Population forecasting

with Bayesian hierarchical models

https://github.com/violetacIn/SIPP

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Content

Production of population projections: problems and solutions

• Difficulties and new demands

• New methods and implementation in



Future plans

Problem and solution

for migration, fertility, mortality (by age, time & Z*- characteristics) which give, via ccpm & stochastically: the population predictions

Problem

- estimating and predicting in the presence of:
- small area/population issues and/or rare events/ shocks
- expert assumptions
- uncertainty of parameters and errors in data (e.g. *deregistration*)
- while reporting uncertainty of estimates/predictions

Solution must be based on:

Modeling and combining (prior) information

Types of models

Recent years: functional models, ARDL & bsts models f(age, time)

- smoothing and orthogonal expansions for Fertility and Mortality components
- econometric / decay models for short / intermediate term
- time series / assumptions for long term

New: hierarchical and/or Bayesian models of response(s)

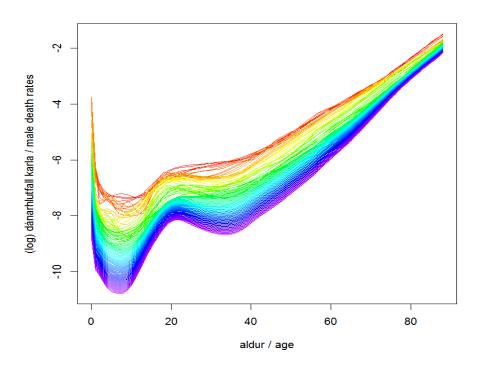
- smoothing/processes (t, space, age,...)
- complex correlation structures, spatial, demographic, social, ... characteristics
- incorporate quantitative & qualitative info: *priors*

^{**} Model averaging options

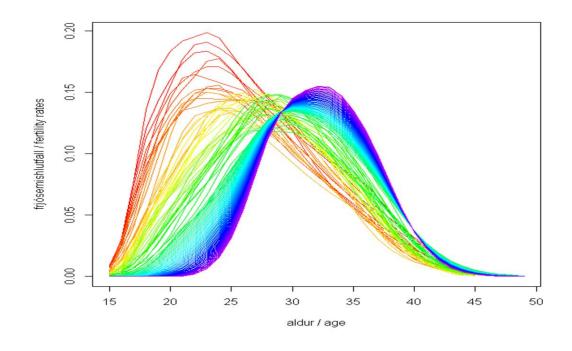
Typical result of functional models

https://cran.r-project.org/web/packages/demography/index.html

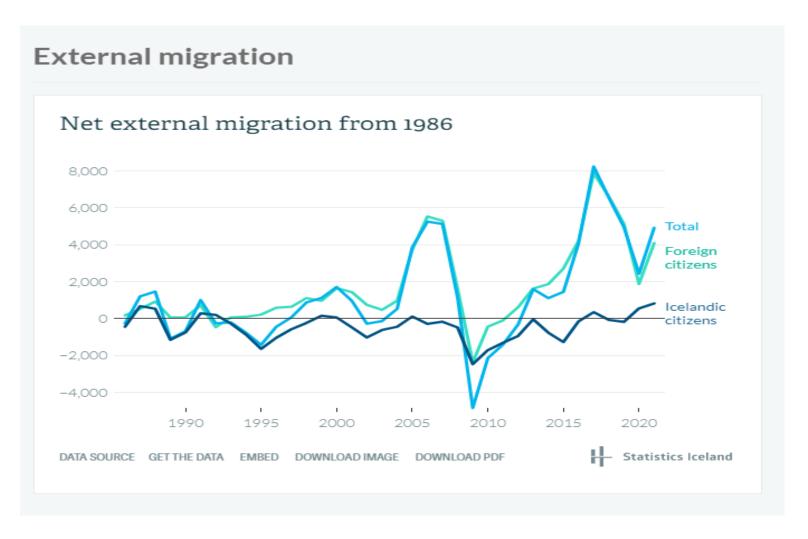
Mortality rates



Fertility rates



Migration issues and options for modeling



Predicting future values of migration/fertility/mortality:

- projections versus forecast
- advantages of Bayesian approach

Past

Disjoint, long and short term migration predictions

 Unique models for predicting mortality and fertility, but only as functions of time, age (and gender)

New

& allowing for local predictions

- Exceptions: shocks (economical, political, natural, ...)

New Models (parametric or not!) & implementation in



$P(Y|a) = F_1(x)$ where $P(a|b) = F_2(c, Z)$ where...

- Type: Hierarchical / Multilevel, Bayesian / frequentist
 - data used: *individual or aggregated* response (γ) versions
 - what: processes, since time series data $\mathbb{P}(\gamma i, ... \gamma n | a)$, versus $\mathbb{P}(\gamma i)$: account for (auto-) correlations
- Why:
- {components/prior information/characteristics/local&total} & uncertainty report
- **R**-Tools:

several Stan-running R packages like brms, arm, bayestestR, ...

and the faster: Ime4, mgcv, ... for frequentist / as initializations / not only (see Laplace approx of mgcv)

Structure, novelty and advantages

x = (year, age, gender, citizenship, municipality, education, ...)

- V1. Counts/rates
- $N(x,...) \sim Poisson(e^{f(x,...)}N_0(x,...))$ (or: neg. binom, over-disperssion issues, etc)
- $f_m(\{x, ...\}) \sim GP(m(\{x, ...\}), C(\{x, ...\}, \{x', ...\})) + ...$
- V2. Microdata
- $N(x,...) \sim B(e^{f(x,...)}N_0(x,...))$
- $f_m(\{x, ...\}) \sim GP(m(\{x, ...\}), C(\{x, ...\}, \{x', ...\})) + ...$
- f_m denotes here: sums of smooths/re/t2 and/or by {grouping factors} OR unknown functions with Gaussian Processes as priors (with m -> long term behaviour, C -> correl between any two response values)

Tests, Correlations, Dimensions

- Variability
- of:

fertility, mortality, migration

- through (and with auto-correl):

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Time & age (s(t), gp(t, age, ...), t2(t, age), ...)
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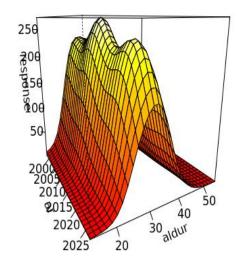
- by:
 - Municipality, Region significant for: migration but not/less for mortality, fertility
 - Other characteristics: education, family related, municipality attributes, ...
 - More grouping characteristics (ut/is, im/e, f/m)

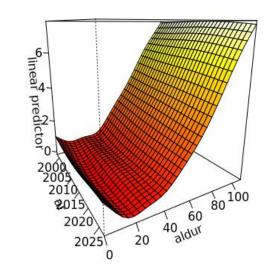
V1. Count data input

https://cran.r-project.org/web/packages/mgcv/index.html

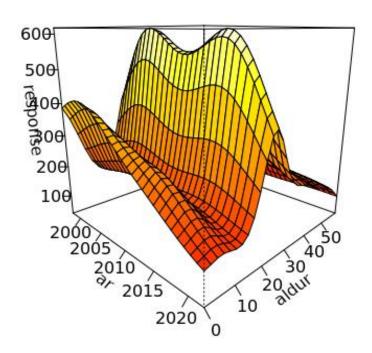
Births

Death rates (log)



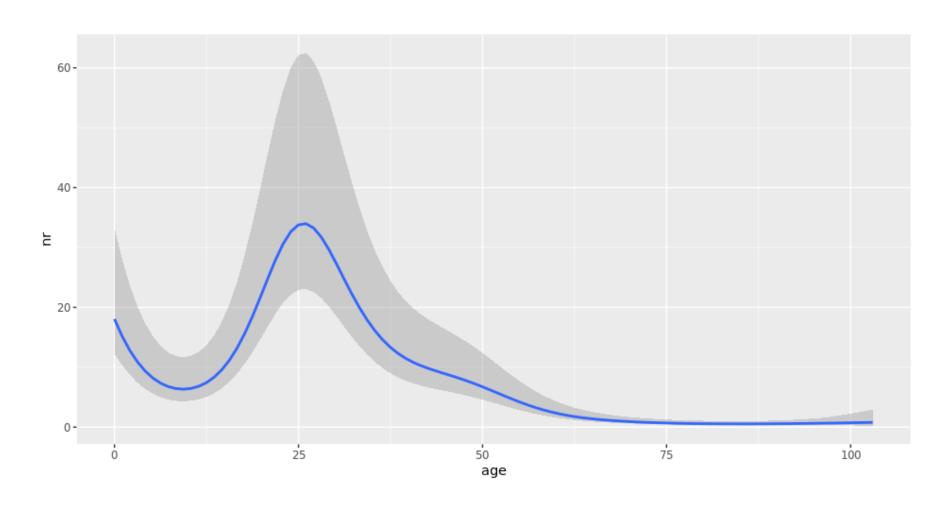


Migration

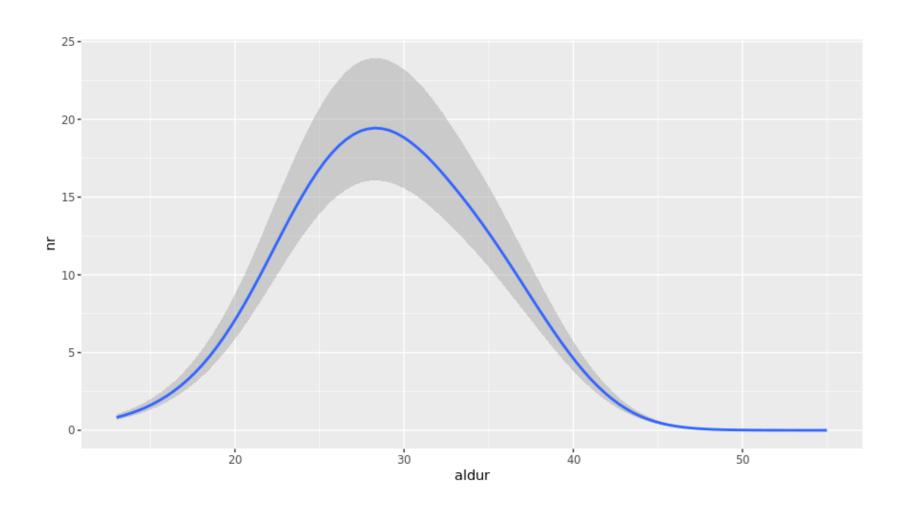


Counts/rates models: all migration categories (f_em_ut)

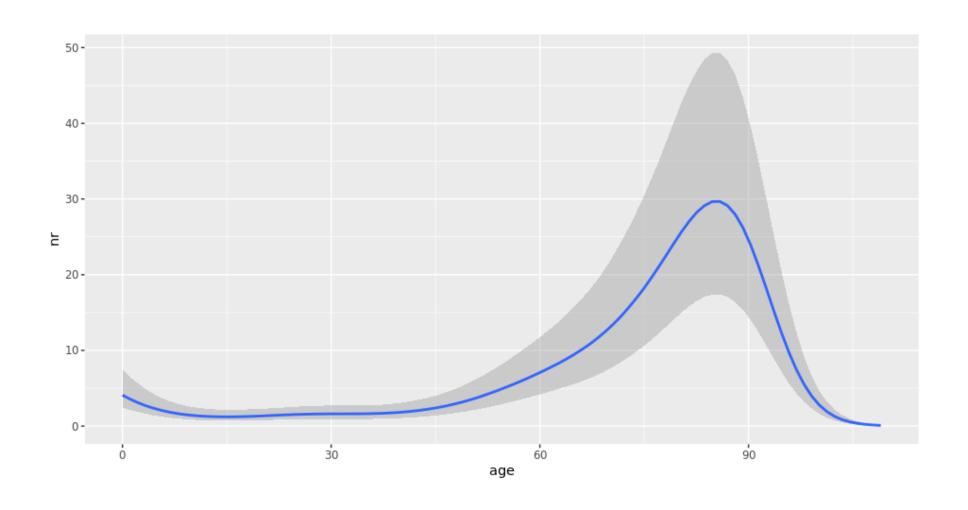
https://cran.r-project.org/web/packages/brms/index.html



Counts/rates: fertility models



Counts/rates: mortality models (addit, s)

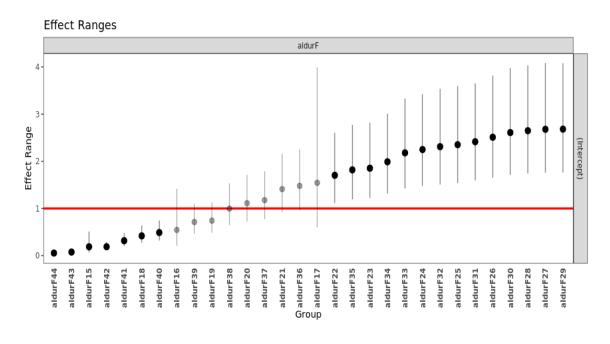


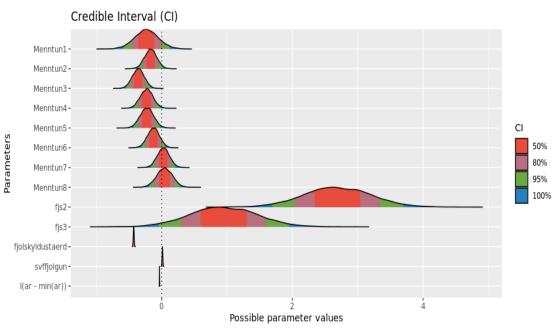
V2. Microdata input

Example 1. Significance of effects for:

Age group effect on fertility (o.r. units)

Characteristics' effects on fertility

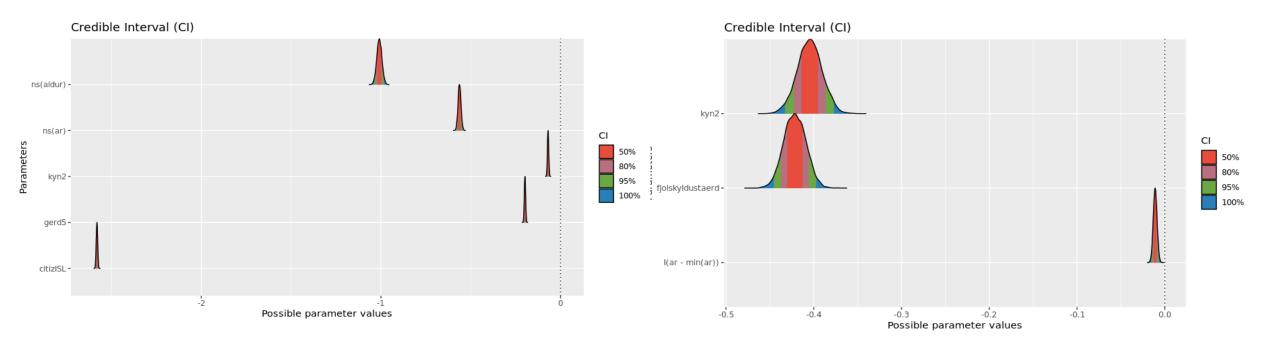




Microdata input

Example 2. Characteristics' effects on:

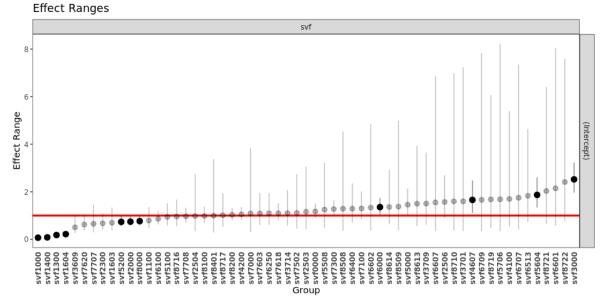


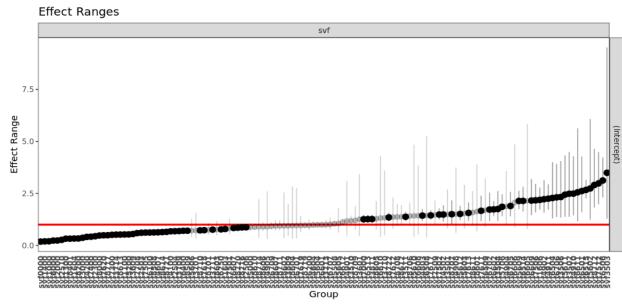


One more example: testing for location effects (although not with **mrf** yet!)

municipality - effect on fertility

municipality – effect on migration





Future*/work in progress/

- finalise stochastic *population* predictions by combining high number of values sampled from the posterior distributions of the demographic components (migration, fertility, mortality) as in *ccpm*
- finalise the model testing
- forecasting with multiple model averaging*

References

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Thank you!