Compton scattering

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I. INTRODUCTION

II. THEORY

II.1. Inelastic scattering of photon

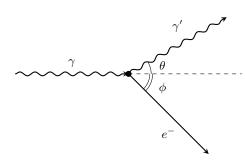


FIG. 1. Compton scattering of a photon by an electron. γ and γ' are the incident and scattered photons. e^- is the recoil electron initially at rest. θ and ϕ are the scattering and recoil angles, respectively.

Following relativistic kinematics, we treat photons as massless particles of energy $E_{\gamma} = h\nu$, where h is the Planck constant and ν is the photon frequency. The energy of an electron is given by $E_e = \sqrt{m_e^2 c^4 + p_e^2 c^2}$, where m_e is the electron rest mass, p_e is the electron momentum, and c is the speed of light. By conservation of energy E and momentum \vec{p} , we have

$$E_{\gamma} + E_e = E_{\gamma}' + E_e',\tag{1}$$

$$\vec{p}_{\gamma} + \vec{p}_e = \vec{p}_{\gamma}' + \vec{p}_e', \tag{2}$$

where the prime denotes the final state. For simplicity, we take the initial electron energy as $E_e = m_e c^2$, that is the particle is initially at rest. Solving Equations (1) and (2), we obtain the energy of the scattered photon as

$$E_{\gamma}' = \frac{E_{\gamma}}{1 + \frac{E_{\gamma}}{m_{\nu}c^2}(1 - \cos\theta)},\tag{3}$$

with θ being the scattering angle, i.e. the angle between the initial and final photon momenta. The kinetic energy of the recoil electron is then approximated as $E'_e = E_\gamma - E'_\gamma$. The scattering scheme is illustrated in Figure 1.

θ	Counting Time	Total Time	Collection Date
$[\deg]$	[s]	[s]	[YYYY-MM-DD]
0	964	1012	2025-03-04
30	1194	1224	2025-03-04
60	1619	1658	2025-03-04
90	1856	1900	2025-03-04
120	1706	1736	2025-03-04
15	1354	1522	2025-03-06
45	1333	1455	2025-03-06
75	1954	2058	2025-03-06
105	1645	1727	2025-03-06
135	1341	1431	2025-03-06

TABLE I.

II.2. Differential cross section

II.3. Total cross section & Attenuation

III. EXPERIMENT SETUP

III.1. Apparatus

III.2. Data Collection

IV. ANALYSIS & RESULTS

IV.1. Energy-angle dependency

IV.2. Scattering rate

V. DISCUSSION & CONCLUSION

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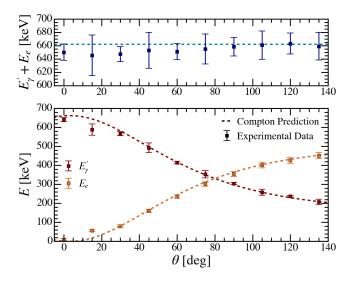


FIG. 2.

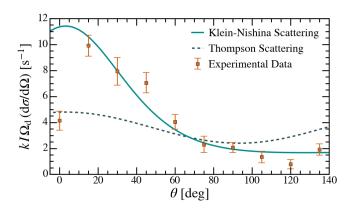


FIG. 3.

Appendix A: Energy Calibration

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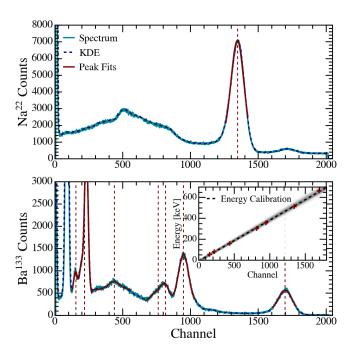


FIG. 4.