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## Assignment – 5

**Polynomial interpolation 2:** Given the data table:

x	1	1.1	1.2	1.3	1.4
f(x)	0.5403	0.48360	0.30236	0.22150	0.18497

Calculate the value of

a)  $f(1.03)$

b)  $f(1.38)$

by applying Newton's forward difference approach and considering the full 4<sup>th</sup> order polynomial. Verify if the values are matching with the one obtained from Lagrange's method discussed in the previous class.

**ANSWER:**

```
function res = Newton(x,order)
%A = [1,8;2.1,20.6;5,13.7];
%X=A(:,1);
%Y=A(:,2);
X=1:0.1:1.4;
Y=[0.54030 0.48360 0.30236 0.22150 0.18497];
n=length(X);
diff=zeros(n,n);
diff(:,1)=Y;
for i=2:n
    for j=1:n-(i-1)
        diff(j,i)=(diff(j+1,i-1)-diff(j,i-1))/(X(j+i-1)-X(j));
    end
end
disp(diff);
res=diff(1,1);
for i=1:order
    f=1;
    for j=1:i
        f=f*(x-X(j));
    end
    res=res+f*diff(1,i+1);
    fprintf('%d %d %d\n',res,f,diff(i+1,1));
end
end
```

### Answer

Using Newton Forward Interpolation

$$f(1.03) = 0.5610$$

$$f(1.38) = 0.2009$$

Using Lagrange's Interpolation

$$f(1.03) = 0.5610$$

$$f(1.38) = 0.3800$$

```
function res = Lagrange(x)

X=1:0.1:1.4;
Y=[0.54030 0.48360 0.30236 0.22150 0.18497];

n=length(X);

res=0;
for i=1:n
    f=1;
    for j=1:n
        if j==i
            continue;
        end
        f=f*(x-X(j))/(X(i)-X(j));
    end
    res=res+Y(i)*f;
end
```

**Polynomial interpolation 3:** Given the data table:

x	1	2	3	4	5	6	7	8	9	10
f(x)	1	0.4444	0.2632	0.1818	0.1373	0.1096	0.0929	0.0775	0.0675	0.0597

- Use Newton-Gregory forward difference formula to interpolate a polynomial through these points.
- Check if a 9<sup>th</sup> order polynomial is any better than a 5<sup>th</sup> order polynomial by

plotting the polynomial alongside data points.

c) Based on this plot write a discussion that if you need to estimate i)  $f(2.22)$  ii)  $f(5.7)$  and iii)  $f(8.11)$ , will you be using the 5<sup>th</sup> order polynomial?

**ANSWER:**

```
function res = Newton2(x,order)
%A = [1,8;2.1,20.6;5,13.7];
A=[1 1;2 .4444;3 .2632;4 .1818;5 .1373;6 .1096;7
.0929;8 .0775;9 .0675;10 .0597];
X=A(:,1);
Y=A(:,2);

n=length(X);
diff=zeros(n,n);
diff(:,1)=Y;
for i=2:n
    for j=1:n-(i-1)
        diff(j,i)=(diff(j+1,i-1)-diff(j,i-1))/(X(j+i-1)-X(j));
    end
end
disp(diff);
res=diff(1,1);

for i=1:order
    f=1;
    for j=1:i
        f=f*(x-X(j));
    end
    res=res+f*diff(1,i+1);
    %fprintf('%d %d %d\n',res,f,diff(i+1,1));
end
end
```

```

X=[1 1;2 .4444;3 .2632;4 .1818;5 .1373;6 .1096;7
.0929;8 .0775;9 .0675;10 .0597];
x=1:.05:10;
y=zeros(1,length(x));

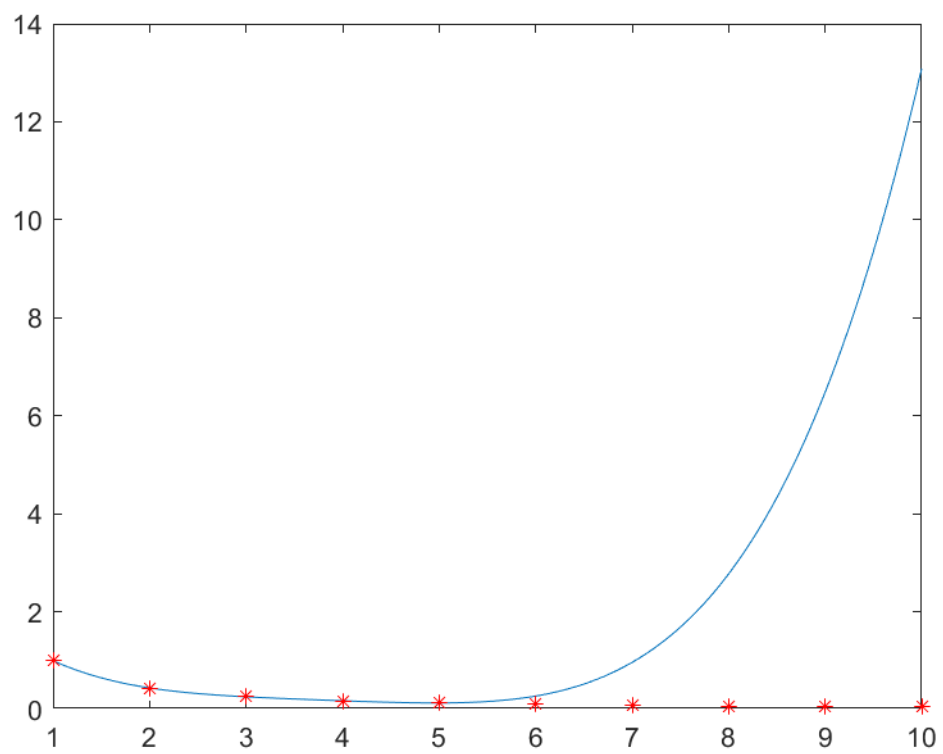
%part 1 with order 9
n=10;
for i=1:length(x)
y(i)=newtonfor(X,x(i),n);
end
plot(x,y,'-');
hold on
plot(X(:,1),X(:,2),'r*')

%%part 2 with order 5
n=5;
for i=1:length(x)
y(i)=newtonfor(X,x(i),n);
end
figure;
plot(x,y,'-');
hold on
plot(X(:,1),X(:,2),'r*')

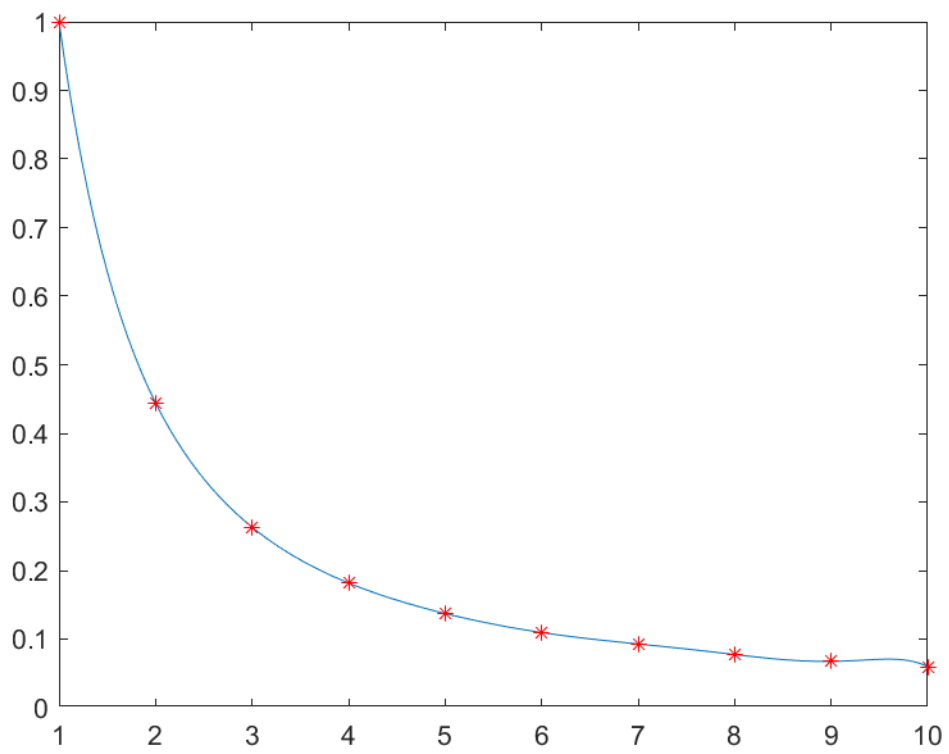
f1=newtonfor(X,2.22,10);
f2=newtonfor(X,5.7,10);
f3=newtonfor(X,8.11,10);

```

**Newton 5:**



**Newton 9:**



Results: It is evident that Newton's 9 order polynomial fits better than the 5 th order one. We can use the 5 th order one to estimate  $f(2.22)$  but for higher values it is essential that we use the 9 th order polynomial.

Since this is a forward difference method if we do not take all the orders, we will not get a good estimate for values towards the end of the data and thus we obtain such plots

Newton's 5 order

$$f(2.2)=0.3900$$

$$f(5.7)=0.1993$$

$$f(8.11)=3.0703$$

Newton's 9 order

$$f(2.2)=0.3930$$

$$f(5.7)=0.1166$$

$$f(8.11)=0.0752$$