

Calculo geral determinantes

Nome: Vinicius Fernandes da Silva
Turma: CT11317

01 - Determinantes:

$$A = \begin{vmatrix} 1 & a & 0 & 1 & a \\ 0 & 1 & 1 & 0 & 1 \\ 0 & -1 & 1 & 0 & -1 \end{vmatrix}$$

$$\det A = 1 - (-1) = 2$$

$$1 - 1 = 0$$

$$B = \begin{vmatrix} 1 & 0 & 0 & 3 \\ a & 1 & -1 & 4 \\ 0 & 0 & 0 & 3 \\ 0 & 1 & 1 & 4 \end{vmatrix}$$

a. (of 2x2)

1. (of (a₁₁))

$$a. \begin{vmatrix} 0 & 0 & 3 & 0 & 0 \\ 0 & 0 & 3 & 0 & 0 \\ 1 & 1 & 4 & 1 & 1 \end{vmatrix}$$

0³

$$a. 0 = 0$$

$$-3 - 3 = -6$$

$$\det A = 2$$

$$\det B = -6$$

02) (Ratic) Calcule x na equação:

$$\begin{vmatrix} x^2 & 0 & x & -\frac{1}{10} \\ 7,5 & 0 & 5 & 2 \\ 10 & 0 & 4 & 2 \\ 1 & 1 & 1 & 1 \end{vmatrix} = 0$$

1. $\text{Cof}(a_{42})$

$$1. \begin{vmatrix} x^2 & x & -0,1 \\ 7,5 & 5 & 2 \\ 10 & 4 & 2 \end{vmatrix} \begin{vmatrix} x^2 & x \\ 7,5 & 5 \\ 10 & 4 \end{vmatrix}$$

$$10x^2 + 20x - 3 + 5 - 8x^2 - 15x = 0$$

$$2x^2 + 5x + 2 = 0$$

$$\Delta = b^2 - 4 \cdot a \cdot c$$

$$\Delta = 5^2 - 4 \cdot 2 \cdot 2$$

$$\Delta = 9$$

$$x = \frac{-5 \pm \sqrt{9}}{2 \cdot 2}$$

$$x_1 = \frac{-5 + 3}{4} = -\frac{1}{2}$$

$$x = \frac{-5 - 3}{4}$$

$$x_2 = \frac{-5 - 3}{4} = -2$$

R: $x = -\frac{1}{2}$ ou $x = -2$

03) (PUCSP) O determinante

$$\begin{vmatrix} x & 0 & 0 & 3 \\ -1 & x & 0 & 0 \\ 0 & -1 & x & 1 \\ 0 & 0 & -1 & -2 \end{vmatrix}$$

Representa o polinômio:

$x \cdot \text{cof}(a_{22})$

$-1 \cdot \text{cof}(a_{32})$

$x \cdot \begin{vmatrix} x & 0 & 3 \\ 0 & x & 0 \\ 0 & -1 & -2 \end{vmatrix}$

$-1 \cdot \begin{vmatrix} x & 0 & 3 \\ -1 & 0 & 0 \\ 0 & -1 & -2 \end{vmatrix}$

$-2x^2 - (-x)$

-3

$x \cdot (-2x^2 + x)$

$-1 \cdot -3 = -3$

$-2x^3 + x^2$

$-2x^3 + x^2 - 3$

04. (UFSCAR) matrix A $f: \mathbb{R} \rightarrow \mathbb{R}$ tal que
 $f(x) = \det A - f(-2) = 8$, então K vale:

$$\begin{vmatrix}
 x & 1 & 0 & 0 & 0 \\
 0 & x & 1 & 0 & 0 \\
 0 & 0 & x & 1 & 0 \\
 0 & 0 & 0 & x & K \\
 0 & 0 & 0 & 1 & x
 \end{vmatrix}$$

$$x \cdot x \cdot x = x^3$$

$$\begin{vmatrix}
 x & K \\
 1 & x
 \end{vmatrix} = x^2 - K$$

$$\det A = x^3 \cdot (x^2 - K)$$

$$f(x) = \det A$$

$$f(-2) = -2^3(-2^2 - K) = 8$$

$$f(-2) = -8(-4 - K) = 8 \Rightarrow 8 = 8$$

INCOMPLETO