

Exercise1: Inventory Management System

Ans1. Data Structures and algorithms are crucial in handling large inventories due to the following reasons -

1. They ease efficient data storage, retrieval, and updating, of essence when handling extensive inventories.
2. Efficient data structures reduce the time complexity of operations, hence improving the overall performance of a system.
3. Suitable data structures guarantee that the system scales at an appropriate level with respect to the quantity of products.

Ans2. Suitable Data Structures

1. Functionality of dynamic array: It is very efficient in scenarios that require quick access through indexes.
2. In this, a key-value pair is efficiently stored for fast lookups by product ID, insertions, and deletion purposes.
3. Elements are kept sorted; this is useful where sorted traversal of products is frequent.

Analysis:-

1. Time Complexity Analysis

- A) Add Product - $O(1)$ on average since the addition of a key-value pair to the HashMap is efficient.
- B) Update Product - $O(1)$ on average, due to the operations of the key look-up and insertion in the HashMap.
- C) Delete Product - $O(1)$ on average, since removal of a key-value pair from the HashMap itself is very efficient.
- D) Retrieve Product - $O(1)$ in average, because search by key is well optimised in HashMap.

2. Discussions for Optimising

- A) Batch Operations - Batch processing helps reduce overhead for handling operations one at a time in scenarios of creation, editing, or deletion of more than one product.
- B) Concurrency Handling - Using ConcurrentHashMap instead of HashMap in a multithreaded environment can offer better performance along with thread-safe operations.
- C) Caching - Products that are accessed frequently could be cached to reduce the time taken in retrieving popular items.

Exercise2: E-commerce Platform Search Function

Big O Notation

Ans1. Big O notation refers to a mathematical approach to the measurement of efficiency. The biggest issues about the efficiency of algorithms are time and space complexity. It gives a ceiling on the execution time of an algorithm based on the size of an input and lets us know how an algorithm scales.

Ans2. The answer to the question is as follows -

A) Best Case: The case where an algorithm performs the fewest steps.

B) Average Case: This is the average case—a case where the algorithm runs for an average number of steps.

C) Worst Case: The situation when the algorithm performs the maximum number of steps.

Analysis:-

Comparing the Time Complexities -

Linear Search:

A. Best Case - $O(1)$ Item at beginning

B. Average Case - $O(n)$ item found at the middle

C. Worst Case - Item found at the end or not at all: $O(n)$.

Binary Search:

A. Best Case - $O(1)$ item located in the middle

B. Average Case - $O(\log n)$ It becomes half and half with each step of the array.

C. Worst Case - $O(\log n)$ Item searched is at the end.

Suitability for the platform -

A. Linear search is easy to implement; besides, it can work with an unsorted array, and it's efficient for small datasets where the expense of sorting isn't warranted.

B. Binary Search is much faster for larger datasets, but it requires a sorted array. The extra time complexity to introduce is $O(n \log n)$ for the sort.

C. Binary Search would mostly be more appropriate for an e-commerce platform since it performs better with large data-sets. Since product searches are happening frequently, the upfront cost of sorting balances out by the fast performance of search.

Exercise 3: Sorting Customer Orders

Understand Sorting Algorithms

Bubble Sort -

A) A comparison-based simple algorithm

B) Repeatedly goes through the list, comparing and swapping adjacent elements if they are out of order.

c) Time Complexity: Best Case $O(n)$, Average and Worst Case $O(n^2)$

Insertion Sort -

A) Builds the sorted array one element at a time.

b) Moves all elements greater than the key by one place ahead of the current position of the corresponding key.

C) Time Complexity: Best Case $O(n)$, Average and Worst Case $O(n^2)$.

Quick Sort -

A) A divide-and-conquer algorithm.

B) Choosing a pivot element in the array, it then partitions around that element.

c) Best and Average Case: $O(n \log n)$, Worst Case: $O(n^2)$

Merge Sort -

A) A divide-and-conquer algorithm.

B) Divide the array into two halves, sort these two halves recursively, and then merge the sorted halves together.

C) Time Complexity: $O(n \log n)$ in all cases

Analysis:-

Comparing the Time Complexities -

Bubble Sort:

Best Case: $O(n)$

Average Case and Worst Case: $O(n^2)$

Easy to implement, but inefficient on large datasets due to its quadratic time complexity.

Quick Sort:

Best and Average Case: $O(n \log n)$

Worst Case: $O(n^2)$ (rare, occurs with poor pivot selection) Normally preferred due to its average-case performance and low memory usage.

Why Quick Sort is Preferred:

Efficiency: With an average and best-case time complexity of $O(n \log n)$, quick sort has the edge over bubble sort.

Memory Usage: Quick sort is an in-place sorting algorithm, meaning that it requires only a small, constant amount of extra storage.

Real-World Performance: Quick sort performs better in practice, generally because of the way it uses the cache and due to the divide-and-conquer approach that supports parallelisation.

Exercise 4: Employee Management System

Array Representation in Memory

- A) Contiguous Memory Allocation: The arrays are contiguous in their memory locations. Each element of the array comes next to the other, and hence it facilitates access to any available element through direct access via an index.
- B. Fixed in size: The declaration of the size of the array cannot be changed during the run time of the program.
- c) Efficient Access: This is an efficient access because the time complexity is $O(1)$, as the memory arrangement is predictable.

Advantages of Arrays -

- A) Constant Time Access: Because the index is direct, access is very fast.
- B) Space Efficiency: Arrays use less overhead because a single block of contiguous memory is used.
- C) Cache Performance: This is so because contiguous memory allocation enhances spatial locality and can, hence, improve cache performance.

Analysis:-

Comparing the Time Complexities -

Add Employee: $O(1)$ – The time complexity of adding an element at the end of the array is constant if space is available.

Search Employee: $O(n)$ – The worst case time complexity of search is $O(n)$ because it potentially needs to scan the entire array.

Traverse Employees: $O(n)$ – Linear time complexity to traverse each and every element in the array.

Delete Employee: $O(n)$ - In the worst case, removing an element might require other elements to be slid over to fill the gap.

Arrays Limitations -

Fixed Size: Arrays are fixed in size. This could result in waste of memory if the array doesn't use all the space available, or running out of capacity if the program doesn't have enough space to store all the elements.

Insertion and Deletion: The process of inserting or deleting elements may prove to be inefficient as other elements should be shifted.

Sparse Data: Arrays are not very good at sparse data structures where the elements are spread over a large range of indices.

When to use Arrays -

Fixed Size Collection: Number of elements is fixed and remains the same.

Fast Access: Need quick access to elements via index.

Memory Contiguity: To avoid extra memory structures overhead; it's good if memory can be contiguous.

Exercise 5: Task Management System

Let us understand the Linked Lists

Types of Linked Lists -

Singly Linked List -

-> Each node contains data and a pointer to the next node in the sequence.

-> Operations are simple but can be performed only in one direction.

Doubly Linked List:

→ Each node holds data, a pointer to the next node, and a pointer to the previous node.

-> It is capable of both forward and backward traversal.

It will use a bit more memory, due to the extra reference.

Analysis:-

Comparing the Time Complexities -

Add Task – $O(n)$: In the worst case, this is the time taken to add a task, as it will need to traverse to the end of the list.

Search Task – $O(n)$: Generally, searching can be a linear time of traversing the entire list, in order to traverse, it needs to look at the entire list.

Traverse Tasks – $O(n)$: Given the fact that every single element in a list must be traversed one at a time in linear time.

Delete Task – $O(n)$: On worst-case terms, deleting a task might need to traverse the list till the particular task is discovered.

Benefits of using Linked Lists over Arrays are as follows -

Dynamic Size — Linked lists can grow and shrink, in contrast to arrays.

More Efficient Insertions/Deletions — Particularly for large lists or when operations are near the head of the list, insertions and deletions tend to be more efficient.

Memory Utilization: If the number of elements is variable or unknown, then linked lists use available memory more appropriately as compared to arrays since, in an array, there is a fixed-size memory block.

Drawbacks of Using Linked Lists -

Access Time: Linked lists need some $O(n)$ access time for reaching an element because the linked lists have the need of sequential traversal, compared to the arrays that provide some $O(1)$ access time.

Memory Overhead: Each node in the list contains extra memory to store a reference to the next one, this just being overhead many times, becoming significant in large lists.

Exercise 6: Library Management System

Linear Search Algorithm is discussed below -

Linear search looks at all the elements of the list one by one until a match is found or the end of the list is reached.

Time Complexity:

Best Case: $O(1)$ (element at start)

Average Case: $O(n)$

Worst Case: $O(n)$ (element at end or not found)

Binary Search Algorithm is discussed below -

It requires a sorted list and accomplishes the searching task by successively halving the search interval, comparing the target value with the middle element, and consequently giving a decision as to which half is to be searched next.

Time Complexity:

-> Best Case: $O(1)$ Middle element is the target

-> Average Case: $O(\log n)$

-> Worst Case: $O(\log n)$

Analysis:-

Comparing the Time Complexities -

Linear Search:

Best Case: $O(1)$

Average Case: $O(n)$

Worst Case: $O(n)$

Binary Search:

Best Case: $O(1)$

Average Case: $O(\log n)$

Worst Case: $O(\log n)$

When to Use Each Algorithm:

Linear Search:

Applications for unsorted lists are discussed below -

Appropriate for small data sets for which sorting is not practical.

Simple to implement and doesn't require additional setup.

Binary Search:

Applications for sorted lists are discussed below -

More efficient for larger data sets thanks to its logarithmic time complexity.

Exercise 7: Financial Forecasting

Definition -

A problem-solving technique in which a function calls itself as a subroutine. Put differently, it allows a function to execute a few times by calling itself in the process of execution.

Base Case and Recursive Case: There should be a base case that stops recursion and a recursive case that makes the problem easier within recursive functions.

Simplification: It can convert any complex problem into its simple problems.

Time Complexity -

A recursive algorithm with $O(n)$ time complexity, where n is the number of periods. At each call, `predictFutureValue` decreases the number of periods by 1, so there will be n recursive calls.

Memoization of Recursive Solution -

This optimisation stores the results from expensive function calls and returns them quickly whenever the same inputs occur again.

Iterative Approach: Another alternative is that this recursive solution can be converted to the iterative version, which would be more memory efficient and avoid the chances of a stack overflow.