

Local population projections with Bayesian hierarchical models

<https://github.com/violetacln/SIPP>

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Why (local/total) population projections?

- One of the key products of Official Statistics ← huge demand, from:
 - National and local administration
 - Policy makers
 - Planning infrastructure: constructions, heating, water and electricity supply
 - Planning future developments in social sectors: health, pensions, education
 - Researchers in multiple domains
 - Individual users

For all demographic components (*migration, fertility, mortality*) as functions of: age, time and/or gender, citizenship, education, locality, ..., in order to be combined *stochastically, via ccpm, into: population projections (total and local)*

- ***Formulation of the statistical problem:***

- *estimating and predicting* in the presence of:
 - small area/population issues and/or rare events/ shocks
 - expert assumptions
 - uncertainty of model parameters
 - errors in input data (e.g. *deregistration*)
- while reporting *uncertainty* of estimates/predictions

- ***Solution must be based on:***

- Modeling and combining (prior) information

New Models and Implementation in

$P(\text{response} / \text{parameters}_0 \vee \text{fcts}) = F_1(\text{attributes}_0)$ where
 $P(\text{parameters}_0 \vee \text{fcts} / \text{parameters}_1) = F_2(\text{attributes}_1)$ where...

- **Type of models:** **Hierarchical / Multilevel**, Bayesian / frequentist
 - data used: *individual* or *aggregated* response (γ) versions
 - what to model: **processes**, since *time series* data $P(\gamma_1, \dots, \gamma_n | a)$ plus other grouping effects --> need to account for complex **(auto-) correlations**
- **Why:**
 - {components/prior information/characteristics/local&total} & **uncertainty** report
- **R-Tools:**

several *Stan*-running R packages like **brms**, arm, bayestestR, ...

and the faster: *lme4*, **mgcv**, ... for frequentist / as initializations / *not only* (see Laplace approx of mgcv)

Structure and novelty

$x=(\text{year, age, gender, citizenship, municipality, education, ...})$

Response = rates/events of local/total demographic components

I. Counts/rates

- $N(x, \dots) \sim \text{Poisson}(e^{f(x, \dots)}, N_0(x, \dots))$ (or: neg. binom, see over-disperssion issues, etc)
- $f = \sum f_m(x, \dots), f_m \sim \text{GP}(m(x, \dots), C(\{x, \dots\}, \{x', \dots\})) + \dots$

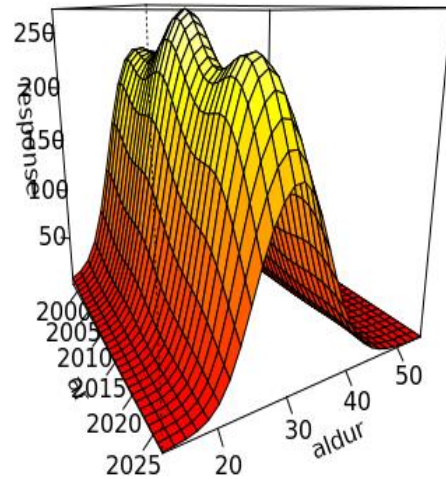
II. Microdata (events)

- $N(x, \dots) \sim B(L(f(x, \dots)), N_0(x, \dots))$
- $f = \sum f_m(x, \dots), f_m \sim \text{GP}(m(x, \dots), C(\{x, \dots\}, \{x', \dots\})) + \dots$
- f_m – [smooths/re/t2](#) and/or [by](#) {grouping factors} OR [unknown functions](#) with [Gaussian Processes](#) as [priors](#) (with $m \rightarrow$ long term behaviour, $C \rightarrow$ correl between any two response values)

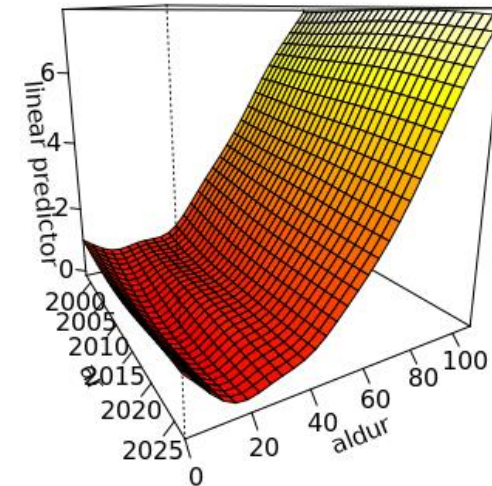
Count data input

<https://cran.r-project.org/web/packages/mgcv/index.html>

Births

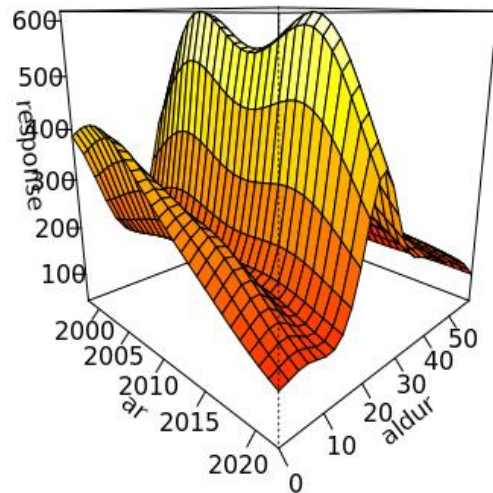


Death rates (log)

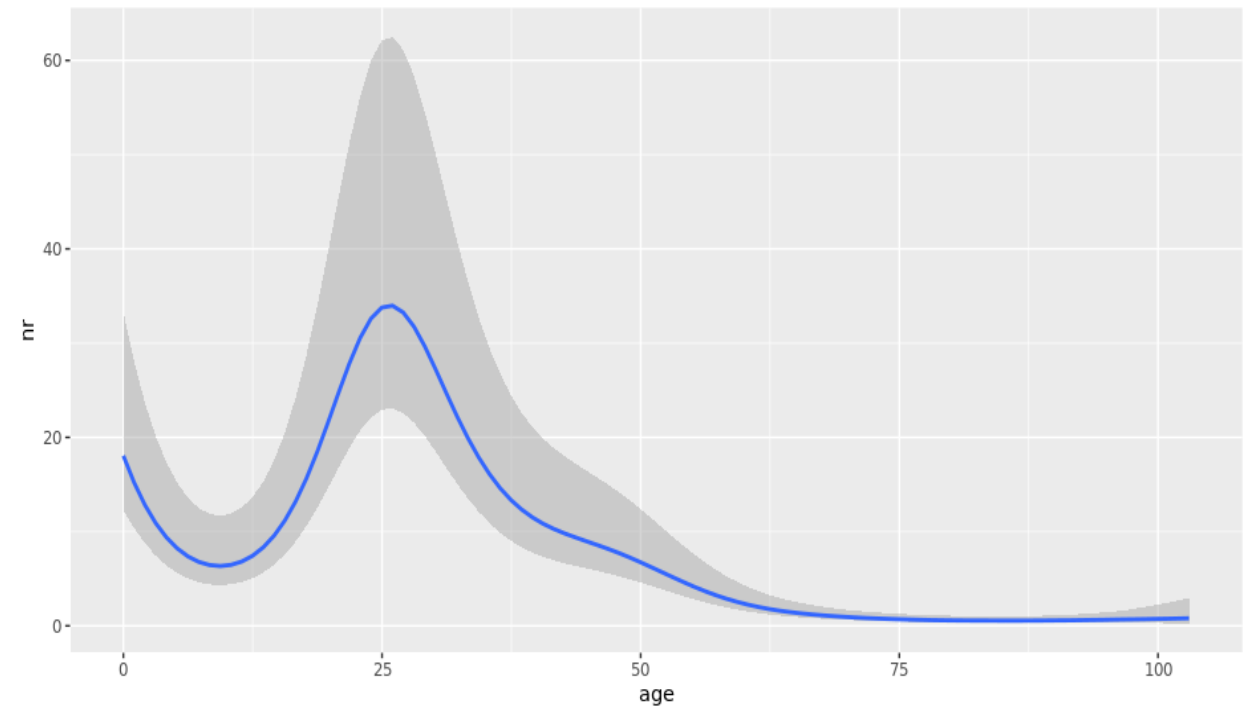


Count data input: migration

<https://cran.r-project.org/web/packages/mgcv/index.html>

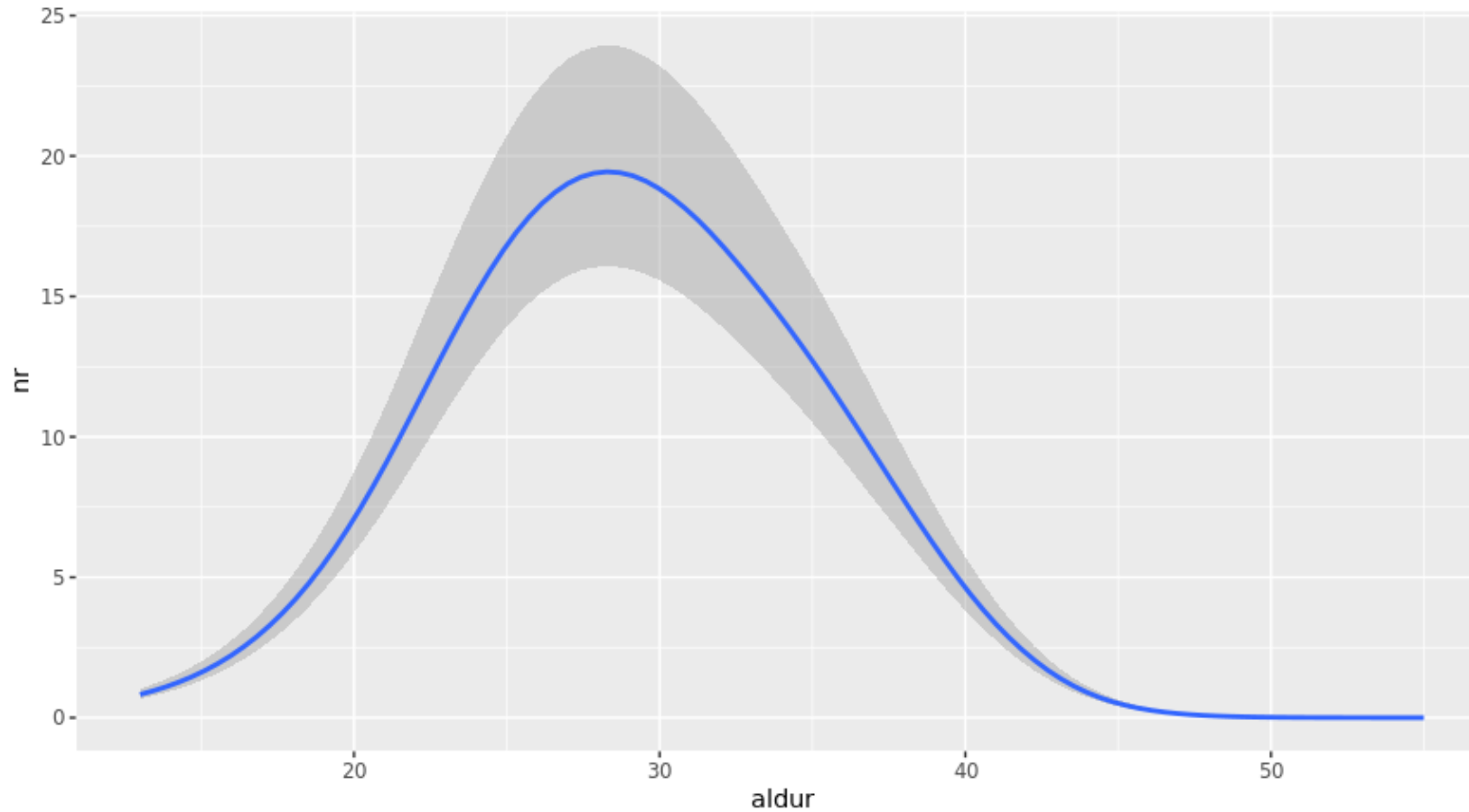


<https://cran.r-project.org/web/packages/brms/index.html>



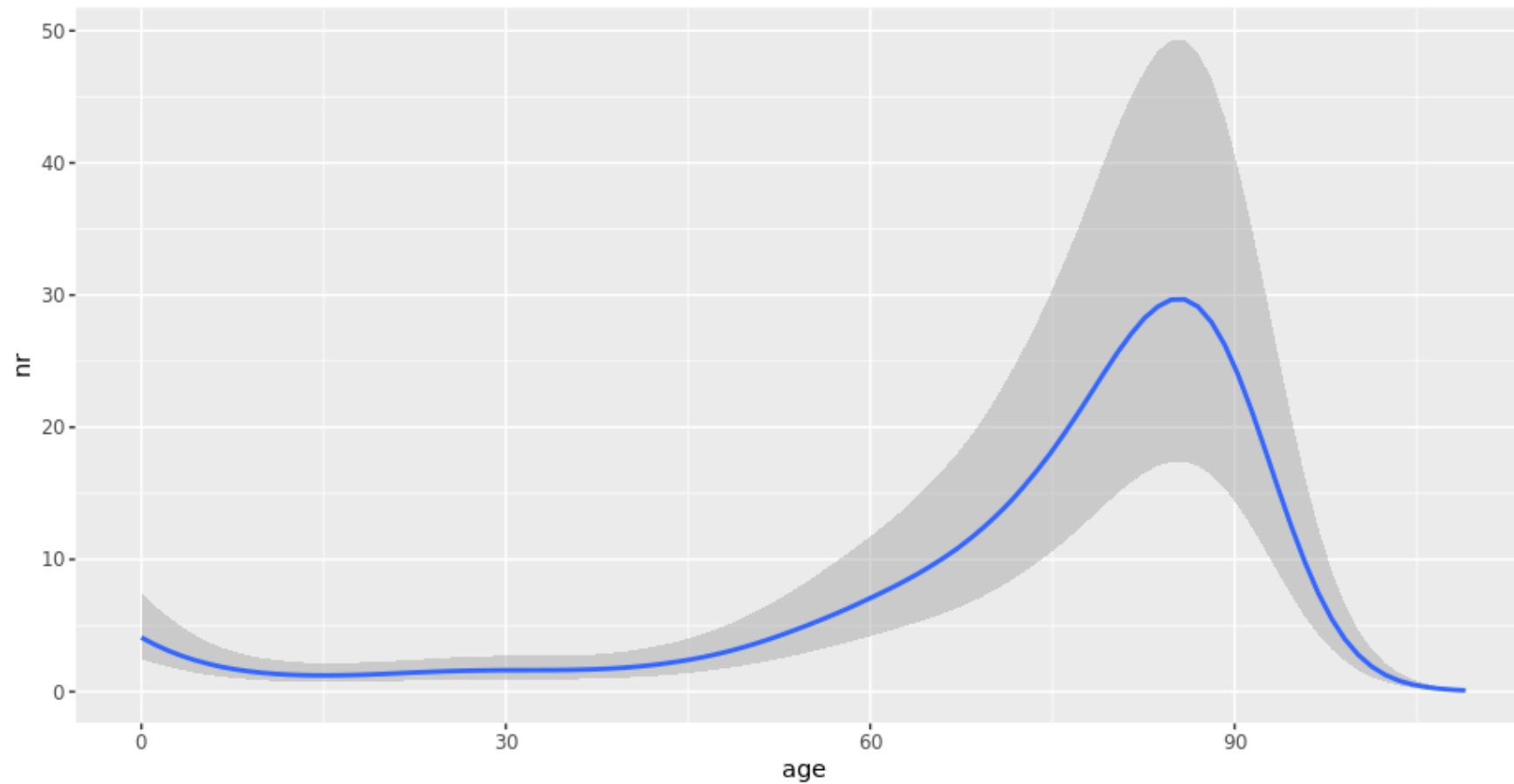
Counts/rates: fertility models

<https://cran.r-project.org/web/packages/brms/index.html>



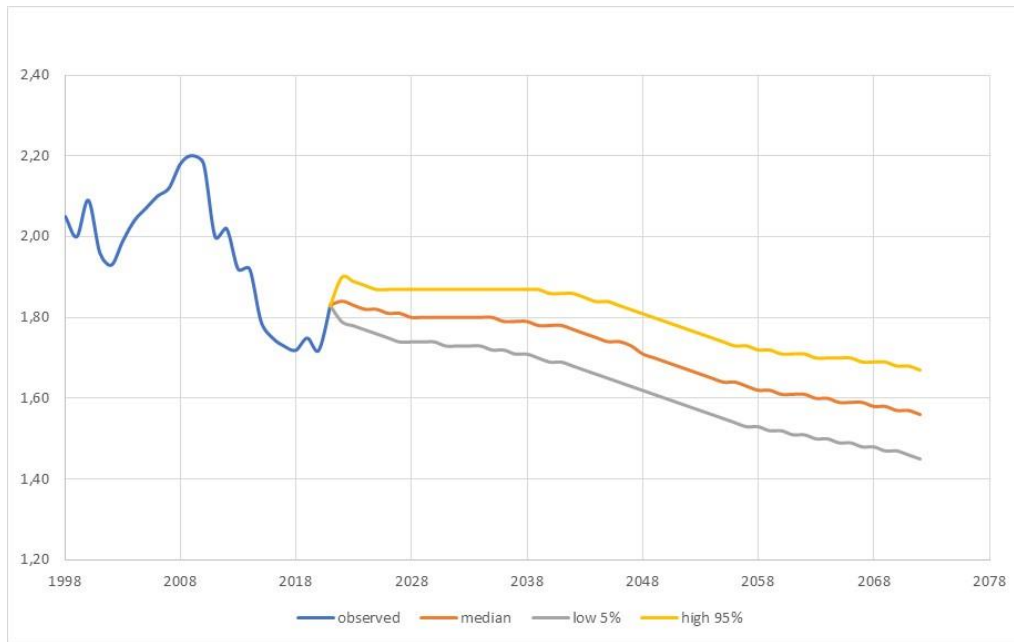
Counts/rates: mortality models (addit, s)

<https://cran.r-project.org/web/packages/brms/index.html>

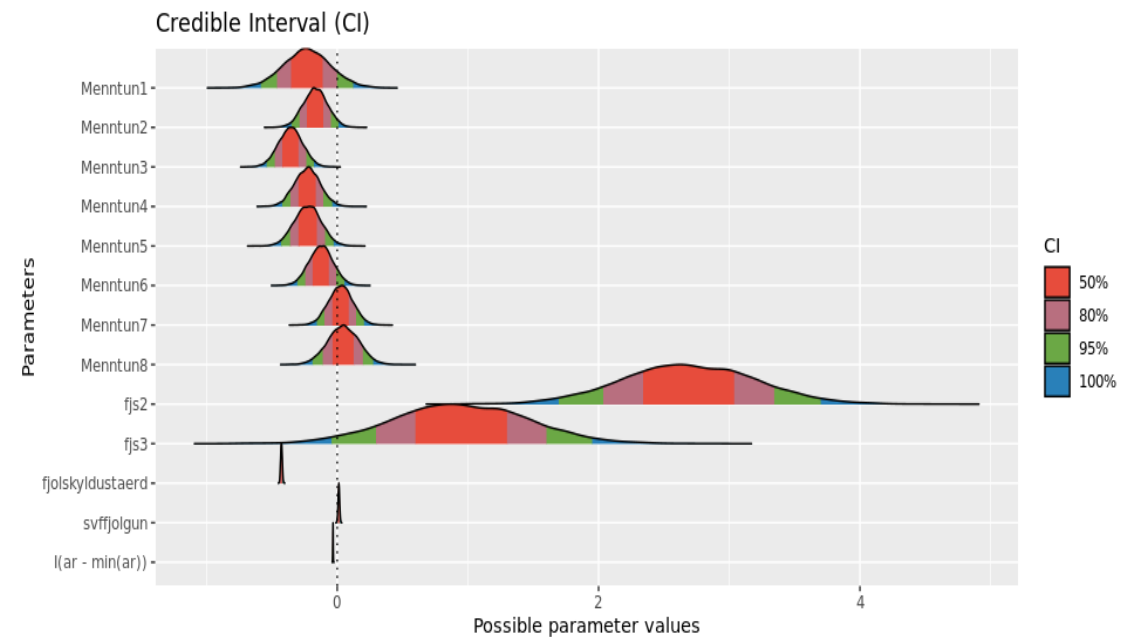


Examples: demographic *rates*' projections and significance of *attributes*' effects (using microdata)

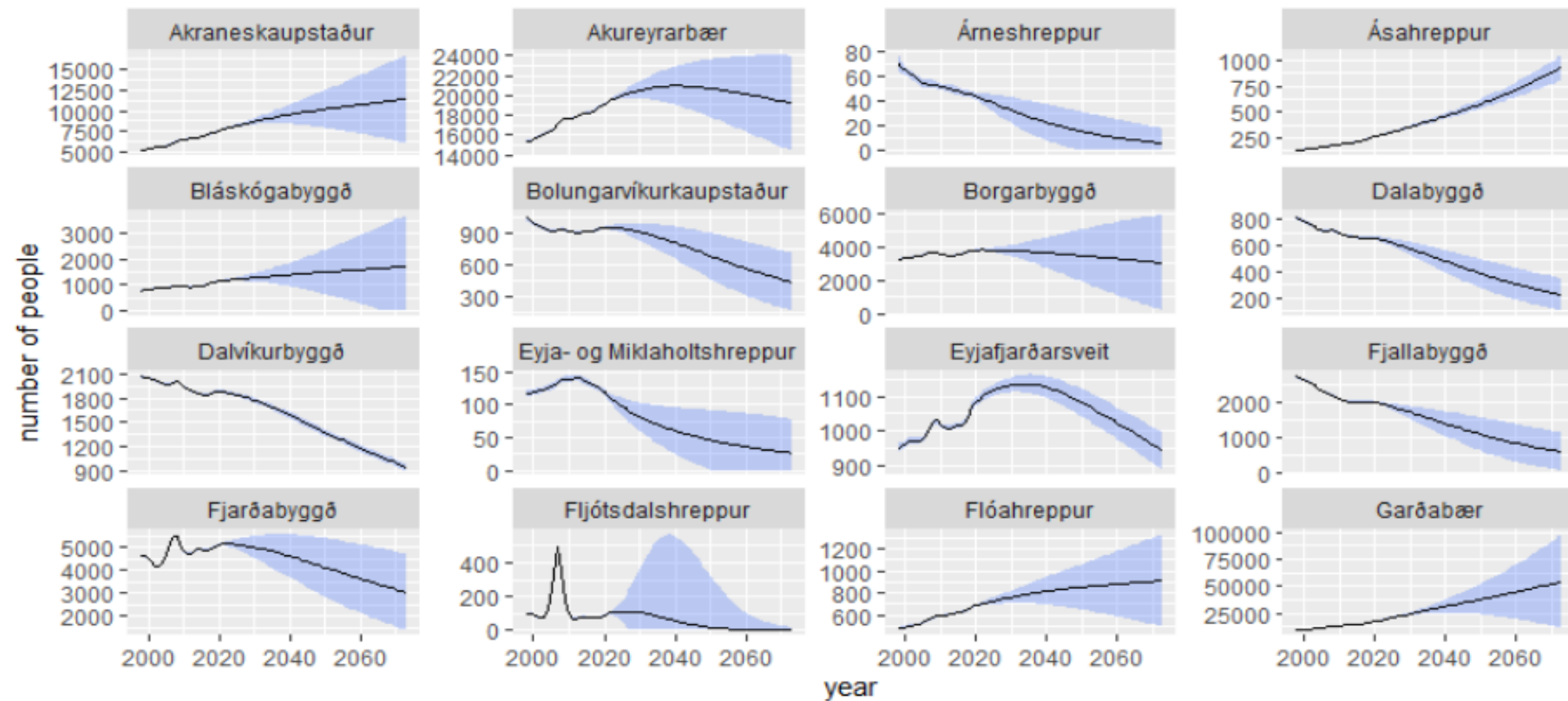
Total fertility rates: median and credible intervals



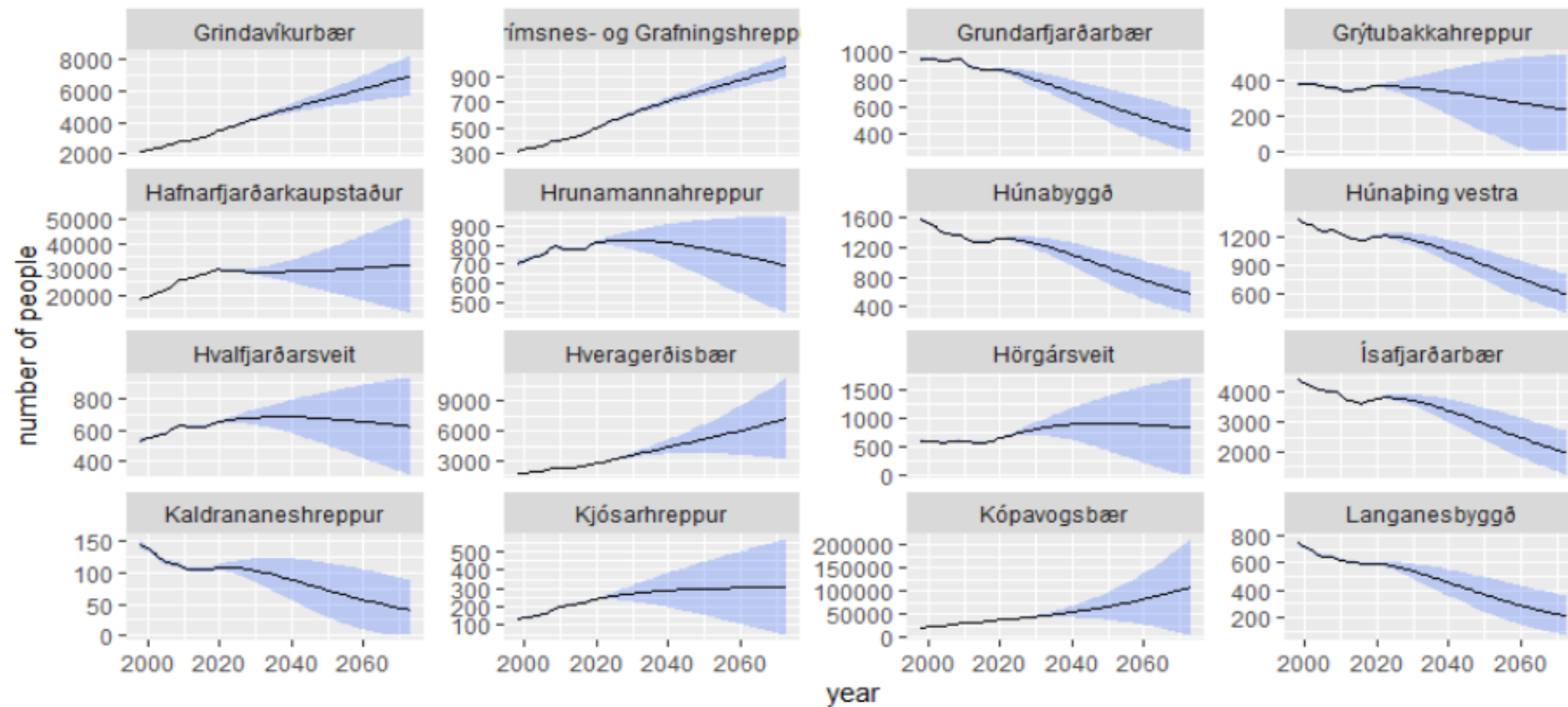
Effects of (individual, family, municipality) attributes on fertility (events)



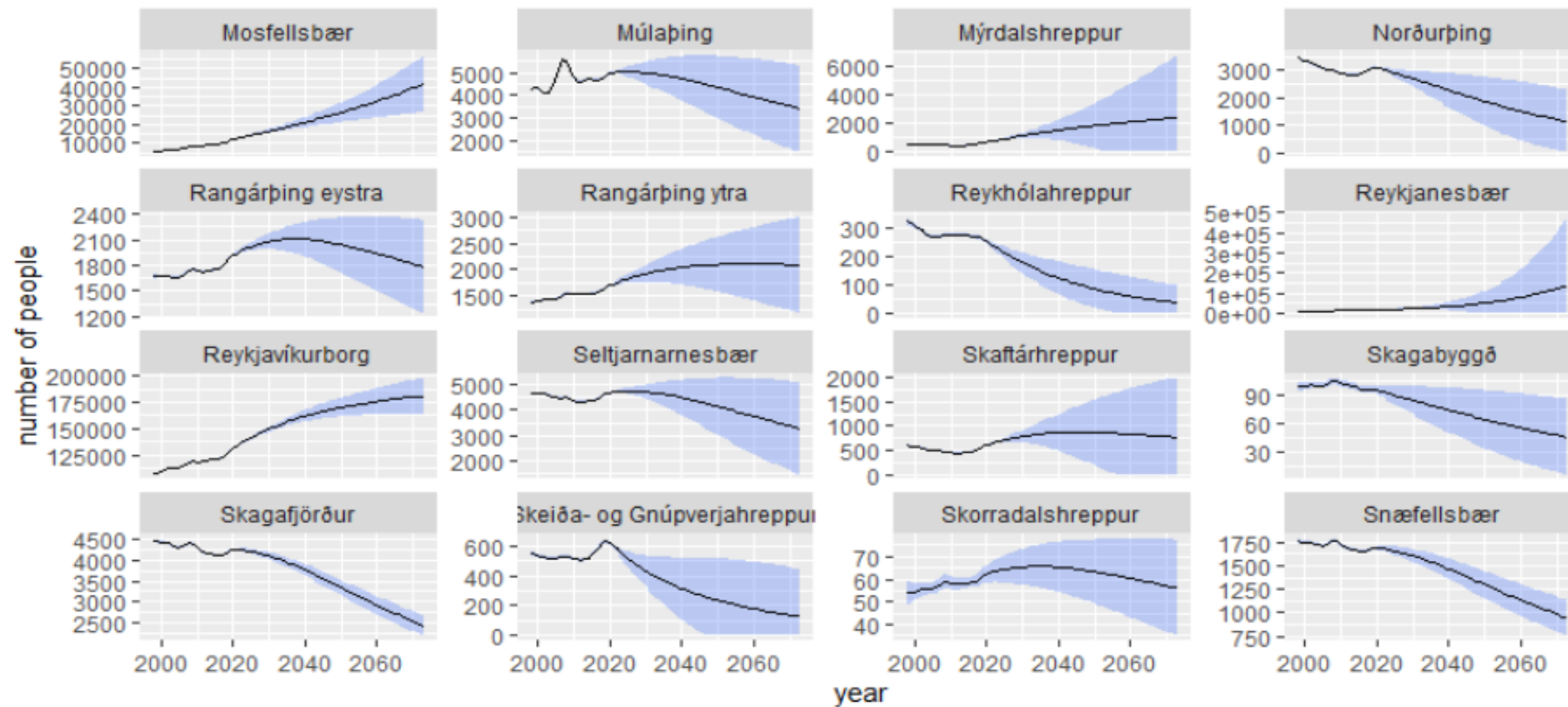
Local population projections



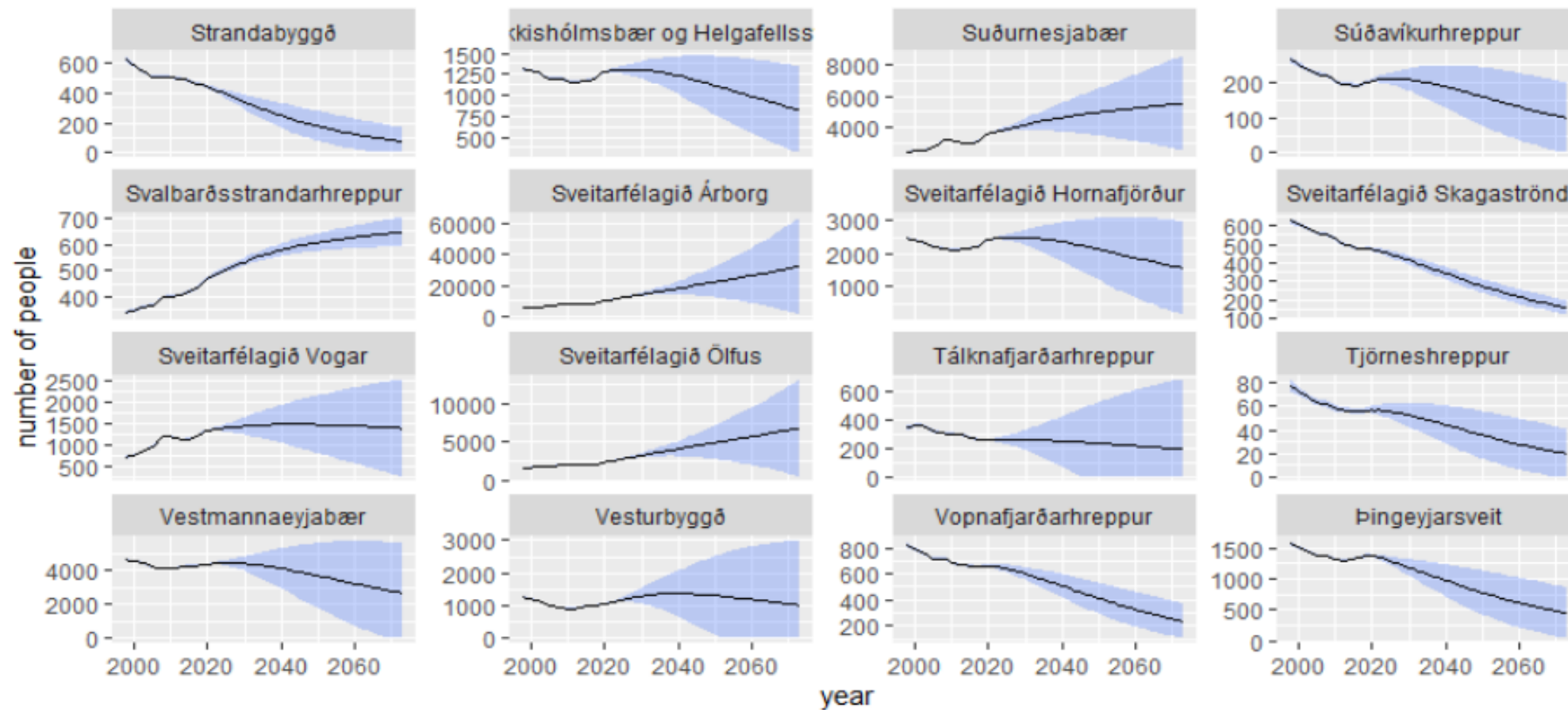
Local population projections



Local population projections



Local population projections



Future work and work in progress

- compare local population projections based on non- and informative *priors* (with users/experts' feedback)
- finalise the evaluation of the *model performance*
- forecasting with *multiple-model averaging*

References

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