

PART-B

1. Write a program to sort a given set of **n integer elements** using **Merge Sort method** and compute its time complexity. Run the program for varied values of $n > 5000$, and record the time taken to sort.
2. Write a program to sort a given set of **n integer elements** using **Quick Sort method** and compute its time complexity. Run the program for varied values of $n > 5000$ and record the time taken to sort.
3. Write a **C program** that accepts the vertices and edges for a graph and stores it as an **adjacency matrix**.
4. Write a program to implement a function to **print In-Degree, Out-Degree** and to display that **adjacency matrix**.
5. Write a program to implement **backtracking algorithm** for solving problems like **N-Queens**.
6. Write a program to implement the **backtracking algorithm** for the **Sum of Subsets problem**.
7. Write a program to implement a **Greedy algorithm** for **Job Sequencing with Deadlines**.
8. Write a program to implement **Dynamic Programming algorithm** for the **Optimal Binary Search Tree Problem**.
9. Write a program that implements **Prim's algorithm** to generate a **Minimum Cost Spanning Tree**.
10. Write a program that implements **Kruskal's algorithm** to generate a **Minimum Cost Spanning Tree**.

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1. Write a C program to sort a given set of n integer elements using Merge Sort method and compute its time complexity. Run the program for varied values of n > 5000, and record the time taken to sort.

```
#include <stdio.h>
#include <stdlib.h>
#include <time.h>
void merge(int a[], int l, int m, int r)
{
    int n1=m-l+1,n2=r-m,L[n1],R[n2],i,j,k;
    for(i=0;i<n1;i++) L[i]=a[l+i];
    for(j=0;j<n2;j++) R[j]=a[m+1+j];
    for(i=0,j=0,k=l;i<n1 && j<n2;) a[k++]=(L[i]<=R[j])?L[i++]:R[j++];
    while(i<n1) a[k++]=L[i++];
    while(j<n2) a[k++]=R[j++];
}
void mergeSort(int a[], int l, int r)
{
    if(l<r){ int m=(l+r)/2;
    mergeSort(a,l,m);
    mergeSort(a,m+1,r);
    merge(a,l,m,r);
    }
}
int main()
{
    int n;
    printf("Enter n (>5000): ");
    scanf("%d",&n);
    int *a=malloc(n*sizeof(int));
    for(int i=0;i<n;i++)
        a[i]=rand()%10000;
    clock_t t=clock();
    mergeSort(a,0,n-1);
    t=clock()-t;
    printf("Time taken: %f sec\n",(double)t/CLOCKS_PER_SEC);
    free(a);
    return 0;
}
```

Output:

```
Enter n (>5000): 6000
Time taken: 0.000882 sec
```

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2. Write a program to sort a given set of n integer elements using Quick Sort method and compute its time complexity. Run the program for varied values of $n > 5000$ and record the time taken to sort.

```
#include <stdio.h>
#include <stdlib.h>
#include <time.h>
void quick(int a[], int l, int h)
{
    if (l >= h) return;
    int i = l, j = h, p = a[(l + h) / 2];
    while (i <= j)
    {
        while (a[i] < p) i++;
        while (a[j] > p) j--;
        if (i <= j)
        {
            int t = a[i];
            a[i] = a[j];
            a[j] = t;
            i++;
            j--;
        }
    }
    quick(a, l, j);
    quick(a, i, h);
}
int main()
{
    int n;
    printf("Enter n (>5000): ");
    scanf("%d", &n);
    int *a = malloc(n * sizeof(int));
    for (int i = 0; i < n; i++)
        a[i] = rand() % 100000;
    clock_t s = clock();
    quick(a, 0, n - 1);
    clock_t e = clock();
    printf("Time: %.6f sec\n", (double)(e - s) / CLOCKS_PER_SEC);
    free(a);
    return 0;
}
```

OUTPUT:

```
Enter n (>5000): 5800
Time: 0.000560 sec
```

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3. Write a C program that accepts the vertices and edges for a graph and stores it as an adjacency matrix.

```
#include <stdio.h>
int main()
{
    int v, e, i, j, src, dest;
    printf("Enter number of vertices: ");
    scanf("%d", &v);
    int adj[v][v];
    // Initialize matrix to 0
    for(i = 0; i < v; i++)
        for(j = 0; j < v; j++)
            adj[i][j] = 0;
    printf("Enter number of edges: ");
    scanf("%d", &e);
    // Read edges
    for(i = 0; i < e; i++)
    {
        printf("Enter edge (src dest): ");
        scanf("%d%d", &src, &dest);
        adj[src][dest] = 1;      // For directed graph
        adj[dest][src] = 1;      // For undirected graph, keep this line
    }
    // Display adjacency matrix
    printf("Adjacency Matrix:\n");
    for(i = 0; i < v; i++)
    {
        for(j = 0; j < v; j++)
            printf("%d ", adj[i][j]);
        printf("\n");
    }
    return 0;
}
```

Output:

```
Enter number of vertices: 3
Enter number of edges: 2
Enter edge (src dest): 0 1,1 2
Enter edge (src dest): Adjacency Matrix:
0 1 0
1 0 0
0 0 0
```

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4. Write a program to implement a function to print In-Degree, Out-Degree and to display that adjacency matrix.

```
#include <stdio.h>
#define MAX 10
void displayAdjMatrix(int adj[MAX][MAX], int v)
{
    printf("\nAdjacency Matrix:\n");
    for(int i = 0; i < v; i++) {
        for(int j = 0; j < v; j++) {
            printf("%d ", adj[i][j]);
        }
        printf("\n");
    }
}
void computeDegrees(int adj[MAX][MAX], int v)
{
    int indegree, outdegree;
    printf("\nVertex\tIn-Degree\tOut-Degree\n");
    for(int i = 0; i < v; i++)
    {
        indegree = outdegree = 0;
        // Calculate Out-Degree (row-wise)
        for(int j = 0; j < v; j++)
            outdegree += adj[i][j];
        // Calculate In-Degree (column-wise)
        for(int j = 0; j < v; j++)
            indegree += adj[j][i];
        printf("%d\t%d\t%d\n", i, indegree, outdegree);
    }
}
int main()
{
    int v, e, src, dest;
    int adj[MAX][MAX] = {0};
    printf("Enter number of vertices: ");
    scanf("%d", &v);
    printf("Enter number of edges: ");
    scanf("%d", &e);
    printf("Enter edges (source destination):\n");
    for(int i = 0; i < e; i++) {
        scanf("%d %d", &src, &dest);
        adj[src][dest] = 1; // directed edge
    }
    displayAdjMatrix(adj, v);
    computeDegrees(adj, v);
    return 0;
}
```

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}

OUTPUT:

Enter number of vertices: 4

Enter number of edges: 4

Enter edges (source destination):

0 1

0 2

1 2

2 3

Adjacency Matrix:

0 1 1 0

0 0 1 0

0 0 0 1

0 0 0 0

Vertex In-Degree Out-Degree

0 0 2

1 1 1

2 2 1

3 1 0

5. Write a program to implement backtracking algorithm for solving problems like N-Queens.

```
#include <stdio.h>
#include <stdlib.h>
#define MAX 20
int board[MAX], n;
int isSafe(int row, int col)
{
    for (int i = 0; i < row; i++)
        if (board[i] == col || abs(board[i] - col) == abs(i - row))
            return 0;
    return 1;
}
void printSolution()
{
    for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++)
            printf("%c ", board[i] == j ? 'Q' : '.');
        printf("\n");
    }
    printf("\n");
}
void solveNQueens(int row)
{
    if (row == n) { printSolution(); return; }
    for (int col = 0; col < n; col++) {
```

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```
if (isSafe(row, col)) {
    board[row] = col;
    solveNQueens(row + 1);
}
}
int main()
{
    printf("Enter number of Queens: ");
    scanf("%d", &n);
    solveNQueens(0);
    return 0;
}
```

Output:

Enter number of Queens: 4

. Q ..
... Q
Q ...
. Q ..

.. Q .
Q ...
... Q
. Q ..

6. Write a program to implement the backtracking algorithm for the Sum of Subsets problem.

```
#include <stdio.h>
#define MAX 20
int n, target, set[MAX], subset[MAX];
void sumOfSubsets(int idx, int currSum, int start)
{
    if (currSum == target)
    { // Found a valid subset
        printf("{ ");
        for (int i = 0; i < idx; i++)
            printf("%d ", subset[i]);
        printf("}\n");
        return; // Continue to find other subsets
    }
    for (int i = start; i < n; i++)
    {
        if (currSum + set[i] <= target)
        { // Choose the element
            subset[idx] = set[i];
            sumOfSubsets(idx + 1, currSum + set[i], i + 1);
        }
    }
}
```

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```
}
```

```
int main()
```

```
{
```

```
    printf("Enter number of elements: ");
```

```
    scanf("%d", &n);
```

```
    printf("Enter elements of the set: ");
```

```
    for (int i = 0; i < n; i++)
```

```
        scanf("%d", &set[i]);
```

```
    printf("Enter target sum: ");
```

```
    scanf("%d", &target);
```

```
    printf("Subsets with sum %d:\n", target);
```

```
    sumOfSubsets(0, 0, 0);
```

```
    return 0;
```

```
}
```

Output:

Enter number of elements: 4

Enter elements of the set: 3 4 5 2

Enter target sum: 7

Subsets with sum 7:

{ 3 4 }

{ 5 2 }

7. Write a program to implement a Greedy algorithm for Job Sequencing with Deadlines.

```
#include <stdio.h>
```

```
#define MAX 20
```

```
typedef struct
```

```
{
```

```
    char id;
```

```
    int deadline;
```

```
    int profit;
```

```
} Job;
```

```
void jobSequencing(Job jobs[], int n)
```

```
{
```

```
    int i, j, maxDeadline = 0;
```

```
    int slot[MAX];
```

```
    char result[MAX];
```

```
    // Find maximum deadline
```

```
    for (i = 0; i < n; i++)
```

```
        if (jobs[i].deadline > maxDeadline)
```

```
            maxDeadline = jobs[i].deadline;
```

```
    // Sort jobs by decreasing profit (Greedy choice)
```

```
    for (i = 0; i < n - 1; i++)
```

```
        for (j = i + 1; j < n; j++)
```

```
            if (jobs[i].profit < jobs[j].profit)
```

```
            {
```

```
                Job temp = jobs[i];
```

```
                jobs[i] = jobs[j];
```

```
                jobs[j] = temp;
```

```
            }
```

```
    // Initialize all slots as free
```

```
    for (i = 0; i < maxDeadline; i++)
```

```
        slot[i] = -1;
```

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```
// Assign jobs to slots
for (i = 0; i < n; i++)
{
    for (j = jobs[i].deadline - 1; j >= 0; j--)
    {
        if (slot[j] == -1)
        {
            // If slot is free
            slot[j] = i;      // Assign job index
            break;
        }
    }
}
// Print the scheduled jobs
printf("\nScheduled Jobs: ");
for (i = 0; i < maxDeadline; i++)
    if (slot[i] != -1)
        printf("%c ", jobs[slot[i]].id);
}
int main()
{
    int n, i;
    Job jobs[MAX];
    printf("Enter number of jobs: ");
    scanf("%d", &n);
    printf("Enter Job ID, Deadline, and Profit for each job:\n");
    for (i = 0; i < n; i++)
        scanf(" %c %d %d", &jobs[i].id, &jobs[i].deadline, &jobs[i].profit);
    jobSequencing(jobs, n);
    return 0;
}
```

Output:

```
Enter number of jobs: 5
Enter Job ID, Deadline, and Profit for each job:
A 2 100
B 1 19
C 2 27
D 1 25
E 3 15
Scheduled Jobs: C A E
```

8. Write a program to implement Dynamic Programming algorithm for the Optimal Binary Search Tree Problem.

```
#include <stdio.h>
#define MAX 20
#define INF 999999
int main()
{
    int n, i, j, k, l, r;
    int freq[MAX], cost[MAX][MAX], weight[MAX][MAX], root[MAX][MAX];
    printf("Enter number of keys: ");
```

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```
scanf("%d", &n);
printf("Enter frequency of %d keys:\n", n);
for (i = 1; i <= n; i++)
    scanf("%d", &freq[i]);
// Initialize cost and weight for single keys
for (i = 1; i <= n; i++)
{
    cost[i][i] = freq[i];
    weight[i][i] = freq[i];
    root[i][i] = i;
}
// For chains of length 2 to n
for (l = 2; l <= n; l++)
{
    for (i = 1; i <= n - l + 1; i++)
    {
        j = i + l - 1;
        cost[i][j] = INF;
        weight[i][j] = weight[i][j - 1] + freq[j];
        for (r = i; r <= j; r++)
        {
            int c = ((r > i) ? cost[i][r - 1] : 0) +
                ((r < j) ? cost[r + 1][j] : 0) +
                weight[i][j];
            if (c < cost[i][j])
            {
                cost[i][j] = c;
                root[i][j] = r;
            }
        }
    }
}
printf("\nOptimal Cost of OBST: %d\n", cost[1][n]);
printf("Root of OBST: Key %d\n", root[1][n]);
return 0;
}
```

Output:

Enter number of keys: 4
Enter frequency of 4 keys:
4 2 6 3
Optimal Cost of OBST: 26
Root of OBST: Key 3

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9. Write a program that implements Prim's algorithm to generate a Minimum Cost Spanning Tree.

```
#include <stdio.h>
#include <limits.h>
#define MAX 20
int main()
{
    int n, i, j, k;
    int cost[MAX][MAX], selected[MAX] = {0}, min, u, v, edge_count = 0, total_cost = 0;
    printf("Enter number of vertices: ");
    scanf("%d", &n);
    printf("Enter the adjacency matrix (0 if no edge):\n");
    for (i = 0; i < n; i++)
        for (j = 0; j < n; j++)
        {
            scanf("%d", &cost[i][j]);
            if (cost[i][j] == 0)
                cost[i][j] = INT_MAX; // Treat 0 as no edge
        }
    selected[0] = 1; // Start from vertex 0
    printf("\nEdges in Minimum Spanning Tree:\n");
    while (edge_count < n - 1)
    {
        min = INT_MAX;
        u = v = -1;
        for (i = 0; i < n; i++)
        {
            if (selected[i])
            {
                for (j = 0; j < n; j++)
                {
                    if (!selected[j] && cost[i][j] < min)
                    {
                        min = cost[i][j];
                        u = i;
                        v = j;
                    }
                }
            }
        }
        if (u != -1 && v != -1)
        {
            printf("%d - %d : %d\n", u, v, cost[u][v]);
            total_cost += cost[u][v];
            selected[v] = 1;
            edge_count++;
        }
    }
    printf("\nTotal cost of MST: %d\n", total_cost);
    return 0;
}
```

Output:

Enter number of vertices: 4

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Enter the adjacency matrix (0 if no edge):

```
0 2 0 6  
2 0 3 8  
0 3 0 0  
6 8 0 0
```

Edges in Minimum Spanning Tree:

```
0 - 1 : 2  
1 - 2 : 3  
0 - 3 : 6
```

Total cost of MST: 11

10. Write a program that implements Kruskal's algorithm to generate a Minimum Cost Spanning Tree.

```
#include <stdio.h>  
#include <stdlib.h>  
#define MAX 20  
typedef struct  
{  
    int u, v, weight;  
} Edge;  
int parent[MAX];  
int find(int i) {  
    while (parent[i] != i)  
        i = parent[i];  
    return i;  
}  
void union_sets(int i, int j)  
{  
    int a = find(i);  
    int b = find(j);  
    parent[a] = b;  
}  
int compare(const void *a, const void *b)  
{  
    return ((Edge *)a)->weight - ((Edge *)b)->weight;  
}  
int main()  
{  
    int n, e, i, count = 0, total_cost = 0;  
    Edge edges[MAX];  
    printf("Enter number of vertices: ");  
    scanf("%d", &n);  
    printf("Enter number of edges: ");  
    scanf("%d", &e);  
    printf("Enter edges (u v weight):\n");  
    for (i = 0; i < e; i++) {  
        scanf("%d %d %d", &edges[i].u, &edges[i].v, &edges[i].weight);  
    }  
    // Initialize parent for union-find  
    for (i = 0; i < n; i++)  
        parent[i] = i;
```

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```
// Sort edges by weight
qsort(edges, e, sizeof(Edge), compare);
printf("\nEdges in Minimum Spanning Tree:\n");
for (i = 0; i < e && count < n - 1; i++)
{
    int u_set = find(edges[i].u);
    int v_set = find(edges[i].v);
    if (u_set != v_set) {
        printf("%d - %d : %d\n", edges[i].u, edges[i].v, edges[i].weight);
        total_cost += edges[i].weight;
        union_sets(u_set, v_set);
        count++;
    }
}
printf("\nTotal cost of MST: %d\n", total_cost);
return 0;
```

Output:

Enter number of vertices: 4

Enter number of edges: 5

Enter edges (u v weight):

0 1 10

0 2 6

0 3 5

1 3 15

2 3 4

Edges in Minimum Spanning Tree:

2 - 3 : 4

0 - 3 : 5

0 - 1 : 10

Total cost of MST: 19