



- 12 lengths ( $l$ ), at each measure 16 10-periods. The actual periods and uncertainties ( $\mu_T, \sigma_T$ ) are reduced using Bayesian statistics with equal-probabilistic priors

$$-2 \log(\mathcal{L}) = N \cdot \log(2\pi\sigma_T^2) + \sum \left( \frac{T - \mu_T}{\sigma_T} \right)^2$$

$$\mu_T, \sigma_T = \arg \min_{\mu_T, \sigma_T} -2 \log(\mathcal{L})$$

- The gravitational field strength (and the COM offset) is then obtained via the chi-square maximum likelihood fitting  $\chi^2 = \sum \left( \frac{(y - \hat{y}(x))}{\sigma_y} \right)^2$ , with  $y = \left( \frac{T}{2\pi} \right)^2$ ,  $x = l$ , and  $\hat{y}(x) = \frac{x + l_0}{g}$  (using the  $I_M \sim Md^2 \ll Ml^2$  approximation).
- However, measurements of  $l$  is typically off by 2mm, which we model as uniform distribution centering at  $l$  with widths of 4mm. Sampling values of  $l$  and repeating the chi-square optimization, we obtain the following distribution of fitted parameters.
- Main source of systematic errors: the  $I_M$  approximation ( $\sim 1\%$ ), (exhausted) human reaction speed ( $\sim 2 \times \frac{0.2s}{20s} \sim 2\%$ ). We note that by taking many measurements at the same length and performing a Bayesian fitting, the latter is greatly reduced. An additional source of error is the pivot of the pendulum being bended due to the wire stiffness. In total,  $\sigma_g^{sys} \simeq 0.09 \text{ m s}^{-2}$ .

