistent” in their choices as possible, with a monetary incentive of \$2 for consistency (in addition to \$3 for completion).

<sup>2</sup> Respondents saw a set of 4 blurry images for each of the 3 product categories (automobiles, shoes, and watches) similar to the generated watch designs from the disentanglement model. They were then asked for a one word description of the images. We find that greater than 99% of respondents identify the product category depicted in the images. We also used generated watch designs and find that 97% of respondents identify the product category as watches.

<sup>4</sup> Respondents were instructed to choose between two possible watch designs based only on visual style. No other information such as price or other product characteristics were provided.

<sup>7</sup> Respondents demographic variables (e.g., age, gender, income, education) as well as Likert and psychographic questions about how important visual appearance was to the respondent were obtained.

**Estimation of HB Conjoint Analysis Model** We estimated posterior distributions of HB model parameters  $\{\{\beta_i\}_{i=1}^N, \Theta, \mu_\Theta, \Lambda_\beta\}$  with Markov chain Monte Carlo (MCMC) sampling using the No-U-Turn (NUTS) sampler (Hoffman, Gelman et al. 2014). Sampling consisted of 1 chain,<sup>4</sup> each with 2,000 draws of which 2,000 were used for sampler tuning. Convergence of MCMC chains was determined via acceptance criteria of the sampler and its targets (65%), and chain divergences from trace plots (less than 5% draws diverging). Hyperparameter values for prior distributions were determined from overlap of prior draws with posterior draws, and by using both in-sample and out-of-sample hit rates.

<sup>4</sup>Note that we obtained better prediction accuracy numbers with more chains and across parallel GPUs, but report those with a single deterministic chain for replicability.

Our codebase was written in Python using the PyMC library (Patil, Huard, and Fonnesbeck 2010) which leverages the Jax, NumPyro, and Aesara graph compilation libraries to achieve graphical processing unit (GPU) acceleration. Estimation using 1 RTX8000 takes around 15 minutes, with estimation using multiple GPUs approximately dividing the computational time by the number of GPUs, but we note this is heavily dependent on GPU system configuration with CUDA/OpenCL kernel libraries.

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