

78  
15, 17, 25, 24, 20, 21, 32, 28, 12, 25, 25, 26

- >  $H_0$ : population median is 20
- >  $\alpha = 0.05$
- >  $X$
- > wilcox.test(x, alt = "less", mu = 20)

wilcoxon signed rank test with continuity correction

data = x  
 $\mu = 18.5$  p.value = 0.9732  
alternative hypothesis: true location is less than 20

$\checkmark \alpha = 0.05$

66

3

a) 63, 65, 60, 89, 61, 71, 98, 51, 69, 32;  
 63, 62, 39, 72, 65  
 using wilcoxon signed Rank test (dtypo, thgt)  
 population median is 60 against alternative  
 it is greater than 60. S.T. cos.

$H_0$  population median is 60

?  $x = c(63, 65, 60 \dots)$   
 ? wilcox.test(x; alt = "greater", m=60)

wilcoxon signed rank test with continuity  
 correction

data: x,

V< 79.5 p-value: 0.04781

alternative hypothesis: true location is greater  
 than 60

e)  $X = \{612, 619, 631, 628, 643, 640, 655, 6\cancel{4}1, 670$   
663)

>  $X$

>  $m = 625$

[1] 625

>  $SP = \text{length}(X[m:m])$

>  $SP$

[1] 8

>  $s_n = \text{length}(X[x:m])$

[1] 2

>  $n = SP + s_n$

[1] 10

>  ~~$P^v$~~ ,  $pbinom(SP, n, 0.5)$

>  $P^v$

[1] 0.9892518

$\therefore P\text{value} > 0.01$ , we accept  $H_0$

group	type	observation
5a	A	20, 23, 18, 17, 18, 22, 24
B		19, 15, 17, 20, 16, 17
C		21, 14, 22, 19, 20
D		15, 14, 16, 18, 14, 16

names (d)

values "ind"

one way test (values ind, data, df unequal)

one way analysis of means

data = value ind

p = 6.8445, num. df = 3, chisq = 20 pvalue = 0.002

onova = anova (values = ind, data = s)

onova = anova (formula = value - ind, data = d)

Terms ind Residents

sum of squares 91.4781 84.0619

deg of freedom 3 20

∴ pvalue < 0.05 we reject  $H_0$

s)		T.O condition	
High	High	100s.	
high	450	140	
	330	200	
Low	240	160	

$H_0$ :  $C_i \neq T_O$  are independent

$\geq x = c(460, 330, 240, 140, 200, 160)$

$\geq m = 3$

$\geq n = 2$

$\geq y = \text{matrix}(x, nrow = m, ncol = n)$

$\geq y$

$C_1, J$	$C_1, 1$	$C_1, 2$
460	140	
$C_2, J$	330	200
		160
$C_3, J$	240	

$\geq p = \text{chisq.test}(y)$

$\geq p =$  Pearson's chi-squared test

$\geq \text{data} = y$

$\geq X^2 = 39.726 \cdot df = 2 \cdot pvalue = 2.3647 \cdot 0^{-9}$

$\geq pvalue < 0.05 \text{ we reject } H_0$

3)

varieties

A

B

C

D

observations

50, 52

53, 55, 53

60, 58, 57, 56

52, 54, 54, 53

62

 $H_0$ : The means of variety are equal $\rightarrow X_1 = ((50, 52))$  $\rightarrow X_2 = ((53, 55, 53))$  $\rightarrow X_3 = ((60, 58, 57, 56))$  $\rightarrow X_4 = ((52, 54, 54, 53))$  $\rightarrow d = \text{stack}(list(b_i = X_1, X_2, X_3, X_4)))$ values(d)  $\rightarrow [1] \text{ 'values' - ind'}$ 

one way test (covariance = 0, data = d, var.equal = T)

one way analysis of var

data = values \$ind

F = 11.735, num df = 3, denom df = 9, pvalue = 0.00183

onova

call:

asv(formula = value ~ ind, data = d)

Tennis

sum of squares

IND

Residuals

71.07692

18.06667

Reg of freedom

3

9

Residential standard error = 1.420746

estimated effects may be unbalanced.

 $\therefore p\text{value} < 0.05$  we reject  $H_0$

5)  $H_0: \mu_1 = \mu_2$  against  $H_1: \mu_1 \neq \mu_2$   
data:  $x = c(63, 63, 68, 69, 71, 71, 72)$

> f test + one sample test

data:  $x$   
> f.test(x, df = 6, p.value = TRUE)  
f = 45.94, df = 6, p-value = 5.22e-09  
alternative hypothesis: true mean is not equal to  
the confidence interval  
 $[64.66999, 91.62]$

Sample estimate

mean of  $x$

64.142

$\therefore 5.22 \times 10^{-9} < 0.01$   
we reject hypothesis

### Practical No - 10

61

#### Anova and chi-squared test

		cleanliness of home	
		clean	dirty
child	clear	70	50
	Impure	80	20
	dirty	35	45

$H_0:$  cleanliness of child & home are independent.

> x = c(70, 80, 35, 50, 20, 45),

> m = 3

> n = 2

> y = matrix(x, nrow = m, ncol = n)

> g

	<del>[1,]</del>	<del>[2,]</del>	<del>[3,]</del>
<del>[1,]</del>	70	50	
<del>[2,]</del>	80	20	
<del>[3,]</del>	35	45	

> p\_value\_chi\_sq(y)

> p\_value

person's chi squared test

data: y  
 $\chi^2 = 25.646$  df = 2 p-value = 2.698e-06

p-value < 0.05 we reject  $H_0$ : ch & home are independent

68

```
> n1 = 1000  
> n2 = 1500  
> p1 = 0.02  
> p2 = 0.01  
> p = (n1 * p1 + n2 * p2) / (n1 + n2)  
> p  
[1] 0.014  
> q = 1 - p  
> q  
[1] 0.986  
> zcal = (p1 - p2) / sqrt(p1 * q1 / (n1) + p2 * q2 / (n2))  
[2] 2.084842  
> pvalue = 2 * (1 - pnorm(qabs(zcal)))  
> pvalue  
[1] 0.03703364
```

69

```
> H0 = H0: H1 is against H0: H0 is H0,  
> n = 400  
> m0 = 99  
> m1 = 100  
> vox = 64  
> sd = sqrt(vox)  
> zcal = (m1 - m0) / (sd / sqrt(n))  
> zcal  
[1] -2.5  
> pval = 2 * (1 - pnorm(qabs(zcal)))  
> pval  
[1] 0.0124  
.. pvalue < 0.05, we reject H0
```

- The p value is greater than 0.05. we accept the null hypothesis. i.e. no increase in mass at 5% level of significance.

Practical no-9

59

1)  $n = 100$   
 $m_1 = 55$   
 $m_2 = 55$   
 $s_d = 7$   
 $z_{cal} = (m_1 - m_2) / (s_d / \sqrt{n})$   
 $z_{cal}$   
 $[1] = 4.285714$   
 $pvalue = 2 * (1 - pnorm (abs(z_{cal})))$   
 $pvalue$   
 $[1] 1.82153e-05$   
Since pvalue is less than 0.05 we reject the null hypothesis.

2)  $p = 0.5$   
 $n = 700$   
 $q = 1-p$   
 $c_1 = 0.5$   
 $p = 350 / 700$   
 $z_{cal} = (p - p) / (s_q + (p * q / n))$   
 $z_{cal}$   
 $[1] 0$   
 $pvalue = 2 * (1 - pnorm (abs(z_{cal})))$   
 $pvalue$   
 $[1] 1$

58

a) The weight reducing diet program.

After - (114, 119, 107, 112, 115, 111, 111).  
 Before - (126, 125, 115, 130, 123, 119, 112, 120, 119, 118)

$H_0: \mu_x = \mu_y$

$\rightarrow x = c(110, 125, 115, 130, 123, 119, 112, 120, 119, 118)$

$\rightarrow y = c(114, 119, 107, 112, 115, 111, 111, 120, 119, 118)$

$\rightarrow t\text{-test}(x, y, \text{paired:} T, \text{alternative:} "less")$

$t = -1.7 \quad df = 9 \quad p\text{-value} = 0.119$

95% - percent confidence interval

- Inf 9.416556

The p-value is greater than 0.05 we accept  $H_0$ .  
 The diet program reduce weight

58

55)  $\rightarrow x = c(66, 67, \dots, 90, 92)$

$\rightarrow y = c(64, 66, \dots, 85, 97)$

$\rightarrow t\text{-test}(x, y)$

data: x and y

$t = -0.63938 \quad df = 17.974 \quad p\text{-value} = 0.5304$

Monotone hypothesis: True difference in mean is not equal to 0.05 percent confidence interval:

-17.853992 . . . . . 6.853992

Sample estimates:

mean & SD mean of y

80 . . . . . 83

Since p-value is greater than 0.05 we accept  $x = y$  at level of significance

6)  $x = c(71, 72, \dots, 75)$

$y = c(74, 77, \dots, 78)$

$\rightarrow t\text{-test}(x, y, \text{paired:} T, \text{alternative:} "greater")$

data: x and y

$t = -4.4691 \quad df = 9, \quad p\text{-value} = 0.9992$

alternative hypothesis: true difference in mean is greater than 0.05 percent confidence interval:

-5.676639 . . . . . Inf

Sample estimates

mean of the differences

-3.6

Q) Two groups with subjects scored N follows

group A: 15, 12, 13, 17, 20, 19, 13, 20, 22, 21  
group B: 16, 10, 14, 21, 20, 19, 13, 15, 17, 21  
n = 10, 10

$t = 0.16$ ,  $df = 18$ ,  $p\text{-value} = 0.8573$

$t = 0.16$ ,  $df = 18$ ,  $p\text{-value} = 0.8573$

as percent confidence interval

$\pm 8.62 \pm 0.5$  S.E.M.

mean of  $X$  mean of  $y$   
16.7 17.5

The p-value is greater than 0.05 so we accept  $H_0$  at 1% level of significance

Q3) Two types of medicines are used on 5 and 7 patients for reduce their weight

med A: (10, 12, 13, 11, 14)  
med B: (8, 9, 12, 14, 15, 10, 9)

$H_0: \mu_1 = \mu_2$

> med A - C (10, 12, 13, 11, 14)

> med B - C (8, 9, 12, 14, 15, 10, 9)

> T-test (med A vs med B)

$t = 0.80354$ ,  $df = 9$ ,  $p\text{-value} = 0.41406$

as percent confidence interval

$1.7811 \quad 3.78117$

$\therefore$  The p-value is greater than 0.05 we accept  $H_0$  at 1% level of significance

25

>sd1: sqrt(covariance)

>sd1  
 [1] 2.512215

[1] 2.512215  
 >x1=c(72,76,74,70,76,78,70,72,78,79,74,  
 75,78,72,74,80)

>x1  
 [1] 72 76 74 70 70 78 70 72 78 79 74  
 75 78 72 74 80

>n1= length(x1)

>n1  
 [1] 17

>m1=mean(x1)

>m1  
 [1] 74.58824

>covariance=(n1-1)\*cov(x1)/n1

>covariance

[1] 10.47751

>sd2: sqrt(covariance)

>sd2

[1] 3.6236598

>t.test(x1, x2)

p-value ~ 0.1387

>0.05 is accepted  $H_0: \rho_1 = \rho_2$

$\rho_1$

Practical-8

56

Small sample test

(Q.1) >x1=c(80,100,110,105,112,70,110,116,101,  
 88,83,95,89,107,125)

>length(x1)

[1] 15

>t.test(x1)

t = 240.29 df: 14 p.value: 8.819e-15

95 percent confidence interval 91.37775 109.28892

∴ The p-value is less than 0.05 we reject

$H_0: H_1: H_1$  at 5% level of significance

$p_1 = 44/150$   
 $p_2 = 48$   
 $n_1 = 170$   
 $n_2 = 150/200$   
 $p_1 =$   
 $n_1 = 15$   
 $(p_1 \times p_1 + p_2 \times p_2) / (n_1 + n_2)$   
 $p =$

$n_1 = 0.164444$   
 $p = 1 - p$

$q =$

$n_1 = 0.535556$   
 $> z_{\text{cal}} = (p_1 - p_2) / \sqrt{p_1 \times p_2 \times (1/n_1 + 1/n_2)}$

$> z_{\text{cal}}$

$n_1 = 0.734358$ ,  
 since p-value is greater we accept  
 $H_0: p_1 = p_2$

55

$\textcircled{a} > n_1 = 400$   
 $> n_2 = 600$   
 $> p_1 = 200 / 600$   
 $> p_2 = 300 / 600$   
 $> p = (p_1 \times p_1 + p_2 \times p_2) / (n_1 + n_2)$   
 $> q = 1 - p$   
 $> z_{\text{cal}} = (p_1 - p_2) / \sqrt{p_1 \times p_2 \times (1/n_1 + 1/n_2)}$   
 $> z_{\text{cal}}$   
 $\textcircled{b} 4.724751$   
 $> \text{pvalue} = 2 * [1 - \text{pnormabs}(z_{\text{cal}}))]$   
 $> \text{pvalue}$   
 $\textcircled{c} 2.303472e-06$   
 since pvalue is accepted  $H_0: p_1 = p_2$

$\textcircled{d} > x_1 = c(78, 72, 74, 73, 79, 76, 82, 72, 75, 78, 77, 71, 78, 76, 70)$   
 $> x_2$   
 $\textcircled{e} 74, 77, 74, 73, 79, 76, 82, 72, 75, 78, 77, 73, 76, 77$

$> n_1 = \text{length}(x_1)$   
 $> n_2$   
 $\textcircled{f} 14$   
 $\text{mean}(x_1)$   
 $> mx_1$   
 $\textcircled{g} 76.21429$   
 $> \text{variance} = (n-1)^{-1} \sum \text{var}(x_i) / n_1$   
 $> \text{variance}$   
 $\textcircled{h} 6.311224$

82

```

> zcal ("z calculated is :"; zcal)
> zcal = 3 - 15.80639
> pvalue = 2 * pnorm (abs (zcal))
> pvalue
[1] 0.0

```

so as we reject  $H_0$  at  $\alpha = 0.05$

- a) A study at race level to hospitals release following data: is calculated sample size 84 sample mean 61.7,  $s_{\bar{x}} = 7.0$ , sample size 33 sample mean 59.4,  $s_{\bar{x}} = 7$ .  $H_0: \mu_1 = \mu_2$  against  $\mu_1 > \mu_2$  at 1% level of significance

```

>n1
[1] 84
>n2
[1] 33
>m1
[1] 59.4
>m2
[1] 61.7
>s1
[1] 7.0
>s2
[1] 7.0
>mx1
[1] 59.4
>mx2
[1] 61.7
>sd1
[1] 7.0

```

$s_{\bar{x}} = 7.5$

[1] 7.5

>zcal = (m1 - m2) / sqrt ((sd1^2/n1) + (sd2^2/n2))  
>zcal

[1] 1.13111

>zcal ("z calculated is :"; zcal)

>zcal = 1.13111

>pvalue = 2 \* pnorm (abs (zcal))

>pvalue

[1] 0.258006

since pvalue is greater than 0.01 we accept

- a-3) From each of two population of oranges the following samples are collected whether the proportion of bad oranges are equal or not
- i) sample size = 250  
ii) sample size = 200  
iii) no. of bad orange in 1st sample = 44  
iv) no. of bad orange in 2nd sample = 30

$H_0: P_1 = P_2$

$H_A: P_1 \neq P_2$

>n1 = 250

>n2

[1] 250

>m1 = 200

>n2

[1] 200

52  
 >2cal  
 C) -0.6862964  
 >pvalue = 2 \* C1-pnorm (abs (2cal))  
 >pvalue  
 C) 0.5116234  
 since pvalue is more than 0.05 we accept  
 H0: N=50

~~P1 29.11.10~~

Practical no-7  
 53  
 Large sample test  
 .) Two random samples of size 1000 and 2000 are drawn from two populations with standard deviations 2 and 3 respectively. Test the hypothesis that two population means are equal or not at 5% level if significant sample means are 67 and 68 respectively.  
 → >n1 = 1000  
 >n1  
 C) 1000  
 >n2 = 2000  
 >n2  
 C) 2000  
 >mx1 = 67  
 >mx1  
 >67  
 >mx2 = 68  
 >mx2  
 C) 68  
 >sdl = 2  
 >sdl  
 C) 2  
 >sdi = 3  
 >sdi  
 C) 3  
 >zcal = (mx1 - mx2) / sqrt (sdl^2/n1 + sdi^2/n2)  
 >zcal  
 C) -15.80686

17

[1] 8.33333  
> cat(z calculated is "", zcal)  
z calculated is : 8.33333  
> pvalue = 2 \* (1 - pnorm (abs (zcal)))  
> pvalue.

[1] 0  
since pvalue is less than 0.05 we reject H<sub>0</sub>.

Q.3) we want to test the hypothesis H<sub>0</sub>: P = 0.2 against H<sub>1</sub>: P ≠ 0.2  
if population proportion is assumed to be 0.2 and sample size n is selected  
and if sample proportion is calculated 0.625 test the  
hypothesis at 1% level of significance.

→ > P = 0.2  
> Q = 1 - P  
> P = 0.125  
> n = 400  
> zcal = (p - P) / sqrt(P \* Q \* (n / 100))  
> zcal  
[1] -3.75  
> pvalue = 2 \* (1 - pnorm (abs (zcal)))  
> pvalue.  
[1] 0.0001768346

Since pvalue is less than 0.05 we reject H<sub>0</sub>

Q.4) In a big city 325 men out of 500 men were  
found to be self employed. Test this using Z-test to  
support the conclusion that exactly half of the  
men are self-employed

→ > p = 0.5  
> n = 500  
> p = 325 / 500  
> Q = 1 - p  
> zcal = (p - P) / sqrt(P \* Q \* (n / 100))  
> zcal  
[1] -2.041241  
> pvalue = 2 \* (1 - pnorm (abs (zcal)))  
> pvalue  
[1] 0.04121683  
since pvalue is less than 0.05 we reject H<sub>0</sub>.

Q.5) Test the hypothesis of H<sub>0</sub>: μ = 50 against H<sub>1</sub>: μ ≠ 50

A sample of 30 is collected.  
50, 49, 52, 44, 45, 48, 46, 45, 49, 45, 40, 47, 55,  
54, 46, 58, 47, 44, 59, 60, 61, 41, 52, 44, 55, 56,  
46, 45, 48, 49.  
→ m0 = 50  
> x = c(50, 49, 52, ..., 48, 49)  
> n = length(x) > n [1] 30  
> mx = mean(x) > mx [1] 49.3333  
> variance = (n - 1) \* var(x) / n [1] 30.45556  
> sd = sqrt(variance) > sd [1] 5.563772  
> zcal = (mx - m0) / sd / (sqrt(n))

a)  $X \sim N(50, 10)$

Find: i)  $P(X \leq 60)$  ii)  $P(X > 65)$  iii)  $P(45 \leq X \leq 60)$

> pnorm(60, 50, 10)

[i] 0.8413447

> pnorm(65, 50, 10) - pnorm(45, 50, 10)

[ii] 0.5328072

> 1 - pnorm(65, 50, 10)

[iii] 0.0668672

✓

M

Practical no:- 6

i) Test the hypothesis  $H_0: \mu = 20$  against  $H_1: \mu \neq 20$ . A sample of size 400 with selective and sample mean is 20.2 and a standard deviation 2.25. Test that at 5% level of significance.

> m0 = 20

> mx = 20.2

> sd = 2.25

> n = 400

> zcal =  $(mx - m_0) / (sd / \sqrt{n})$

> zcal

[i] 1.777778

> cat ("2 calculator is" / 2 cat)

> calculated is = 1.777778

> pvalue

[ii] 0.07544056

since pvalue is more than 0.05 we accept  $H_0: \mu = 20$

ii) we want to test the hypothesis  $H_0: \mu = 250$  against  $H_1: \mu \neq 250$ . A sample of size 100 has a mean of 275 and SD of 30. Test the hypothesis at 5% level of significance.

> mb = 250

> mn = 275

> sd = 30

> n = 100

> zcal =  $(mx - mb) / (sd / \sqrt{n})$

> zcal

Q1

> x = qnorm(0.4, 10, 2)

> k

[1] 9.493306

Q2  $X \sim N(100, 36)$

i)  $P(X \leq 110)$  ii)  $P(X > 105)$  iii)  $P(X \leq 92)$

v)  $P(95 \leq X \leq 105)$  vi)  $P(X < k) = 0.9$

> a = rnorm(100, 100, 6)

> a

[1] 0.9522096

> b = 1 - pnorm(105, 100, 6)

> b

[1] 0.2023284

> c = pnorm(92, 100, 6)

> c

[1] 0.09121122

> d = pnorm(110, 100, 6) - pnorm(95, 100, 6)

> d

[1] 0.7498813

> k = qnorm(0.9, 100, 6)

> k

[1] 104.6893

Q3 Generate 10 random sample and find sample mean, median, variance and standard deviation

> x = rnorm(10, 10, 3)

> x

[1] 13.937393 12.040522 11.512806 9.774476  
[5] 3.884007 8.433805 15.813018 14.174675  
[9] 6.495235 9.30591

> am = mean(x)

[1] 10.73711

> me = median(x)

[1] 10.64364

> n = 10

[1] 10

> var = (n-1) \* var(x) / n

> var

[1] 9.995247

> sd = sqrt(var)

> sd

[1] 3.161526

Q4) plot the standard curve

> x = seq(-3, 3, by = 0.1)

> x

> y = dnorm(x)

> y

> plot(x, y, xlab = "X values", ylab = "probability",  
main = "standard normal curve")

Practical no-4

$$8A \quad P(X=x) = \binom{n}{x} p^x q^{n-x}$$

$n=8$ ,  $p=0.6$ ,  $q=0.4 \rightarrow$  given

$$1. \quad P(X=7) = \binom{8}{7} (0.6)^7$$

$$= 8 \times 0.2799 \times 0.4$$

$$= 0.08957$$

$$2. \quad P(X \leq 3) = P(0) + P(1) + P(2) + P(3)$$

$$= 8(0.6)^0 (0.4)^8 + 8((0.6)^1 (0.4)^7) + 8((0.6)^2 (0.4)^6) + 8((0.6)^3 (0.4)^5) \\ = 0.1736704$$

$$3. \quad P(X=2 \text{ or } 3) = P(2) + P(3)$$

$$= 0.04128768 + 0.12366304 \\ = 0.161515012$$

✓

M'

Practical-5

49

Normal Distribution

$$X \sim N(\mu, \sigma^2)$$

$$1. \quad P(X=x) = dnorm(x, \mu, \sigma)$$

$$2. \quad P(X \leq x) = pnorm(x, \mu, \sigma)$$

$$3. \quad P(X > x) = 1 - pnorm(x, \mu, \sigma)$$

4. To find the value of  $x$ , so that  $P(X \leq x) = Q$

$$qnorm(Q, \mu, \sigma)$$

5. To generate a random sample of size  $n$ , rnorm(n,  $\mu$ ,  $\sigma$ )

1. A random variable  $X$  follows normal distribution with  $\mu=10$ ,  $\sigma=2$ , find:

$$\text{i)} P(X \leq 7) \quad \text{ii)} P(X > 12) \quad \text{iii)} P(5 \leq X \leq 12)$$

$$\text{iv)} P(X < 10) = 0.4$$

$$> P_1 = pnorm(7, 10, 2)$$

$$[1] 0.6668072$$

$$> P_2 = 1 - pnorm(12, 10, 2)$$

$$> P_2$$

$$[1] 0.1586553$$

$$> P_3 = pnorm(12, 10, 2) - pnorm(5, 10, 2)$$

$$> P_3$$

$$[1] 0.8351351$$

Find c.d.f of following pmf. draw the graph.  
of pdf

x	1	2	3	4
p(x)	0.4	0.3	0.2	0.1

$$\rightarrow x = (1, 2, 3, 4)$$

$$\text{prob} = (0.4, 0.3, 0.2, 0.1)$$

>a: cumsum (prob)

>a

$$\{1\} 0.4 \quad 0.7 \quad 0.9 \quad 1.0$$

plot (x, a, "s")

x	0	1	2	3	4	5	6	7	8
p(x)	0.2	0.3	0.2	0.2	0.2	0.1			

$\rightarrow$

$$x = (0, 1, 2, 3, 4)$$

$$\text{prob} = (0.2, 0.3, 0.2, 0.2, 0.1)$$

>a: cumsum (prob)

>a

$$\{1\} 0.2 \quad 0.5 \quad 0.7 \quad 0.9 \quad 1.0$$

plot (x, a, "s")



here the second condition does not satisfy  
 . It is not pmf  
 Q: Following is a pmf of  $X$ . Find mean & variance

$x$	1	2	3	4	5
$p(x)$	0.1	0.15	0.2	0.3	0.25
$x \cdot p(x)$	0.1	0.3	0.6	1.2	1.25
1	0.1	0.15	0.2	0.3	0.25
2	0.15	0.3	0.6	1.2	1.25
3	0.2	0.6	1.8	2.4	2.5
4	0.3	0.9	2.7	3.6	3.75
5	0.25	0.75	2.25	3.75	3.75
					13.53

$$\text{Mean} = E(X) = \sum x \cdot p(x) = 13.53$$

$$\text{Variance} = V(X) = \sum x^2 \cdot p(x) - [E(X)]^2 \\ = 13.53 - 11.9025 \\ = 1.6475$$

$$\rightarrow x = \{1, 2, 3, 4, 5\}$$

$$\rightarrow \text{prob} = \{0.1, 0.15, 0.2, 0.3, 0.25\}$$

$$\rightarrow a = x * \text{prob}$$

>a

$$[1] 0.1 0.3 0.6 1.2 1.25$$

$$\rightarrow \text{sum}(a)$$

$$[1] 3.43$$

$$\rightarrow \text{mean} = \text{sum}(a)$$

$$[1] 3.43$$

### Practical no 3:

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$$b = (x^2) * \text{prob}$$

>b

$$[1] 0.16 0.66 1.80 4.80 6.25$$

>sum(b)

$$[1] 13.55$$

$$>\text{var} = \text{sum}(b - \text{mean})^2$$

>var

$$[1] 1.6475$$

Q: Following is a pmf of  $X$  and find mean, variance ( $CX$ )

$x$	5	10	15	20	25
$p(x)$	0.1	0.3	0.2	0.25	0.15

$\rightarrow x = \{5, 10, 15, 20, 25\}$

$$\rightarrow \text{prob} = \{0.1, 0.3, 0.2, 0.25, 0.15\}$$

$$a = x * \text{prob}$$

>a

$$[1] 0.50 3.00 3.00 5.00 3.75$$

>sum(a)

$$[1] 15.25$$

$$\text{mean} = \text{sum}(a)$$

$$[1] 15.25$$

$$\rightarrow b = (x^2) * \text{prob}$$

>b

$$[1] 2.50 30.00 45.00 100.00 93.75$$

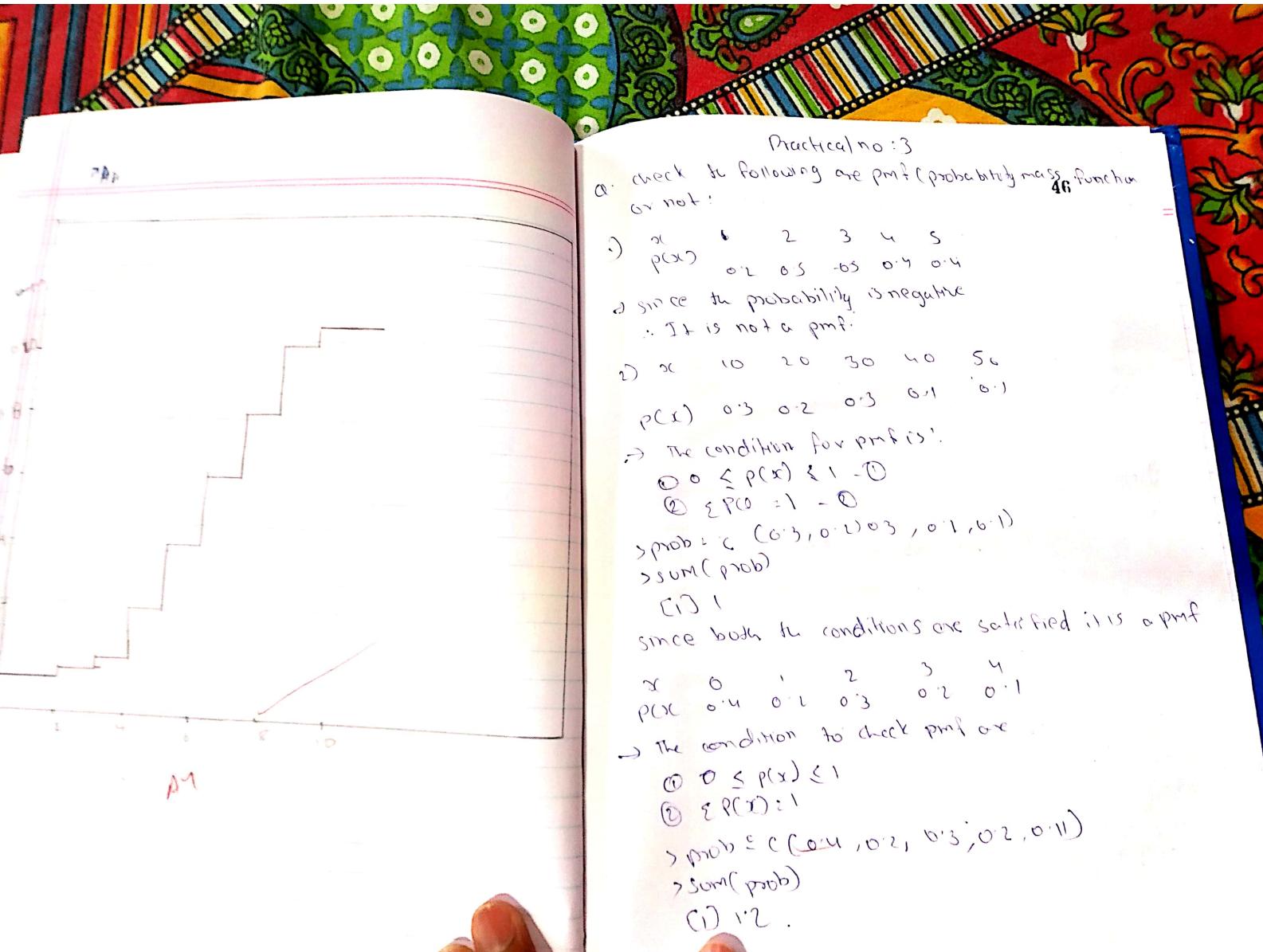
>sum(b)

$$[1] 271.25$$

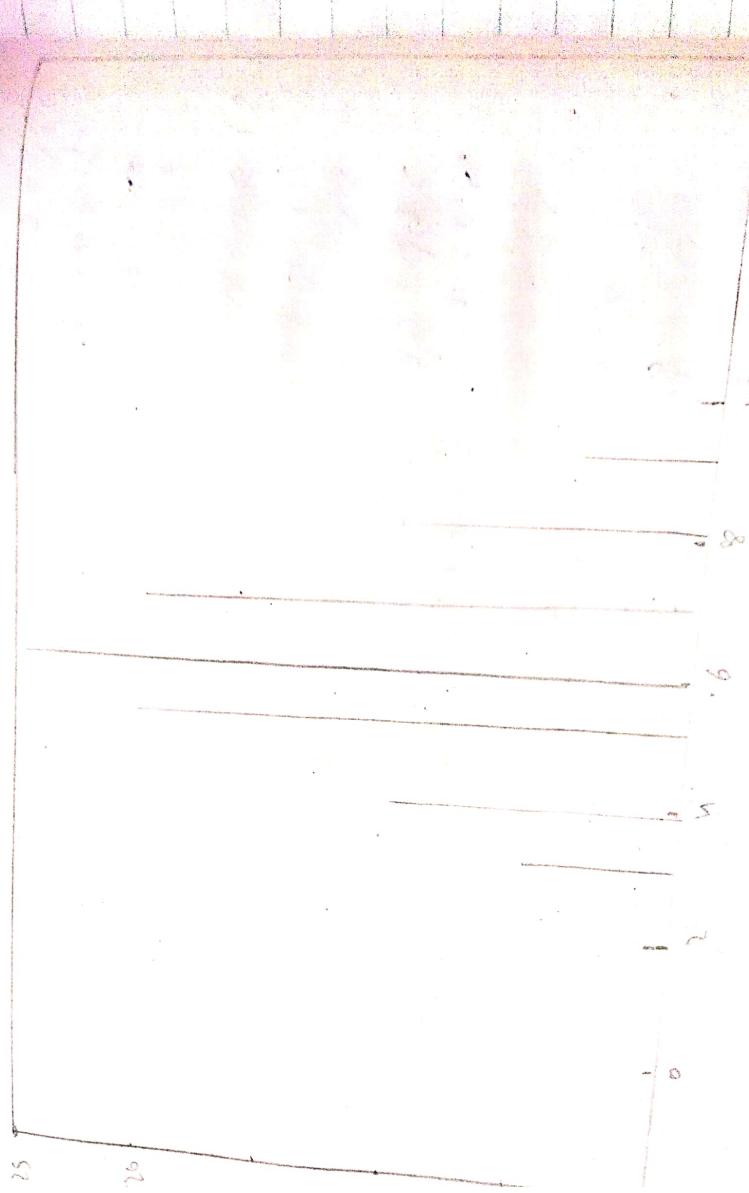
$$\rightarrow \text{var} = \text{sum}(b) - \text{mean}^2$$

>var

$$[1] 38.6875$$



```
#  
#> plot(x,y)  
#> CP = polyom(x,y)  
#> plot(x,CP, ncp=10)
```



Shaykhah 0.0 [ ]

(d'w'g) mawqif

1518L2 00.0 [ ]

(d's'l) mawqif

826 55h b.0f13

(d'u's) mawqif

52 a. d's

u:u:s (s)

{S98810 0 [ ]}

(d'u's) mawqif

10. d's

00:000 [ ]

50-21[ ]

(d'u's) mawqif

21[ ]e000e45

(d'u's) mawqif

100.0 [ ]

(d'u's) mawqif

621.0 [ ]

(d'u's) mawqif

21[ ]e000e85

(d'u's) mawqif

bhab5 e [ ]

(d'u's) mawqif

10. d's

5:u:b[ ]

43

- Q1)  $\text{P}(X \leq 5)$   
 To find  $P(X \leq 5)$   
 we need to sum up all the probabilities from  $x = 0$  to  $x = 5$ .  
 $P(X \leq 5) = P(X=0) + P(X=1) + P(X=2) + P(X=3) + P(X=4) + P(X=5)$   
 $= 0.15 + 0.25 + 0.25 + 0.15 + 0.15 + 0.15$   
 $= 1.15$

Answers

- Q2)  $\text{P}(X > 10)$   
 To find  $P(X > 10)$   
 we need to sum up all the probabilities from  $x = 11$  to  $x = 15$ .  
 $P(X > 10) = P(X=11) + P(X=12) + P(X=13) + P(X=14) + P(X=15)$   
 $= 0.15 + 0.25 + 0.25 + 0.15 + 0.15$   
 $= 0.85$

Note:-

- Q3) A salesman has a 30% probability of meeting a customer to be won over.  
 If he meets 10 such customers, what is the probability of meeting at least 6 of them?  
 To solve this problem, we can use binomial distribution formula:  
 $P(X=x) = \binom{n}{x} p^x (1-p)^{n-x}$   
 where  $n=10$ ,  $p=0.3$ ,  $x \geq 6$ .

Ans

- Q1)  $\text{P}(X \leq 5)$   
 To find  $P(X \leq 5)$   
 we need to sum up all the probabilities from  $x = 0$  to  $x = 5$ .  
 $P(X \leq 5) = P(X=0) + P(X=1) + P(X=2) + P(X=3) + P(X=4) + P(X=5)$   
 $= 0.15 + 0.25 + 0.25 + 0.15 + 0.15 + 0.15$   
 $= 1.15$

Answers

- Q2)  $\text{P}(X > 10)$   
 To find  $P(X > 10)$   
 we need to sum up all the probabilities from  $x = 11$  to  $x = 15$ .  
 $P(X > 10) = P(X=11) + P(X=12) + P(X=13) + P(X=14) + P(X=15)$   
 $= 0.15 + 0.25 + 0.25 + 0.15 + 0.15$   
 $= 0.85$

Note:-

- Q3) A salesman has a 30% probability of meeting a customer to be won over.  
 If he meets 10 such customers, what is the probability of meeting at least 6 of them?  
 To solve this problem, we can use binomial distribution formula:  
 $P(X=x) = \binom{n}{x} p^x (1-p)^{n-x}$   
 where  $n=10$ ,  $p=0.3$ ,  $x \geq 6$ .

Ans

- Q1)  $\text{P}(X \leq 10)$   
 To find  $P(X \leq 10)$   
 we need to sum up all the probabilities from  $x = 0$  to  $x = 10$ .  
 $P(X \leq 10) = P(X=0) + P(X=1) + P(X=2) + P(X=3) + P(X=4) + P(X=5) + P(X=6) + P(X=7) + P(X=8) + P(X=9) + P(X=10)$   
 $= 0.15 + 0.25 + 0.25 + 0.15 + 0.15 + 0.15 + 0.15 + 0.15 + 0.15 + 0.15 + 0.15$   
 $= 1.85$

- Q2)  $\text{P}(X > 10)$   
 To find  $P(X > 10)$   
 we need to sum up all the probabilities from  $x = 11$  to  $x = 15$ .  
 $P(X > 10) = P(X=11) + P(X=12) + P(X=13) + P(X=14) + P(X=15)$   
 $= 0.15 + 0.25 + 0.25 + 0.15 + 0.15$   
 $= 0.85$

- Q3)  $\text{P}(X \geq 10)$   
 To find  $P(X \geq 10)$   
 we need to sum up all the probabilities from  $x = 10$  to  $x = 15$ .  
 $P(X \geq 10) = P(X=10) + P(X=11) + P(X=12) + P(X=13) + P(X=14) + P(X=15)$   
 $= 0.15 + 0.25 + 0.25 + 0.15 + 0.15 + 0.15$   
 $= 1.15$

- Q4)  $\text{P}(X \leq 10)$   
 To find  $P(X \leq 10)$   
 we need to sum up all the probabilities from  $x = 0$  to  $x = 10$ .  
 $P(X \leq 10) = P(X=0) + P(X=1) + P(X=2) + P(X=3) + P(X=4) + P(X=5) + P(X=6) + P(X=7) + P(X=8) + P(X=9) + P(X=10)$   
 $= 0.15 + 0.25 + 0.25 + 0.15 + 0.15 + 0.15 + 0.15 + 0.15 + 0.15 + 0.15 + 0.15$   
 $= 1.85$

42  
 Blackcat no. 2  
 Second (Dislike) situation:  
 Total note 5 trials  
 P(Success) =  $P(\text{Success})$   
 $P(\text{Success}) = \frac{1}{2}$   
 No of successes out of 5  
 $P(\text{Success}) = \frac{1}{2} + \frac{1}{2} + \frac{1}{2} + \frac{1}{2} + \frac{1}{2} = 5 \times \frac{1}{2} = 2.5$   
 If no of heads = 6 then  
 $P(\text{Success}) = \frac{1}{2} + \frac{1}{2} + \frac{1}{2} + \frac{1}{2} + \frac{1}{2} + \frac{1}{2} = 6 \times \frac{1}{2} = 3$   
 If no of heads = 7  
 $P(\text{Success}) = \frac{1}{2} + \frac{1}{2} + \frac{1}{2} + \frac{1}{2} + \frac{1}{2} + \frac{1}{2} + \frac{1}{2} = 7 \times \frac{1}{2} = 3.5$   
 If no of heads = 8  
 $P(\text{Success}) = \frac{1}{2} + \frac{1}{2} = 8 \times \frac{1}{2} = 4$   
 If no of heads = 9  
 $P(\text{Success}) = \frac{1}{2} + \frac{1}{2} = 9 \times \frac{1}{2} = 4.5$   
 If no of heads = 10  
 $P(\text{Success}) = \frac{1}{2} + \frac{1}{2} = 10 \times \frac{1}{2} = 5$   
 If no of heads = 11  
 $P(\text{Success}) = \frac{1}{2} + \frac{1}{2} = 11 \times \frac{1}{2} = 5.5$   
 If no of heads = 12  
 $P(\text{Success}) = \frac{1}{2} + \frac{1}{2} = 12 \times \frac{1}{2} = 6$   
 If no of heads = 13  
 $P(\text{Success}) = \frac{1}{2} + \frac{1}{2} = 13 \times \frac{1}{2} = 6.5$   
 If no of heads = 14  
 $P(\text{Success}) = \frac{1}{2} + \frac{1}{2} = 14 \times \frac{1}{2} = 7$   
 If no of heads = 15  
 $P(\text{Success}) = \frac{1}{2} + \frac{1}{2} = 15 \times \frac{1}{2} = 7.5$   
 If no of heads = 16  
 $P(\text{Success}) = \frac{1}{2} + \frac{1}{2} = 16 \times \frac{1}{2} = 8$   
 If no of heads = 17  
 $P(\text{Success}) = \frac{1}{2} + \frac{1}{2} = 17 \times \frac{1}{2} = 8.5$   
 If no of heads = 18  
 $P(\text{Success}) = \frac{1}{2} + \frac{1}{2} = 18 \times \frac{1}{2} = 9$   
 If no of heads = 19  
 $P(\text{Success}) = \frac{1}{2} + \frac{1}{2} = 19 \times \frac{1}{2} = 9.5$   
 If no of heads = 20  
 $P(\text{Success}) = \frac{1}{2} + \frac{1}{2} = 20 \times \frac{1}{2} = 10$

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$\begin{bmatrix} h \\ 0 \\ 8 \end{bmatrix}$	$\begin{bmatrix} 8 \\ 6 \\ 1 \end{bmatrix}$	$\begin{bmatrix} 10 \\ 8 \\ 1 \end{bmatrix}$	$\begin{bmatrix} 2 \\ 3 \\ 1 \end{bmatrix}$
$\begin{bmatrix} 6 \\ 7 \\ 13 \end{bmatrix}$	$\begin{bmatrix} 17 \\ 20 \\ 18 \end{bmatrix}$	$\begin{bmatrix} 11 \\ 9 \\ 10 \end{bmatrix}$	$\begin{bmatrix} 2 \\ 3 \\ 1 \end{bmatrix}$
$\begin{bmatrix} h \\ 1 \\ b \end{bmatrix}$	$\begin{bmatrix} 12 \\ 11 \\ 15 \end{bmatrix}$	$\begin{bmatrix} 5 \\ 6 \\ 7 \end{bmatrix}$	$\begin{bmatrix} 2 \\ 3 \\ 1 \end{bmatrix}$
$\begin{bmatrix} 8 \\ 11 \\ 11 \end{bmatrix}$	$\begin{bmatrix} 2 \\ 3 \\ 1 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$	$\begin{bmatrix} 2 \\ 3 \\ 1 \end{bmatrix}$
$\begin{bmatrix} 2 \\ 3 \\ 1 \end{bmatrix}$	$\begin{bmatrix} 3 \\ 4 \\ 5 \end{bmatrix}$	$\begin{bmatrix} 3 \\ 4 \\ 5 \end{bmatrix}$	$\begin{bmatrix} 2 \\ 3 \\ 1 \end{bmatrix}$
$\begin{bmatrix} h \\ 2 \\ 0 \end{bmatrix}$	$\begin{bmatrix} 8 \\ 3 \\ 2 \end{bmatrix}$	$\begin{bmatrix} 4 \\ 5 \\ 6 \end{bmatrix}$	$\begin{bmatrix} 2 \\ 3 \\ 1 \end{bmatrix}$
$\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$	$\begin{bmatrix} 2 \\ 3 \\ 1 \end{bmatrix}$
$\begin{bmatrix} h \\ 1 \\ b \end{bmatrix}$	$\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$	$\begin{bmatrix} 2 \\ 3 \\ 1 \end{bmatrix}$
$\begin{bmatrix} 8 \\ 11 \\ 11 \end{bmatrix}$	$\begin{bmatrix} 2 \\ 3 \\ 1 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$	$\begin{bmatrix} 2 \\ 3 \\ 1 \end{bmatrix}$
$\begin{bmatrix} 2 \\ 3 \\ 1 \end{bmatrix}$	$\begin{bmatrix} 3 \\ 4 \\ 5 \end{bmatrix}$	$\begin{bmatrix} 3 \\ 4 \\ 5 \end{bmatrix}$	$\begin{bmatrix} 2 \\ 3 \\ 1 \end{bmatrix}$
$\begin{bmatrix} h \\ 2 \\ 0 \end{bmatrix}$	$\begin{bmatrix} 8 \\ 3 \\ 2 \end{bmatrix}$	$\begin{bmatrix} 4 \\ 5 \\ 6 \end{bmatrix}$	$\begin{bmatrix} 2 \\ 3 \\ 1 \end{bmatrix}$
$\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$	$\begin{bmatrix} 2 \\ 3 \\ 1 \end{bmatrix}$

→  $\max(\text{numbers}) = 10, \min = 2, \text{delta} = (1, 2, 3, 4, 5, 6, 7, 8)$

$$\begin{bmatrix} 2 \\ 3 \\ 1 \end{bmatrix}$$

mediana

h 6  
(x) 5  
1 2 3  
(x) 4  
mediana 3

0 4 5 6 7 8 9 10

in da favona 6

0 1 2 3 4 5 6 7 8 9 10  
find sum-product square root, maximum minimum value  
(x) 1 2 3 4 5 6 7 8 9 10  
84964837  
84964837  
84964837  
(x) 1 2 3 4 5 6 7 8 9 10

41

$\rightarrow$   $\text{sum} \times \text{product}$

$$\begin{aligned}& \text{sum} = \text{product} \\& \text{sum} = F(x) \\& \text{product} = F(x) \\& \text{product} = \text{sum} \times \text{product}\end{aligned}$$

$\rightarrow$  find the sum, product, square root, for all following values

$$\begin{aligned}& \text{sum} = 5 + 2 + 3 + 5 + 7 \\& \text{product} = 5 \times 2 \times 3 \times 5 \times 7\end{aligned}$$

$$= 368$$

$$\begin{aligned}& \rightarrow (5, 6, 7, 8) + (2, 3, 1, 6) \\& \rightarrow (5, 6, 7, 8) + (2, 3, 1, 6)\end{aligned}$$

$$\begin{aligned}& \rightarrow (5, 6, 7, 8) + 10 \\& \rightarrow (5, 6, 7, 8) + 10\end{aligned}$$

$$\begin{aligned}& \rightarrow 47 - 25 = 22 \\& \rightarrow (2, 3, 4, 7) + (-2, 3, 4, 7) \\& \rightarrow (2, 3, 5, 7) \times (2, 3, 5, 7)\end{aligned}$$

$$\begin{aligned}& \rightarrow 12 - 15 = -3 \\& \rightarrow (2, 3, 5, 7) \times (2, 3, 5, 7) \\& \rightarrow (2, 3, 5, 7)^2\end{aligned}$$

$\rightarrow$   $\text{square root} = \sqrt{a^2 + b^2}$  where  $a$  &  $b$  are the sides of a right-angled triangle

$$\begin{aligned}& \rightarrow \sqrt{5^2 + 12^2} = \sqrt{25 + 144} = \sqrt{169} = 13 \\& \rightarrow \sqrt{(2, 3, 5, 7)^2} = \sqrt{(2, 3, 5, 7) \times (2, 3, 5, 7)} \\& \rightarrow \sqrt{(2, 3, 5, 7)^2} = (2, 3, 5, 7)\end{aligned}$$

$$\begin{aligned}& \rightarrow \sqrt{25} = 5 \\& \rightarrow \sqrt{25} = 5\end{aligned}$$

## Practical no - 1

39

Basics of R software :

- i) It is a software for data analysis and statistical computing
- ii) It is a software by which effective date handling and outcome storage is possible
- iii) It is capable of graphical display
- iv) It's a free software

```

> x^2 + 1 - 51 * x * 5 + 6 / 5
> 2^2 + abs(x + 5) + 4 * x * 5 + 6 / 5
[1] 30.2
  
```

```

> x = 20, y = 2x, z = x + y, 5z
> x = 20
  
```

```

> y = 2 * x
> z = x + y
> sqrt(z)
[1] 7.7459
  
```

3)  $x = 16, y = 15, z = 5$

- a)  $x * y / 2$
- b)  $x * y^2$
- c)  $\sqrt{x * y^2}$
- d)  $\text{round}(\sqrt{x * y^2})$

$x = 10$

$y = 15$

$z = 3$

$x * y + z$

$x * y * z$

$[1] 250$

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II

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