



UNIT OF
EXCELLENCE
MARÍA
DE MAEZTU

Exploring ecological and social interactions through the lens of complex systems

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PhD defense
19th July 2023



INTERACTIONS

A large flock of small, dark birds, likely starlings, is shown flying in a massive, dense, swirling formation against a clear blue sky. The birds are concentrated in the upper half of the frame, creating a sense of organized chaos and collective movement.

EMERGENT BEHAVIOR

Objectives

Study emergent behavior in natural and information ecosystems

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Study emergent behavior in natural and information ecosystems

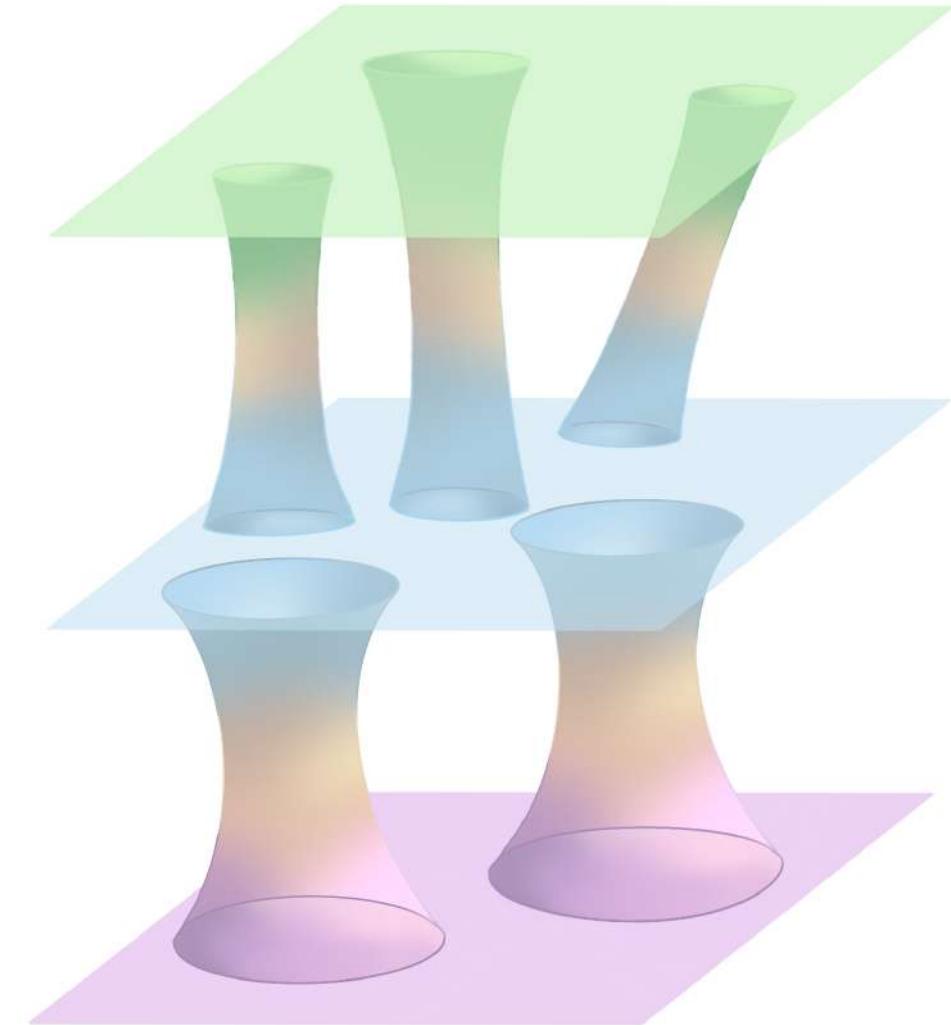
How different interactions affect the behavior of our systems

Objectives

Study emergent behavior in natural and information ecosystems

How different interactions affect the behavior of our systems

At different scales



Scales

(macro)

patterns

species

individuals

(micro)

Objectives



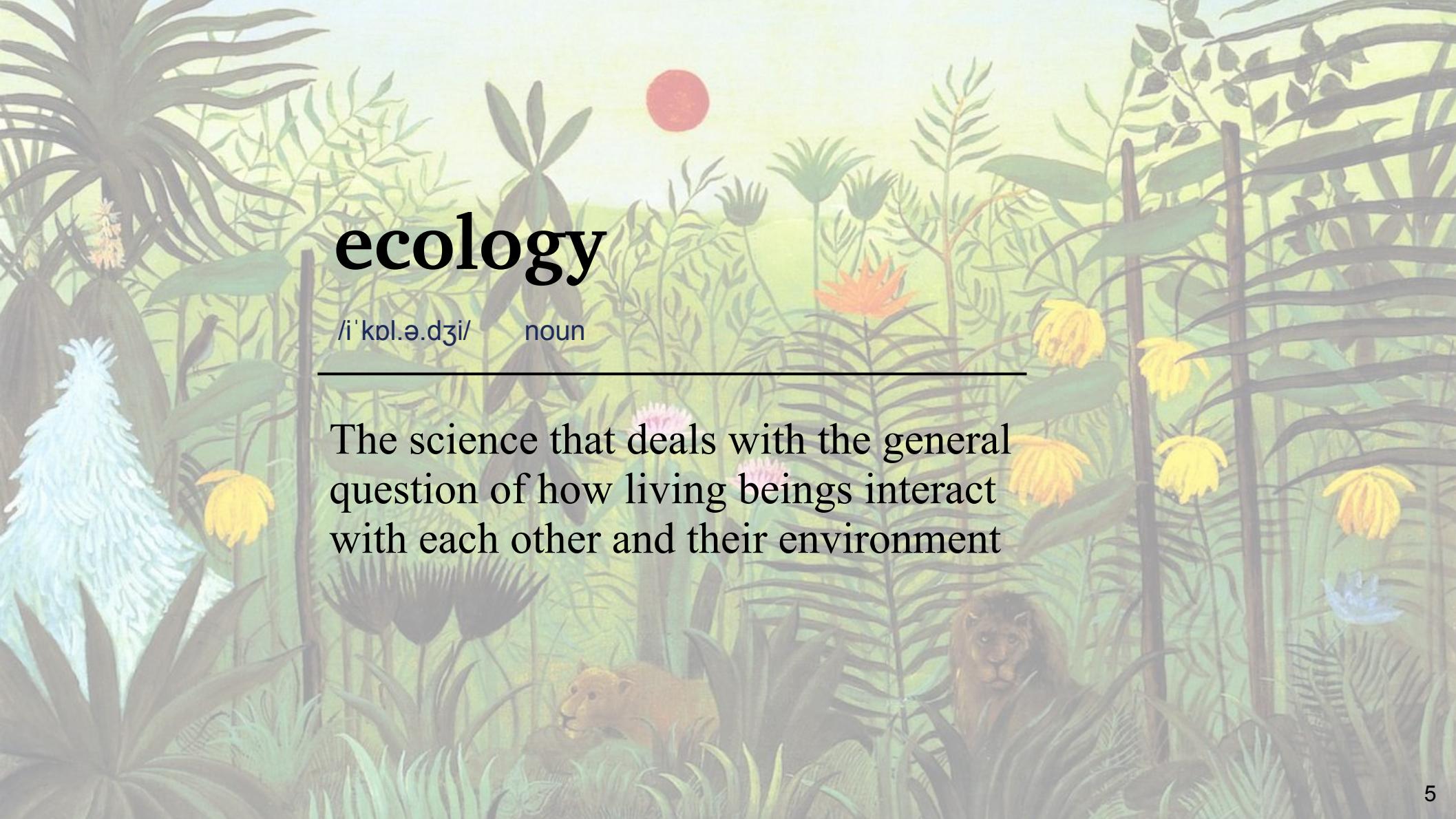
Study emergent behavior in **natural** and **information** ecosystems

How different interactions affect the behavior of our systems

At different scales

PART I

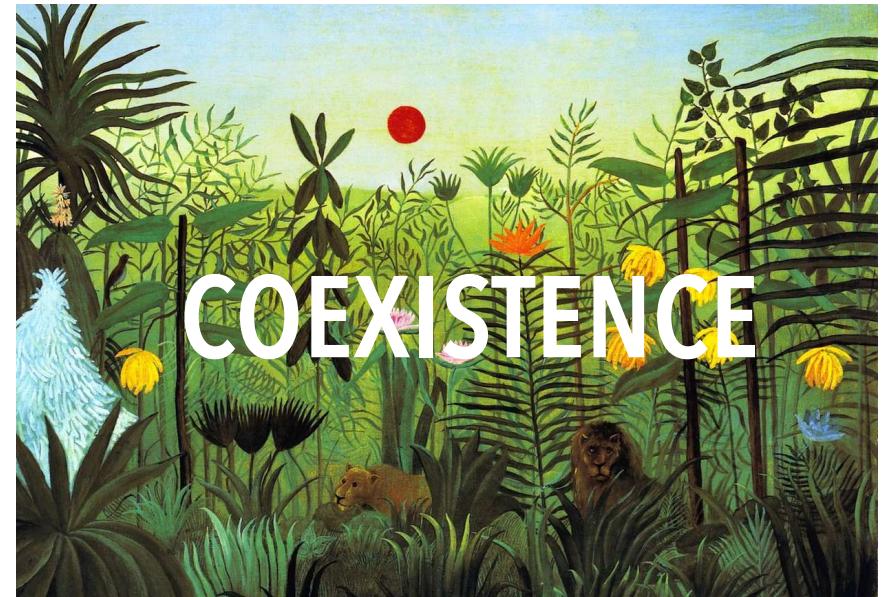
ECOLOGICAL SYSTEMS



ecology

/ɪ'kɒl.ə.dʒi/ noun

The science that deals with the general question of how living beings interact with each other and their environment



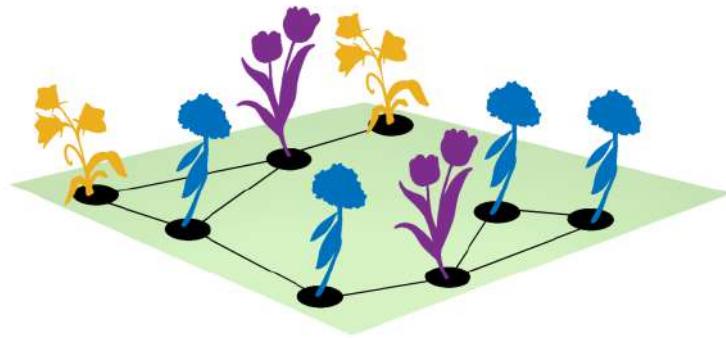
Why are there so many species living together?

Heterogeneous interactions



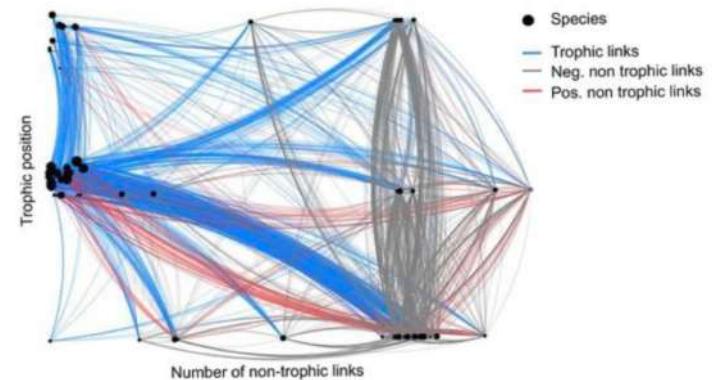
Interactions represented as **complex networks**

Space



Calleja-Solanas et al. PRE 2022

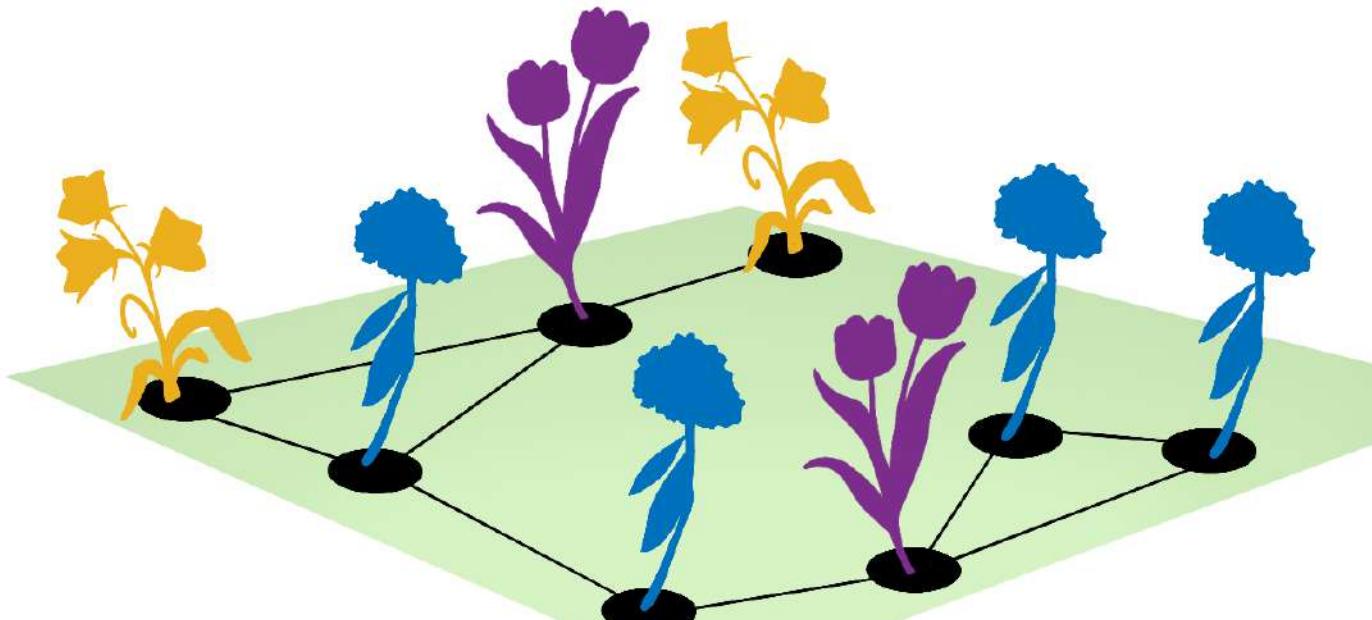
≠ types of interactions



Kefi et al. PLOS Bio 2016

Ch 3

Structured interactions & coexistence in competitive communities



Competition

Plankton paradox

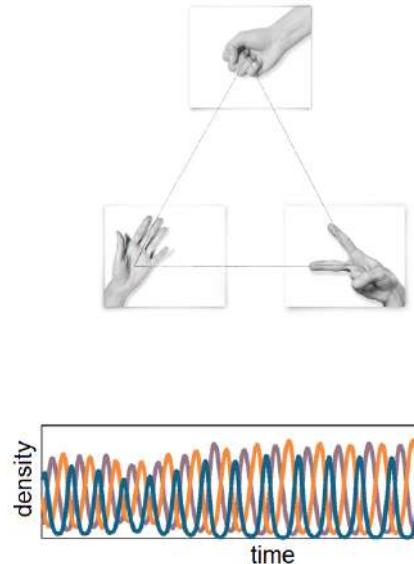


Competition

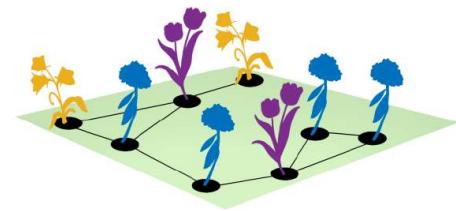
Plankton paradox



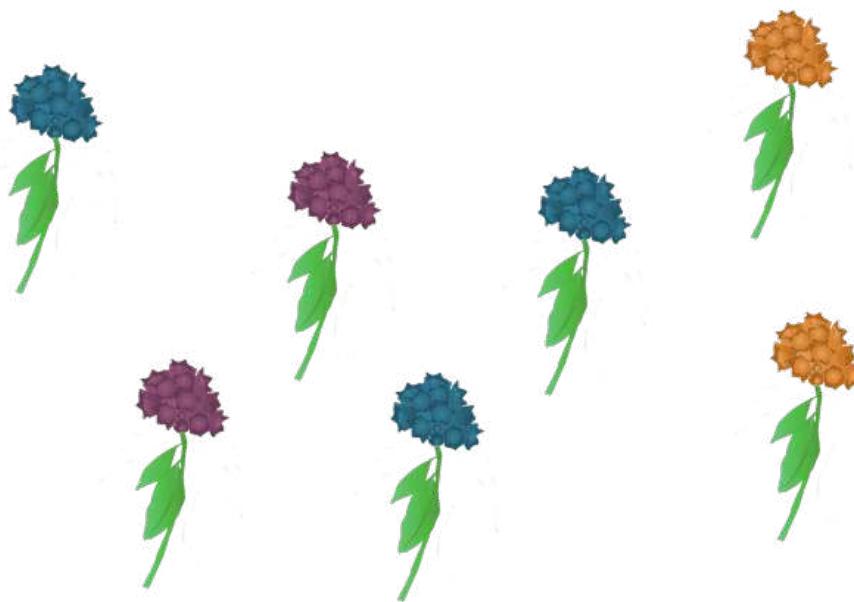
Intransitive



Space



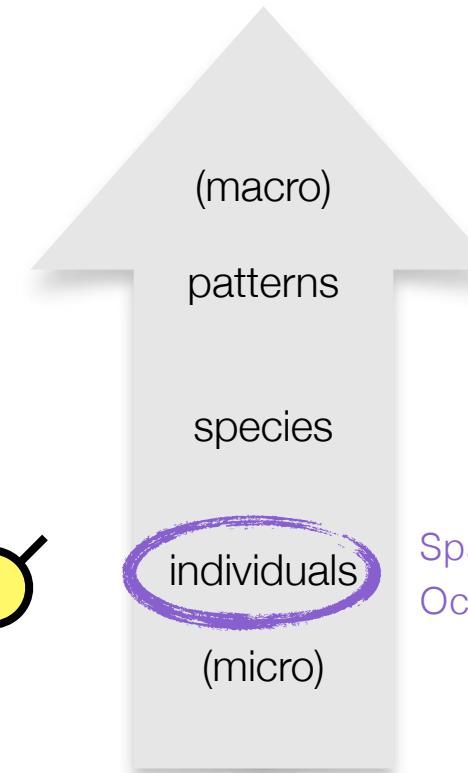
Allesina et al. *Nature* 2017
Kishoni et al. *Nature comm* 2016



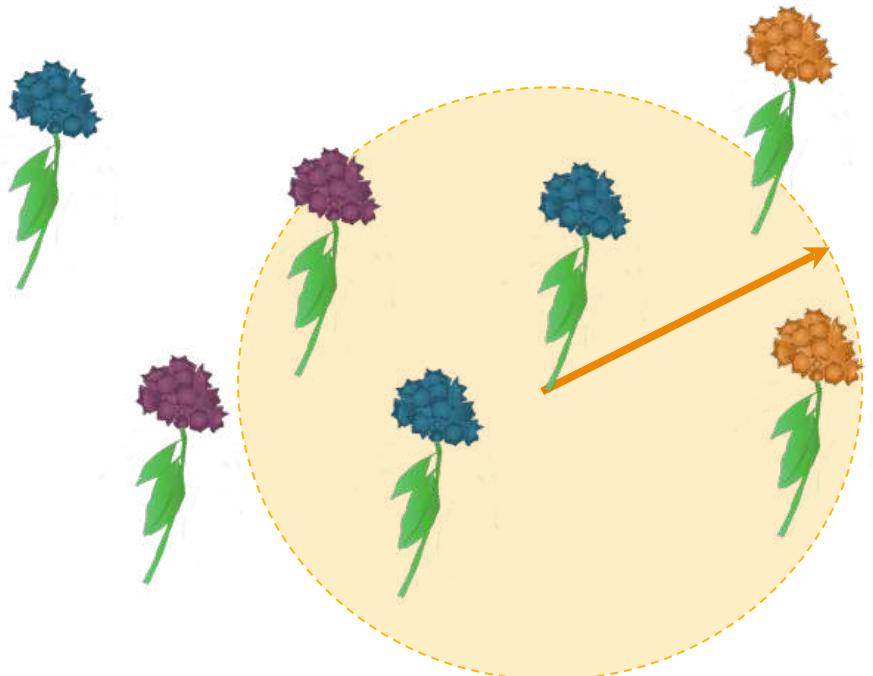
Information about
spatial location



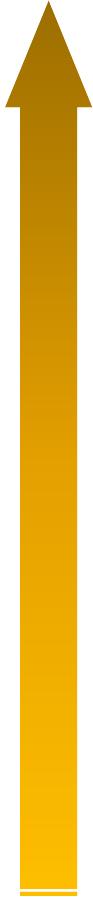
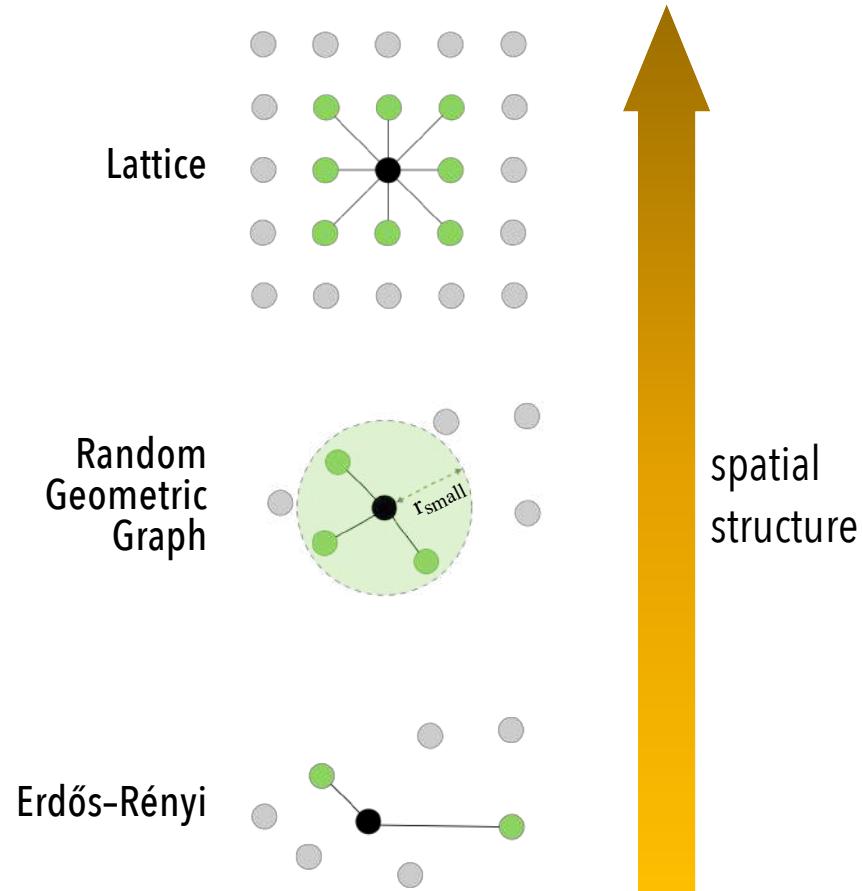
Structured Interactions



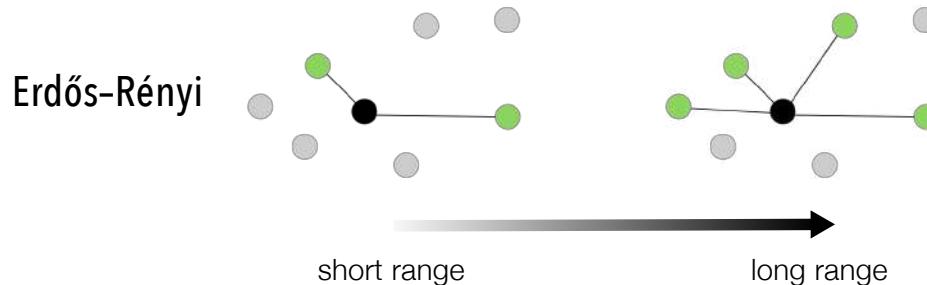
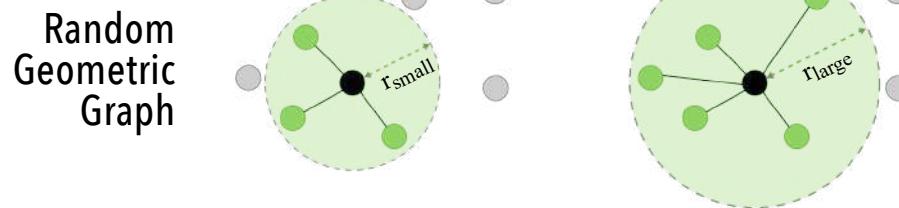
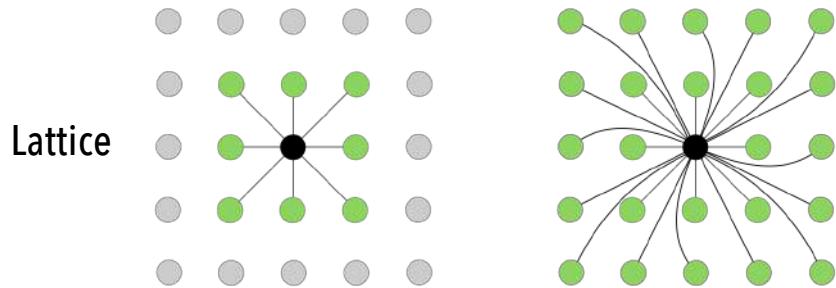
Spatial location
Occupied by 1 individual



Interaction range



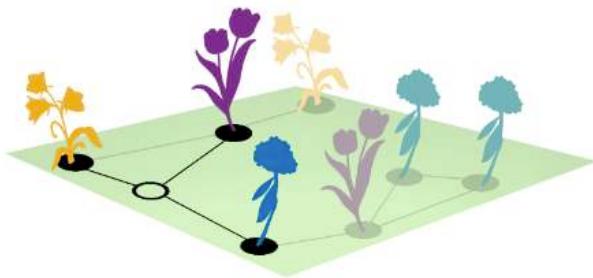
spatial
structure



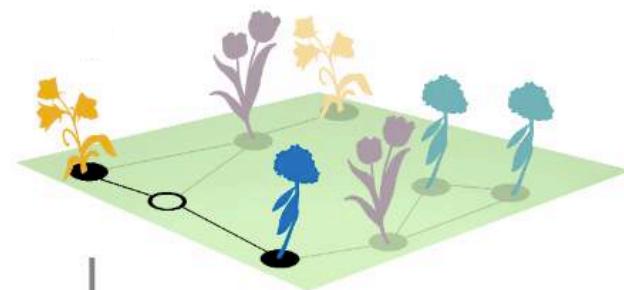
Q: How does coexistence depends on space?

- Interaction range
- Spatial structure

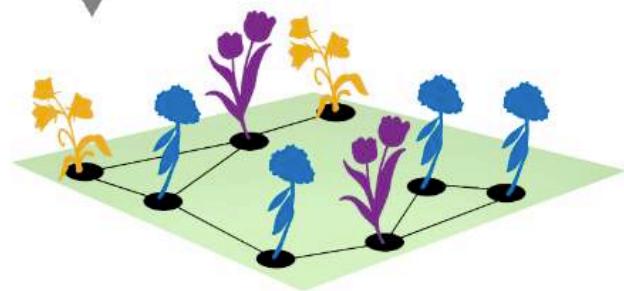
competition in neighborhood



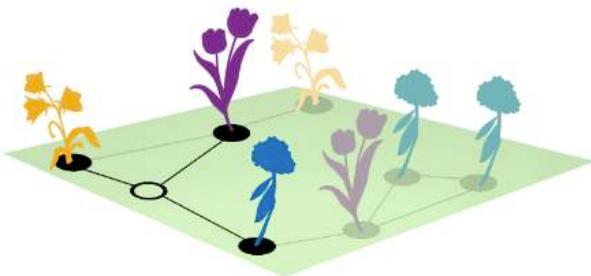
between two random neighbors



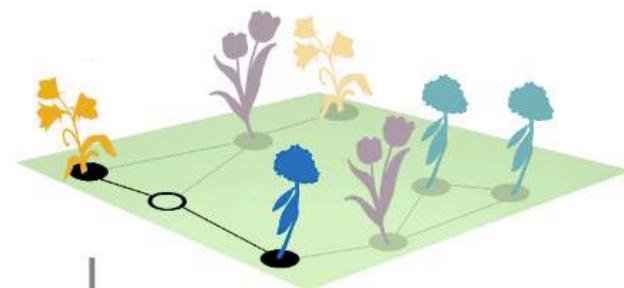
winner reproduces



competition in neighborhood



between two random neighbors



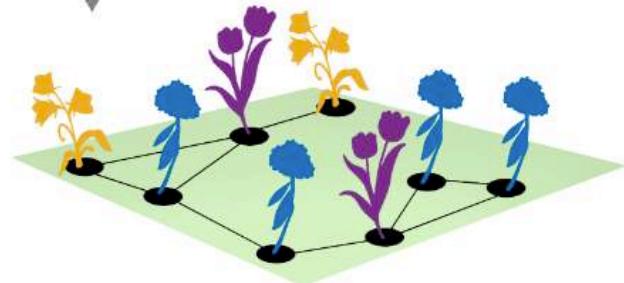
- Pairwise
- Intransitive

Three plant species are shown: a blue hydrangea-like plant, a yellow sunflower-like plant, and a purple tulip-like plant. Arrows point from the blue plant to the yellow and purple plants, and from the purple plant to the yellow plant, illustrating pairwise competition.

$$\begin{pmatrix} 0.5 & 0.34 & 0.75 \\ 0.66 & 0.5 & 0.25 \\ 0.25 & 0.75 & 0.5 \end{pmatrix}$$

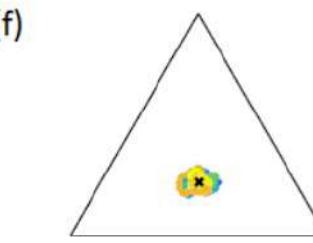
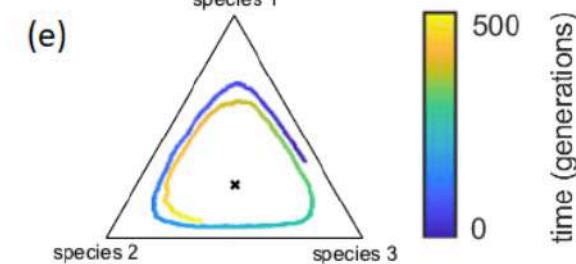
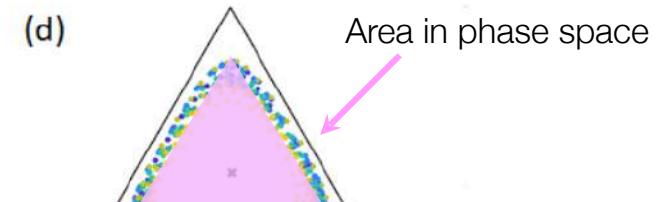
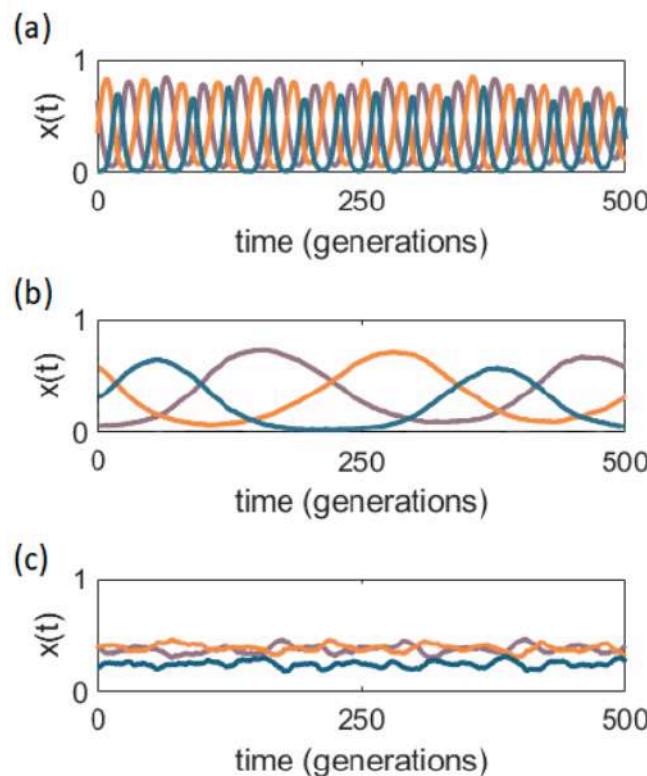
prob. species i defeats species j

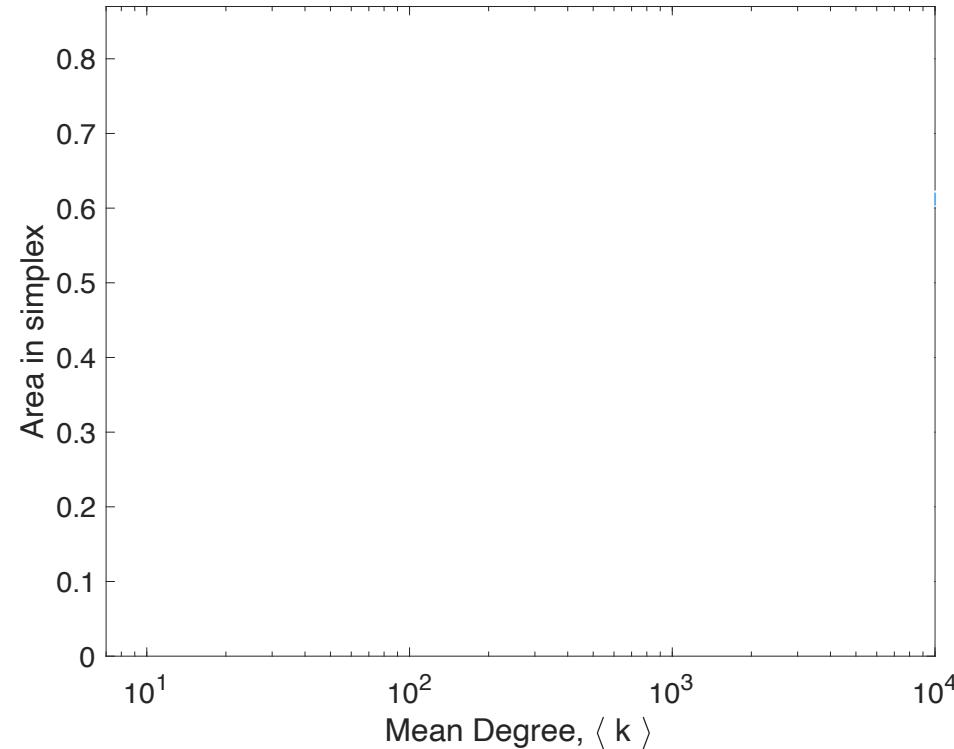
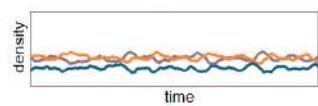
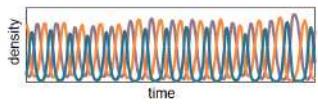
winner reproduces



Results

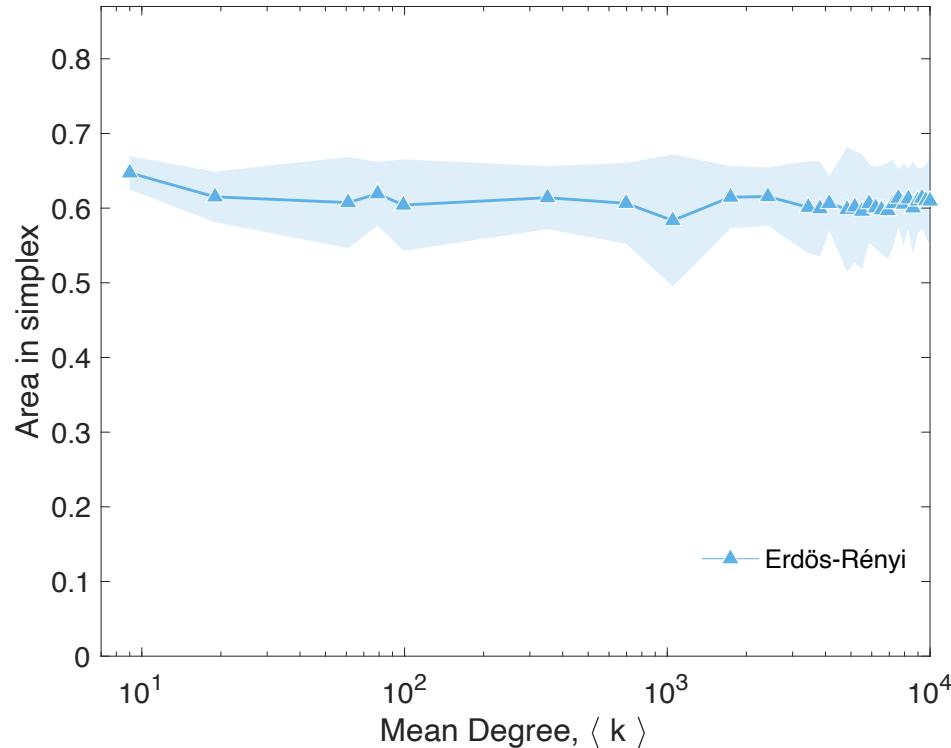
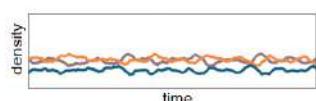
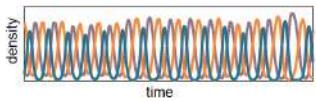
Dynamics changes depending on structure





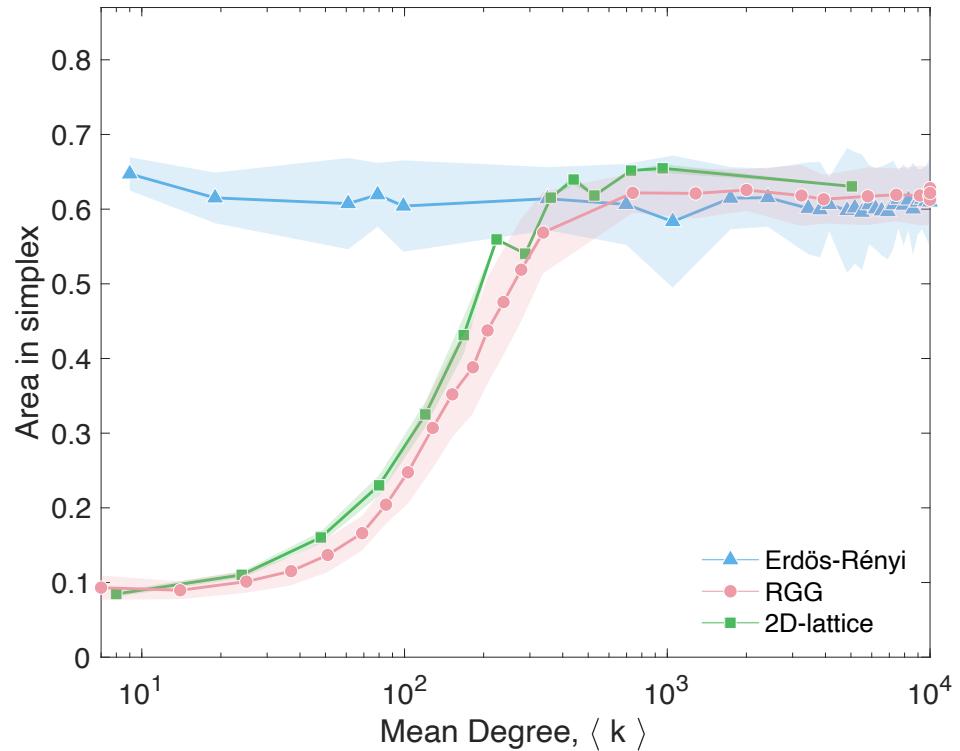
short range
interactions

long range
interactions



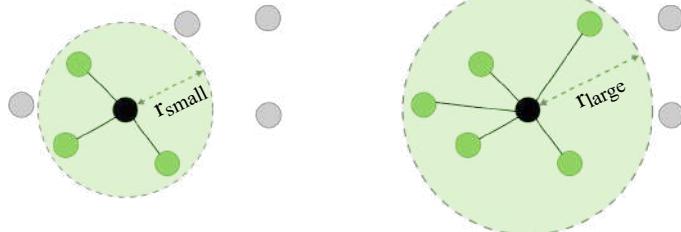
short range
interactions

long range
interactions



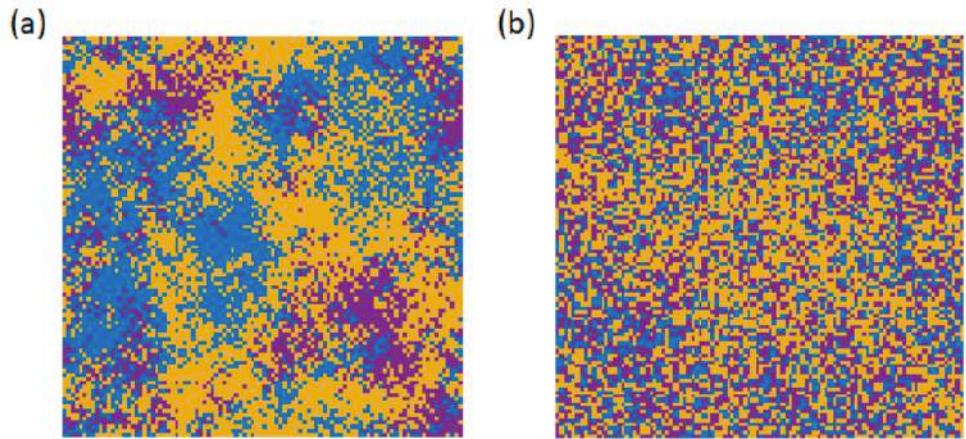
short range
interactions

long range
interactions



Dynamical behavior depends
on structured interactions

But why?

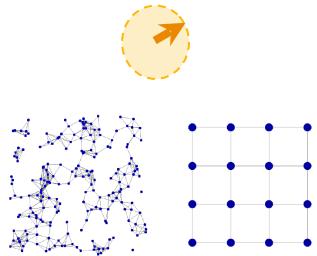


short range
interactions

long range
interactions

Short range interactions
create clusters that reduce competition

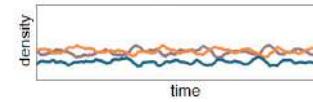
Conclusions

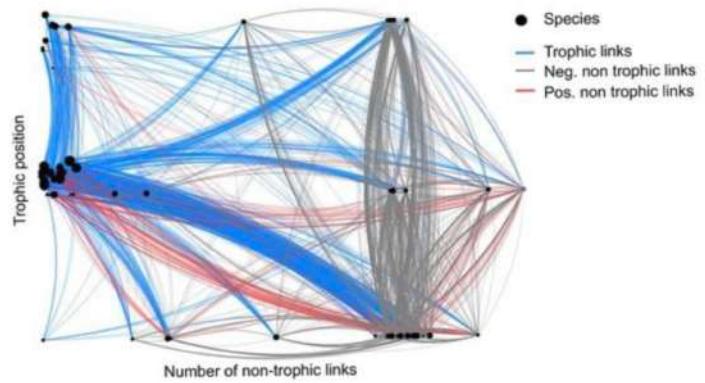


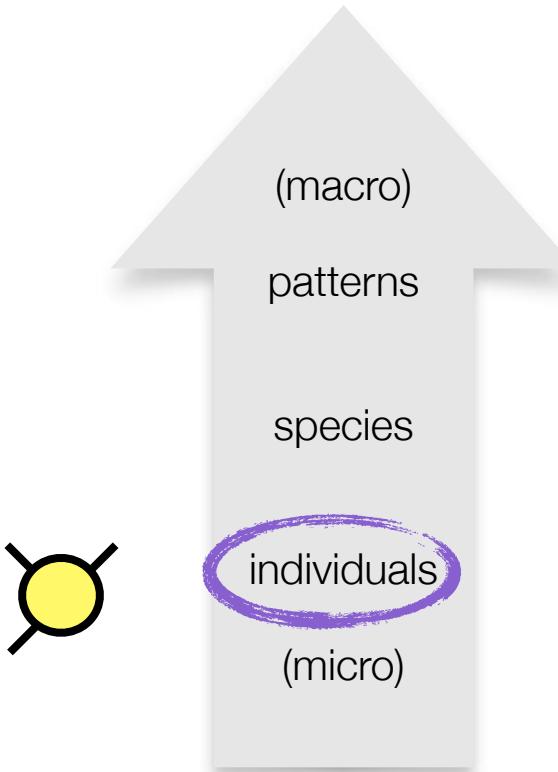
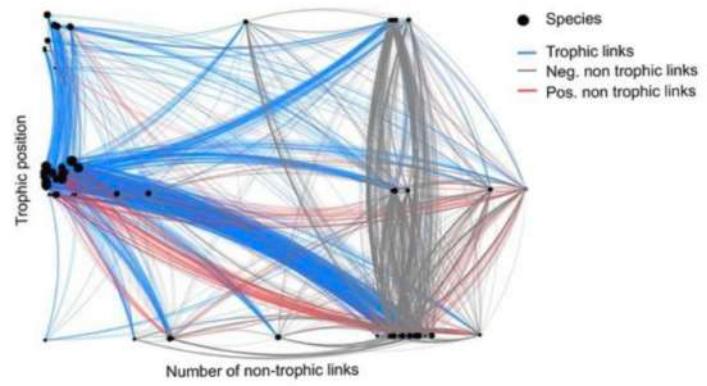
short-range interactions
+
spatially structured network

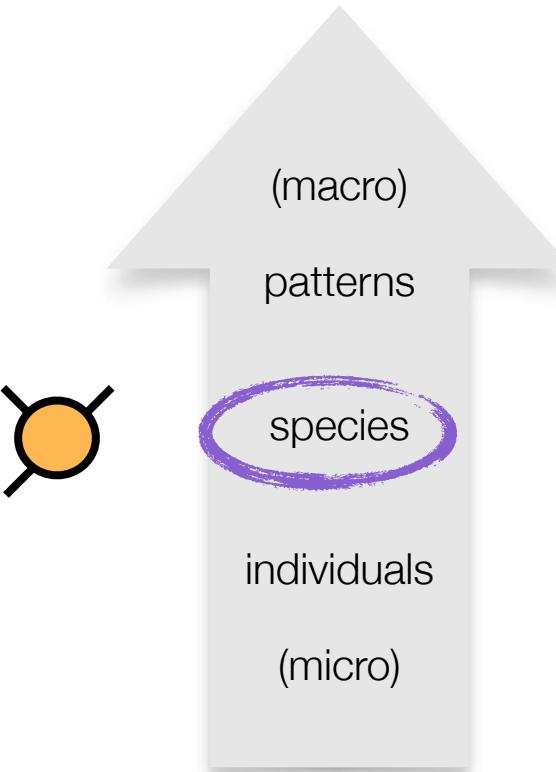
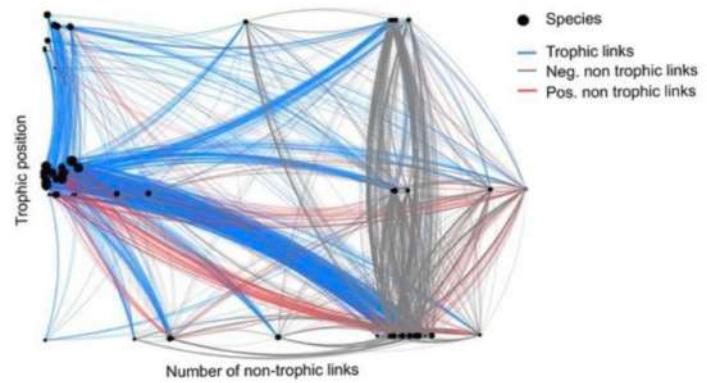


stable coexistence









Ch 4

Structural predictors of species survival in complex communities



Olena Shmahalo/Quanta Magazine



Environmental changes may alter species interactions



Biodiversity loss, cascades of extinctions

How does an ecosystem break?

Are there predictors of species survival?

Predictors typically are...

- general measures of whole network structure
- with only one type of interaction

Ex: PageRank as predictor of importance for coextinctions in food webs

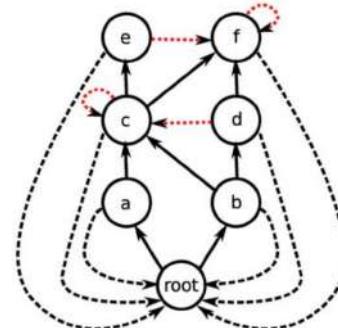
OPEN  ACCESS Freely available online

PLOS COMPUTATIONAL BIOLOGY

Googling Food Webs: Can an Eigenvector Measure Species' Importance for Coextinctions?

Stefano Allesina^{1*}, Mercedes Pascual^{2,3,4}

¹ National Center for Ecological Analysis and Synthesis, Santa Barbara, California, United States of America, ² Department of Ecology and Evolutionary Biology, University of Michigan, Ann Arbor, Michigan, United States of America, ³ Santa Fe Institute, Santa Fe, New Mexico, United States of America, ⁴ Howard Hughes Medical Institute



Predictors typically are...

- general measures of whole network structure
- with only one type of interaction

Q: Do predictors change if we take more interactions into account simultaneously?

Ex: PageRank as predictor of importance for coextinctions in food webs

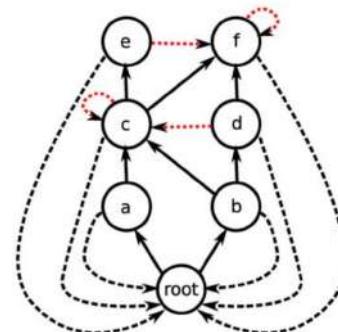
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PLOS COMPUTATIONAL BIOLOGY

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We focus on:

- properties of species ...
- ... coexisting in a network with different interaction types

We focus on:

- properties of species ...
- ... coexisting in a network with different interaction types

$$\dot{x}_i = x_i \left(\sum_i \Lambda_{ij} x_j - \sum_{jk} \Lambda_{jk} x_j x_k \right)$$

local fitness mean fitness

Replicator equation

x_i = relative abundance

$$\Lambda_{ij} = \alpha A_{ij}$$



$\alpha > 0$ mutualism
 $\alpha < 0$ competition

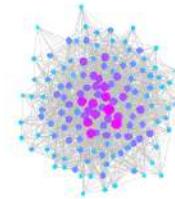
Environmental change
=
change in α

$$\dot{x}_i = x_i \left(\sum_i \Lambda_{ij} x_j - \sum_{jk} \Lambda_{jk} x_j x_k \right)$$

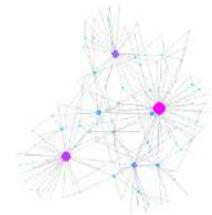
$$\Lambda_{ij} = \alpha A_{ij}$$



Erdős-Rényi

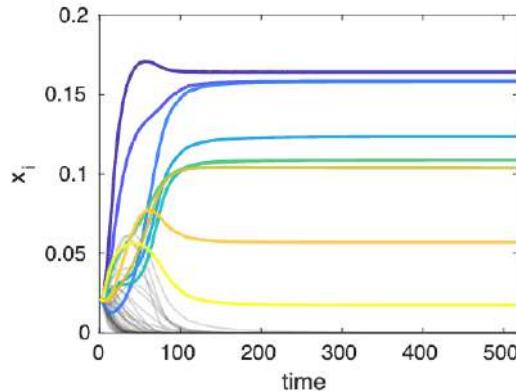


Scale-free
(Holme-Kim,
Barabási-Albert)

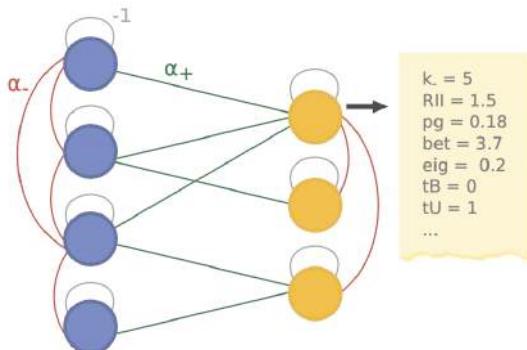


Empirical

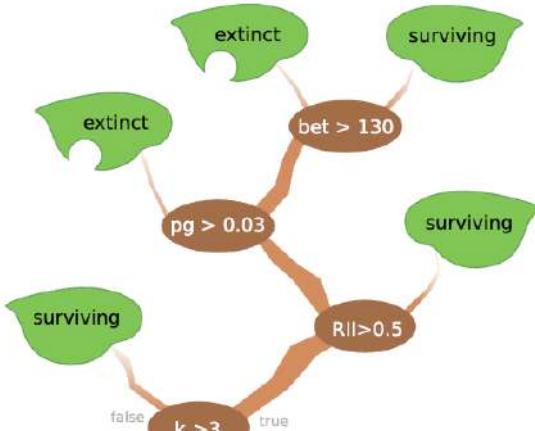




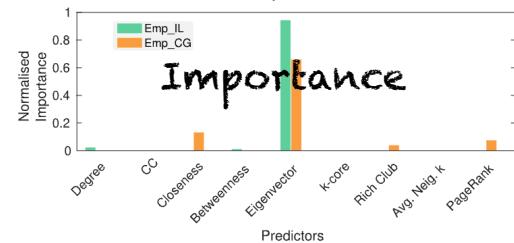
Simulate replicator
dynamics:
Track survivors



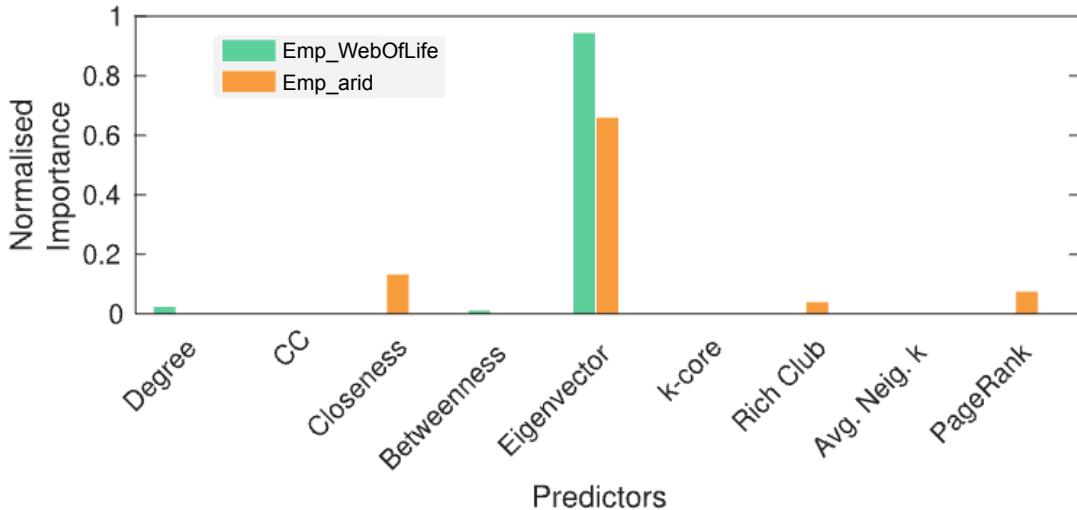
- Node properties:
- Centrality
 - Meso-scale
 - Signed



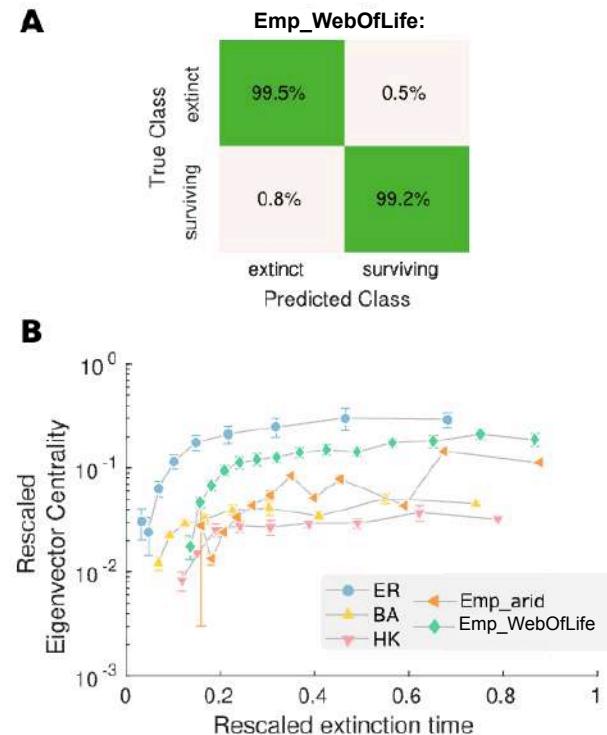
Decision tree



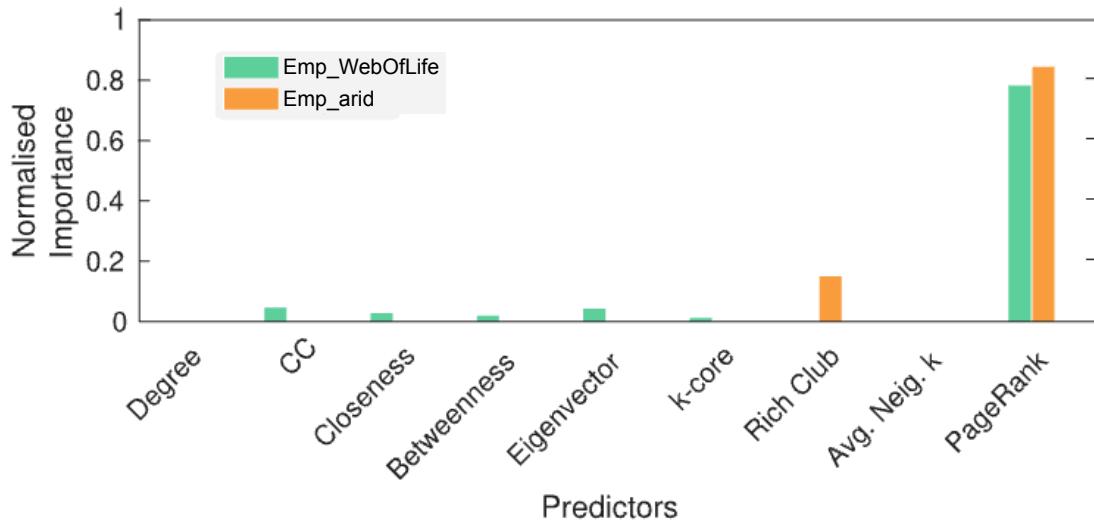
Results: Mutualism



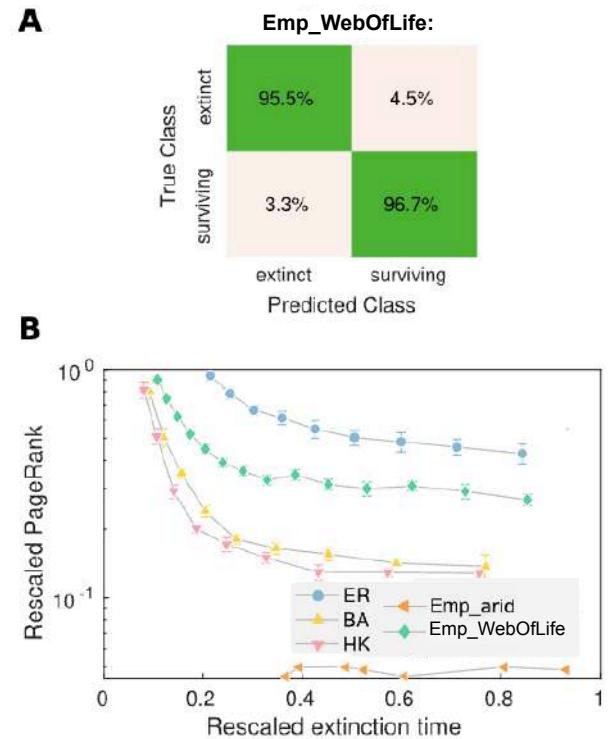
Predictor = High Eigenv. Cent. increases survival



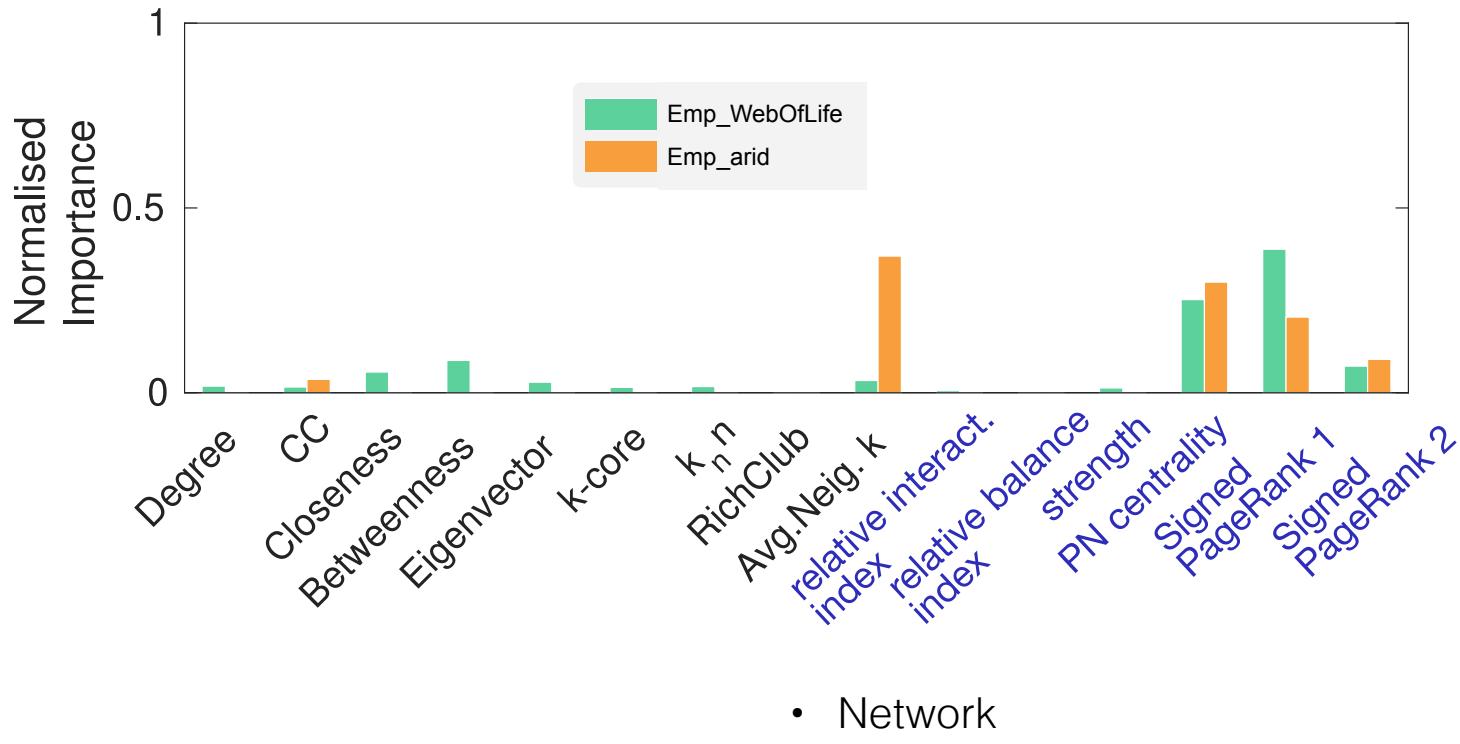
Results: Competition



Predictor = Low PR increases survival

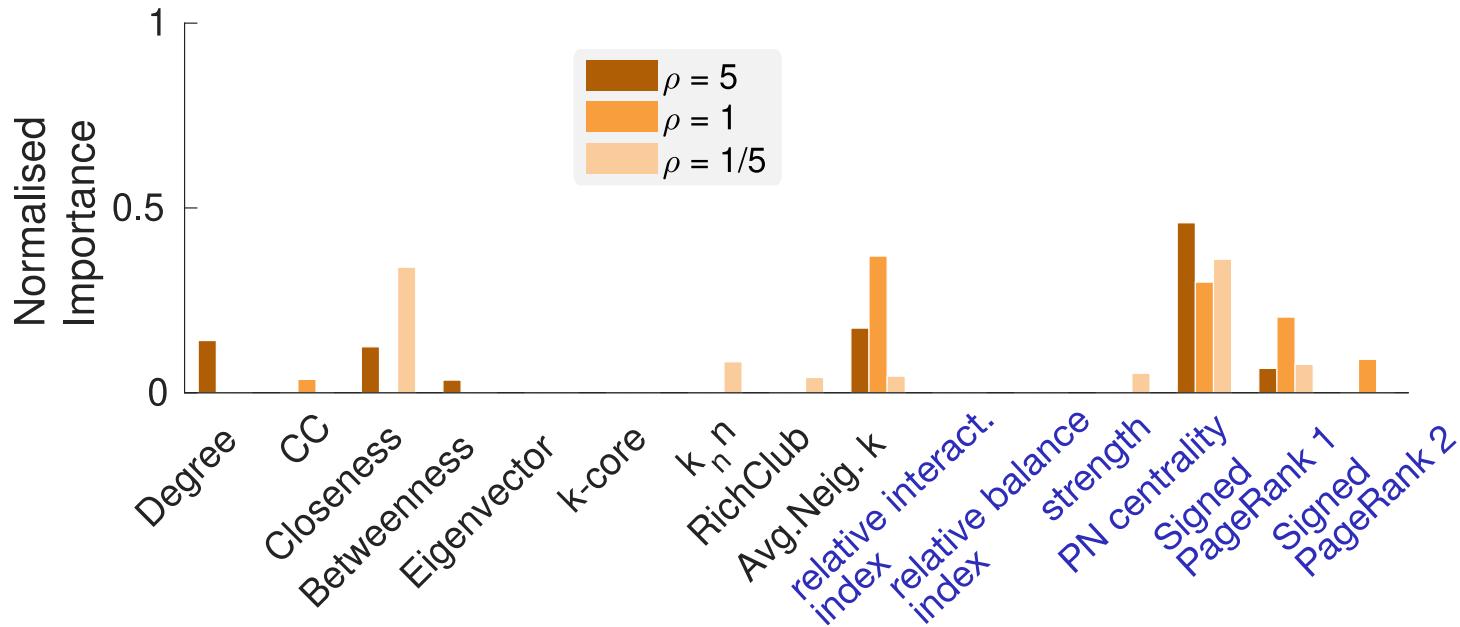


Results: Mutualism & Competition



No universal predictors...

Results: Mutualism & Competition



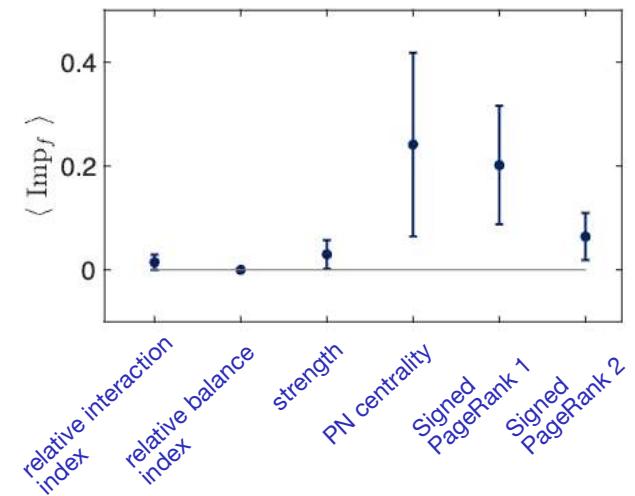
No universal predictors...

- Network
- Interaction strength

Results: Mutualism & Competition

No universal predictors...

But they usually depend on interaction strength and sign



Conclusions

Competition & Mutualism

Structural predictors are...

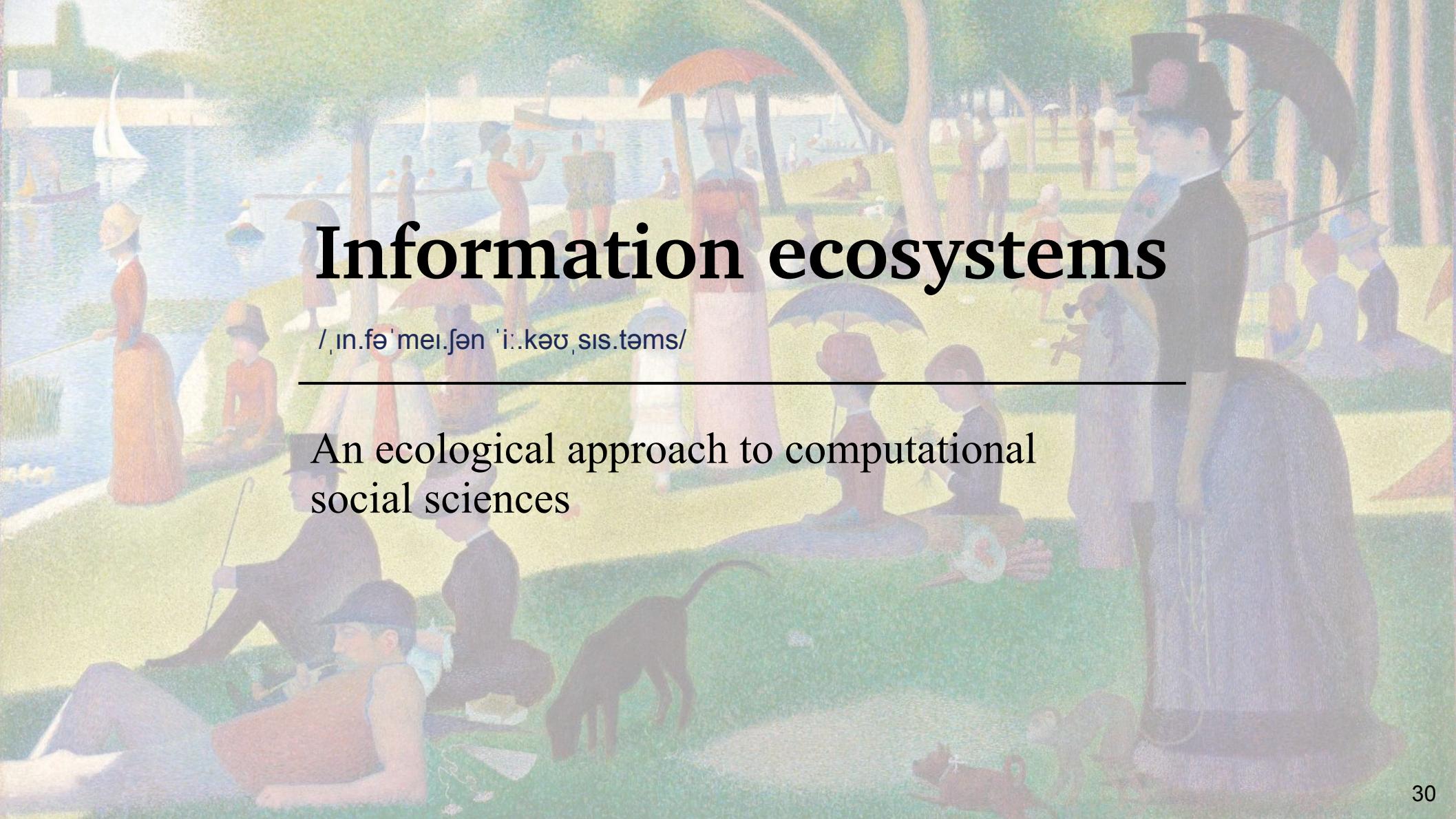
- Different from competition or mutualism alone
- Different for every ecosystem



Ecosystems are composed of several types of interactions...
Revisit results obtained for single interactions!

PART II

INFORMATION ECOSYSTEMS

A pointillist painting depicting a leisurely picnic on a grassy bank of a river. In the foreground, several people are seated on the grass, including a man in a top hat and a woman in a red dress. A small dog is visible near the center. In the background, a large crowd of people is gathered under umbrellas and trees along the riverbank, with sailboats on the water.

Information ecosystems

/ɪn.fə'mei.ʃən 'iː.kəʊ.sis.təms/

An ecological approach to computational
social sciences

Spot the differences!



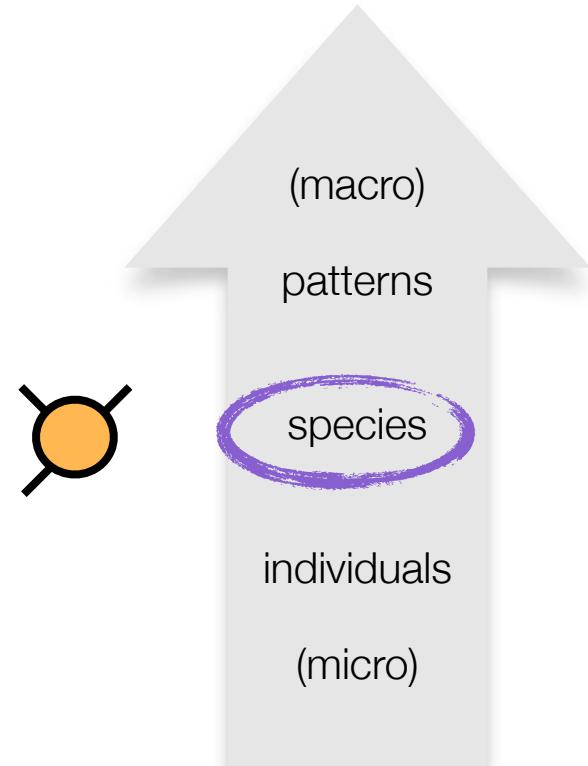
Natural Ecosystems



- Species
- Abundances
- Resources
- :

Information Ecosystems

- Memes/hashtags, users
- Popularity, visibility
- Users' attention
- :





Natural Ecosystems

- Species
- Abundances
- Resources
- :

Information Ecosystems

- Memes/hashtags, users
- Popularity, visibility
- Users' attention
- :

Exploit tools and theories from Theoretical Ecology
to understand Human Behavior!!

Neutral theory for competing attention in social networks

Carlos A. Plata^{1,2}, Emanuele Pigani¹, Sandro Azaele¹, Violeta Calleja-Solanas^{1,3}, Maria J. Palazzi^{1,4}, Albert Solé-Ribalta^{1,5}, Javier Borge-Holthoefer^{1,4}, Sandro Meloni^{1,3}, and Samir Suweis^{1,6,7}



ARTICLE

<https://doi.org/10.1038/s41467-021-22184-2>

OPEN

An ecological approach to structural flexibility in online communication systems

Maria J. Palazzi¹, Albert Solé-Ribalta^{1,2}, Violeta Calleja-Solanas^{1,3}, Sandro Meloni¹, Carlos A. Plata^{1,4,5}, Samir Suweis^{1,6} & Javier Borge-Holthoefer^{1,4}



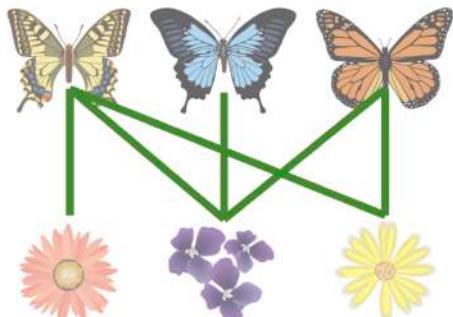
ARTICLE

<https://doi.org/10.1038/s41467-019-09311-w>

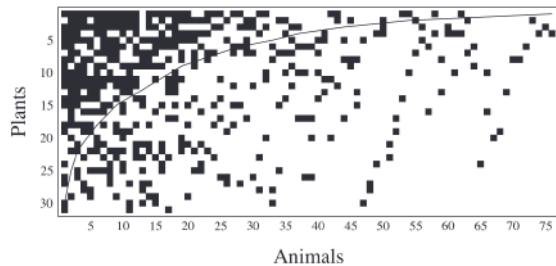
OPEN

Accelerating dynamics of collective attention

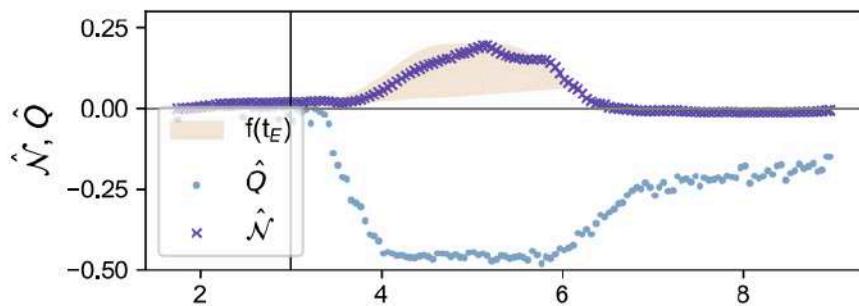
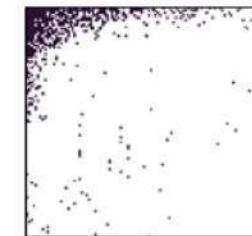
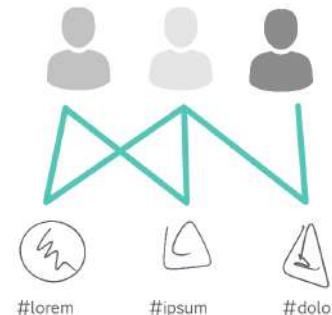
Philipp Lorenz-Spreen^{1,2}, Bjarke March Mønsted^{1,3}, Philipp Hövel^{1,4} & Sune Lehmann^{1,5}



Rohr et al. *Science* 345 (2014)

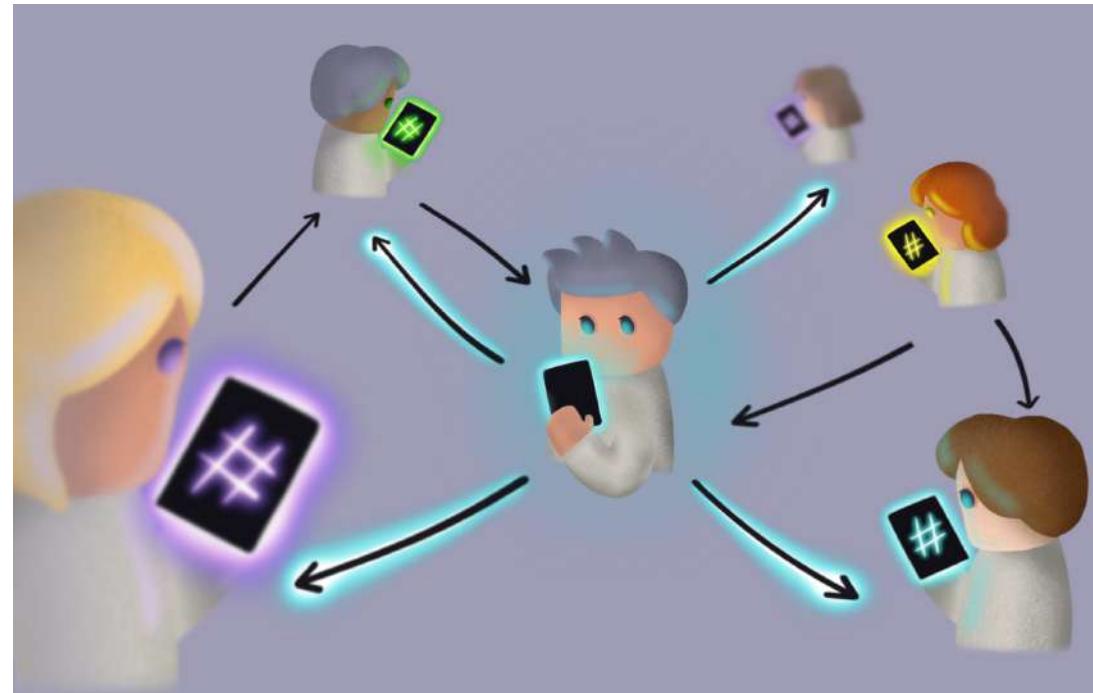


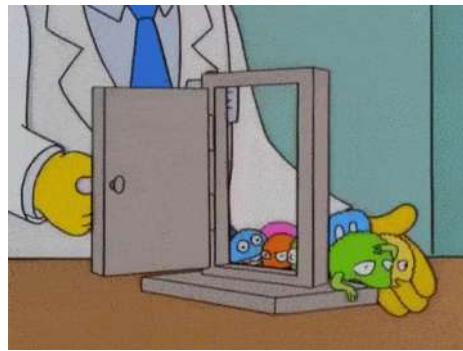
Bascompte et al. *PNAS* 100 (2003)



Ch 5

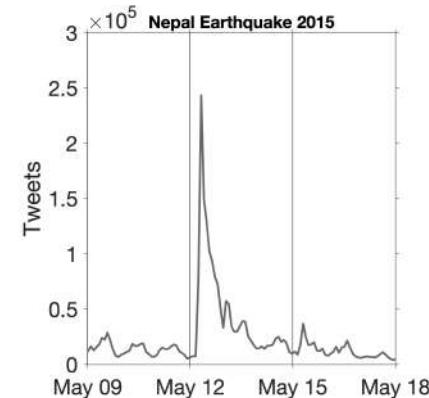
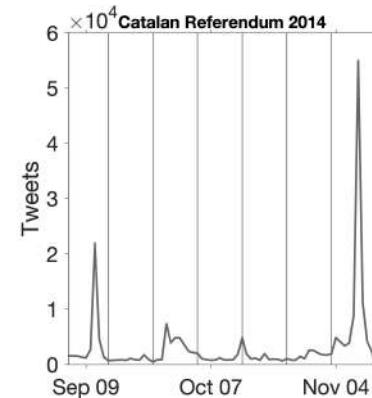
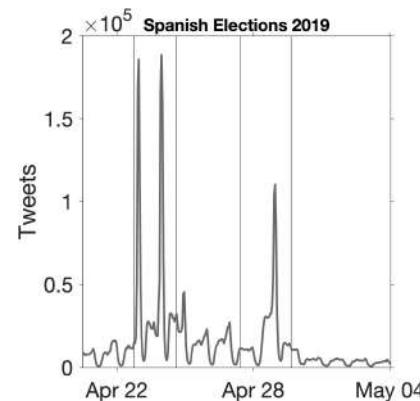
Quantifying the drivers behind collective attention

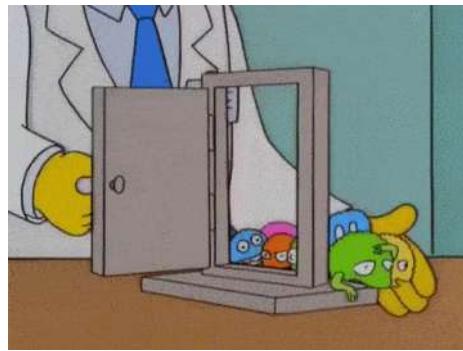




- Cognitive bottleneck
- Attention is the new currency
- Competition for attention

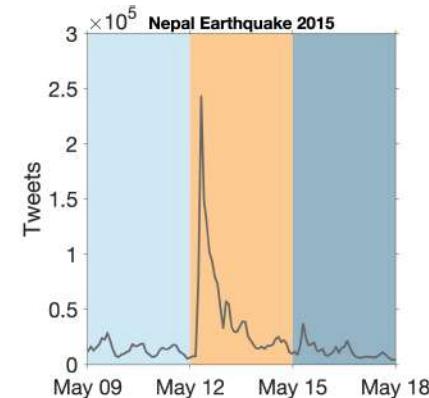
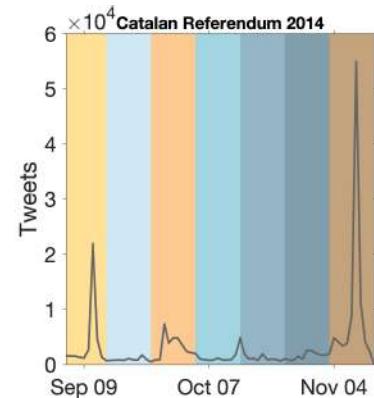
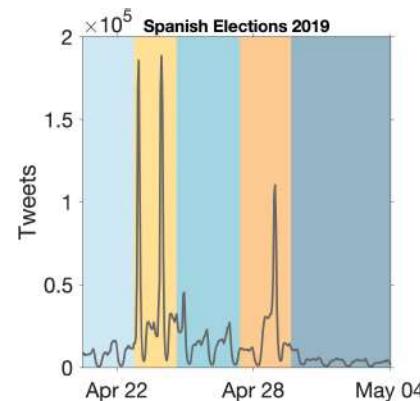
Collective attention during events





- Cognitive bottleneck
- Attention is the new currency
- Competition for attention

Collective attention during events



Q1: How can we quantitatively characterize competition?

Method based on:



- Generalized Lotka-Volterra equations
- Niche theory

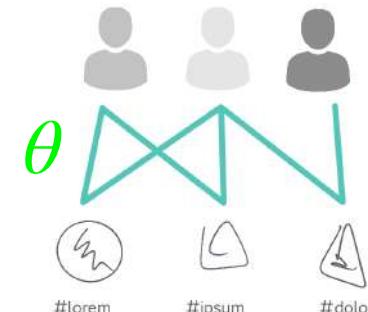
Q1: How can we quantitatively characterize competition?

Method based on:



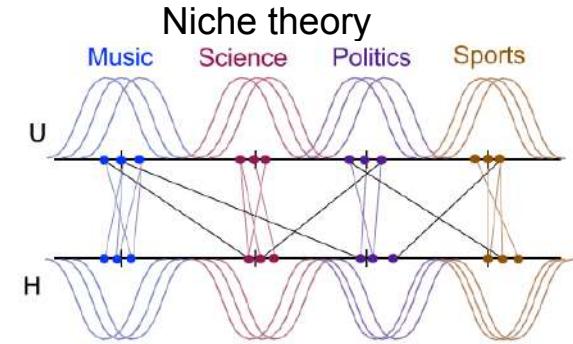
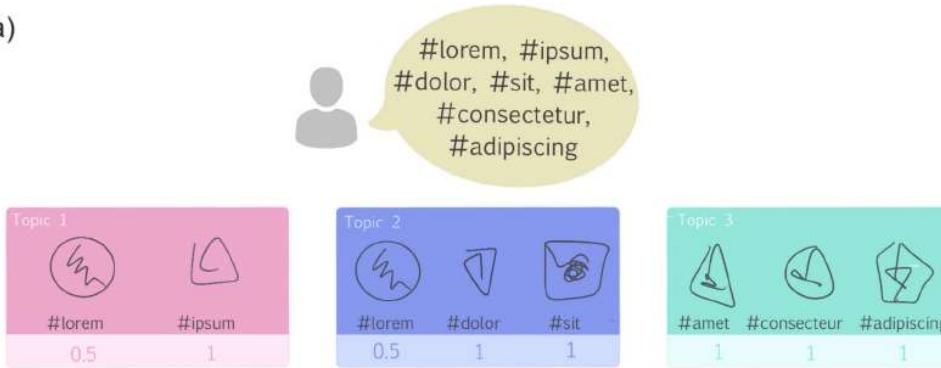
- Generalized Lotka-Volterra equations
- Niche theory

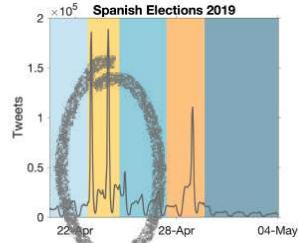
$$\frac{dn_i^U}{dt} = n_i^U \left(\rho_i^U - \sum_j \beta_{ij}^{UU} n_j^U + \frac{\sum_k \gamma_{ik}^{UH} n_k^H}{1 + h \sum_l \theta_{il} n_l^H} \right)$$
$$\frac{dn_k^H}{dt} = n_k^H \left(\rho_k^H - \sum_l \beta_{kl}^{HH} n_l^H + \frac{\sum_i \gamma_{ki}^{HU} n_i^U}{1 + h \sum_j \theta_{kj} n_j^U} \right)$$



Quantifying competition & mutualism

a)





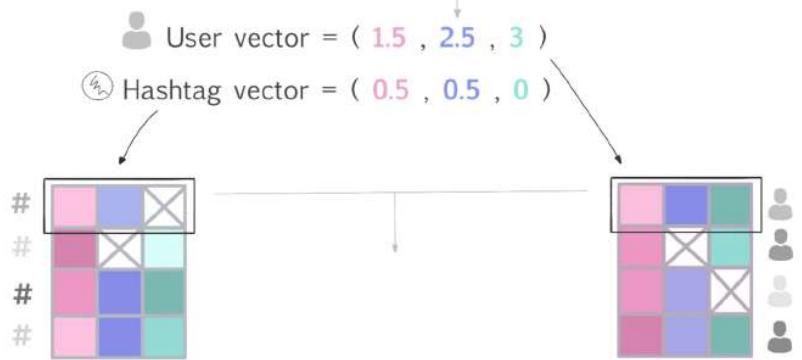
Some topics and their

Quantifying competition & mutualism

a)



b)

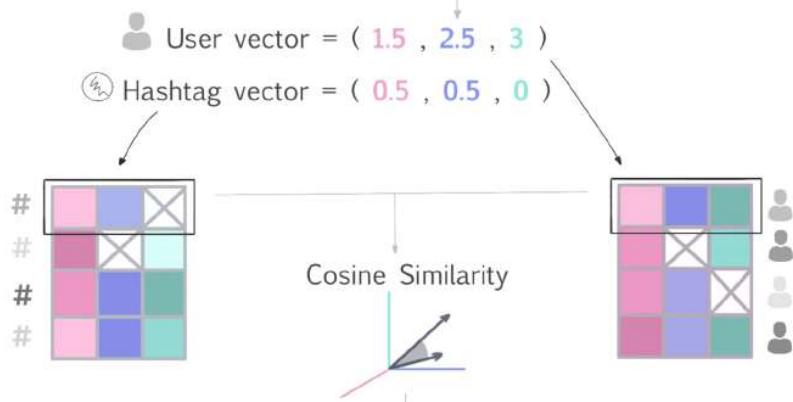


Quantifying competition & mutualism

a)



b)

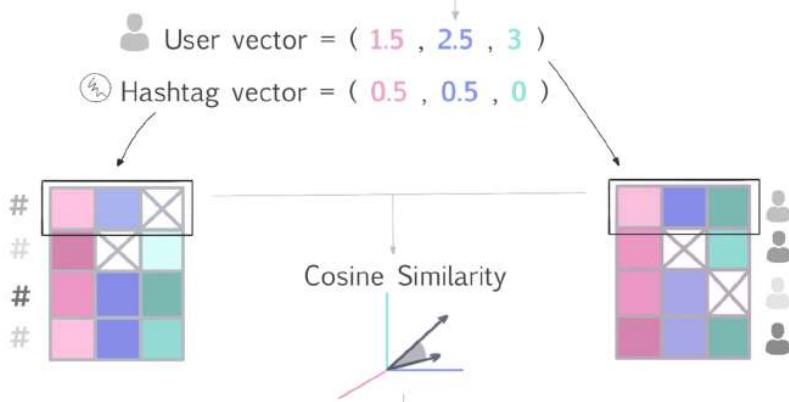


Quantifying competition & mutualism

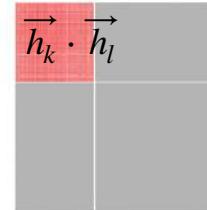
a)



b)

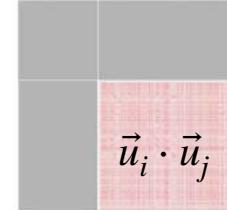


$$\beta^{UU}$$



Hashtag-Hashtag
competition matrix

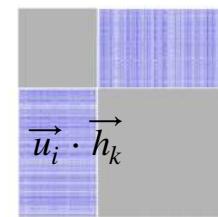
$$\beta^{HH}$$



User-User
competition matrix

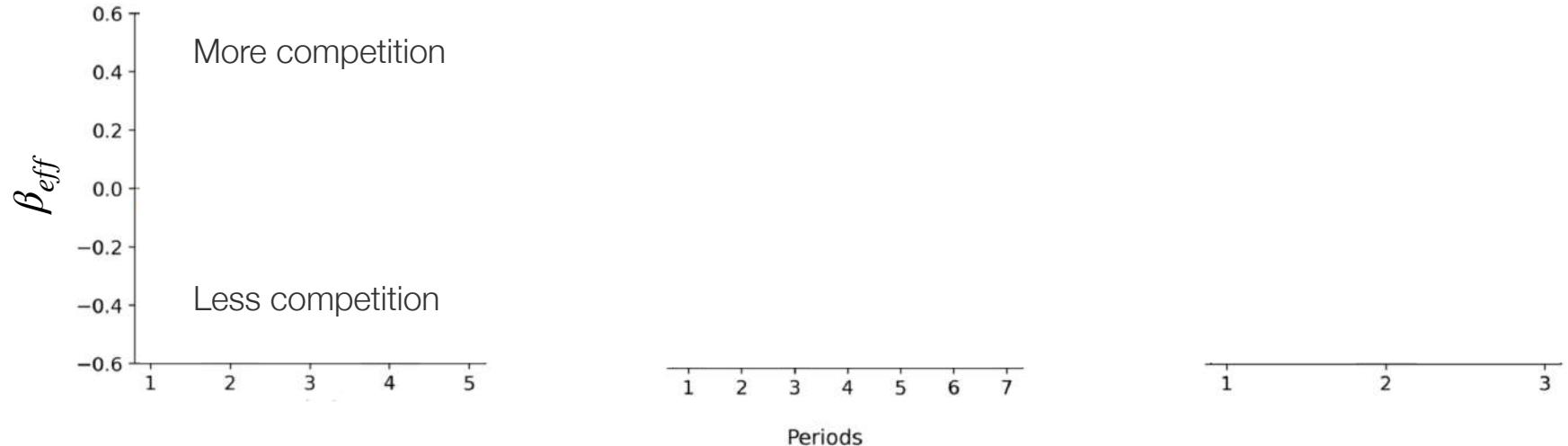
Interaction Weights
1
0
-1

$$\gamma^{UH}\theta$$



User-Hashtag
mutualism matrix

Results



What weights more?



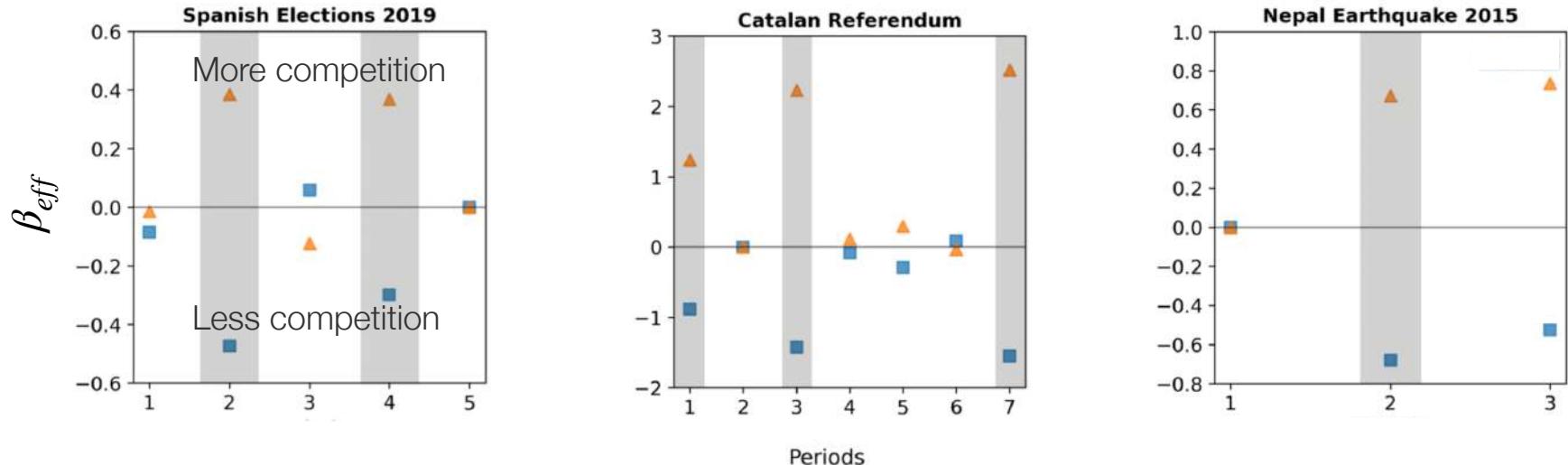
Users **effective** competition



Hashtags **effective** competition

$$\beta_{eff} = (\beta - \beta_{calm}) - (\gamma - \gamma_{calm})$$

Results



What weights more?



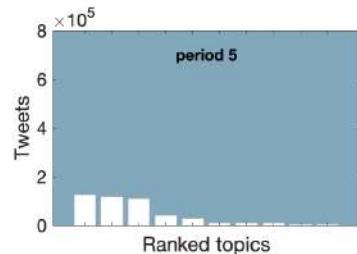
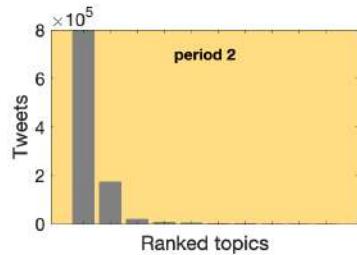
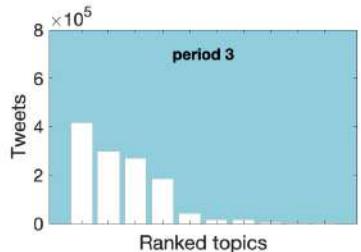
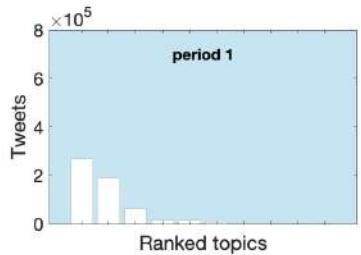
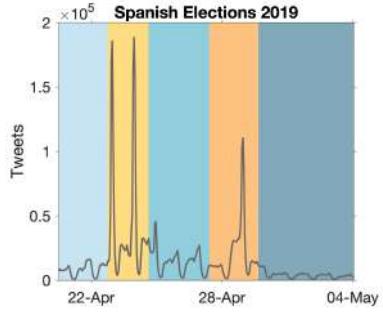
Users **effective** competition ↓ during **peaks**



Hashtags **effective** competition ↑ during **peaks**

$$\beta_{eff} = (\beta - \beta_{calm}) - (\gamma - \gamma_{calm})$$

Topic evolution:

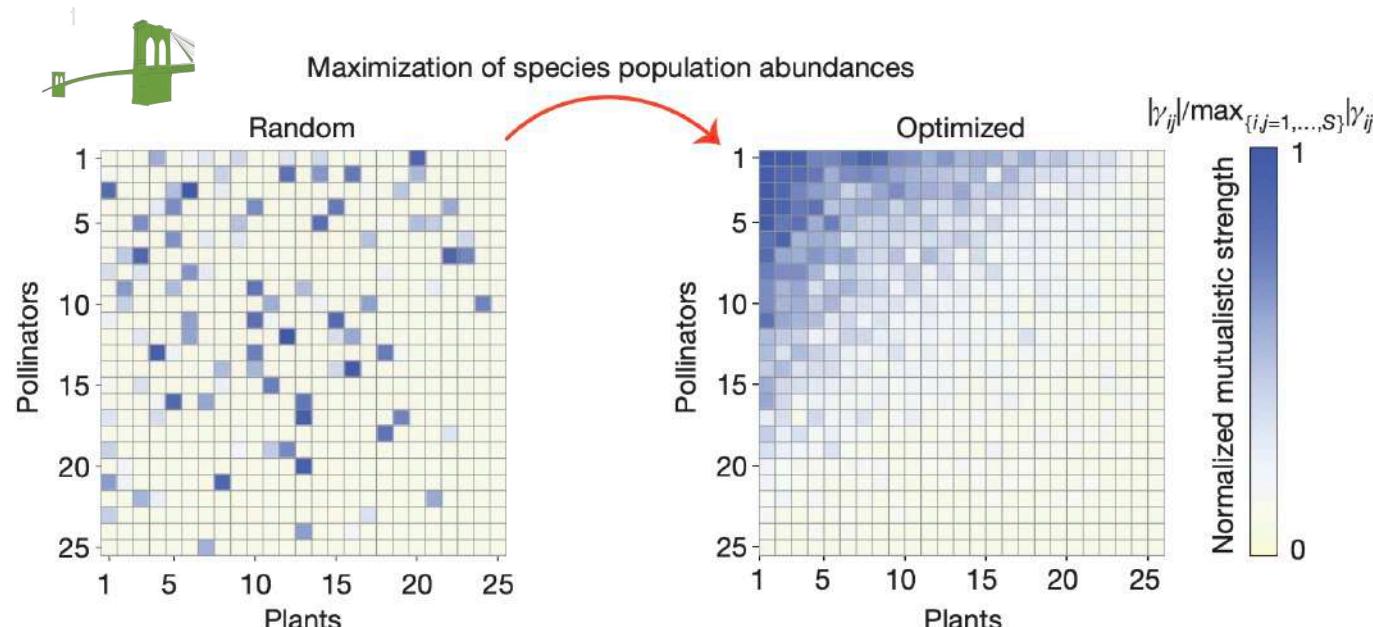


During peaks:

one or two topics generate almost the 90% of the tweets

Q2: What are the drivers behind collective attention?

Assumption: users maximize their visibility

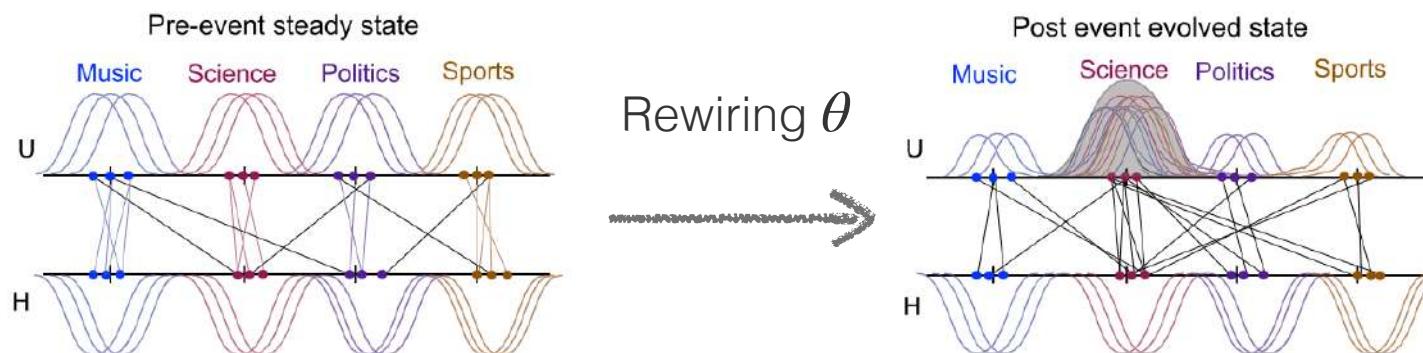


Suweis et al. *Nature* 500 (2013)

Cai et al. *Nature Communications* 11, (2020)

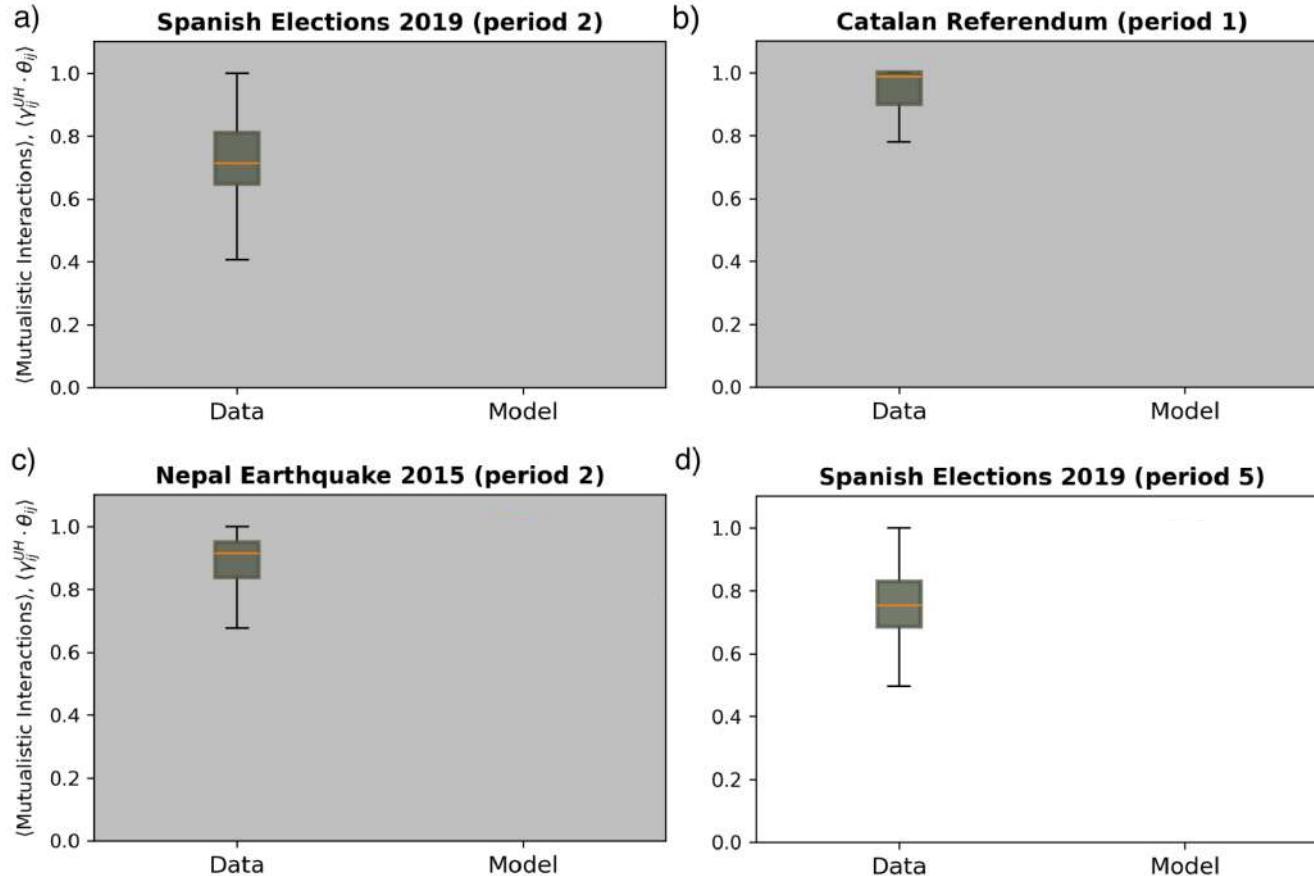
Q2: What are the drivers behind collective attention?

Assumption: users maximize their visibility



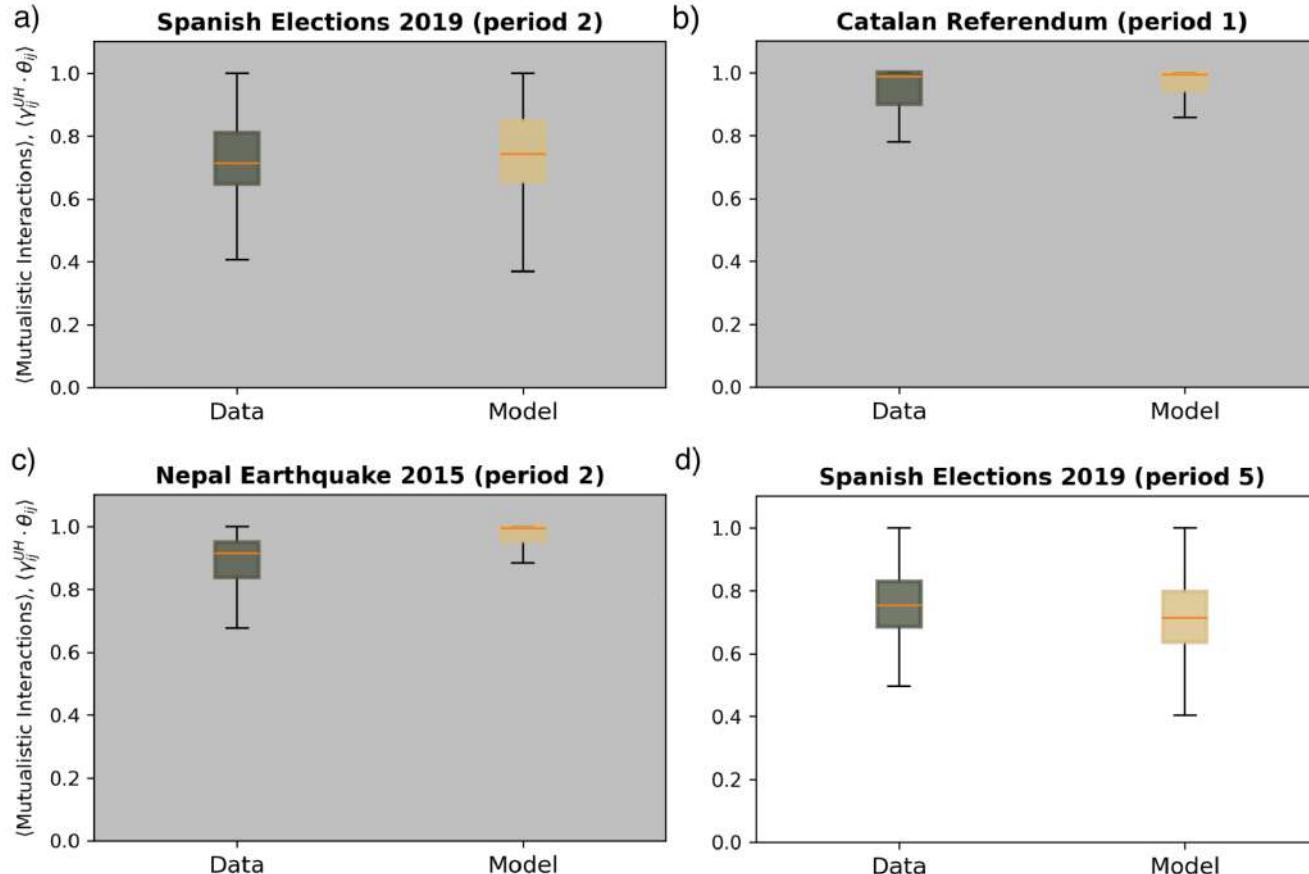
Results

Comparison empirical interactions with optimization model



Results

Comparison empirical interactions with optimization model



It's a match!

Conclusions



An analogy between natural and information ecosystems can quantify the competition for attention experienced by agents during events

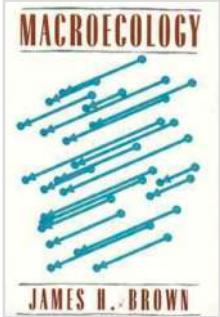
- Users effectively reduce net competition
- Hashtags experience stronger competition
- The driver is visibility optimization



Ch 6

Finding macroecological patterns in information ecosystems



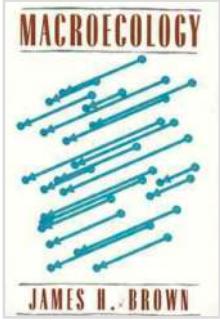


Universal statistical laws across ecosystems

- Abundance
- Distribution
- Diversity

Important for:

- Finding mechanisms
- Modeling
- Health and prediction

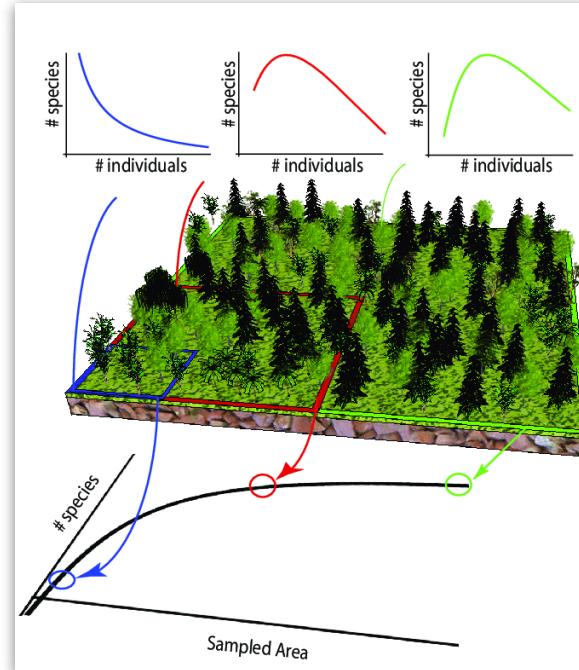


Universal statistical laws across ecosystems

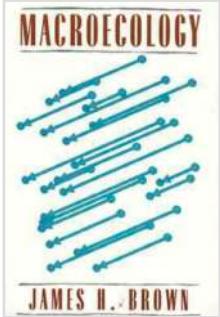
- Abundance
- Distribution
- Diversity

Important for:

- Finding mechanisms
- Modeling
- Health and prediction



S. Azale, et al. Rev. Mod. Phys. 88, 035003 (2016)



Universal statistical laws across ecosystems

- Abundance
- Distribution
- Diversity



- Species = Hashtags
- Abundance = Popularity
- Sampling

Important for:

- Finding mechanisms
- Modeling
- Health and prediction

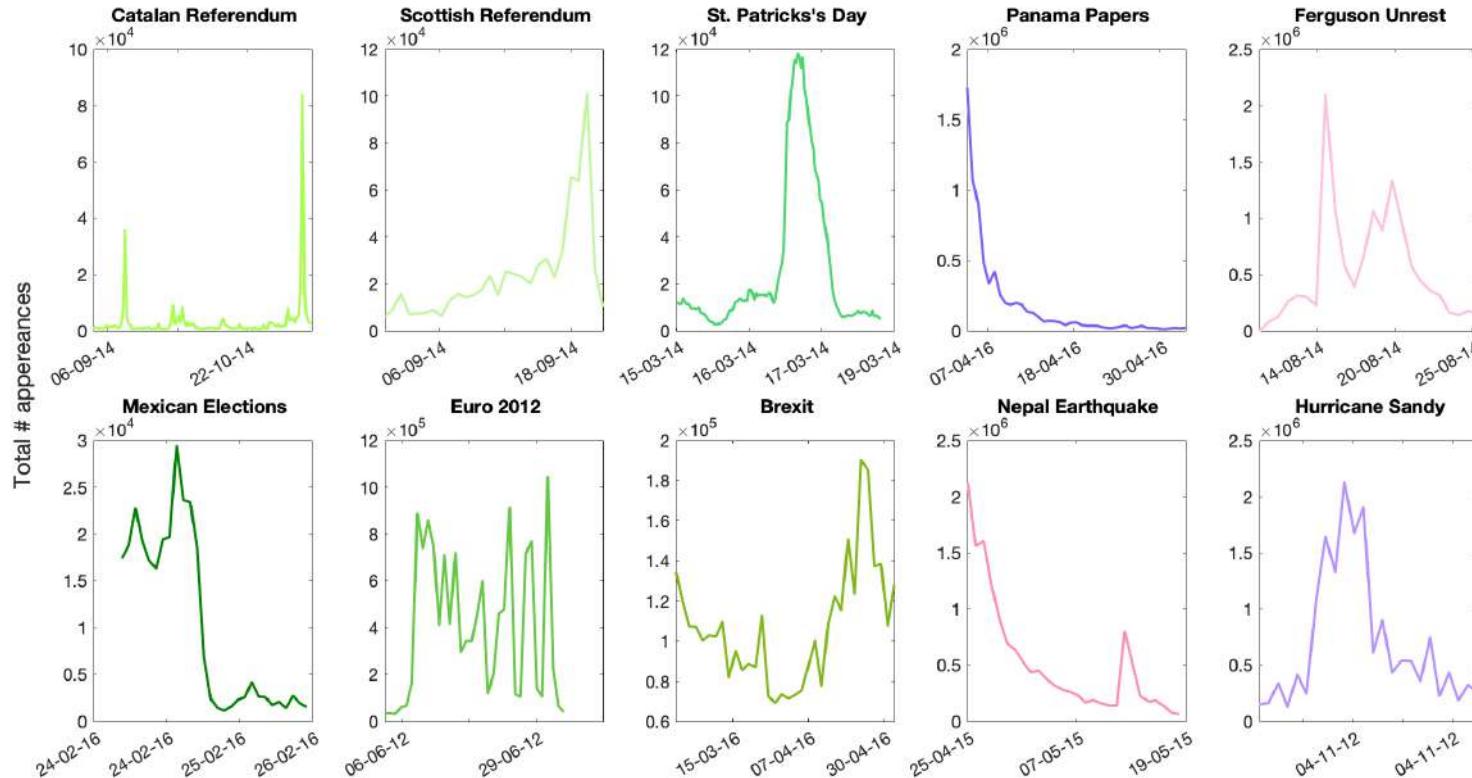
Q: How do these laws apply to
Information Ecosystems?

10 “Events” datasets + 1 “Random” sample of Twitter Activity

Dataset	Type	Posts	Hashtags	Days
Mexican Elections	E	191788	158	1
Scottish Referendum	E	429901	313	23
Catalan Referendum	E	222783	375	69
St. Patrick's Day	E	2882010	1591	3
Brexit	E	182629	1689	69
UK random sample	R	1649482	1833	9
Ferguson Unrest	U	8782071	2811	17
Panama Papers	U	5044378	3696	23
Euro 2012	E	8992157	4361	34
Nepal Earthquake	U	12004187	5032	23
Hurricane Sandy	U	5658525	5353	6

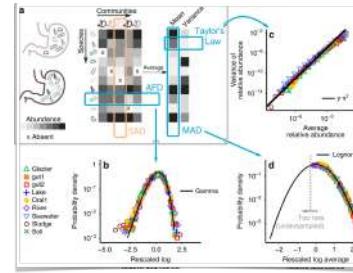
10 “Events” datasets + 1 “Random” sample of Twitter Activity

HETEROGENEOUS!

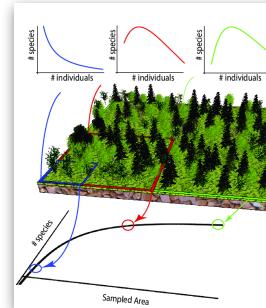


Patterns

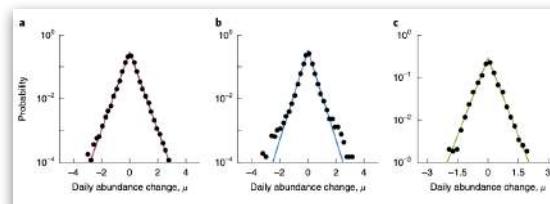
- Taylor's Law
- Mean Abundance Distribution *MAD*
- Abundance Fluctuations Distribution *AFD*
- Relative Species Abundance *RSA*
- Species-Area Curve *SAC*
- Short-Term Abundance Change *STAC*



J. Grilli. *Nature Communications* 11, 4743 (2020)



S. Azaele, et al. *Rev. Mod. Phys.* 88, 035003 (2016)

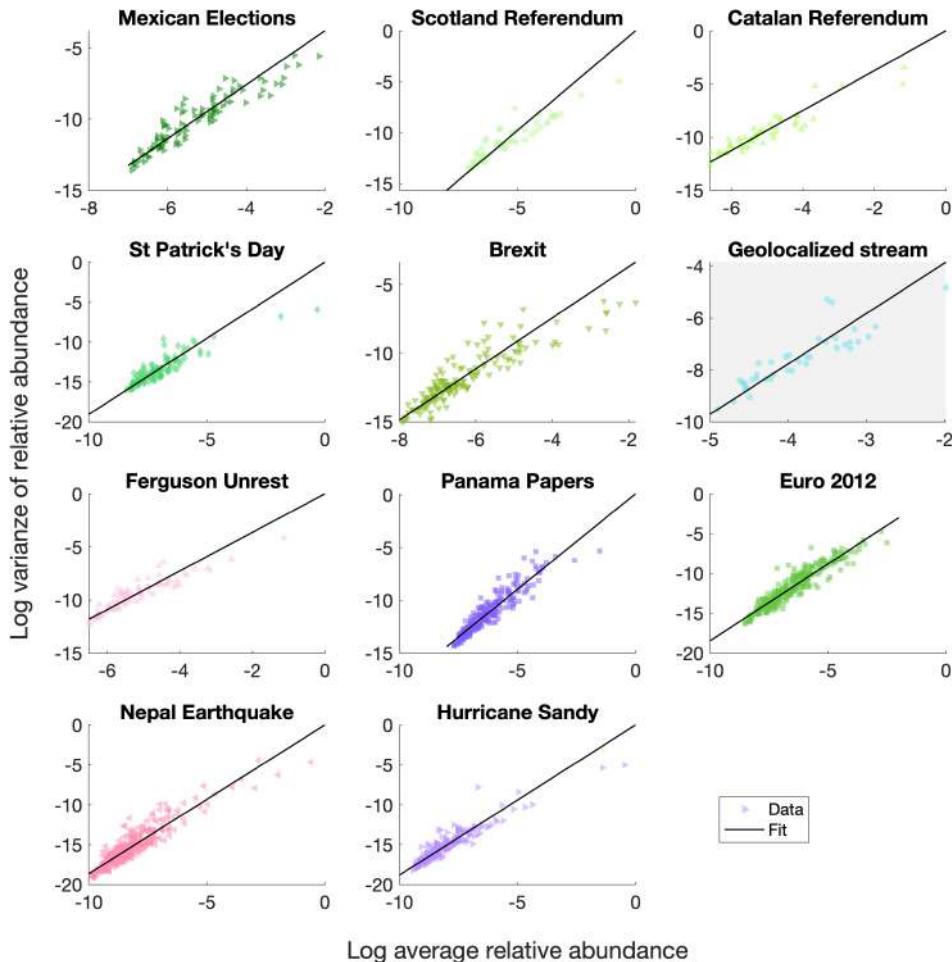


Ji, et al. *Nature Microbiology* 5, 768–775 (2020)

Taylor's Law

Connects mean abundance of a hashtag
with its variance

$$\sigma_h^2 \sim \bar{x}_i^2$$



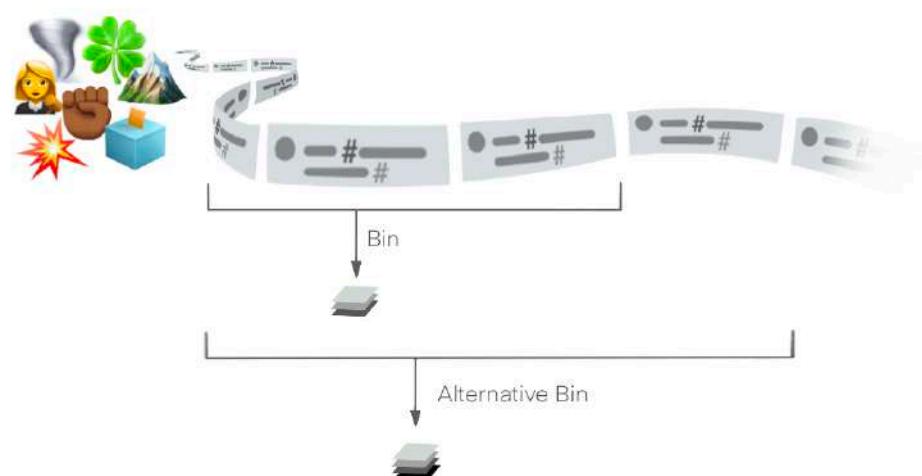
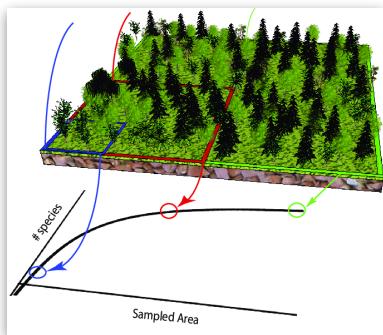
Species-Area Curve - SAC

How diversity scales with sampling size

$$\langle s(N) \rangle = s_{tot} \left(1 - \int d\eta \frac{\exp \frac{-(\eta - \mu)^2}{2\sigma^2}}{\sqrt{2\pi\sigma^2}} \left(\frac{\beta}{\beta + e^\eta N} \right)^\beta \right)$$

J. Grilli. Nature Communications 11, 4743 (2020)

S. Azaele, et al. Rev. Mod. Phys. 88, 035003 (2016)



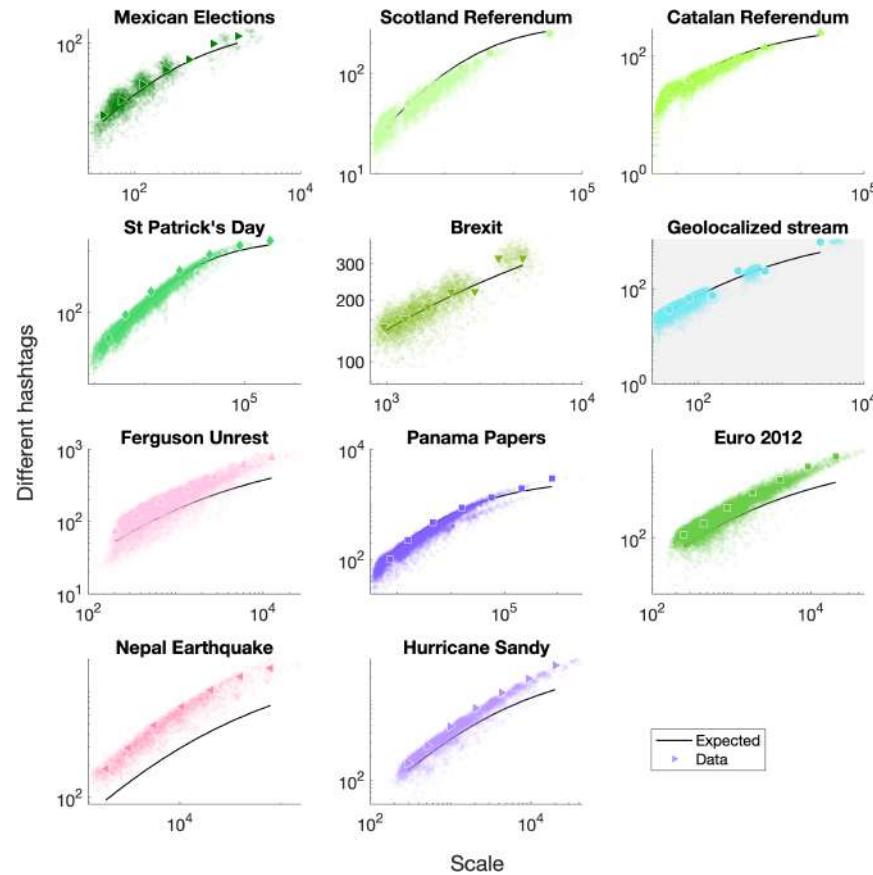
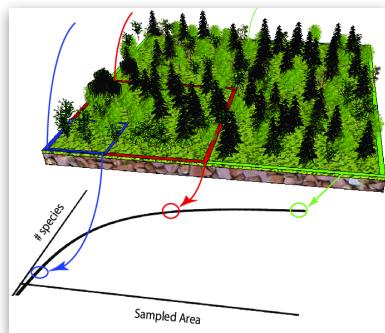
Species-Area Curve - SAC

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J. Grilli. *Nature Communications* 11, 4743 (2020)

S. Azaele, et al. *Rev. Mod. Phys.* 88, 035003 (2016)



Short-Term Abundance Change - STAC

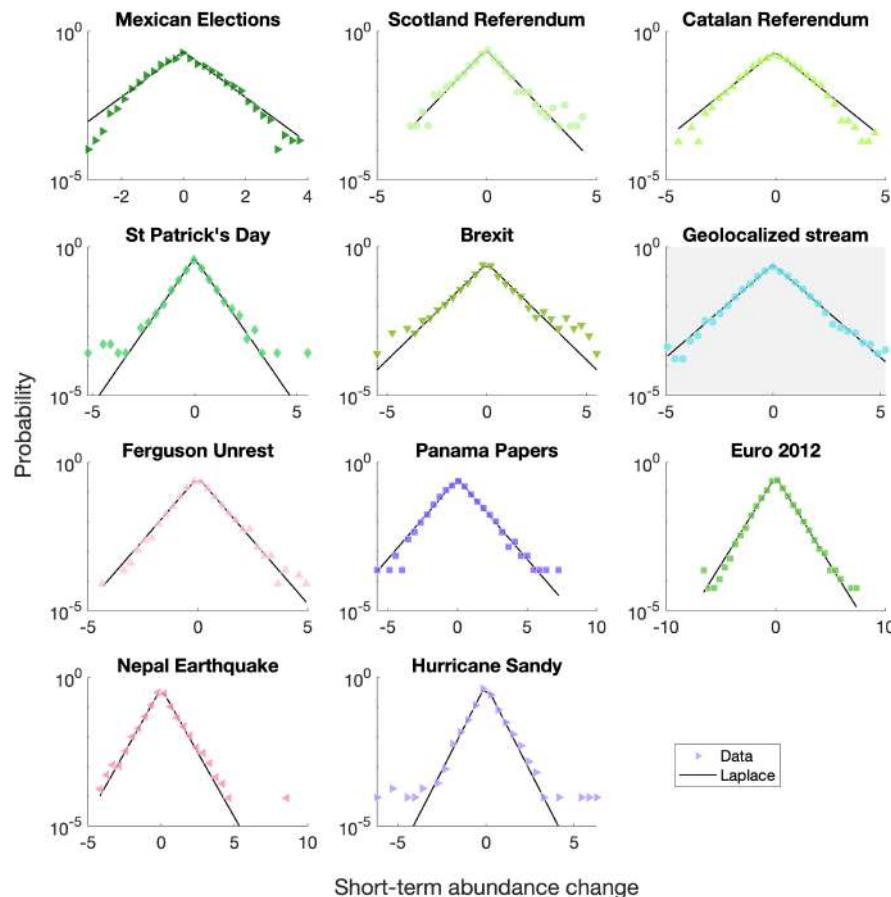
Distribution of ratio between
abundances at consecutive times

$$\lambda_{hb} = \log \left(\frac{x_{hb+1}}{x_{hb}} \right)$$

Laplace distribution

$$p(\lambda) = \frac{1}{2\gamma} \exp \left(\frac{-|\lambda - u|}{\gamma} \right)$$

Ji, et al. *Nature Microbiology* 5, 768–775 (2020)



Conclusions

Q: How do these laws apply to Information Ecosystems?

- Same patterns as in ecology!
- Patterns are universal



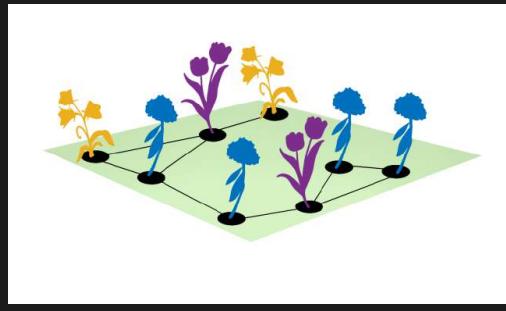
General conclusions

- ★ Reinforce the crucial role of interactions
 - Taking **structured interactions / multiple interaction types** into account change ecological behavior

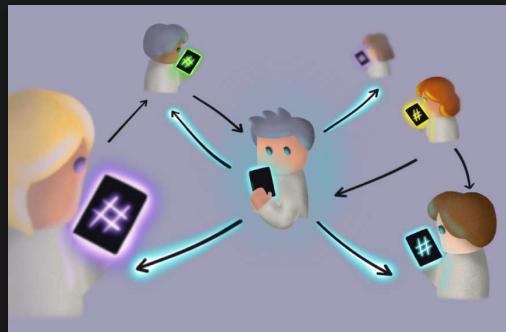
- ★ Take advantage of developments of one domain to understand another
 - Mapping ecological interactions on social networks to understand human behavior

Outlook

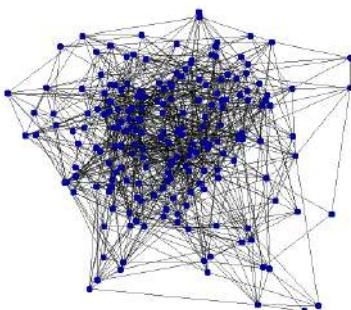
- ★ How higher-order interactions change the competition game
- ★ What are the underlying mechanisms of information ecosystems' patterns
- ★ How patterns change during events



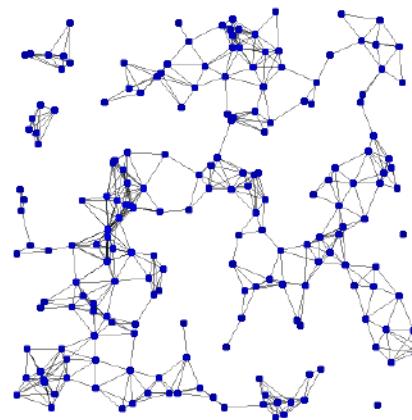
QUESTIONS?



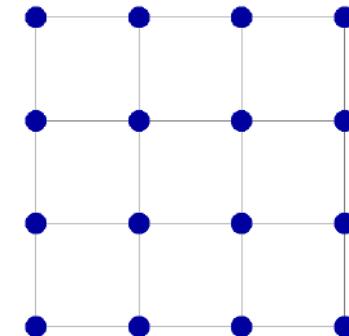
Erdős Rényi



Random Geometric Graph
(RGG)



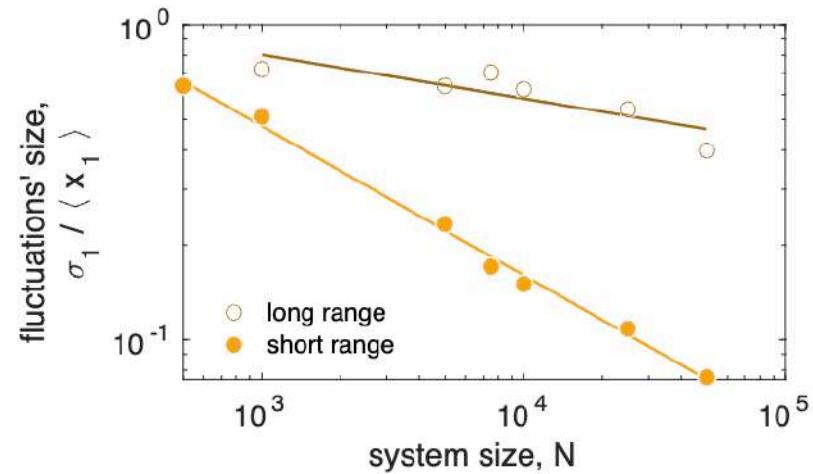
Lattice



Spatial structure



✓ Small fluctuations are noise



✓ Stability after a perturbation

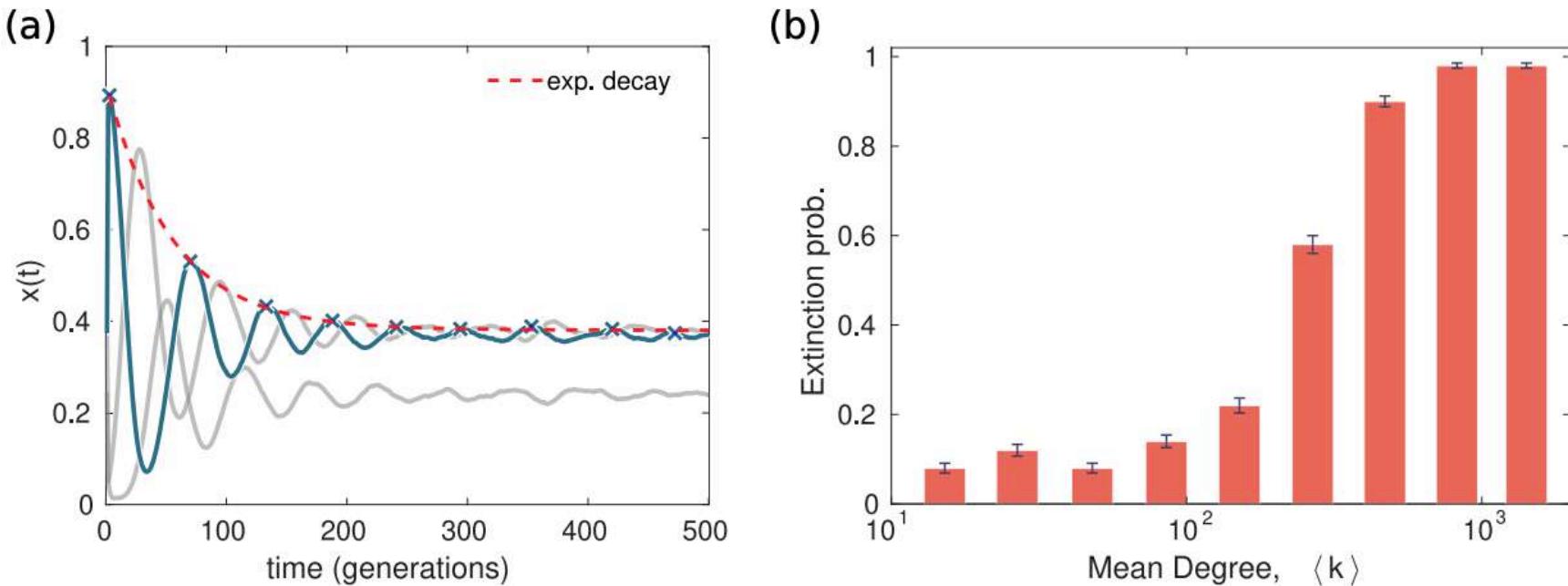
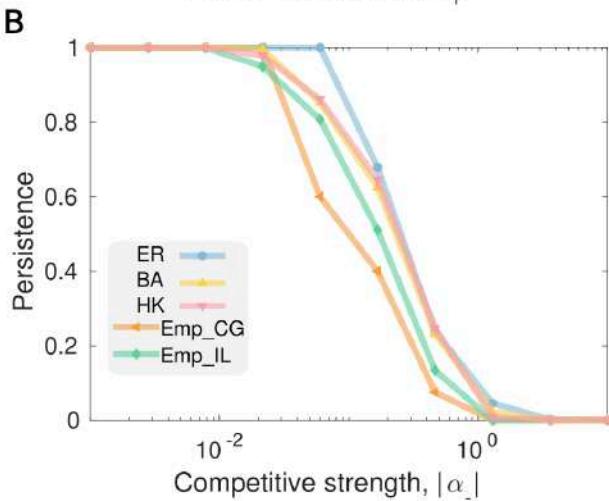
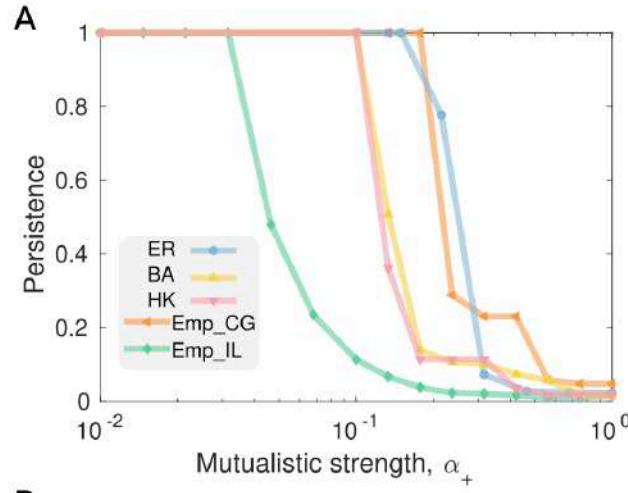
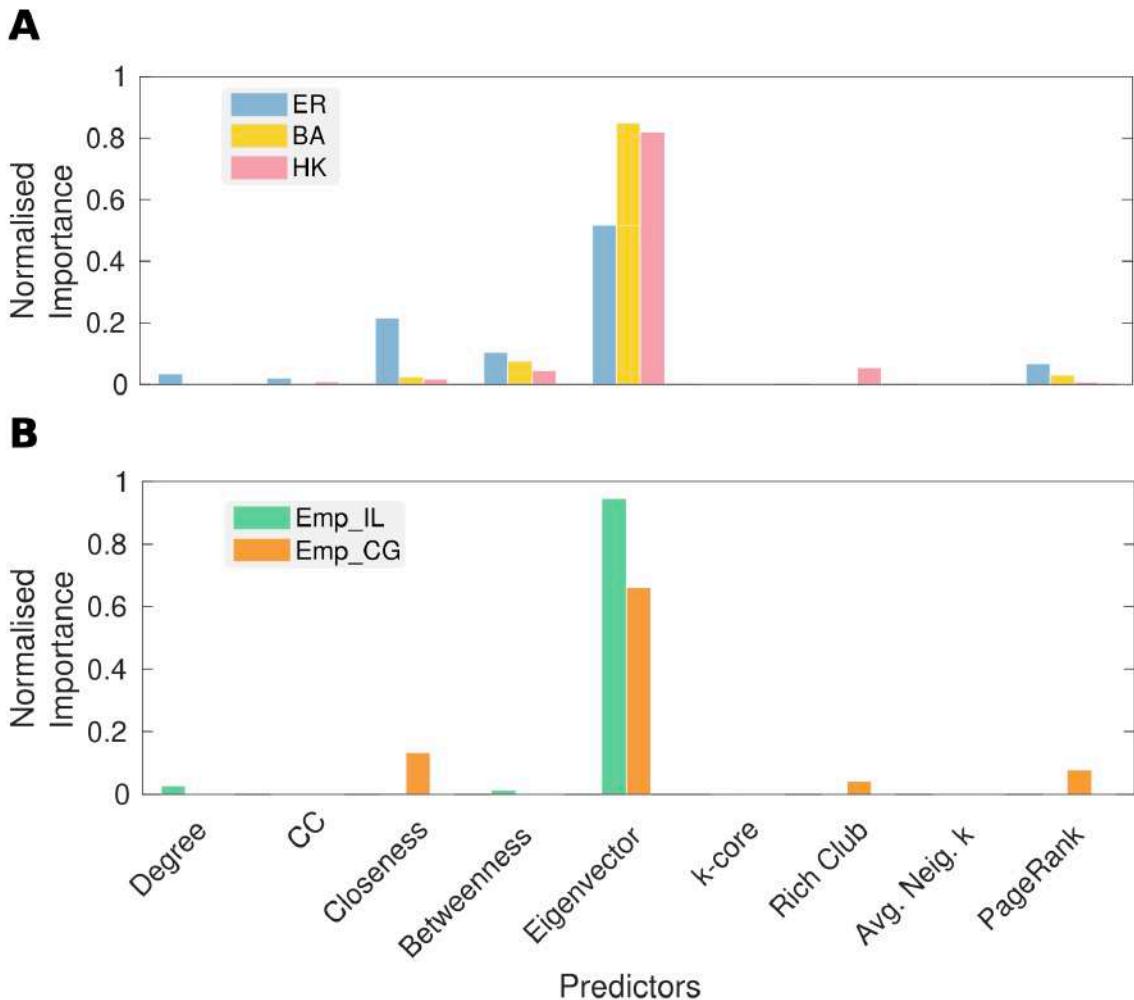


FIG. 5. (a) Time evolution of the recovery from a 90% pulse perturbation in a 3-species community for the dominance matrix H of Eq. (1). The relative abundance of one species (blue) is artificially modified from its equilibrium value to be the 90% of the whole population, whereas other species' relative abundances (in gray) are proportionally decreased. The simulation is performed in a RGG of 10^4 individuals and $R_{\text{RGG}} = 0.03$. The red line represents the fit of the local maxima of the relative abundance (blue crosses) to the function $ae^{-\alpha} + b$ with $\alpha = 0.018$, $a = 0.53$ and $b = 0.38$. (b) For the same setting than in (a), we have varied the interaction range to obtain how the extinction probability varies with the average degree. Each bar corresponds to the mean over 50 different networks with 95% confidence intervals shown as error bars.



Persistence decreases with high interaction strength in absolute value

Results: Mutualism



F.1 PERSISTENCE NOT EQUAL TO 50%

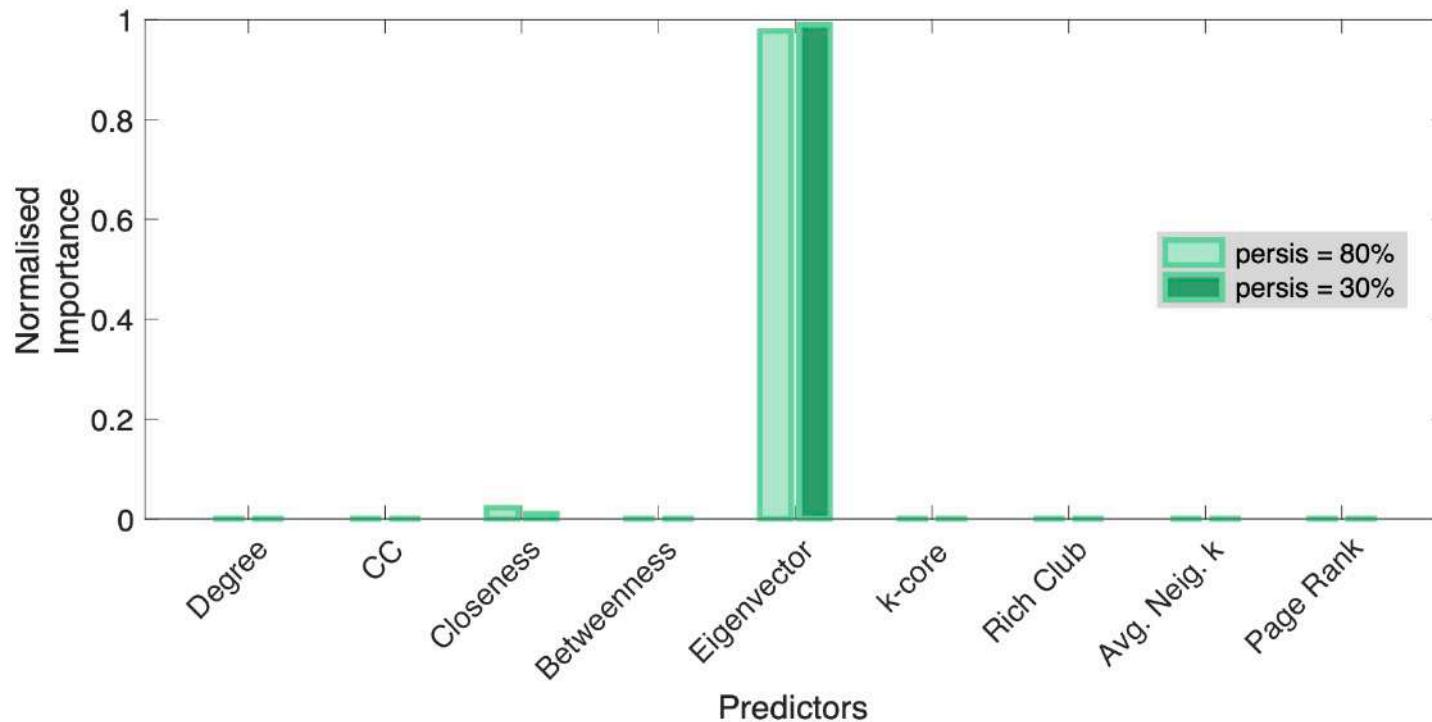
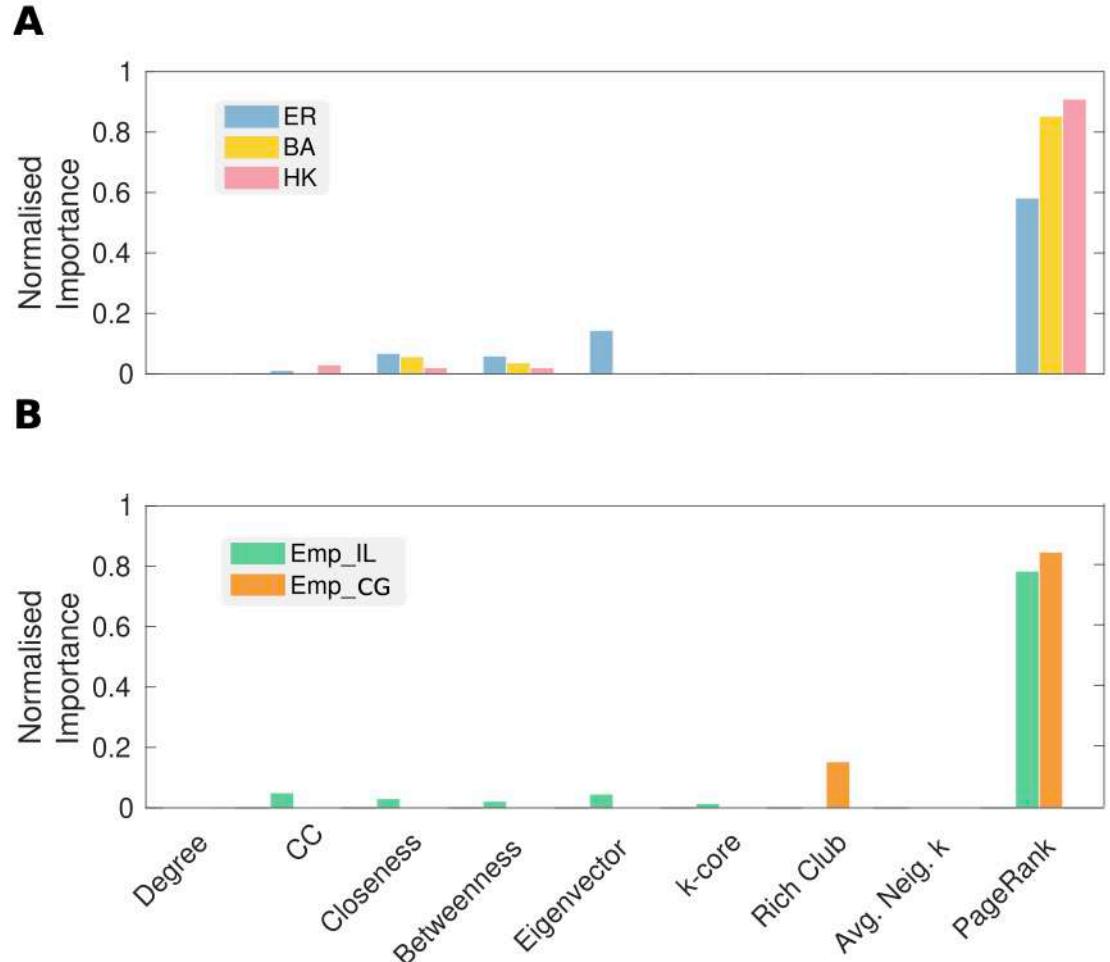
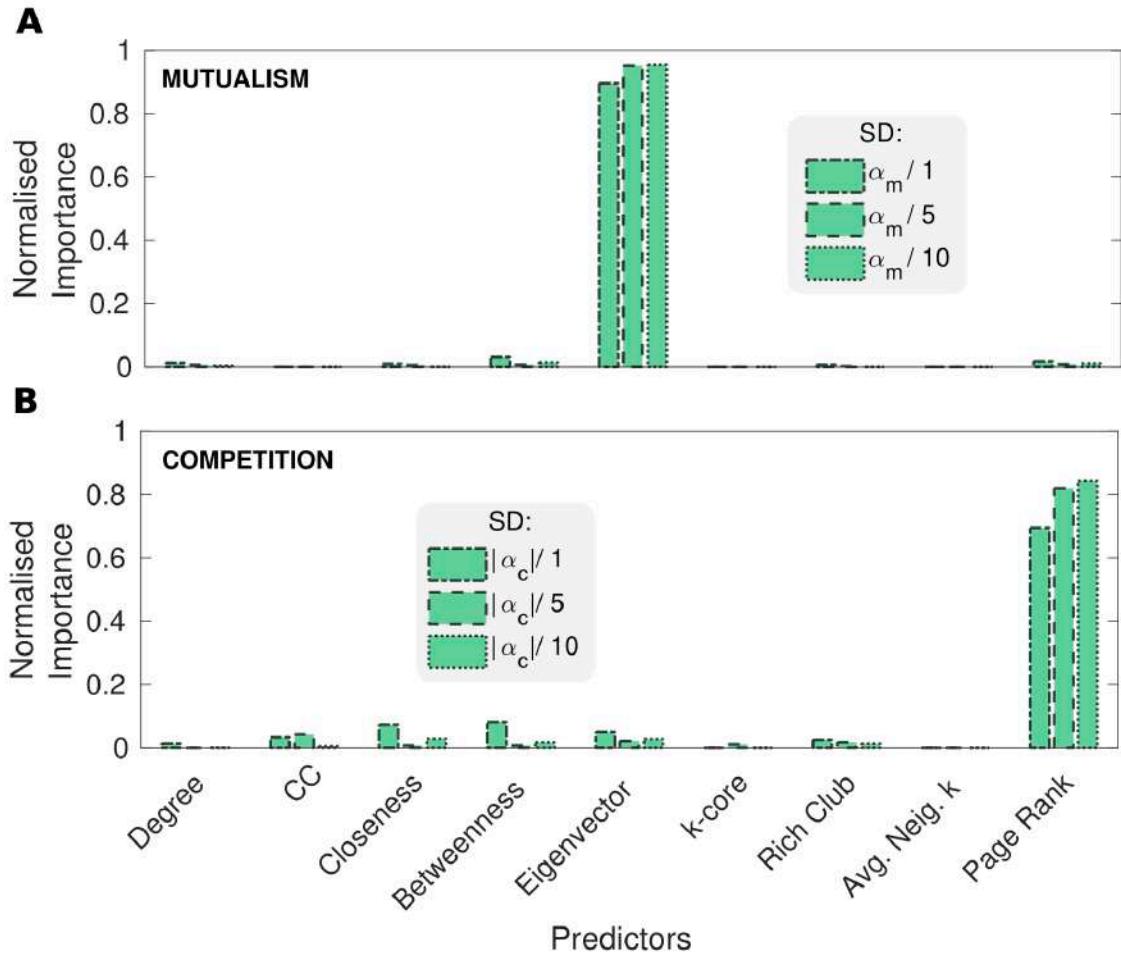


Figure F.1.1: Normalized importance for empirical network Emp_IL ($N = 1500$) with only mutualistic interactions when persistence is 30% ($\alpha_+ = 0.05$) and 80% ($\alpha_+ = 0.03$).

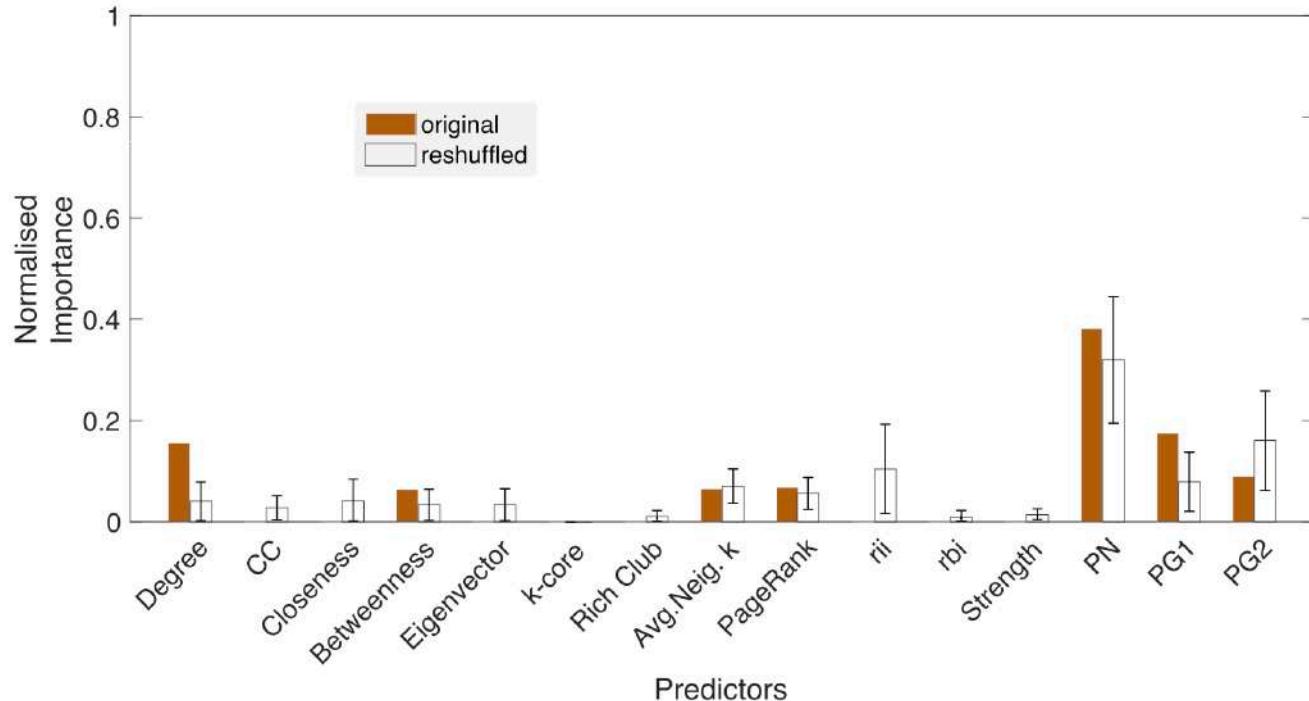
Results: Competition



The importance is not modified
when we add Gaussian noise
to α



Results: Mutualism & Competition



Catalan Referendum

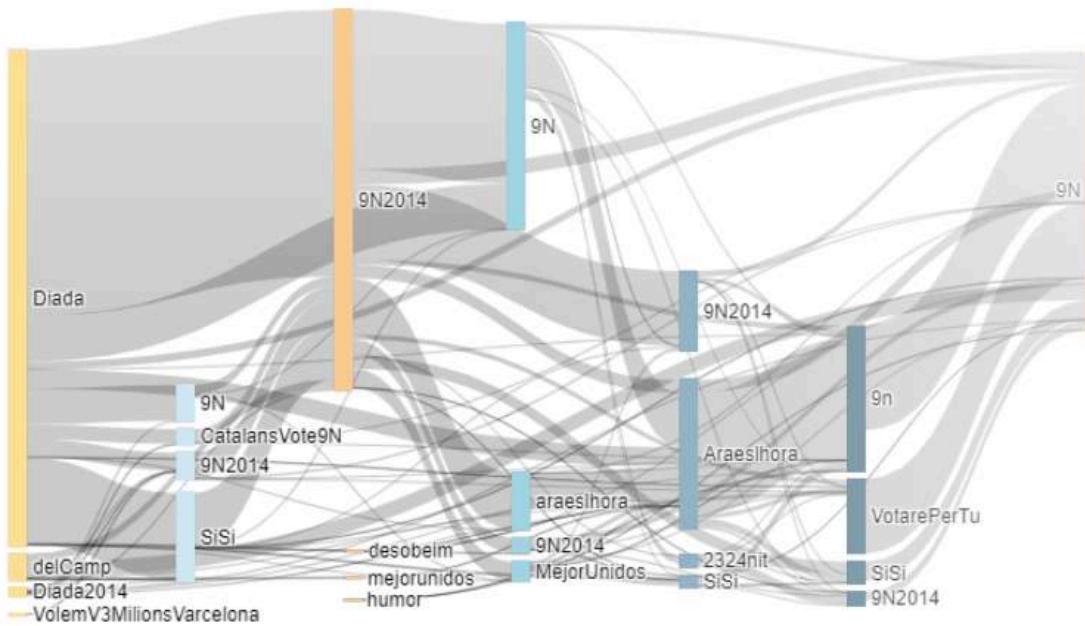


Figure 5.2.3: Topics' development for the Catalan referendum dataset is illustrated with an alluvial diagram. Boxes represent topics (communities in the co-occurrence network). Their colors encode the different periods, and their sizes are proportional to the number of tweets that belong to each topic. To ensure readability visibility, only the four largest topics are shown for each period. Flows represent the volume of tweets moving from one topic in a certain period to another topic in successive periods.

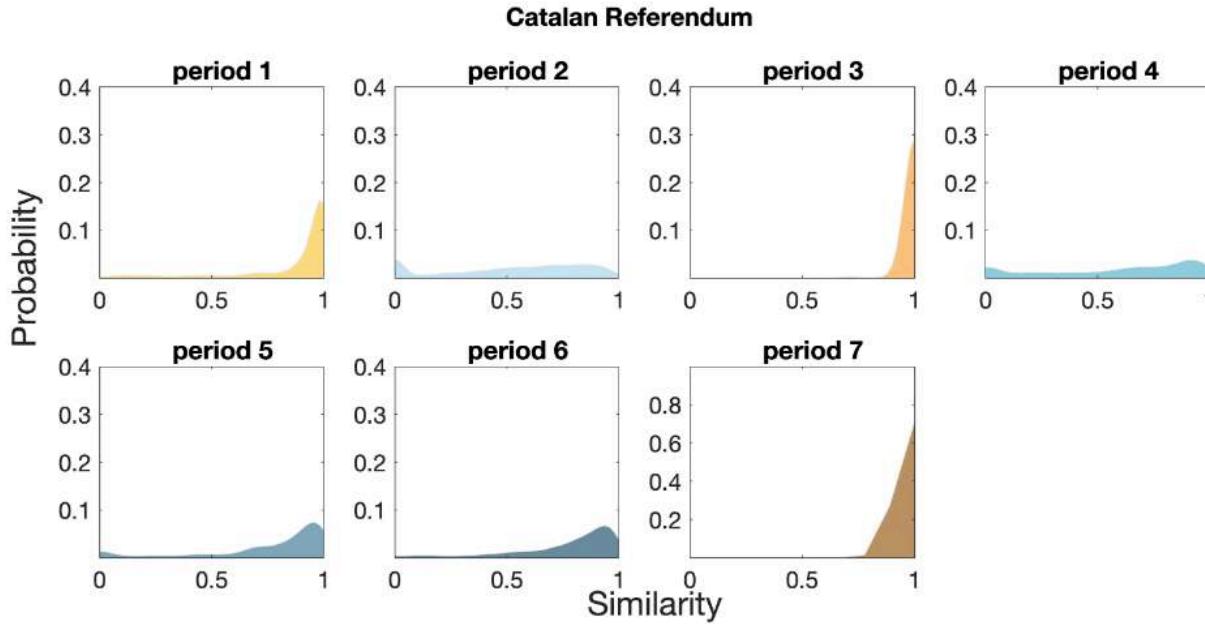


Figure 5.2.4: Cosine similarity distribution of user-topic vectors for the most active users of the Catalan referendum dataset. The cosine similarity has been calculated following Eq. 5.1. The most active users are the ones that have taken part in the discussion for at least 90% of the time and posted a minimum of 10 tweets within the whole period, which comprise around 400 accounts.

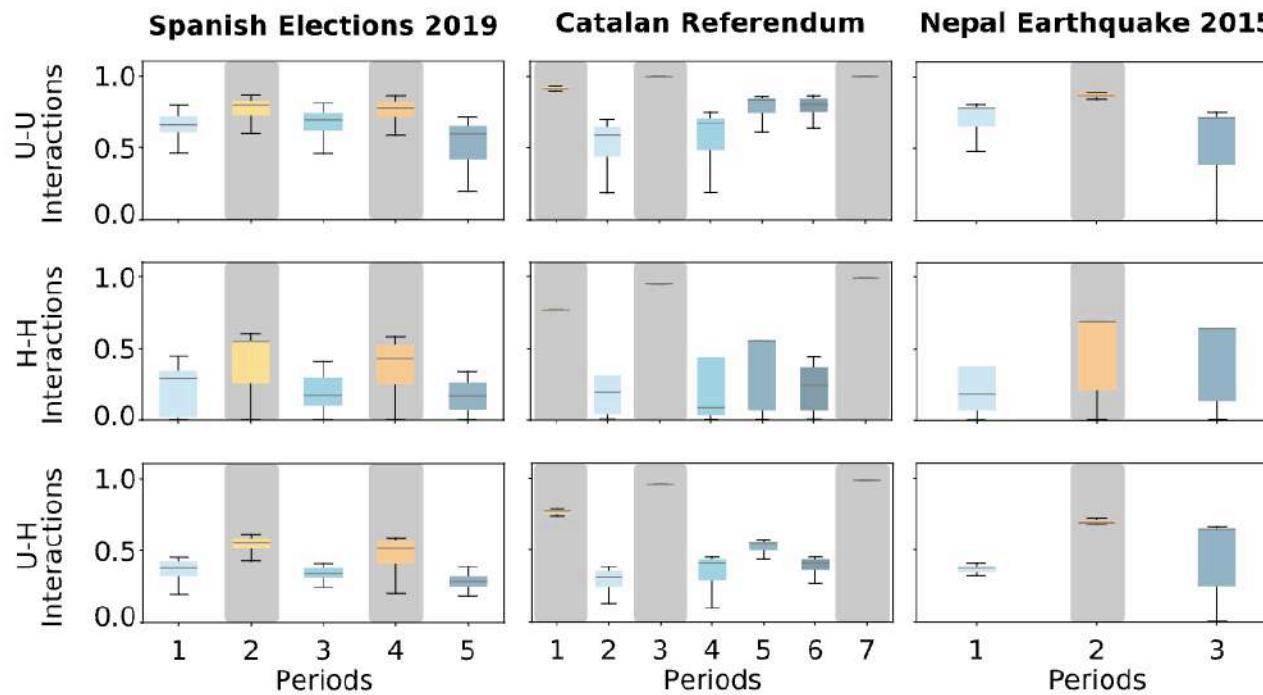
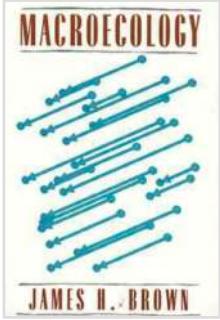


Figure 5.2.5: Strength estimations for hashtag-hashtag and user-user competitive interactions (first and second row), and user-hashtag mutualism (third row) for the 400 most active users and the hashtags they wrote. The interaction strength is the average value of the elements of the matrices β^{HH} , β^{UU} , and γ^{UH} .



Universal statistical laws across ecosystems

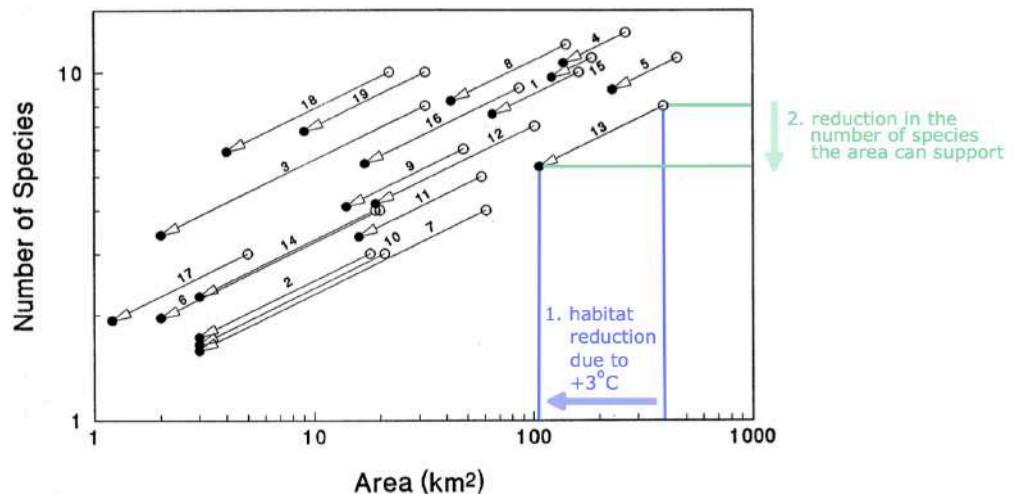
- Abundance
- Distribution
- Diversity

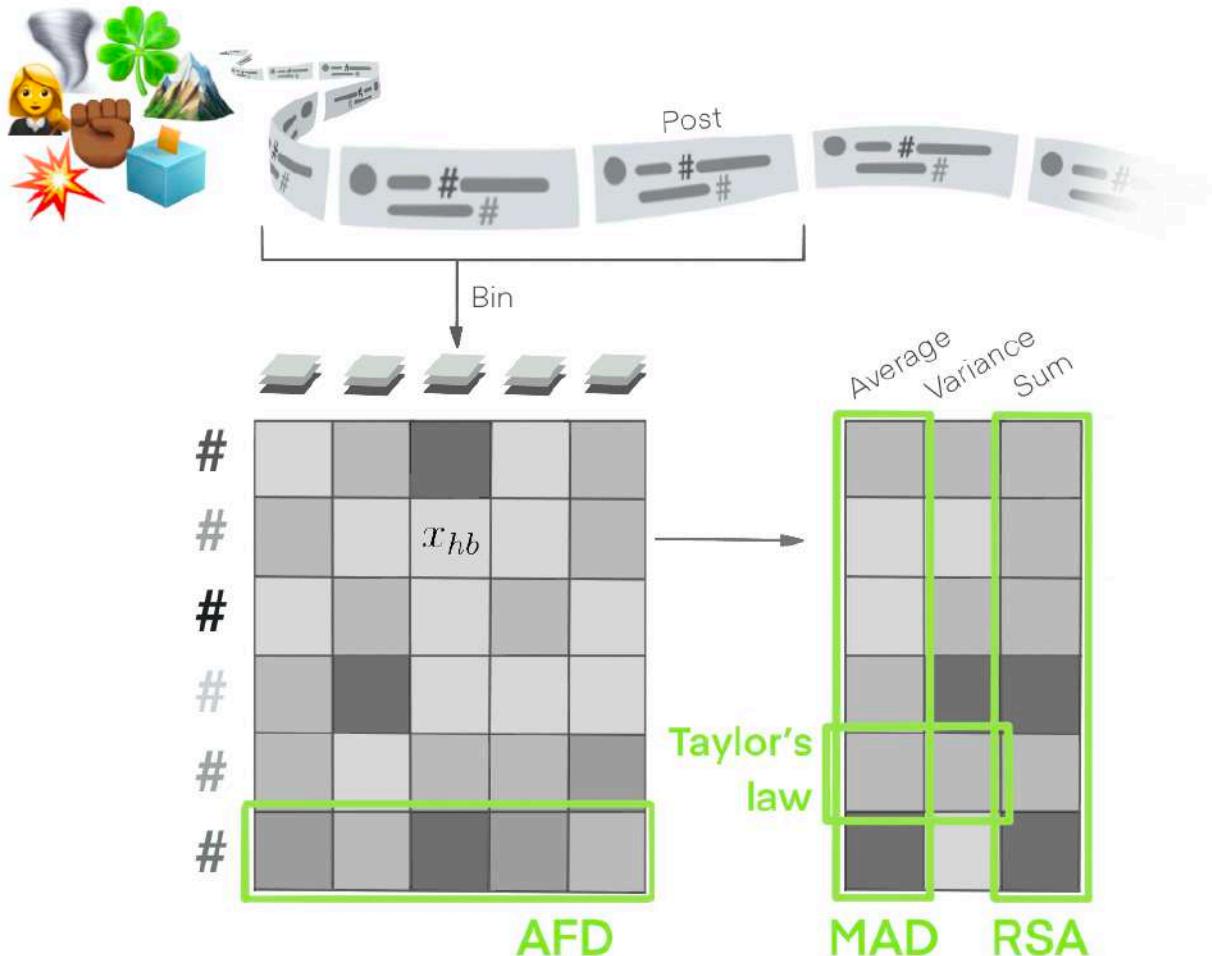


Important for:

- Finding mechanisms
- Modeling
- Health and prediction

- Species = Hashtags
- Abundance = Popularity
- Sampling



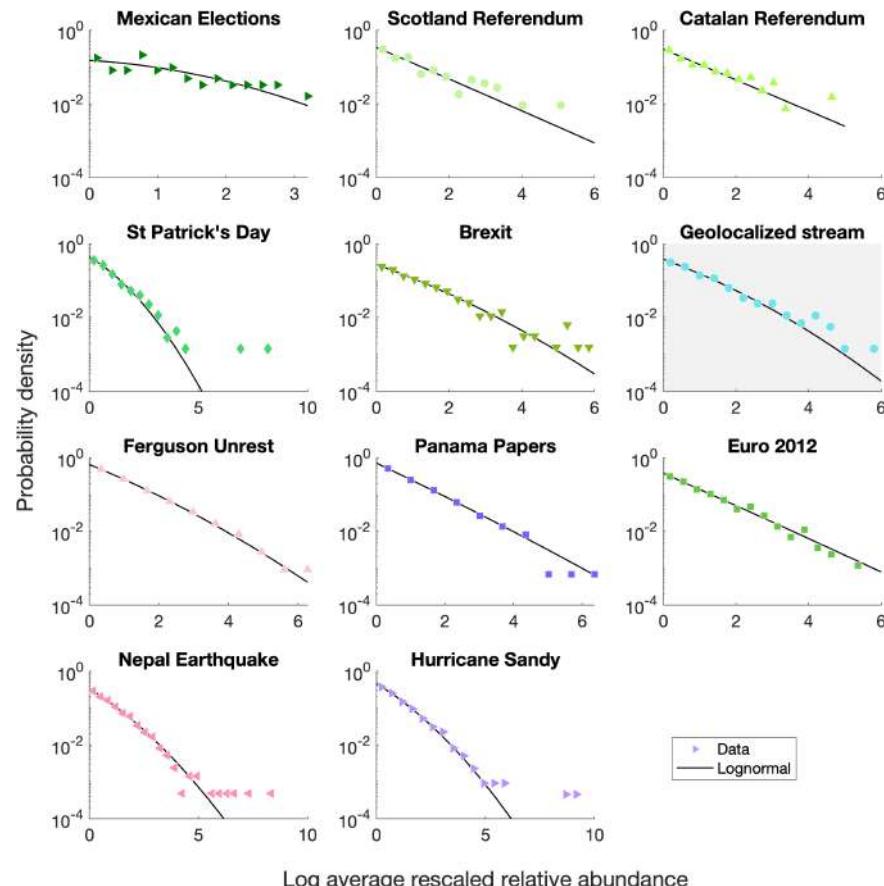
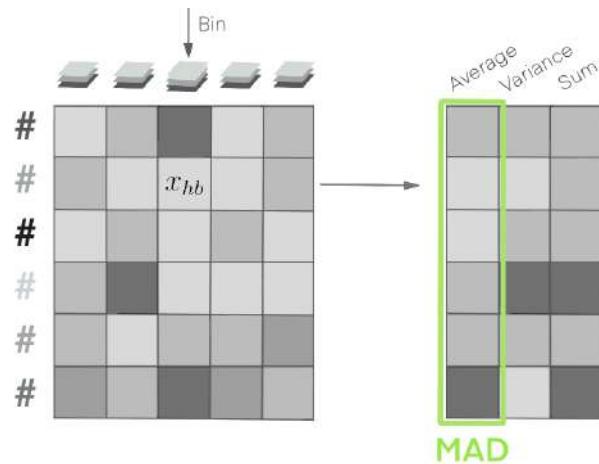


Mean Abundance Distribution - MAD

Lognormal distribution

J. Grilli. Nature Communications 11, 4743 (2020)

$$p(\bar{x}) = \frac{1}{\sqrt{2\pi\sigma^2\bar{x}}} \exp\left(-\frac{(\log\bar{x} - \mu)^2}{2\sigma^2}\right)$$

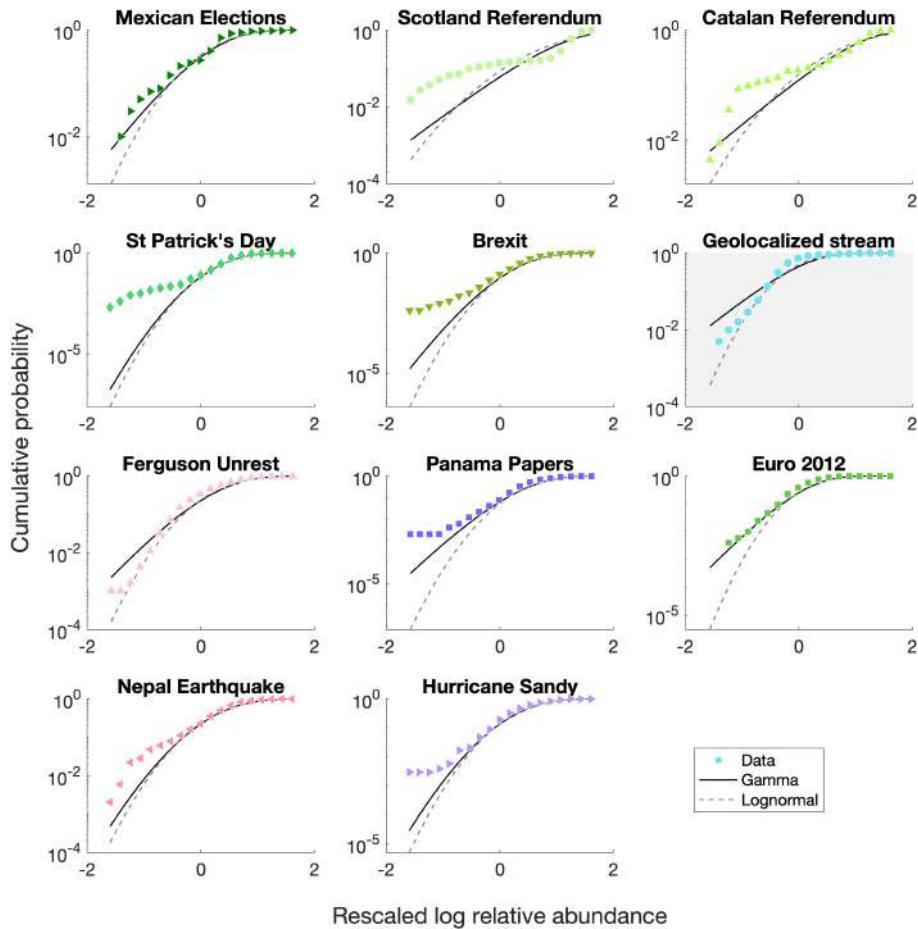
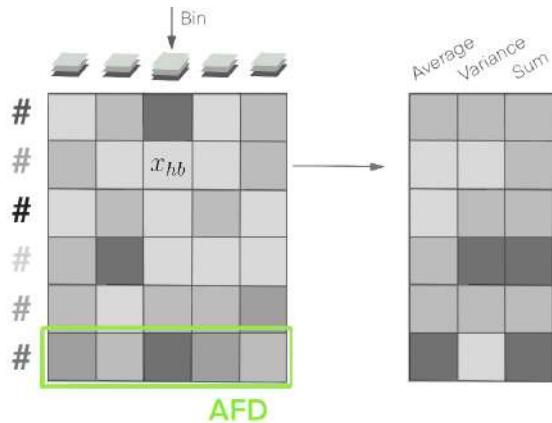


Abundance Fluctuations Distribution - AFD

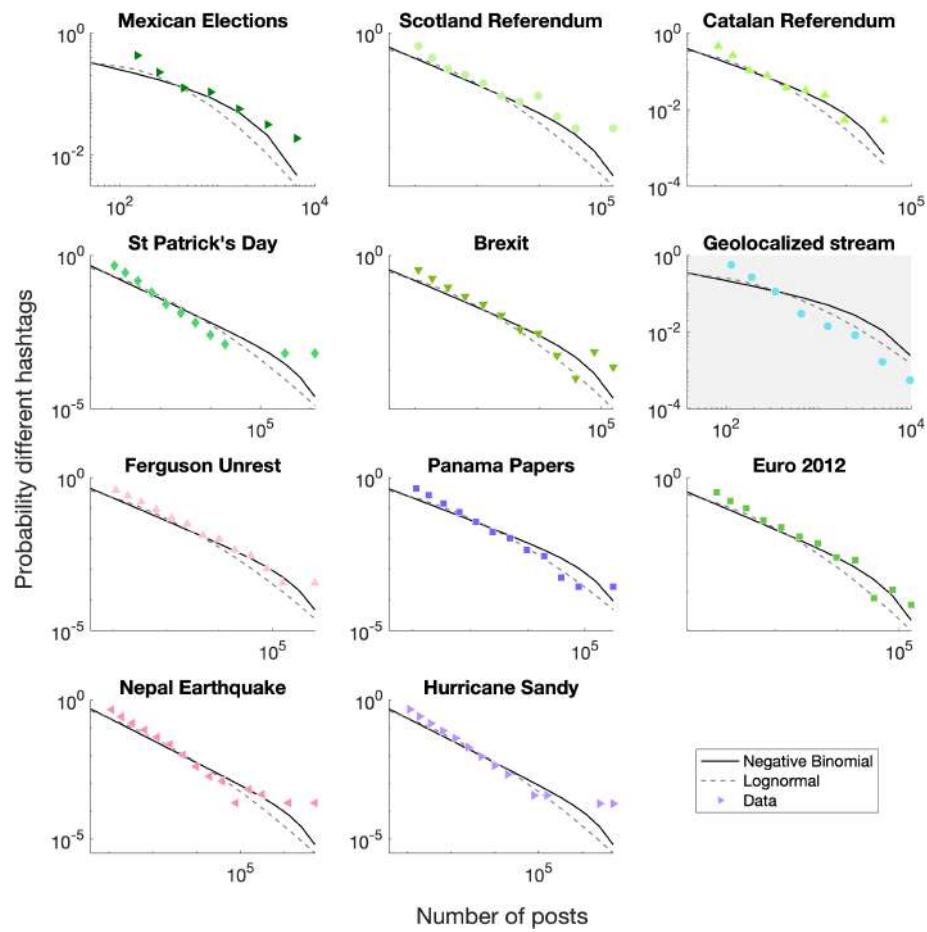
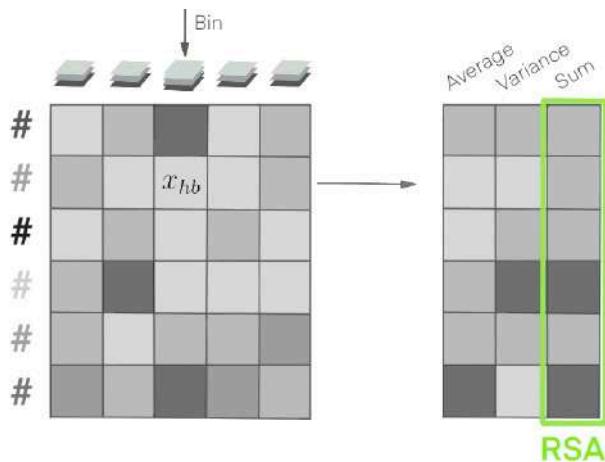
Gamma distribution

J. Grilli. *Nature Communications* 11, 4743 (2020)

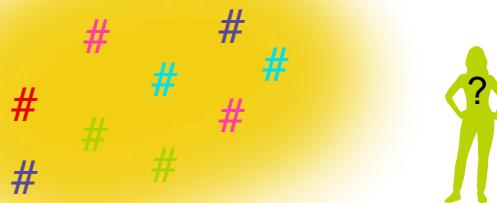
$$\rho_h(x) = \frac{1}{\Gamma(\beta_h)} \left(\frac{\beta_h}{\bar{x}_h} \right)^{\beta_h} \bar{x}^{\beta_h-1} \exp \left(-\beta_h \frac{x}{\bar{x}_h} \right)$$



Relative Species Abundance - RSA

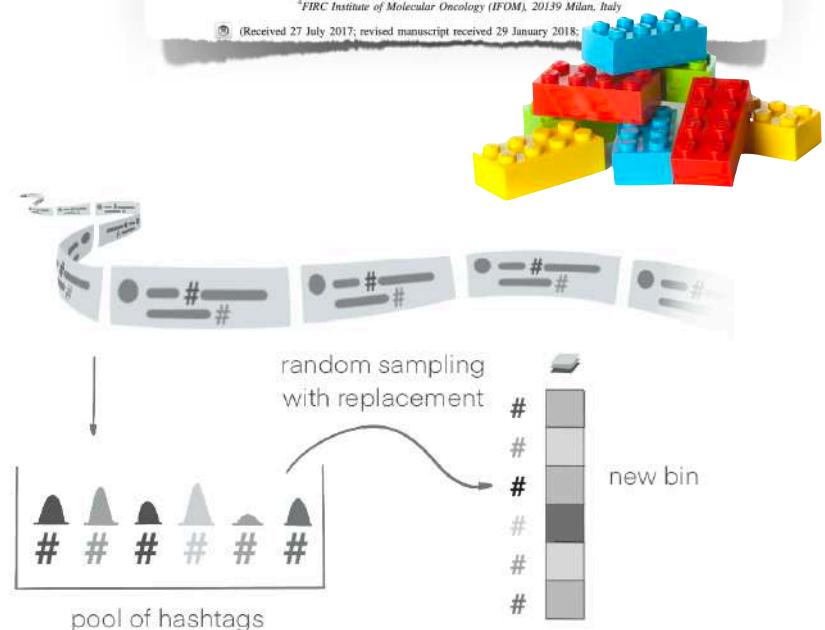


MODEL FOR HASHTAG SAMPLING

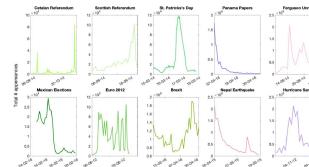


SUP: given a set of **# frequencies**,
multinomial random sampling

$$P(n_1, \dots, n_H, N_b) = \frac{N_b!}{\prod n_h!} \prod f_h^{n_h}$$



MODEL FOR HASHTAG SAMPLING



Taylor's Law



Mean Abundance Distribution *MAD*



Abundance Fluctuations Distribution *AFD*



Relative Species Abundances. *RSA*



Species-Area Curve *SAC*



Daily Abundance Change *STAC*



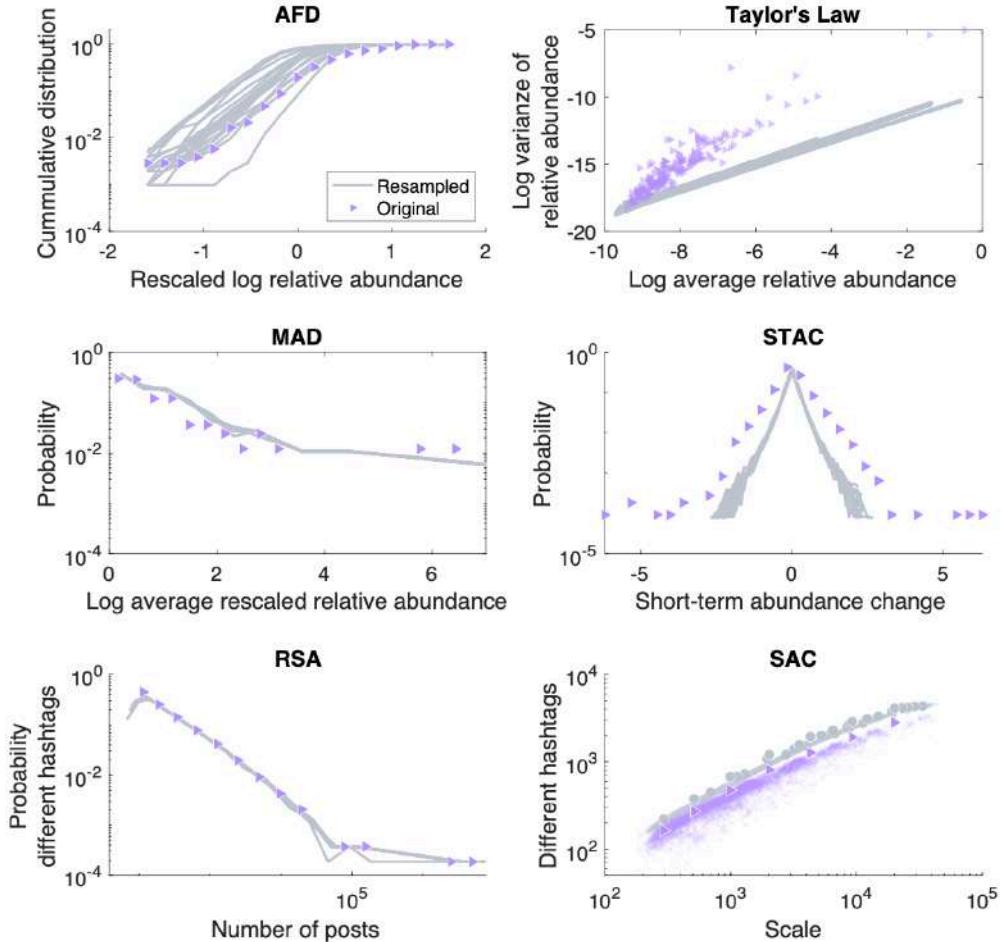


Figure 6.5.2: Macropatterns obtained by the multinomial random sampling model for the largest dataset (Hurricane Sandy) confronted with the original patterns, in colored dots. Each gray line corresponds to a resampling of the entire dataset.

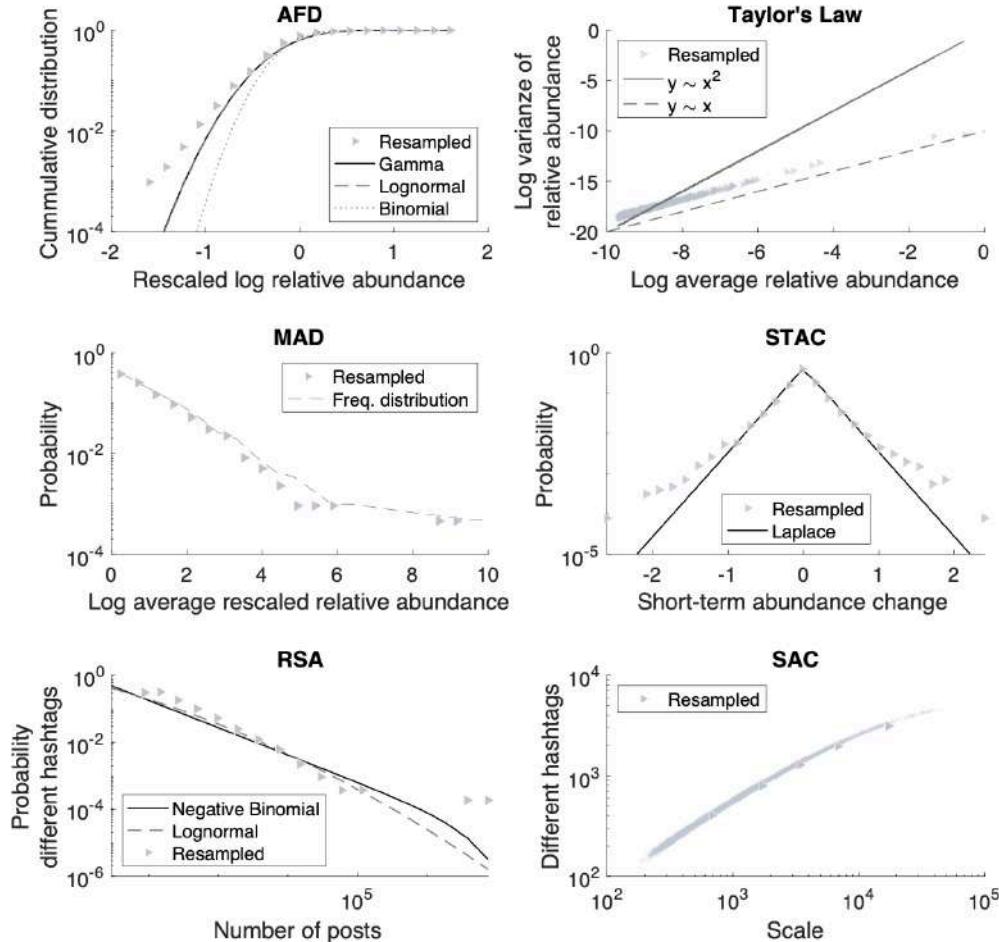


Figure H.3.1: Macropatterns (gray dots) obtained by multinomial random sampling of the largest dataset (Hurricane Sandy) and their fits to theoretical predictions. The dots correspond to one of the gray lines of Figure 6.5.2.