

**Degree of BEng/MEng in Chemical Engineering**

**CP203/CP211 Thermodynamics and Chemical Principles**

**Date: Friday 7th May 2021**

**Time: 14:00-17:00**

**Duration: 3 hours**

**Answer All Questions**

**The paper is divided into TWO sections**

**Answer each section in a separate booklet**

**There are 100 marks available in each section of the paper**

**Calculators must not be used to store text and/or formulae nor be capable of communication. Invigilators may require calculators to be re-set.**

**Remember to clearly state any assumptions you make when solving each question.**

**Equation sheets and periodic table are provided at the end of the paper.**

**PLEASE TURN OVER**

## Section A: Answer All Questions

- QA1.** Methane gas is continually fed into a steady-state isothermal compressor at an inlet absolute pressure of 500 bar and temperature of 200 K. The gas exits the compressor at an absolute pressure of 750 bar. The compressibility factor of methane in this range of conditions obeys the following equation:

$$Z = a + bP$$

with the constants taking the values  $a = 0.28$  and  $b = 0.00208 \text{ bar}^{-1}$ .

Calculate the final volume of the gas in  $\text{cm}^3$  and the molar work of compression in  $\text{kJ/mol}$ .

[16 marks]

- QA2.** Calculate the value of the Joule-Thomson coefficient for a gas that is described by the following equation of state:

$$P = \frac{RT}{v - b}$$

where  $b$  is a constant with the value  $0.03 \text{ m}^3 \text{ mol}^{-1}$ . The constant pressure heat capacity of the gas is  $c_P = 21 \text{ J mol}^{-1} \text{ K}^{-1}$ .

[16 marks]

- QA3.** A thermodynamic cycle is composed of four steps: **i)** reversible isothermal expansion at  $130^\circ\text{C}$ ; **ii)** irreversible adiabatic expansion to a temperature of  $20^\circ\text{C}$ ; **iii)** reversible isothermal compression at  $20^\circ\text{C}$ ; **iv)** reversible adiabatic compression back to the initial state at  $130^\circ\text{C}$ . The entropy change in the first step of the process is  $\Delta S_1 = 18 \text{ J mol}^{-1} \text{ K}^{-1}$  and the entropy change in step **ii)** is  $\Delta S_2 = 3 \text{ J mol}^{-1} \text{ K}^{-1}$ .

Choose the correct sketch of the cyclic process on a temperature-entropy (TS) diagram (among 4 options).

Calculate the efficiency of the real heat engine, as well as the efficiency of a Carnot engine operating between the same two temperatures.

[20 marks]

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- QA4.** A vapour mixture composed of 75% of heptane and 25% of octane (molar basis), at a temperature of 100 °C, is in equilibrium with a liquid mixture of the same components. The vapour phase can be assumed to be an ideal gas and the liquid phase can be assumed to form an ideal mixture. Making use of the data presented in **Table QA4**, calculate the pressure in bar and the mole fraction of heptane in the liquid phase.

[18 marks]

**Table QA4:** Physical data for pure heptane and octane.

Component	heptane	octane
Enthalpy of Vaporisation at 100 °C (kJ mol <sup>-1</sup> )	36	41
Boiling Temperature at 1 bar (°C)	98.5	125.7

- QA5.** An ideal gas, initially at 25 °C, is compressed adiabatically so that its final pressure is three times its initial pressure. The constant volume heat capacity of the gas is  $c_V = 18.5 \text{ J mol}^{-1} \text{ K}^{-1}$ .

Calculate the ratio of heat capacities,  $\gamma$ , and the final temperature of the gas in °C.

[12 marks]

- QA6.** An adiabatic turbine operates with an inlet stream of air at 6 bar and 400 K. The air leaves the turbine at 2 bar and 330 K. Over this range of conditions, you can assume that air behaves as an ideal gas, with a constant pressure heat capacity of  $c_P = 30 \text{ J mol}^{-1} \text{ K}^{-1}$ .

Calculate the entropy change during operation of the turbine in  $\text{J mol}^{-1} \text{ K}^{-1}$ .

Calculate the efficiency of the turbine relative to its isentropic mode of operation at the same inlet conditions and outlet pressure.

[18 marks]

**[PLEASE TURN OVER]**

## Section B: Answer All Questions

**QB1.** Given that the insertion of a tube (0.34 mm bore) into bulk water results in the rise of a column of water above the incident bulk liquid surface to a height of 6.1 mm, at 325 K, determine the surface tension of water at this temperature. [10 marks]

**QB2.** Data for the surface tension of an uncharged surfactant, measured with increasing concentration at 25 °C, is analysed using the Gibbs equation, giving a gradient of  $-9.475 \times 10^{-3} \text{ N m}^{-1}$ , from a plot of  $\gamma$  against  $\log(\text{concentration})$ .

- i) Calculate  $\Gamma$  for the system studied.
  - ii) Calculate the area occupied by one molecule of the surfactant.
  - iii) Discuss what change would be expected in the area occupied per molecule if the surfactant were charged.
- [15 marks]

**QB3.** An adsorption surface experiences  $9.83 \times 10^{26}$  collisions per square metre per second from a pure diatomic gas at 0.35 atm and 323 K. Determine the gas present. [10 marks]

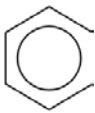
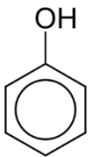
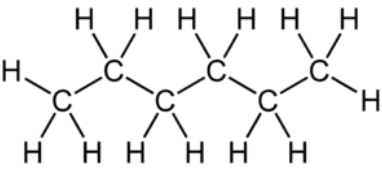
**QB4.** Using the Antoine equation:

$$\log P = A - \frac{B}{T + C}$$

where T is temperature in °C and P is pressure in Torr, and the data provided in **Table QB4**:

- i) Calculate the boiling points of phenol, hexane and benzene.
- ii) Explain the trend in boiling points for these three molecules.

**Table QB4:** Antoine constants and chemical structures of chemicals in QB4

Chemical	benzene	phenol	hexane
Chemical structure			
Temperature range/°C	8 to 103	107 to 182	-29 to 92
A	6.90565	7.1330	6.87601
B	1211.033	1516.79	1171.17
C	220.790	174.95	224.41

[14 marks]

**PLEASE TURN OVER**

- QB5.** a) What assumptions are made in the derivation of the Langmuir equation?  
Use a diagram to illustrate your answer.
- b) A material has a monolayer capacity of  $12.30 \text{ mmol g}^{-1}$  for nitrogen adsorption at 77 K. Given that the area occupied by 1 molecule of nitrogen is  $1.62 \times 10^{-15} \text{ cm}^2$ , what is the surface area of the material?  
Comment on the answer obtained in the context of your understanding of this parameter.

[16 marks]

**QB6.** Define the term 'equilibrium vapour pressure' and discuss:

- i) the molecular basis of this physical quantity
- ii) the effect of temperature
- iii) the effect of surface area.

[14 marks]

**QB7.** Using an appropriate sketch, explain the expected trend in the surface tension of benzene with increasing temperature.

[8 marks]

**QB8.** Given the data in **Table QB8** for adsorption of ethanol on a mesoporous carbon at 28 °C, at which temperature the saturated vapour pressure for ethanol is 70.9 mbar, and that the molar heat of condensation for ethanol is - 38.56 kJ mol<sup>-1</sup>, determine:

- i) the monolayer coverage
- ii) the value of the C constant for the process
- iii) the heat of adsorption

Note that you may use graph paper or software to plot your graphs.

**Table QB8:** Molar uptakes for adsorption of ethanol on mesoporous carbon

$p/p^\circ$	$p/n(p^\circ - p) / \text{g mmol}^{-1}$
0.05	0.0077
0.15	0.0179
0.25	0.0284
0.35	0.0392

[13 marks]

**Information:**

$$g = 9.81 \text{ m s}^{-2}$$

$$R = 8.314 \text{ J K}^{-1} \text{ mol}^{-1}$$

$$\text{Avogadro's number} = 6.023 \times 10^{23} \text{ molecule mol}^{-1}$$

$$\text{Boltzmann Constant} = 1.38 \times 10^{-23} \text{ J K}^{-1} \text{ molecule}^{-1}$$

$$1 \text{ atm} = 101325 \text{ Pa}$$

**[PLEASE TURN OVER]**

# Thermodynamics Equation Sheet

All symbols have the same meaning as given in class materials.

First Law (general)

$$\Delta U = Q + W - \Delta\left(\frac{1}{2}mv^2\right) - \Delta(mgz)$$

Gibbs phase rule

$$F = 2 - \pi + N$$

Thermal expansion coefficient

$$\alpha = \frac{1}{V} \left( \frac{\partial V}{\partial T} \right)_{P,m}$$

Isothermal compressibility

$$\beta = -\frac{1}{V} \left( \frac{\partial V}{\partial P} \right)_{T,m}$$

Heat capacities

$$C_V = \left( \frac{\partial U}{\partial T} \right)_V = T \left( \frac{\partial S}{\partial T} \right)_V$$

$$C_P = \left( \frac{\partial H}{\partial T} \right)_P = T \left( \frac{\partial S}{\partial T} \right)_P$$

$$C_P - C_V = T \left( \frac{\partial V}{\partial T} \right)_P \left( \frac{\partial P}{\partial T} \right)_V$$

Van der Waals equation of state

$$P = \frac{RT}{v-b} - \frac{a}{v^2}$$

Virial equation of state

$$Z = 1 + \frac{B}{v} + \frac{C}{v^2} + \frac{D}{v^3} + \dots$$

Thermodynamic potentials

$$H = U + PV$$

$$A = U - TS$$

$$G = H - TS$$

Fundamental thermodynamic relations

$$dU = TdS - PdV$$

$$dH = TdS + VdP$$

$$dA = -SdT - PdV$$

$$dG = -SdT + VdP$$

Maxwell equations

$$\left( \frac{\partial T}{\partial V} \right)_S = - \left( \frac{\partial P}{\partial S} \right)_V$$

$$\left( \frac{\partial T}{\partial P} \right)_S = \left( \frac{\partial V}{\partial S} \right)_P$$

$$\left( \frac{\partial S}{\partial P} \right)_T = - \left( \frac{\partial V}{\partial T} \right)_P$$

$$\left( \frac{\partial S}{\partial V} \right)_T = \left( \frac{\partial P}{\partial T} \right)_V$$

Internal energy and enthalpy

$$\left( \frac{\partial U}{\partial V} \right)_T = T \left( \frac{\partial P}{\partial T} \right)_V - P$$

$$\left( \frac{\partial U}{\partial P} \right)_T = -T \left( \frac{\partial V}{\partial T} \right)_P - P \left( \frac{\partial V}{\partial P} \right)_T$$

$$\left( \frac{\partial H}{\partial V} \right)_T = T \left( \frac{\partial P}{\partial T} \right)_V + V \left( \frac{\partial P}{\partial V} \right)_T$$

$$\left( \frac{\partial H}{\partial P} \right)_T = -T \left( \frac{\partial V}{\partial T} \right)_P + V$$

Carnot relationship

$$\left| \frac{Q_1}{Q_2} \right| = \frac{T_1}{T_2}$$

Entropy

$$\Delta S = \int_1^2 \frac{dQ_{\text{rev}}}{T}$$

$$dS = \frac{C_P}{T} dT - \left( \frac{\partial V}{\partial T} \right)_P dP$$

$$\Delta S_{\text{IG}} = C_P \ln \frac{T_2}{T_1} - nR \ln \frac{P_2}{P_1}$$

## Thermodynamics Equation Sheet

Joule-Thomson coefficient

$$\left(\frac{\partial T}{\partial P}\right)_H = \frac{V}{C_P}(\alpha T - 1)$$

Phase equilibrium

$$\frac{dP^{sat}}{dT_b} = \frac{\Delta h}{T_b \Delta v}$$

$$\frac{dP^{sat}}{dT_b} = \frac{\Delta h P^{sat}}{RT_b^2}$$

$$\ln P^{sat} = A - \frac{B}{T_b + C}$$

Multi-component systems ( $m$  or  $M$  stand for any extensive property)

$$dU = TdS - PdV + \sum_{i=1} \mu_i dn_i$$

$$\mu_i = \left(\frac{\partial G}{\partial n_i}\right)_{T,P,n_j}$$

$$m = \sum_i x_i \bar{m}_i$$

$$\Delta M_{\text{Mix}} = \sum_i n_i \bar{m}_i - \sum_i n_i m_i^0$$

$$\sum_i x_i d\bar{m}_i = 0$$

Ideal mixture

$$\mu_i = \mu_i^0 + RT \ln x_i$$

$$U = \sum_i n_i u_i^0$$

$$H = \sum_i n_i h_i^0$$

$$V = \sum_i n_i v_i^0$$

$$S = \sum_i n_i s_i^0 - nR \sum_i x_i \ln x_i$$

$$G = \sum_i n_i \mu_i^0 + nRT \sum_i x_i \ln x_i$$

$$Py_i = P_i^{sat} x_i$$

Relative volatility

$$\alpha_{ij} = \frac{P_i^{sat}}{P_j^{sat}}$$

## Chemical Principles Equation Sheet

All symbols have the same meaning as given in class materials.

$$V = -\frac{\mu_A \mu_B}{4\pi\epsilon R^3} [-2 \cos \theta_A \cos \theta_B + \sin \theta_A \sin \theta_B \cos(\phi_B - \phi_A)]$$

$$\frac{M_t}{M_e} = A_1 [1 - e^{-(k_1 t)^{\beta_1}}] + A_2 [1 - e^{-(k_2 t)^{\beta_2}}]$$

$$F_{electrostatic} = -k \frac{q_1 \cdot q_2}{r^2}$$

$$\eta = \eta_0 e^{\frac{E_a}{RT}}$$

$$E_{electrostatic} = k \frac{q_1 \cdot q_2}{r}$$

$$V = -\frac{\mu Q \cos \theta}{4\pi\epsilon R^2}$$

$$\epsilon_r = \frac{\epsilon}{\epsilon_0}$$

$$V = -\frac{\alpha Q^2 e^2}{32\pi^2 \epsilon^2 R^4}$$

$$E_{electrostatic} = \frac{q_1 \cdot q_2}{4\pi\epsilon_r r}$$

$$V = -\frac{\alpha_B \mu_A^2 (3 \cos^2 \theta_A + 1)}{32\pi^2 \epsilon^2 R^6}$$

$$K.E. = \frac{1}{2} m v^2$$

$$V = -\frac{3h(\nu_A \nu_B) \alpha_A \alpha_B}{512(\nu_A + \nu_B) \pi^4 \epsilon^4 R^6}$$

$$\langle v^2 \rangle^{\frac{1}{2}} = \left( \frac{3RT}{M} \right)^{\frac{1}{2}}$$

$$p = p^* e^{\frac{V_m \Delta P}{RT}}$$

**Error! Bookmark not**

**defined.** 
$$\frac{\left( \frac{3RT}{M_A} \right)^{\frac{1}{2}}}{\left( \frac{3RT}{M_B} \right)^{\frac{1}{2}}} = \left( \frac{M_B}{M_A} \right)^{\frac{1}{2}}$$

$$p = p^* e^{\frac{2\gamma V_m}{rRT}}$$

$$d^2 = 2Dt$$

$$p_{in} = p_{out} + \frac{2\gamma}{r}$$

$$D = \frac{\lambda^2}{2\tau}$$

$$p_{in} = p_{out} + \frac{4\gamma}{r}$$

$$D = D_0 e^{-\frac{E_a}{RT}}$$

$$\gamma = \frac{F}{L}$$

$$D = \frac{k_B T}{6\pi\eta a}$$

$$\frac{2\gamma}{r} = \rho gh$$





## Chemical Principles Equation Sheet

$$\gamma = \frac{r h \rho g}{2 \cos \theta}$$

$$ratio = \frac{V}{A \cdot L}$$

$$PV = nRT$$

$$\left(p + \frac{n^2 a}{V^2}\right)(V - nb) = nRT$$

$$\Gamma = \frac{-1}{RT} \left( \frac{d\gamma}{d \ln c} \right)_{p,T}$$

$$\Gamma = \frac{-1}{2.303RT} \left( \frac{d\gamma}{d \log c} \right)_{p,T}$$

$$A = \frac{1}{N_A \Gamma}$$

$$\Delta G = \Delta H - T \Delta S$$

$$Z = \frac{P}{(2\pi m k_B T)^{\frac{1}{2}}}$$

$$T = \frac{\text{Number of sites}}{\text{Collision rate}}$$

$$\frac{P}{n_{ads}} = \frac{1}{K n_m} + \frac{P}{n_m}$$

$$s = n_m A_m L$$

$$\frac{d \ln K}{dT} = \frac{\Delta_f H^\circ}{RT^2}$$

$$\left( \frac{d \ln p}{d \left( \frac{1}{T} \right)} \right)_\theta = \frac{\Delta_{ad} H^\circ}{R}$$

$$\Delta G = -RT \ln K$$

$$\frac{p}{n(p^o - p)} = \frac{1}{n_m c} + \frac{(c - 1)}{n_m c} \cdot \frac{p}{p^o}$$

$$c = \exp \left( \frac{|\Delta H_A| - |\Delta H_L|}{RT} \right)$$

$$\theta = c_1 \ln(c_2 p)$$

$$\theta = c_1 p^{\frac{1}{c_2}}$$

$$\theta_A = \frac{B_A P_A}{1 + \sum_i B_i P_i}$$

$$V_{ads} = \frac{(K \cdot p)^{\frac{1}{2}} \cdot V_m}{\left[ 1 + (K \cdot p)^{\frac{1}{2}} \right]}$$

$$\log w = \log w_o - D \log_{10}^2 \left( \frac{p^o}{p} \right)$$

$$D = B \left( \frac{T}{\beta} \right)^2$$

$$\frac{M_t}{M_e} = 1 - e^{-kt}$$

$$k = A e^{-\frac{E_a}{RT}}$$

# Periodic Table

Group	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
Period																		
1	1 H 1.008																	
2	3 Li 6.941	4 Be 9.012																
3	11 Na 22.99	12 Mg 24.31																
4	19 K 39.10	20 Ca 40.08	21 Sc 44.96	22 Ti 47.87	23 V 50.94	24 Cr 52.00	25 Mn 54.94	26 Fe 55.85	27 Co 58.93	28 Ni 58.69	29 Cu 63.55	30 Zn 65.41	31 Ga 69.72	32 Ge 72.64	33 As 74.92	34 Se 78.96	35 Br 79.90	36 Kr 83.80
5	37 Rb 85.47	38 Sr 87.62	39 Y 88.91	40 Zr 91.22	41 Nb 92.91	42 Mo 95.94	43 Tc 98	44 Ru 101.1	45 Rh 102.9	46 Pd 106.4	47 Ag 107.9	48 Cd 112.4	49 In 114.8	50 Sn 118.7	51 Sb 121.8	52 Te 127.6	53 I 126.9	54 Xe 131.3
6	55 Cs 132.9	56 Ba 137.3	71 Lu 175.0	72 Hf 178.5	73 Ta 180.9	74 W 183.8	75 Re 186.2	76 Os 190.2	77 Ir 192.2	78 Pt 195.1	79 Au 197.0	80 Hg 200.6	81 Tl 204.4	82 Pb 207.2	83 Bi 209.0	84 Po 209	85 At 210	86 Rn 222
7	87 Fr 223	88 Ra 226	103 Lr 260	104 Rf 267	105 Db 268	106 Sg 271	107 Bh 272	108 Hs 270	109 Mt 276	110 Ds 281	111 Rg 280	112 Uub 285	113 Uut 284	114 Uuq 289	115 Uup 288	116 Uuh 293	117 Uus —	118 Uuo 294
*Lanthanoids			57 La 138.9	58 Ce 140.1	59 Pr 140.9	60 Nd 144.2	61 Pm 145	62 Sm 150.3	63 Eu 151.9	64 Gd 157.2	65 Tb 158.9	66 Dy 164.9	67 Ho 167.2	68 Er 167.2	69 Tm 168.9	70 Yb 173.0		
†Actinoids			89 Ac 227	90 Th 232.0	91 Pa 231.0	92 U 238.0	93 Np 237	94 Pu 244	95 Am 243	96 Cm 247	97 Bk 247	98 Cf 251	99 Es 252	100 Fm 257	101 Md 258	102 No 259		

# Thermodynamics Steam Tables

		TEMPERATURE: $t^{\circ}\text{C}$ (TEMPERATURE: $T$ kelvins)									
$P/\text{kPa}$ ( $t^{\text{sat}}/^{\circ}\text{C}$ )		sat. liq.	sat. vap.	150 (423.15)	175 (448.15)	200 (473.15)	220 (493.15)	240 (513.15)	260 (533.15)	280 (553.15)	300 (573.15)
325 (136.29)	V	1.076	561.75	583.58	622.41	660.33	690.22	719.81	749.18	778.39	807.47
	U	572.847	2545.7	2568.7	2609.6	2649.6	2681.2	2712.7	2744.0	2775.3	2806.6
	H	573.197	2728.3	2758.4	2811.9	2864.2	2905.6	2946.6	2987.5	3028.2	3069.0
	S	1.7004	6.9640	7.0363	7.1592	7.2729	7.3585	7.4400	7.5181	7.5933	7.6657
350 (138.87)	V	1.079	524.00	540.58	576.90	612.31	640.18	667.75	695.09	722.27	749.33
	U	583.892	2548.2	2567.1	2608.3	2648.6	2680.4	2712.0	2743.4	2774.8	2806.2
	H	584.270	2731.6	2756.3	2810.3	2863.0	2904.5	2945.7	2986.7	3027.6	3068.4
	S	1.7273	6.9392	6.9982	7.1222	7.2366	7.3226	7.4045	7.4828	7.5581	7.6307
375 (141.31)	V	1.081	491.13	503.29	537.46	570.69	596.81	622.62	648.22	673.64	698.94
	U	594.332	2550.6	2565.4	2607.1	2647.7	2679.6	2711.3	2742.8	2774.3	2805.7
	H	594.737	2734.7	2754.1	2808.6	2861.7	2903.4	2944.8	2985.9	3026.9	3067.8
	S	1.7526	6.9160	6.9624	7.0875	7.2027	7.2891	7.3713	7.4499	7.5254	7.5981
400 (143.62)	V	1.084	462.22	470.66	502.93	534.26	558.85	583.14	607.20	631.09	654.85
	U	604.237	2552.7	2563.7	2605.8	2646.7	2678.8	2710.6	2742.2	2773.7	2805.3
	H	604.670	2737.6	2752.0	2807.0	2860.4	2902.3	2943.9	2985.1	3026.2	3067.2
	S	1.7764	6.8943	6.9285	7.0548	7.1708	7.2576	7.3402	7.4190	7.4947	7.5675
425 (145.82)	V	1.086	436.61	441.85	472.47	502.12	525.36	548.30	571.01	593.54	615.95
	U	613.667	2554.8	2562.0	2604.5	2645.7	2678.0	2709.9	2741.6	2773.2	2804.8
	H	614.128	2740.3	2749.8	2805.3	2859.1	2901.2	2942.9	2984.3	3025.5	3066.6
	S	1.7990	6.8739	6.8965	7.0239	7.1407	7.2280	7.3108	7.3899	7.4657	7.5388
450 (147.92)	V	1.088	413.75	416.24	445.38	473.55	495.59	517.33	538.83	560.17	581.37
	U	622.672	2556.7	2560.3	2603.2	2644.7	2677.1	2709.2	2741.0	2772.7	2804.4
	H	623.162	2742.9	2747.7	2803.7	2857.8	2900.2	2942.0	2983.5	3024.8	3066.0
	S	1.8204	6.8547	6.8660	6.9946	7.1121	7.1999	7.2831	7.3624	7.4384	7.5116
475 (149.92)	V	1.091	393.22	393.31	421.14	447.97	468.95	489.62	510.05	530.30	550.43
	U	631.294	2558.5	2558.6	2601.9	2643.7	2676.3	2708.5	2740.4	2772.2	2803.9
	H	631.812	2745.3	2745.5	2802.0	2856.5	2899.1	2941.1	2982.7	3024.1	3065.4
	S	1.8408	6.8365	6.8369	6.9667	7.0850	7.1732	7.2567	7.3363	7.4125	7.4858
500 (151.84)	V	1.093	374.68	.....	399.31	424.96	444.97	464.67	484.14	503.43	522.58
	U	639.569	2560.2	.....	2600.6	2642.7	2675.5	2707.8	2739.8	2771.7	2803.5
	H	640.116	2747.5	.....	2800.3	2855.1	2898.0	2940.1	2981.9	3023.4	3064.8
	S	1.8604	6.8192	.....	6.9400	7.0592	7.1478	7.2317	7.3115	7.3879	7.4614
525 (153.69)	V	1.095	357.84	.....	379.56	404.13	423.28	442.11	460.70	479.11	497.38
	U	647.528	2561.8	.....	2599.3	2641.6	2674.6	2707.1	2739.2	2771.2	2803.0
	H	648.103	2749.7	.....	2798.6	2853.8	2896.8	2939.2	2981.1	3022.7	3064.1
	S	1.8790	6.8027	.....	6.9145	7.0345	7.1236	7.2078	7.2879	7.3645	7.4381
550 (155.47)	V	1.097	342.48	.....	361.60	385.19	403.55	421.59	439.38	457.00	474.48
	U	655.199	2563.3	.....	2598.0	2640.6	2673.8	2706.4	2738.6	2770.6	2802.6
	H	655.802	2751.7	.....	2796.8	2852.5	2895.7	2938.3	2980.3	3022.0	3063.5
	S	1.8970	6.7870	.....	6.8900	7.0108	7.1004	7.1849	7.2653	7.3421	7.4158
575 (157.18)	V	1.099	328.41	.....	345.20	367.90	385.54	402.85	419.92	436.81	453.56
	U	662.603	2564.8	.....	2596.6	2639.6	2672.9	2705.7	2738.0	2770.1	2802.1
	H	663.235	2753.6	.....	2795.1	2851.1	2894.6	2937.3	2979.5	3021.3	3062.9
	S	1.9142	6.7720	.....	6.8664	6.9880	7.0781	7.1630	7.2436	7.3206	7.3945
600 (158.84)	V	1.101	315.47	.....	330.16	352.04	369.03	385.68	402.08	418.31	434.39
	U	669.762	2566.2	.....	2595.3	2638.5	2672.1	2705.0	2737.4	2769.6	2801.6
	H	670.423	2755.5	.....	2793.3	2849.7	2893.5	2936.4	2978.7	3020.6	3062.3
	S	1.9308	6.7575	.....	6.8437	6.9662	7.0567	7.1419	7.2228	7.3000	7.3740
625 (160.44)	V	1.103	303.54	.....	316.31	337.45	353.83	369.87	385.67	401.28	416.75
	U	676.695	2567.5	.....	2593.9	2637.5	2671.2	2704.2	2736.8	2769.1	2801.2
	H	677.384	2757.2	.....	2791.6	2848.4	2892.3	2935.4	2977.8	3019.9	3061.7
	S	1.9469	6.7437	.....	6.8217	6.9451	7.0361	7.1217	7.2028	7.2802	7.3544
650 (161.99)	V	1.105	292.49	.....	303.53	323.98	339.80	355.29	370.52	385.56	400.47
	U	683.417	2568.7	.....	2592.5	2636.4	2670.3	2703.5	2736.2	2768.5	2800.7
	H	684.135	2758.9	.....	2789.8	2847.0	2891.2	2934.4	2977.0	3019.2	3061.0
	S	1.9623	6.7304	.....	6.8004	6.9247	7.0162	7.1021	7.1835	7.2611	7.3355
675 (163.49)	V	1.106	282.23	.....	291.69	311.51	326.81	341.78	356.49	371.01	385.39
	U	689.943	2570.0	.....	2591.1	2635.4	2669.5	2702.8	2735.6	2768.0	2800.3
	H	690.689	2760.5	.....	2788.0	2845.6	2890.1	2933.5	2976.2	3018.5	3060.4
	S	1.9773	6.7176	.....	6.7798	6.9050	6.9970	7.0833	7.1650	7.2428	7.3173
700 (164.96)	V	1.108	272.68	.....	280.69	299.92	314.75	329.23	343.46	357.50	371.39
	U	696.285	2571.1	.....	2589.7	2634.3	2668.6	2702.1	2735.0	2767.5	2799.8
	H	697.061	2762.0	.....	2786.2	2844.2	2888.9	2932.5	2975.4	3017.7	3059.8
	S	1.9918	6.7052	.....	6.7598	6.8859	6.9784	7.0651	7.1470	7.2250	7.2997
725 (166.38)	V	1.110	263.77	.....	270.45	289.13	303.51	317.55	331.33	344.92	358.36
	U	702.457	2572.2	.....	2588.3	2633.2	2667.7	2701.3	2734.3	2767.0	2799.3
	H	703.261	2763.4	.....	2784.4	2842.8	2887.7	2931.5	2974.6	3017.0	3059.1
	S	2.0059	6.6932	.....	6.7404	6.8673	6.9604	7.0474	7.1296	7.2078	7.2827

Note:  $u$  and  $h$  are in units of  $\text{kJ kg}^{-1}$ ;  $s$  in units of  $\text{kJ kg}^{-1} \text{K}^{-1}$ ;  $v$  is in units of  $\text{cm}^3 \text{g}^{-1}$