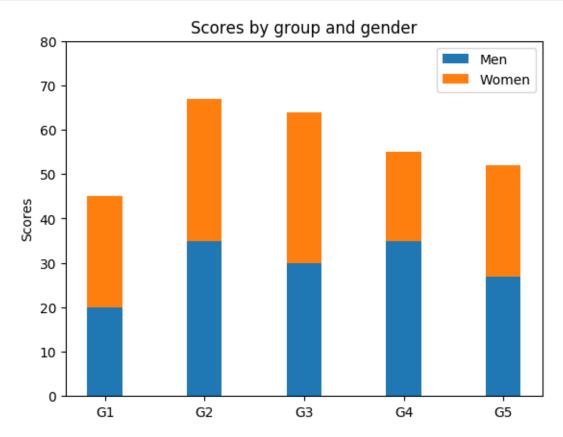
## UNITCOMMITMENT+2

### April 24, 2021

```
[45]: histogram([[1,1,1,1,2,2,2,3,3,3], [4,4,4,4,3,3,3,2,2,2]], stacked=True,
     N = 5
     menMeans = (20, 35, 30, 35, 27)
     womenMeans = (25, 32, 34, 20, 25)
     menStd = (2, 3, 4, 1, 2)
     womenStd = (3, 5, 2, 3, 3)
     ind = np.arange(N) # the x locations for the groups
     width = 0.35
                     # the width of the bars: can also be len(x) sequence
     p1 = plt.bar(ind, menMeans, width)#, yerr=menStd)
     p2 = plt.bar(ind, womenMeans, width,
                  bottom=menMeans)#, yerr=womenStd)
     plt.ylabel('Scores')
     plt.title('Scores by group and gender')
     plt.xticks(ind, ('G1', 'G2', 'G3', 'G4', 'G5'))
     plt.yticks(np.arange(0, 81, 10))
```

```
plt.legend((p1[0], p2[0]), ('Men', 'Women'))
plt.show()
```



## 0.1 MIXED INTEGER LINEAR PROGRAMMING

```
[46]: [3000.0 400.0 440.0
                                     50.0
                                             2.0 400.0
                               2.0
                                                           40.0
                                                                  75.0 5200.0
                                                                                43.5
      50.07
      [2500.0 345.0 365.0
                                             3.0 350.0
                                                                  74.0 4700.0
                               2.0
                                     70.0
                                                           50.0
                                                                                43.0
      44.0]
                                             2.0 205.0
                                                                  65.0 1320.0
      [2670.0 180.0 220.0
                               2.0
                                     78.0
                                                           40.0
                                                                                50.5
      36.01
      [3132.0
                61.0 210.0
                               2.0
                                     52.0
                                             3.0 197.0
                                                           40.0
                                                                  56.0 1291.0
                                                                                59.0
      29.01
      [2020.0 165.0 165.0
                               2.0
                                     54.2
                                             2.0 155.0
                                                           30.0
                                                                  67.0 1280.0
                                                                                37.1
      43.0]
      [1940.0 158.0 158.0
                               2.0
                                     39.0
                                             2.0 150.0
                                                           60.0
                                                                  70.0 1105.0
                                                                                44.8
      35.0]
      [2980.0
                 0.0
                       90.0
                               2.0
                                     17.4
                                             2.0
                                                   98.0
                                                           34.0
                                                                  60.0 560.0
                                                                                40.2
      33.0]
      [2544.0
                       87.0
                               3.0
                                             2.0
                                                   76.0
                                                           55.0
                                                                  80.0 554.0
                                                                                46.5
                32.0
                                     15.2
      40.07
      [3220.0
                 0.0
                       20.0
                               2.0
                                      4.0
                                             3.0
                                                   20.0
                                                           40.0
                                                                  40.0 300.0
                                                                                56.3
      43.07
                                                   12.0
      [1560.0
                 9.0
                       12.0
                               2.0
                                      2.4
                                             2.0
                                                           22.0
                                                                  22.0 250.0
                                                                                57.6
      23.01
```

```
[47]: M=sum([UNITCOMIT[n][1] for n in range(10)])
M
```

[47]: 1350.00000000000

```
[48]: table(UNITCOMIT.change_ring(CDF).round(1))
```

[48]: <repr(<sage.misc.table.table at 0x7fe0091d5650>) failed: TypeError: object of type 'sage.matrix.matrix\_complex\_double\_dense.Matrix\_complex\_double\_dense' has no len()>

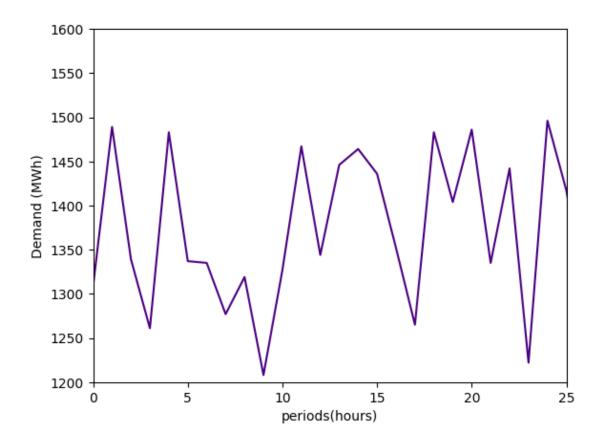
```
[49]: UNITCOMITTMENT=[['unit','energy','fixed-cost','initial','max-gen','min-downtime','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min-gen','min
```

[49]: unit energy fixed-cost initial max-gen min-downtime min-gen min-uptime operating-max-gen ramp-down ranp-up start-cost variable-

cost							
coal1	coal	208	400	440	2	50	3
400		40	75	5200	43		
coal2	coal	117	345	365	2	70	2
350		50	74	4700	43		
gas1	gas	174	180	220	3	78	3
205		40	65	1320	50		
gas2	gas	172	60	210	1	52	2
197		40	56	1291	59		
gas3	gas	95	165	165	2	54	2
155		30	67	1280	37		
gas4	gas	144	98	158	2	39	2
150		60	70	1105	44		
diesel1	diesel	54	70	90	2	17	3
98		34	60	560	40		
diesel2	diesel	55	76	87	2	15	3
76		20	35	554	41		
diesel3	diesel	80	0	20	2	3	1
20		18	60	300	116		
diesel4	diesel	16	0	12	2	2	1
12		5	12	250	77		

[50]: raw\_demand= [1259.0, 1439.0, 1289.0, 1211.0, 1433.0, 1287.0, 1285.0, 1227.0, \_\_ →1269.0, 1158.0, 1277.0, 1417.0, 1294.0, 1396.0, 1414.0, 1386.0, 1302.0, 1215.0, 1433.0, 1354.0, 1436.0, 1285.0, 1392.0, 1172.0, →1446.0, 1367.0, 1243.0, 1275.0, 1363.0, 1258, 1394.0, 1345.0, 1217.0, 1432.0, 1431.0, 1356.0, 1360.0, 1364.0, 1286.0, 1440.0, →1440.0, 1313.0, 1389.0, 1385.0, 1265.0, 1442.0, 1435.0, 1432.0, 1280.0, 1411.0, 1440.0, 1258.0, 1333.0, 1293.0, 1193.0, 1440.0, →1306.0, 1264.0, 1244.0, 1368.0, 1437.0, 1236.0, 1354.0, 1356.0, 1383.0, 1350.0, 1354.0, 1329.0, 1427.0, 1163.0, 1339.0, 1351.0, L  $\rightarrow$ 1174.0, 1235.0, 1439.0, 1235.0, 1245.0, 1262.0, 1362.0, 1184.0, 1207.0, 1359.0, 1443.0, 1205.0, 1192.0, 1364.0, 1233.0, 1281.0, 1  $\rightarrow$ 1295.0, 1357.0, 1191.0, 1329.0, 1294.0, 1334.0, 1265.0, 1207.0, 1365.0, 1432.0, 1199.0, 1191.0, 1411.0, 1294.0, 1244.0, 1256.0,  $\hookrightarrow$ 1257.0, 1224.0, 1277.0, 1246.0, 1243.0, 1194.0, 1389.0, 1366.0, 1282.0, 1221.0, 1255.0, 1417.0, 1358.0, 1264.0, 1205.0, 1254.0,  $\hookrightarrow$ 1276.0, 1435.0, 1335.0, 1355.0, 1337.0, 1197.0, 1423.0, 1194.0, 1310.0, 1255.0, 1300.0, 1388.0, 1385.0, 1255.0, 1434.0, 1232.0, U →1402.0, 1435.0, 1160.0, 1193.0, 1422.0, 1235.0, 1219.0, 1410.0, 1363.0, 1361.0, 1437.0, 1407.0, 1164.0, 1392.0, 1408.0, 1196.0, L  $\hookrightarrow$ 1430.0, 1264.0, 1289.0, 1434.0, 1216.0, 1340.0, 1327.0, 1230.0, 1362.0, 1360.0, 1448.0, 1220.0, 1435.0, 1425.0, 1413.0, 1279.0, →1269.0, 1162.0, 1437.0, 1441.0, 1433.0, 1307.0, 1436.0, 1357.0, 1437.0, 1308.0, 1207.0, 1420.0, 1338.0, 1311.0, 1328.0, 1417.0, →1394.0, 1336.0, 1160.0, 1231.0, 1422.0, 1294.0, 1434.0, 1289.0]

```
[51]: import random
      demand=[]
      demand+=[raw_demand[i]+50 for i in range(len(raw_demand))]#random.
       \hookrightarrow randint (150,300)
      for i in range(5):
       print(demand[i])
     1309.00000000000
     1489.00000000000
     1339.00000000000
     1261.00000000000
     1483.00000000000
[52]: import random
      spanning=[]
      spanning.append(41)
      spanning1=[0+random.randint(30,50) for i in range(0,len(raw_demand)-1)]#random.
       \rightarrow randint (150,300)
      for i in range(len(raw_demand)-1):
          spanning.append(spanning1[i])
      len(spanning)
[52]: 192
[53]: demand[0]+spanning[0]
[53]: 1350.00000000000
[54]: import matplotlib.pyplot as plt
      plt.plot(demand, color='indigo')
      plt.ylabel('Demand (MWh)')
      plt.xlabel('periods(hours)')
      plt.axis([0, 25, 1200,1600])
      plt.show()
```



```
[55]: N=10
      T=50
      K=N*T
      R = PolynomialRing(RR, 'Gen', K)
      Gen = R.gens()
      #tim = S.gens()
      Gen=[SR(Gen[i]) for i in srange(0,K)];
      R = PolynomialRing(RR, 'gen', 20)
      S = PolynomialRing(RR, 'tim', 20)
      gen = R.gens()
      tim = S.gens()
      gen_i_time_j=[SR(gen[i])*SR(tim[j]) for i in srange(0,10) for j in srange(0,10)_u
      ⇔];
      len(gen_i_time_j)
      R = PolynomialRing(RR, 'Gen', K)
      Gen = R.gens()
      tim = S.gens()
      Gen=[SR(Gen[k]) for k in srange(0,K)];
      p = MixedIntegerLinearProgram(maximization=False, solver = "GLPK") #Variables x_
      \rightarrow and y ve assume only real and non-negative values.
      v = p.new_variable(real=True, nonnegative=True)
```

```
w = p.new_variable(binary=True, nonnegative=True)
t =p.new_variable(binary=True, nonnegative=True)
s=p.new_variable(binary=True, nonnegative=True)
h = p.new_variable(integer=True, nonnegative=True)
Var=[v[Gen[k]] for k in range(K)]
var1=[h[Gen[k]] for k in range(K)]
indic_su=[w[Gen[k]] for k in range(K)]
indic sd=[t[Gen[k]] for k in range(K)]
indic_on_off=[s[Gen[k]] for k in range(K)]
gencostt=[sum([UNITCOMIT[n][10]*Var[T*n+t] for n in range(N)]) for t in,
 \rightarrowrange(T)]
startcostt=[sum([UNITCOMIT[n][9]*indic_su[T*n+t] for n in range(N)]) for t in_u
 \rightarrowrange(T)]
shutcostt=[sum([UNITCOMIT[n][0]*indic_sd[T*n+t] for n in range(N)]) for t in_
\rightarrowrange(T)]
z1=sum(gencostt)
z2=sum(startcostt)
z3=sum(shutcostt)
z=z1+z2+z3
show(z)
#OBJECTIVE FUNCTION
p.set_objective(z)
tgent=[sum([Var[T*n+t]for n in range(N)]) for t in range(T)]
#CONNSTRATNTS
#Initial condition
[p.add_constraint(Var[T*n] == UNITCOMIT[n][1]) for n in range(N)]
#power balance constraints
[p.add_constraint(tgent[t] == demand[t]+spanning[t])for t in range(T)]
#[p.add_constraint(tqent[j] >= demand[j]) for j in range(J)]
#Power generation at each time period should be within the allowable limit
[p.add_constraint(Var[T*n+t]>= (UNITCOMIT[n][4])*indic_on_off[T*n+t]) for n in_u
→range(N) for t in range(T)]
[p.add_constraint(Var[T*n+t] <= (UNITCOMIT[n][2])*indic_on_off[T*n+t]) for n in_u
 →range(N) for t in range(T)]
#Ramp up and ramp down constraints
[p.add_constraint(Var[T*n+t+1]-Var[T*n+t] <= UNITCOMIT[n][7]) for n in range(N)
\rightarrowfor t in range(T-1)]
[p.add\ constraint(Var[T*n+t+1]-Var[T*n+t]>= (-1)*UNITCOMIT[n][4])\ for\ n\ in_{l}
→range(N) for t in range(T-1)]
\#sum\_indic\_on\_off = [sum([indic\_on\_off[10*i+j] \ for \ i \ in \ range(I)]) \ for \ j \ in\_location = [sum([indic\_on\_off[10*i+j] \ for \ i \ in\_location])]
 \rightarrow range(J)]
```

```
#sum_indic_on_off1=[sum([indic_on_off[10*i+j] for i in range(I)]) for j in
\rightarrow range(7, J)]
#show(sum_indic_on_off1)
#[p.add_constraint(sum_indic_on_off[i] <= 9) for i in range(10)]
\#[p.add\_constraint(sum([indic\_on\_off[i]])>=1)  for i in range(8*J,10*J)]
#[p.
\rightarrow add\_constraint(indic\_su[J*i+j] == (indic\_on\_off[J*i+j] - indic\_on\_off[J*i+j-1]))_{\sqcup}
\rightarrow for i in range(I) for j in range(1,J)]
[p.add_constraint(indic_on_off[T*8+T-7]==1)]
[p.add_constraint(indic_on_off[T*3+T-4]==1)]
#print(indic_on_off[10*0])
#Minimum uptime and minimum down time constraints
#for n in range(N):
    #for t in range(1,T-2):
             #if (indic\_on\_off[T*n+t]-indic\_on\_off[T*n+t-1]==1):
                 #[p.
\rightarrow add_constraint(indic_on_off[T*n+t]+indic_on_off[T*n+t+1]==2)]
            #elif (indic on off[T*n+t]-indic on off[T*n+t-1]==-1):
                 #υ.
\rightarrow add_constraint(indic_on_off[T*n+t]+indic_on_off[T*n+t+1]+indic_on_off[T*n+t+2]=0)
    \#[p.add\ constraint(indic\ su[i]==1)\ if\ Var[i]-Var[i-1]==Var[i]\ else\ p.
\rightarrow add\_constraint(indic\_su[i]==0)
#for i in range(100)]
for i in range(1,len(Var)):
    if (Var[i]-Var[i-1]==Var[i]):
        p.add_constraint(indic_su[i] == 1)
    else :
        p.add_constraint(indic_su[i]==0)
Set1=[Var[T*n+t] for n in range(N) for t in range(T)]
Set2=[indic_su[T*n+t] for n in range(N) for t in range(T)]
Set3=[indic_on_off[T*n+t] for n in range(N) for t in range(T)]
Set4=[indic_sd[T*n+t] for n in range(N) for t in range(T)]
Z1=(p.solve())
\#Z2=(p.solve(2))
\#Z3=(p.solve(3))
Val1=[p.get_values(Set1[k]) for k in range(K)]
```

```
Val2=[p.get_values(Set2[k]) for k in range(K)]
Val3=[p.get_values(Set3[k]) for k in range(K)]
Val4=[p.get_values(Set4[k]) for k in range(K)]
D=[[Val1[T*n+t]for n in range(N)] for t in range(T)]
for n in range(N):
    Val2[T*n]=0
for n in range(0,N):
    for t in range(1,T):
        if (Val1[T*n+t]-Val1[T*n+t-1]==Val1[T*n+t] and Val1[T*n+t]>0):
            Val2[T*n+t]=1
        else:
            Val2[T*n+t]=0
for n in range(0,N):
    for t in range(1,T):
        if (Val1[T*n+t]-Val1[T*n+t-1] == (-1*Val1[T*n+t-1]) and Val1[T*n+t-1] > 0):
            Val4[T*n+t]=1
        else:
            Val4[T*n+t]=0
\#startcostt = sum([sum([UNITCOMIT[i][9]*Val2[10*i+j] for i in range(I)]) for j in_{\square}
\rightarrow range(J)])
\#shutcostt=sum([sum([UNITCOMIT[i][9]*Val4[10*i+j] for i in range(I)]) for j in_{\square}
\rightarrow range(J)])
#Minimum uptime
Fn=[min([T,t+UNITCOMIT[n][5]])for n in range(N) for t in range(T)]
for n in range(1,N):
    for t in range(1,T-1):
        if (Val2[T*n+t]==1):
            #print(s)
             [p.add_constraint(indic_on_off[T*n+s]==1) for s in_
→range(t,Fn[T*n+t])]
#Minimum downtime
Hn=[min([T,t+UNITCOMIT[n][3]])for n in range(N) for t in range(T)]
#print(Hn)
for n in range(N):
    for t in range(T-1):
        if (Val4[T*n+t]==1):
             [p.add_constraint(indic_on_off[T*n+1]==0) for 1 in_
→range(t,Hn[T*n+t])]
\#show(Z1)
\#show(Z2)
\#show(Z3)
```

```
Z=Z1
show(Z)
Schedule=matrix(D)
show(Schedule)
E=[[Val2[T*n+t]for n in range(N)] for t in range(T)]
show(matrix(E))
F=matrix([[Val3[T*n+t]for n in range(N)] for t in range(T)])
show(F)
G=matrix([[Val4[T*n+t]for n in range(N)] for t in range(T)])
show(G)
gencost=[sum([UNITCOMIT[n][10]*Val1[T*n+t] for t in range(T)]) for n in_
\rightarrowrange(N)]
startcost=[sum([UNITCOMIT[n][9]*Val2[T*n+t] for t in range(T)]) for n in_u
\rightarrowrange(N)]
shutcost=[sum([UNITCOMIT[n][0]*Val4[T*n+t] for t in range(T)]) for n in_
→range(N)]
operationcost=[gencost[i]+startcost[i]+shutcost[i] for i in range(10) ]
AVTIME=[sum([Val3[T*n+t] for t in range(T)]) for n in range(N)]
AVOUT=[(1/AVTIME[n])*sum([Val1[T*n+t] for t in range(T)]) for n in range(N)]
```

```
43.536*x_0 + 43.536*x_1 + 43.536*x_2 + 43.536*x_3 + 43.536*x_4 + 43.536*x_5 + 43.
 536 \times x_6 + 43.536 \times x_7 + 43.536 \times x_8 + 43.536 \times x_9 + 43.536 \times x_{10} + 43.536 \times x_{11} + 43.536 \times x_{10}
 \rightarrow 43.536*x_12 + 43.536*x_13 + 43.536*x_14 + 43.536*x_15 + 43.536*x_16 + 43.
 \rightarrow536*x_17 + 43.536*x_18 + 43.536*x_19 + 43.536*x_20 + 43.536*x_21 + 43.536*x_22
 \rightarrow + 43.536*x_23 + 43.536*x_24 + 43.536*x_25 + 43.536*x_26 + 43.536*x_27 + 43.
 \rightarrow536*x_28 + 43.536*x_29 + 43.536*x_30 + 43.536*x_31 + 43.536*x_32 + 43.536*x_33_
 \rightarrow + 43.536*x_34 + 43.536*x_35 + 43.536*x_36 + 43.536*x_37 + 43.536*x_38 + 43.
 \rightarrow536*x_39 + 43.536*x_40 + 43.536*x_41 + 43.536*x_42 + 43.536*x_43 + 43.536*x_44_
 \rightarrow + 43.536*x_45 + 43.536*x_46 + 43.536*x_47 + 43.536*x_48 + 43.536*x_49 + 42.
 \rightarrow985*x_50 + 42.985*x_51 + 42.985*x_52 + 42.985*x_53 + 42.985*x_54 + 42.985*x_55_0
 \rightarrow + 42.985*x_56 + 42.985*x_57 + 42.985*x_58 + 42.985*x_59 + 42.985*x_60 + 42.
 \rightarrow 985*x_61 + 42.985*x_62 + 42.985*x_63 + 42.985*x_64 + 42.985*x_65 + 42.985*x_66_
 \rightarrow + 42.985*x_67 + 42.985*x_68 + 42.985*x_69 + 42.985*x_70 + 42.985*x_71 + 42.
 \rightarrow985*x_72 + 42.985*x_73 + 42.985*x_74 + 42.985*x_75 + 42.985*x_76 + 42.985*x_77_\( \)
 \rightarrow + 42.985*x_78 + 42.985*x_79 + 42.985*x_80 + 42.985*x_81 + 42.985*x_82 + 42.
 \rightarrow985*x_83 + 42.985*x_84 + 42.985*x_85 + 42.985*x_86 + 42.985*x_87 + 42.985*x_88_
 \rightarrow + 42.985*x_89 + 42.985*x_90 + 42.985*x_91 + 42.985*x_92 + 42.985*x_93 + 42.
  985*x_94 + 42.985*x_95 + 42.985*x_96 + 42.985*x_97 + 42.985*x_98 + 42.985*x_99 
 \rightarrow + 50.5*x_100 + 50.5*x_101 + 50.5*x_102 + 50.5*x_103 + 50.5*x_104 + 50.5*x_105_\( \)
 \rightarrow + 50.5*x_106 + 50.5*x_107 + 50.5*x_108 + 50.5*x_109 + 50.5*x_110 + 50.5*x_111_\( \cdot\)
 \rightarrow + 50.5*x_112 + 50.5*x_113 + 50.5*x_114 + 50.5*x_115 + 50.5*x_116 + 50.5*x_117_\to
 \rightarrow + 50.5*x_118 + 50.5*x_119 + 50.5*x_120 + 50.5*x_121 + 50.5*x_122 + 50.5*x_123_\( \)
 \rightarrow + 50.5*x_124 + 50.5*x_125 + 50.5*x_126 + 50.5*x_127 + 50.5*x_128 + 50.5*x_129_\( \)
 \rightarrow + 50.5*x_130 + 50.5*x_131 + 50.5*x_132 + 50.5*x_133 + 50.5*x_134 + 50.5*x_135_
 \rightarrow + 50.5*x_136 + 50.5*x_137 + 50.5*x_138 + 50.5*x_139 + 50.5*x_140 + 50.5*x_141_{\square}
 \rightarrow + 50.5*x_142 + 50.5*x_143 + 50.5*x_144 + 50.5*x_145 + 50.5*x_146 + 50.5*x_147_\( \)
 →+ 50.5*x_148 + 50.5*x_149 + 59*x_150 + 59*x_151 + 59*x_152 + 59*x_153 +<sub>□</sub>
 \rightarrow 59*x_154 + 59*x_155 + 59*x_156 + 59*x_157 + 59*x_158 + 59*x_159 + 59*x_160 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100 + 100
 →59*x_161 + 59*x_162 + 59*x_163 + 59*x_164 + 59*x_165 + 59*x_166 + 59*x_167 +<sub>∪</sub>
 59*x_168 + 59*x_169 + 59*x_170 + 59*x_171 + 59*x_172 + 59*x_173 + 59*x_174 + 
 59*x_175 + 59*x_176 + 59*x_177 + 59*x_178 + 59*x_179 + 59*x_180 + 59*x_181 + 10
 →59*x_182 + 59*x_183 + 59*x_184 + 59*x_185 + 59*x_186 + 59*x_187 + 59*x_188 +<sub>□</sub>
 →59*x_189 + 59*x_190 + 59*x_191 + 59*x_192 + 59*x_193 + 59*x_194 + 59*x_195 +<sub>□</sub>
 59*x_196 + 59*x_197 + 59*x_198 + 59*x_199 + 37.146*x_200 + 37.146*x_201 + 37.
 \rightarrow 146*x_202 + 37.146*x_203 + 37.146*x_204 + 37.146*x_205 + 37.146*x_206 + 37.
 \rightarrow 146*x_207 + 37.146*x_208 + 37.146*x_209 + 37.146*x_210 + 37.146*x_211 + 37.
 \rightarrow 146*x_212 + 37.146*x_213 + 37.146*x_214 + 37.146*x_215 + 37.146*x_216 + 37.
 \rightarrow 146 \times x_217 + 37.146 \times x_218 + 37.146 \times x_219 + 37.146 \times x_220 + 37.146 \times x_221 + 37.
 \rightarrow 146*x_222 + 37.146*x_223 + 37.146*x_224 + 37.146*x_225 + 37.146*x_226 + 37.
 \rightarrow 146*x_227 + 37.146*x_228 + 37.146*x_229 + 37.146*x_230 + 37.146*x_231 + 37.
 \rightarrow 146*x_232 + 37.146*x_233 + 37.146*x_234 + 37.146*x_235 + 37.146*x_236 + 37.
 \rightarrow 146 \times x_{237} + 37.146 \times x_{238} + 37.146 \times x_{239} + 37.146 \times x_{240} + 37.146 \times x_{241} + 37.
 \rightarrow 146 \times x_2 42 + 37.146 \times x_2 43 + 37.146 \times x_2 44 + 37.146 \times x_2 45 + 37.146 \times x_2 46 + 37.
 \rightarrow 146 \times x_2 \times 247 + 37.146 \times x_2 \times 248 + 37.146 \times x_2 \times 249 + 44.84 \times x_2 \times 250 + 44.84 \times x_2 \times 251 + 44.
 \rightarrow 84*x_252 + 44.84*x_253 + 44.84*x_254 + 44.84*x_255 + 44.84*x_256 + 44.84*x_257
 →+ 44.84*x_258 + 44.84*x_259 + 44.84*x_260 + 44.84*x_261 + 44.84*x_262 + 44.
 44.84 \times 263 + 44.84 \times 264 + 44.84 \times 265 + 44.84 \times 266 + 44.84 \times 267 + 44.84 \times 268
 →+ 44.84*x_269 + 44.84*x_270 + 44.84*x_271 + 44.84*x_272 + 44.84*x_273 + 44.
 \rightarrow 84*x_274 + 44.84*x_275 + 44.84*x_276 + 44.84*x_277 + 44.84*x_278 + 44.84*x_279_1
 →+ 44.84*x_280 + 44.84*x_281 + 44.84*x<sub>1</sub>282 + 44.84*x_283 + 44.84*x_284 + 44.
 →84*x_285 + 44.84*x_286 + 44.84*x_287 + 44.84*x_288 + 44.84*x_289 + 44.84*x_290<sub>□</sub>
 →+ 44.84*x_291 + 44.84*x_292 + 44.84*x_293 + 44.84*x_294 + 44.84*x_295 + 44.
```

 $\Rightarrow 84*x_296 + 44.84*x_297 + 44.84*x_298 + 44.84*x_299 + 40.222*x_300 + 40.$ 

#### 3962087.8189999885

```
50 x 10 dense matrix over Real Double Field (use the '.str()' method to see the
→entries)

50 x 10 dense matrix over Integer Ring (use the '.str()' method to see the
→entries)

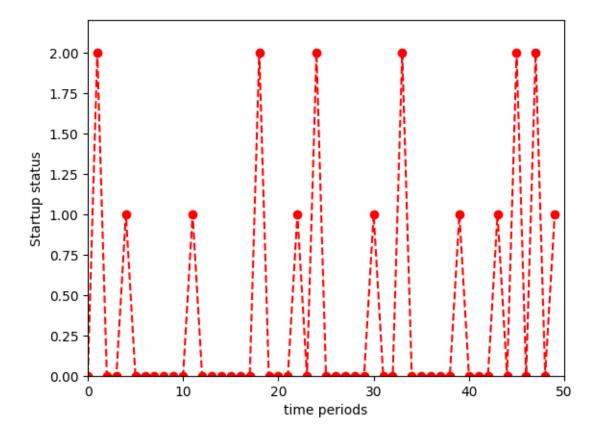
50 x 10 dense matrix over Real Double Field (use the '.str()' method to see the
→entries)

50 x 10 dense matrix over Real Double Field (use the '.str()' method to see the
→entries)

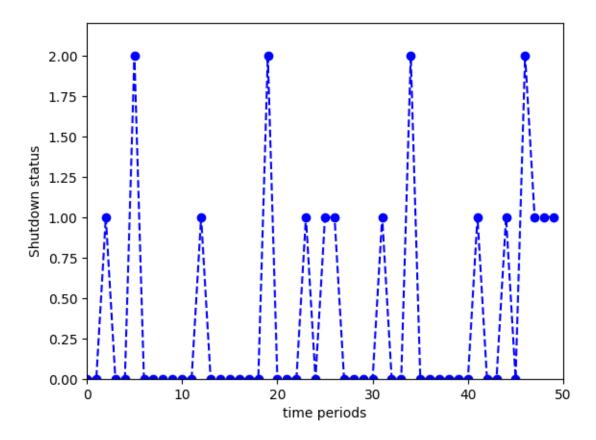
[56]: D=[[Val1[T*n+t]for t in range(T)] for n in range(N)]
k=[[Val1[T*n+t]for n in range(N)] for t in range(T)]
show(k[0][0])
bars = [sum([k[t]]n] for n in range(1,N)]) for t in range(T)]
```

400.0

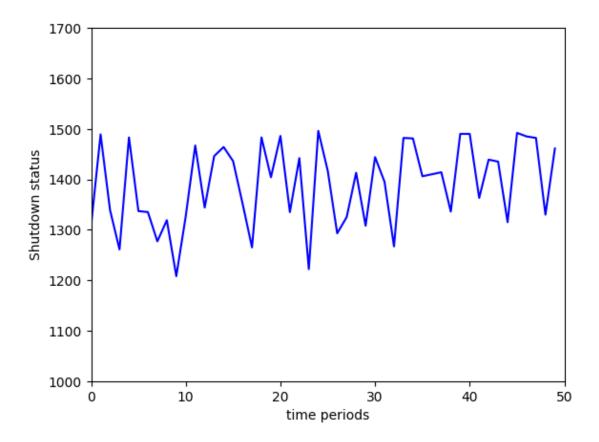
```
[57]: startup=[sum(E[t]) for t in range(T)]
import matplotlib.pyplot as plt
a=plt.plot(startup,'bo', color='red')
b=plt.plot(startup,'r--', color='red')
plt.ylabel('Startup status')
plt.xlabel('time periods')
plt.axis([0,T, 0,2.2])
plt.show()
```



```
[58]: shutdown=[sum(G[t]) for t in range(T)]
#shutdown[44]=1
#shutdown[46]=0
#l=[startup[i] for i in range(45,50)]
#show(l)
import matplotlib.pyplot as plt
plt.plot(shutdown, 'bo', color='blue')
plt.plot(shutdown, 'r--', color='blue')
plt.ylabel('Shutdown status')
plt.xlabel('time periods')
plt.axis([0,T, 0,2.2])
plt.show()
```



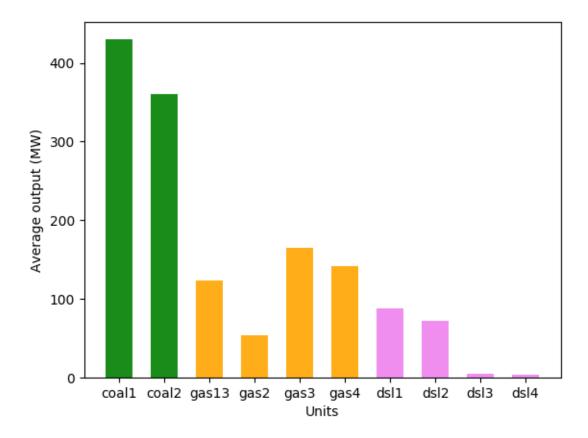
```
[59]: d=[demand[i] for i in range(T)]
    plt.plot(d, color='blue')
    plt.ylabel('Shutdown status')
    plt.xlabel('time periods')
    plt.axis([0,T, 1000,1700])
    plt.show()
```



```
[60]: P=AVOUT
     show(P)
     import matplotlib.pyplot as plt; plt.rcdefaults()
     import numpy as np
     import matplotlib.pyplot as plt
     objects = ('coal1', 'coal2', 'gas13', 'gas2', 'gas3', 'gas4', 'dsl1', 'dsl2', u
      y_pos = np.arange(len(objects))
     performance = P
     plt.bar(y_pos, performance, align='center', alpha=0.9,width=0.6,__
      →color=['green','green','orange','orange','orange','orange','violet','violet','violet','viol
     plt.xticks(y_pos, objects)
     plt.ylabel('Average output (MW)')
     plt.xlabel('Units')
     plt.title('')
     plt.show()
```

[430.4319999999996, 360.428000000000000,

```
123.052,
53.34893617021277,
164.48,
140.956,
88.0530612244898,
72.02000000000001,
4.933333333333336,
3.599999999999988]
```



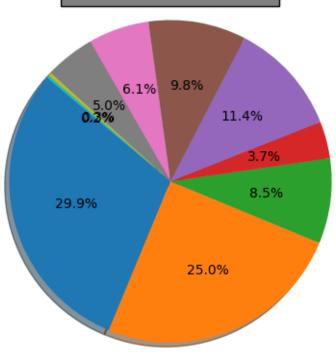
```
[61]: import matplotlib.pyplot as plt
    coal=sum([gencost[i]+startcost[i]+shutcost[i] for i in range(0,2)])
    gas =sum([gencost[i]+startcost[i]+shutcost[i] for i in range(2,6)])
    diesel =sum([gencost[i]+startcost[i]+shutcost[i] for i in range(6,10)])
    cost=AVOUT
    # Data to plot
    labels = 'coal', 'gas', 'diesel'
    #cost=[coal,gas,diesel]
    #colors = ['gold', 'yellowgreen', 'lightcoral']
    explode = ( 0, 0, 0, 0, 0, 0, 0, 0, 0) # explode 1st slice

# Plot
```

```
plt.pie(cost, explode=explode, autopct='%1.1f%%', shadow=True, startangle=140)
plt.title('Total cost by energy type', bbox={'facecolor':'0.5', 'pad':5})

plt.axis('equal')
plt.show()
show(cost)
```

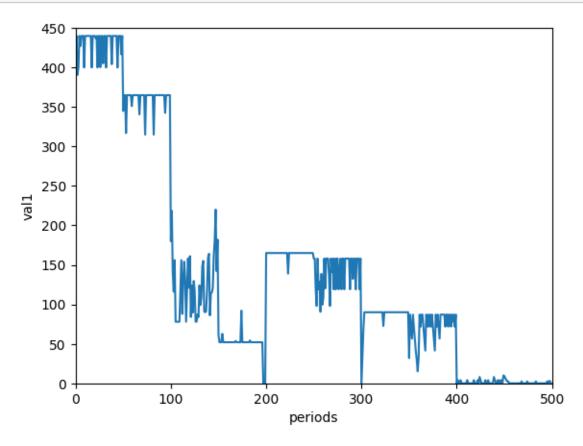
# Total cost by energy type

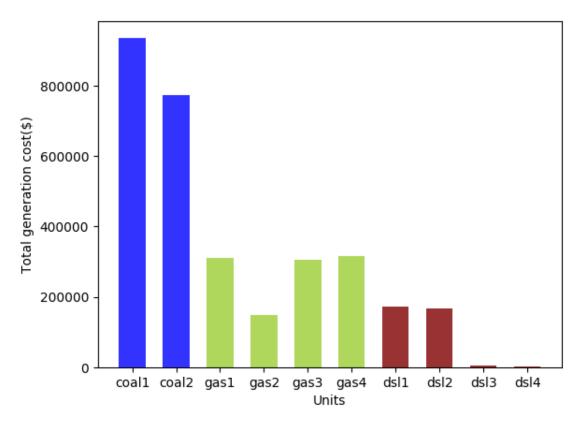


```
[430.4319999999996,
    360.4280000000005,
    123.052,
    53.34893617021277,
    164.48,
    140.956,
    88.0530612244898,
    72.02000000000001,
    4.93333333333336,
    3.5999999999988]

[62]: # import matplotlib.pyplot as plt
plt.plot(Val1)
plt.ylabel('val1')
plt.xlabel('periods')
```

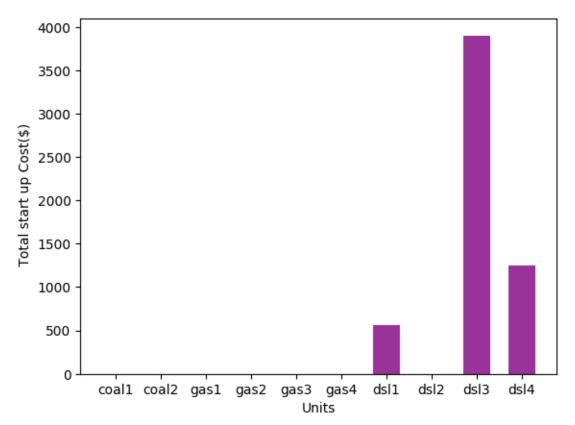
```
plt.axis([0,K, 0,450])
plt.show()
```



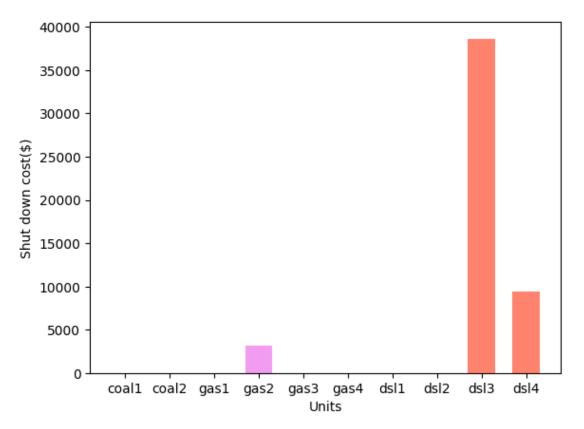


```
[64]: #P=[sum([Val1[J*i+j] for j in range(J)]) for i in range(I)]
P=startcost
import matplotlib.pyplot as plt; plt.rcdefaults()
import numpy as np
import matplotlib.pyplot as plt

objects = ('coal1', 'coal2', 'gas1', 'gas2', 'gas3', 'gas4', 'dsl1', 'dsl2', \( \to \'dsl3', 'dsl4') \)
y_pos = np.arange(len(objects))
performance = P
barWidth = 0.2
```



```
plt.xticks(y_pos, objects)
plt.ylabel('Shut down cost($)')
plt.xlabel('Units')
plt.title('')
plt.show()
```



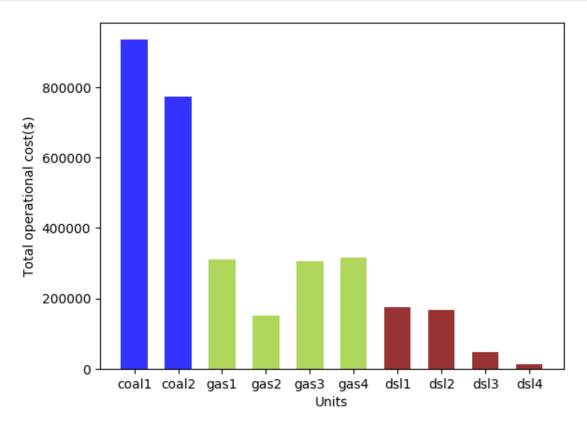
```
[66]: #P=[sum([Val1[J*i+j] for j in range(J)]) for i in range(I)]
```

```
P=operationcost
import matplotlib.pyplot as plt; plt.rcdefaults()
import numpy as np
import matplotlib.pyplot as plt

objects = ('coal1', 'coal2', 'gas1', 'gas2', 'gas3', 'gas4', 'dsl1', 'dsl2', \( \to 'dsl3', 'dsl4') \)
y_pos = np.arange(len(objects))
performance = P

plt.bar(y_pos, performance, align='center', alpha=0.8, width=0.6, \( \to \to \color=['blue', 'blue', 'yellowgreen', 'yellowgreen', 'yellowgreen', 'maroon', 'maro
```

```
plt.xticks(y_pos, objects)
plt.ylabel('Total operational cost($)')
plt.xlabel('Units')
plt.title('')
plt.show()
```



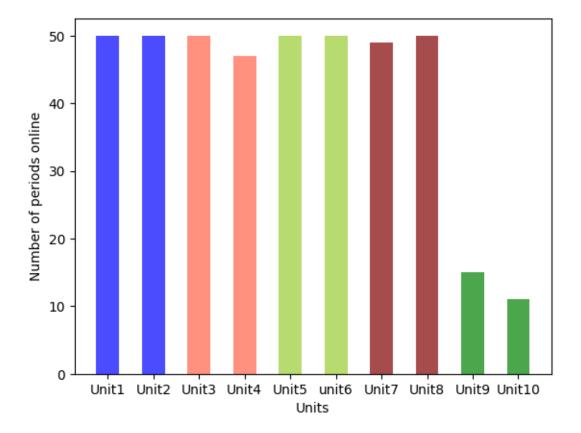
```
[67]: P=[sum([Val3[T*n+t] for t in range(T)]) for n in range(N)]
    show(P)
    import matplotlib.pyplot as plt; plt.rcdefaults()
    import numpy as np
    import matplotlib.pyplot as plt

objects = ('Unit1', 'Unit2', 'Unit3', 'Unit4', 'Unit5', 'unit6', 'Unit7', \underset{\unit6'}, 'Unit8', 'Unit10',)
    y_pos = np.arange(len(objects))
    performance = P

plt.bar(y_pos, performance, align='center', alpha=0.7, width=0.5, \underset{\unit6'}, \unit6', \uni
```

```
plt.xlabel('Units')
plt.title('')
plt.show()
```

[50.0, 50.0, 50.0, 47.0, 50.0, 50.0, 49.0, 50.0, 15.0, 11.0]



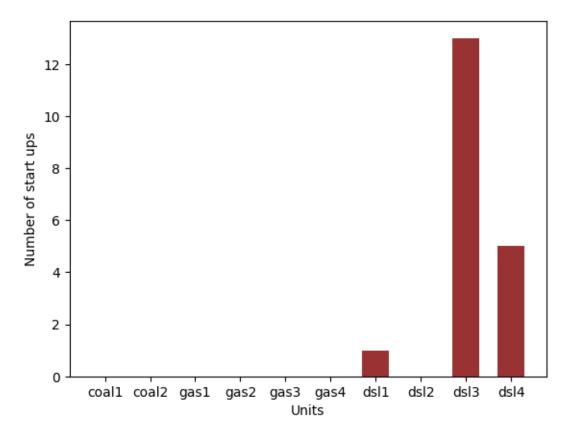
```
[]:
```

```
[68]: P=[sum([Val2[T*n+t] for t in range(T)]) for n in range(N)]
import matplotlib.pyplot as plt; plt.rcdefaults()
import numpy as np
import matplotlib.pyplot as plt

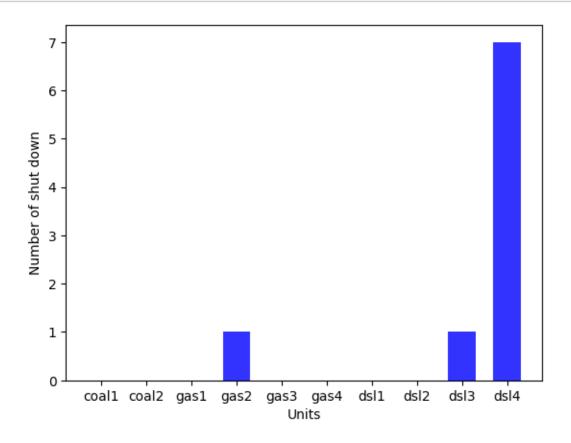
objects = ('coal1', 'coal2', 'gas1', 'gas2', 'gas3', 'gas4', 'dsl1', 'dsl2', \( \to 'dsl3', 'dsl4') \)
y_pos = np.arange(len(objects))
performance = P

plt.bar(y_pos, performance, align='center', alpha=0.8, width=0.6, \( \to \to \color=['blue', 'blue', 'yellowgreen', 'yellowgreen', 'yellowgreen', 'maroon', 'maro plt.xticks(y_pos, objects)
```

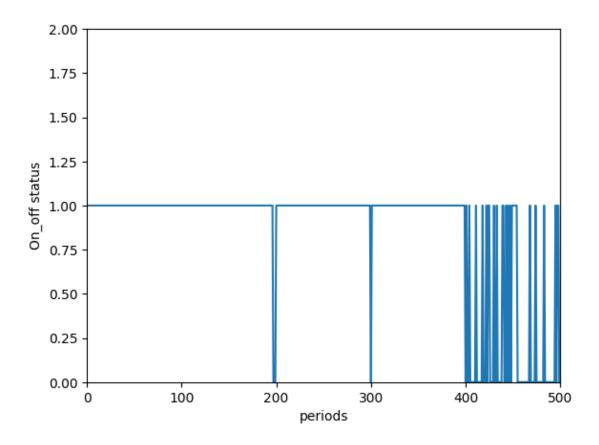
```
plt.ylabel('Number of start ups')
plt.xlabel('Units')
plt.title('')
plt.show()
```



plt.show()



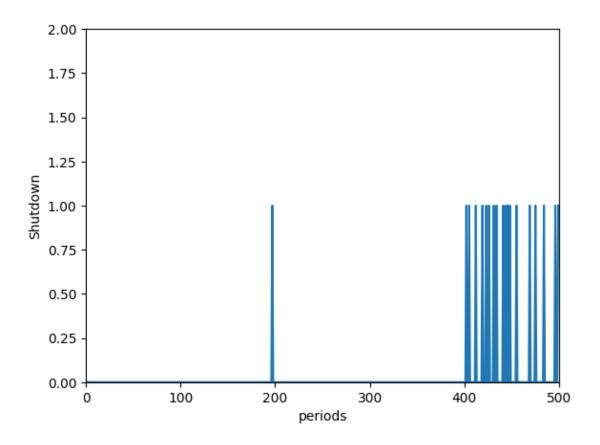
```
[70]: import matplotlib.pyplot as plt
plt.plot(Val3)
plt.ylabel('On_off status')
plt.xlabel('periods')
plt.axis([0,K, 0,2])
plt.show()
```



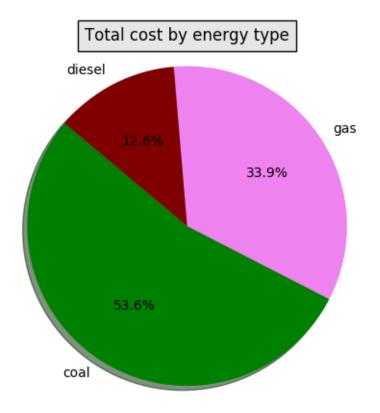
```
[71]: k=[indic_on_off[10*i] for i in range(10)]
    print(sum(k))

    x_2000 + x_2010 + x_2020 + x_2030 + x_2040 + x_2050 + x_2060 + x_2070 + x_2080 +
    x_2090

[72]: sage.misc.sage_timeit_class.SageTimeit
    import matplotlib.pyplot as plt
    plt.plot(Val4)
    plt.ylabel('Shutdown')
    plt.xlabel('periods')
    plt.axis([0,K, 0,2])
    plt.show()
```



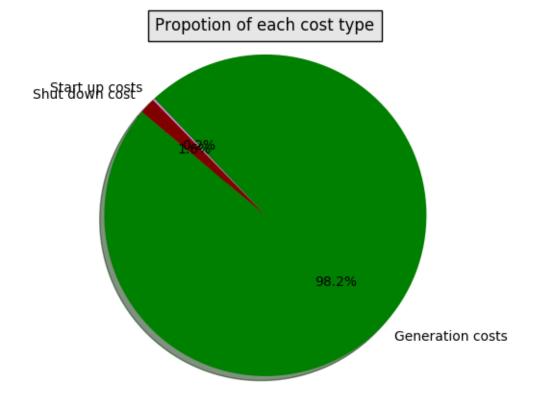
```
[73]: import matplotlib.pyplot as plt
      coal=sum([gencost[i]+startcost[i]+shutcost[i] for i in range(0,2)])
      gas =sum([gencost[i]+startcost[i]+shutcost[i] for i in range(2,6)])
      diesel =sum([gencost[i]+startcost[i]+shutcost[i] for i in range(6,10)])
      cost=[coal,gas,diesel]
      # Data to plot
      labels = 'coal', 'gas', 'diesel'
      cost=[coal,gas,diesel]
      #colors = ['gold', 'yellowgreen', 'lightcoral']
      explode = (0,0,0) # explode 1st slice
      # Plot
      plt.pie(cost, explode=explode, labels=labels, colors=colors,
              autopct='%1.1f%%', shadow=True, startangle=140)
      plt.title('Total cost by energy type', bbox={'facecolor':'0.9', 'pad':5})
      plt.axis('equal')
      plt.show()
      show(cost)
```



### [1.71161425660000e6, 1.08328695600000e6, 401228.606400000]

```
[74]: import matplotlib.pyplot as plt
      Tgencost= sum(gencost)
      Tstartcost= sum(startcost)
      Tshutcost= sum(shutcost)
      \#gas = sum([gencost[i] + startcost[i] + fixedcost[i] for i in range(2,6)])
      \#diesel = sum([gencost[i] + startcost[i] + fixedcost[i] for i in range(6,10)])
      cost=[coal,gas,diesel]
      # Data to plot
      labels = 'Generation costs', 'Start up costs', 'Shut down cost'
      cost=[Tgencost,Tstartcost,Tshutcost]
      colors = ['green', 'violet', 'maroon']
      explode = ( 0,0 , 0) # explode 1st slice
      # Plot
      plt.pie(cost, explode=explode, labels=labels, colors=colors,
              autopct='%1.1f%%', shadow=True, startangle=140)
      plt.title('Propotion of each cost type', bbox={'facecolor':'0.9', 'pad':5})
      plt.axis('equal')
      plt.show()
```

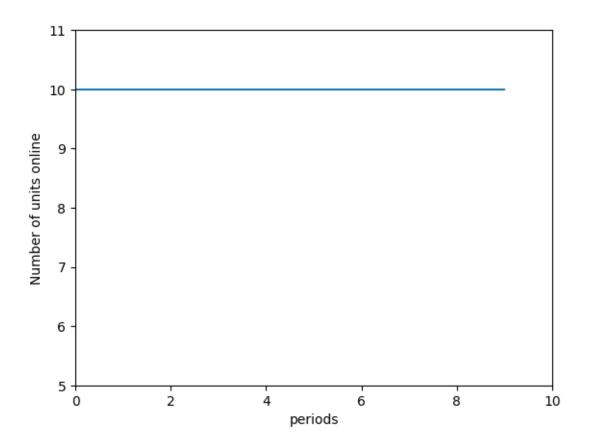
show(cost)

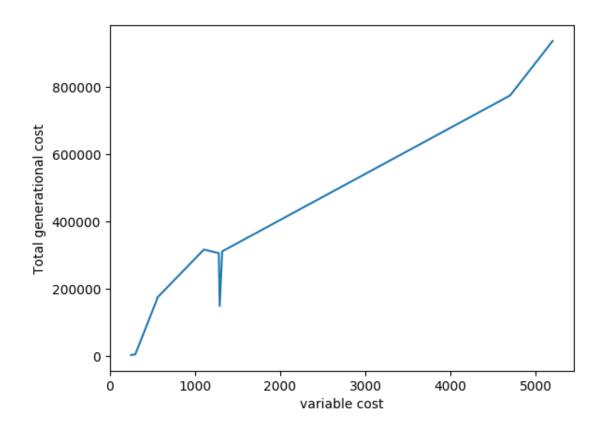


### [3.13928781900000e6, 5710.0000000000, 51132.0000000000]

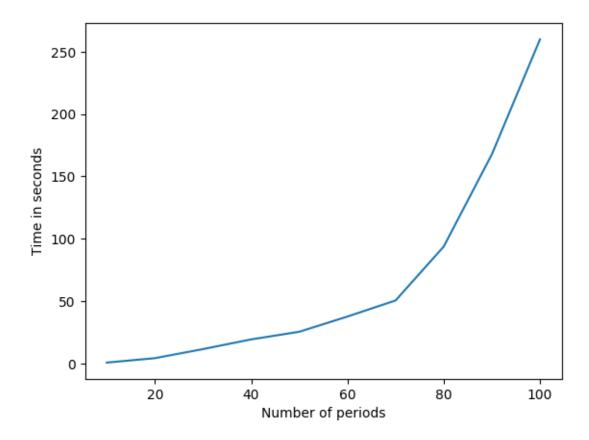
```
[75]: N_online=[sum([Val3[10*i+j] for i in range(10)]) for j in range(10)] show(N_online) import matplotlib.pyplot as plt plt.plot(N_online) plt.ylabel('Number of units online') plt.xlabel('periods') plt.axis([0,10, 5,11]) plt.show()
```

[10.0, 10.0, 10.0, 10.0, 10.0, 10.0, 10.0, 10.0, 10.0, 10.0]





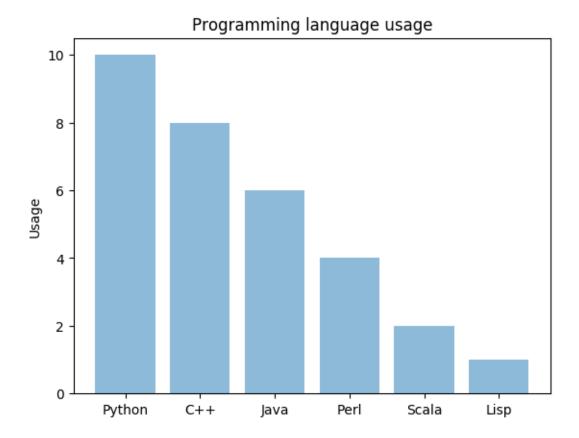
```
[77]: import matplotlib.pyplot as plt
n_periods=[10,20,30,40,50,60,70,80,90,100]
Time =[0.97,4.49,11.77,19.53,25.65,37.83,50.71,93.88,167.73,259.83]
plt.plot(n_periods,Time)
plt.ylabel('Time in seconds')
plt.xlabel('Number of periods')
plt.show()
```



```
[78]: import matplotlib.pyplot as plt; plt.rcdefaults()
   import numpy as np
   import matplotlib.pyplot as plt

objects = ('Python', 'C++', 'Java', 'Perl', 'Scala', 'Lisp')
   y_pos = np.arange(len(objects))
   performance = [10,8,6,4,2,1]

plt.bar(y_pos, performance, align='center', alpha=0.5)
   plt.xticks(y_pos, objects)
   plt.ylabel('Usage')
   plt.title('Programming language usage')
   plt.show()
```



```
[79]: gencostt=[sum([UNITCOMIT[n][10]*Var[T*n+t] for n in range(N)]) for t in

→range(T)]

startcostt=[sum([UNITCOMIT[n][9]*indic_su[T*n+t] for n in range(N)]) for t in

→range(T)]

shutcostt=[sum([UNITCOMIT[n][0]*indic_sd[T*n+t] for n in range(N)]) for t in

→range(T)]
```

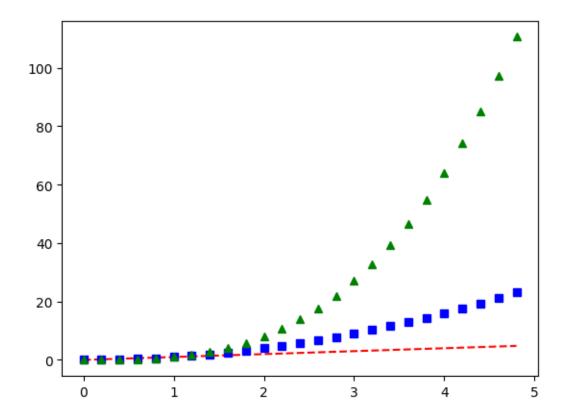
### 0.2 LAGRANGIAN RELAXATION

```
[80]: N=10
    T=10
    K=N*T
    R = PolynomialRing(RR, 'mu', K)
    S = PolynomialRing(RR, 'beta', K)
    mu = R.gens()
    beta=S.gens()
    #tim = S.gens()
    mu=[SR(mu[t]) for t in srange(0,T)];
    beta=[SR(beta[t]) for t in srange(0,T)]
```

```
R = PolynomialRing(RR, 'mu', T)
      S = PolynomialRing(RR, 'beta', T)
      mu = R.gens()
      beta=S.gens()
      mu=[SR(mu[t]) for t in srange(0,T)];
      beta=[SR(beta[t]) for t in srange(0,T) ]
      print(beta)
      H = PolynomialRing(RR, 'indic_su', K)
      S = PolynomialRing(RR, 'indic_on_off', K)
      T = PolynomialRing(RR, 'indic_sd', K)
      R = PolynomialRing(RR, 'Gen', K)
      Gen = R.gens()
      tim = S.gens()
      Gen=[SR(Gen[k]) for k in srange(0,K)];
      indic_su= H.gens()
      indic_on_off=S.gens()
      indic_sd= T.gens()
      tim = S.gens()
      indic_su=[SR(indic_su[k]) for k in srange(K)];
      indic_on_off=[SR(indic_on_off[k]) for k in srange(K)];
      indic_sd=[SR(indic_sd[k]) for k in srange(K)]
     [beta0, beta1, beta2, beta3, beta4, beta5, beta6, beta7, beta8, beta9]
「81]: N=10
      T=10
      gencost=sum([UNITCOMIT[n][10]*Gen[T*n+t] for n in range(N) for t in range(T)])
      startcost=[sum([UNITCOMIT[n][9]*indic_su[T*n+t] for n in range(N) for t in_
       \rightarrowrange(T)])]
      shutcost=[sum([UNITCOMIT[n][0]*indic_sd[T*n+t] for n in range(N) for t in_
       \rightarrowrange(T)])]
      z=gencost
[82]: M=[derivative(z,Gen[k]) for k in range(K)]
[83]: R = PolynomialRing(GF(2), 'indic_su', K)
      S = PolynomialRing(GF(2), 'indic_on_off', K)
      T = PolynomialRing(GF(2), 'indic_sd', K)
      indic su= R.gens()
      indic_on_off=S.gens()
      indic_sd= T.gens()
      #tim = S.qens()
      indic_su=[SR(indic_su[k]) for k in srange(0,K)];
      R = PolynomialRing(RR, 'indic_su', K)
      indic_su = R.gens()
      indic_su=[SR(indic_su[k]) for k in srange(0,K) ];
```

print(indic\_su)

```
[indic su0, indic su1, indic su2, indic su3, indic su4, indic su5, indic su6,
     indic_su7, indic_su8, indic_su9, indic_su10, indic_su11, indic_su12, indic_su13,
     indic_su14, indic_su15, indic_su16, indic_su17, indic_su18, indic_su19,
     indic_su20, indic_su21, indic_su22, indic_su23, indic_su24, indic_su25,
     indic su26, indic su27, indic su28, indic su29, indic su30, indic su31,
     indic_su32, indic_su33, indic_su34, indic_su35, indic_su36, indic_su37,
     indic su38, indic su39, indic su40, indic su41, indic su42, indic su43,
     indic_su44, indic_su45, indic_su46, indic_su47, indic_su48, indic_su49,
     indic su50, indic su51, indic su52, indic su53, indic su54, indic su55,
     indic_su56, indic_su57, indic_su58, indic_su59, indic_su60, indic_su61,
     indic_su62, indic_su63, indic_su64, indic_su65, indic_su66, indic_su67,
     indic_su68, indic_su69, indic_su70, indic_su71, indic_su72, indic_su73,
     indic_su74, indic_su75, indic_su76, indic_su77, indic_su78, indic_su79,
     indic_su80, indic_su81, indic_su82, indic_su83, indic_su84, indic_su85,
     indic_su86, indic_su87, indic_su88, indic_su89, indic_su90, indic_su91,
     indic_su92, indic_su93, indic_su94, indic_su95, indic_su96, indic_su97,
     indic_su98, indic_su99]
[84]: import numpy as np
      import matplotlib.pyplot as plt
      # evenly sampled time at 200ms intervals
      t = np.arange(0., 5., 0.2)
      # red dashes, blue squares and green triangles
      plt.plot(t, t, 'r--', t, t**2, 'bs', t, t**3, 'g^')
      plt.show()
```



```
[85]: import numpy as np
      import matplotlib.pyplot as plt
      D=[[Val1[T*n+t]for t in range(T)] for n in range(N)]
      N = 24
      menMeans = (20, 35, 30, 35, 27)
      womenMeans = (25, 32, 34, 20, 25)
      menStd = (2, 3, 4, 1, 2)
      womenStd = (3, 5, 2, 3, 3)
      ind = np.arange(N) # the x locations for the groups
      width = 0.5
                      # the width of the bars: can also be len(x) sequence
      p1 = plt.bar(ind, tuple(D[0]), width)
     p2 = plt.bar(ind, tuple(D[1]), width)#, yerr=menStd)
      p3 = plt.bar(ind, tuple(D[2]), width)
     p4 = plt.bar(ind, tuple(D[3]), width)
      p5 = plt.bar(ind, tuple(D[4]), width)#, yerr=menStd)
     p6 = plt.bar(ind, tuple(D[5]), width)
     p7 = plt.bar(ind, tuple(D[6]), width)
     p8 = plt.bar(ind, tuple(D[7]), width)#, yerr=menStd)
      p9 = plt.bar(ind, tuple(D[8]), width)
      p10 = plt.bar(ind,tuple(D[9]), width)#, yerr=womenStd)
```

```
[]: # libraries
     import numpy as np
     import matplotlib.pyplot as plt
     from matplotlib import rc
     #import pandas as pd
     # y-axis in bold
     rc('font', weight='bold')
     # Values of each group
     bars1 = D[0]
     bars2 = D[1]
     bars3 = D[2]
     bars4 = D[3]
     bars5 = D[4]
     bars6 = D[5]
     bars7 = D[6]
     bars8 = D[7]
     bars9 = D[8]
     bars10= D[9]
     # Heights of bars1 + bars2 (TO DO better)
     #sition of the bars on the x-axis
```

```
r = [i for i in range(24)]
# Names of group and bar width
names =
¬¬['','','','','','5','','','','','10','','','','','15','','','','','','','','','']
barWidth = 0.5
# Create brown bars
p1=plt.bar(r, bars1,bottom=bars, color='Maroon', edgecolor='white',
→width=barWidth)
# Create green bars (middle), on top of the firs ones
p2=plt.bar(r, bars2, bottom=bars1, color='blue', edgecolor='white',
→width=barWidth)
# Create green bars (top)
p3=plt.bar(r, bars3, bottom=bars2, color='orange', edgecolor='white',
→width=barWidth)
p4=plt.bar(r, bars4,bottom=bars3, color='red', edgecolor='white',u
→width=barWidth)
# Create green bars (middle), on top of the firs ones
p5=plt.bar(r, bars5, bottom=bars4, color='green', edgecolor='white',
→width=barWidth)
# Create green bars (top)
p6=plt.bar(r, bars6, bottom=bars5, color='lightblue', edgecolor='white',
→width=barWidth)
p7=plt.bar(r, bars7,bottom=bars6, color='violet', edgecolor='white',
→width=barWidth)
# Create green bars (middle), on top of the firs ones
p8=plt.bar(r, bars8, bottom=bars7, color='purple', edgecolor='white',
→width=barWidth)
# Create green bars (top)
p9=plt.bar(r, bars9, bottom=bars8, color='lightgreen', edgecolor='white',
→width=barWidth)
p10=plt.bar(r, bars10, color='tomato', edgecolor='white', width=barWidth)
plt.legend((p1, p2,p3, p4,p5, p6,p7, p8, p9, p10),('coal1', 'coal2', 'gas1', u
→ 'gas2', 'gas3', 'gas4', 'diesel1', 'diesel2', 'diesel3', 'diesel4'))
# Custom X axis
plt.xticks(r, names, fontweight='bold')
plt.xlabel("Time")
plt.ylabel('Power Output and Demand (MW)')
plt.title('1 day Unit Commitment Problem')
# Show graphic
plt.show()
```

```
[]: \#P=[sum([Val1[J*i+j] for j in range(J)]) for i in range(I)]
    N_online=[sum([Val3[T*n+t] for n in range(10)]) for t in range(24)]
    P=N_online
    import matplotlib.pyplot as plt; plt.rcdefaults()
    import numpy as np
    import matplotlib.pyplot as plt
    objects = ('1', '', '', '', '5', '','', '', '', '10','', '', '', '', '15', "
     \hookrightarrow '', '', '', '', '20', '', '', '')
    y_pos = np.arange(len(objects))
    performance = P
    plt.bar(y_pos, performance, align='center', alpha=0.8, width=0.5, u
     plt.xticks(y_pos, objects)
    plt.ylabel(' Number of units online')
    plt.xlabel('periods')
    plt.title('')
    plt.show()
[]: A=matrix([[1,2],[3,4]])
[]: A=[i for i in range(101)]
    B=[j for j in range(101,202)]
    C=[A[i]*B[i] for i in range(101)]
    show(sum(C)/102)
[]: 10002*1990000
[]: A=[i for i in range(101)]
[]:
```