

CSC411 Assignment 3

Yue Guo

December 5, 2017

1 20 News Group

1.1 Top 3 Algorithms

Note: I have added a list of the names of all 20 categories in `load_data()` function for debugging purposes. This does not affect my classification algorithm.

1.1.1 Neural Network

1. Hyperparameter: number of layers

Method: K-fold cross validation

I have tried a single layer neural network vs multi-layered neural network. It turns out that the single neural network is the fastest and also most accurate.

2. Train/test loss

- Train accuracy 0.971451299275
- Test accuracy 0.632235793946

3. Reason to pick this algorithm

Neural network is commonly used in NLP, according to our lecture on neural networks. It is good at handling large data set with any features and produce a non-linear decision boundary.

4. My expectations

This meets my expectation because NNs are good at working with a large dataset with many features. When I increase the number of hidden layers, accuracy decreases. I think this is because it overfits.

1.1.2 Random forest

1. Hyperparameter: number of estimators

Method: K-fold cross validation

I have tried Ensemble with 10 to 150 estimators, and 150 works best after comparing results from cross validation.

2. Train/test loss

- Train accuracy 0.974721583878
- Test accuracy 0.59346787042

3. Reason to pick Random forest I have tried decision tree, with different parameters(entropy vs gini) and reduced features, but all end up overfitting. Random forest introduces more randomness and also scales the weights of misclassified data in each iteration. To see decision tree, please uncomment from line 272 to 290 in q1.py.

4. My expectations

This meets my expectations because Random Forest adds more randomness in each step, and ensemble method is more resistant to overfitting because it assigns weights to different features in each step. I also tried `decision_tree`, and it does not generalize well. The number of estimators learns better with a larger group of weak learners.

1.1.3 SVM - Best Classifier

1. Hypterparameter: `rand_state`

Method: K-fold cross validation

In the code, I have tried different `rand_state` and cross validated each. It turns out `rand_state = 0` is the best

2. Train/test loss

- Train accuracy 0.972511932119
- Test accuracy 0.691980881572

3. Reason to pick SVM Because of the natural of this given problem, it is still a classification problem. Using neural nets might be an overkill. SVM produces a linear decision boundary with a margin for two classes. It can be extended to multi-class using algorithms such as one-vs-all.

4. My expectations

SVM is the best out of all. I think it is because it has a linear decision boundary with a margin and does not overfit on training data. The test accuracy is close to single neuron neural net, but still higher.

5. Test confusion matrix

The most confused classes are class 16 `talk.politics.guns` and 18 `talk.politics.misc`

157.0	6.0	4.0	0.0	2.0	0.0	1.0	6.0	2.0	3.0	1.0	4.0	3.0	7.0	6.0	19.0	5.0	22.0	12.0	31.0
2.0	278.0	19.0	12.0	3.0	47.0	3.0	1.0	3.0	2.0	2.0	7.0	9.0	9.0	10.0	2.0	2.0	1.0	1.0	4.0
3.0	18.0	242.0	37.0	10.0	36.0	6.0	4.0	4.0	0.0	1.0	7.0	12.0	2.0	3.0	2.0	5.0	1.0	1.0	1.0
2.0	8.0	37.0	254.0	35.0	9.0	14.0	3.0	1.0	4.0	0.0	3.0	26.0	1.0	2.0	1.0	2.0	4.0	2.0	2.0
1.0	6.0	18.0	22.0	267.0	4.0	12.0	2.0	3.0	1.0	2.0	4.0	10.0	2.0	3.0	0.0	1.0	0.0	0.0	0.0
0.0	24.0	14.0	9.0	4.0	273.0	0.0	2.0	0.0	1.0	0.0	4.0	8.0	1.0	2.0	1.0	0.0	0.0	0.0	1.0
2.0	5.0	3.0	13.0	9.0	2.0	311.0	12.0	4.0	7.0	1.0	6.0	16.0	3.0	3.0	1.0	2.0	0.0	0.0	2.0
7.0	3.0	3.0	2.0	6.0	0.0	6.0	282.0	21.0	3.0	3.0	3.0	9.0	6.0	8.0	2.0	7.0	1.0	6.0	3.0
6.0	3.0	2.0	0.0	5.0	1.0	6.0	15.0	302.0	6.0	2.0	3.0	10.0	4.0	5.0	1.0	8.0	5.0	3.0	1.0
12.0	10.0	18.0	8.0	14.0	6.0	11.0	28.0	16.0	329.0	23.0	19.0	14.0	15.0	18.0	15.0	13.0	12.0	9.0	9.0
1.0	0.0	2.0	1.0	1.0	0.0	2.0	2.0	1.0	20.0	345.0	3.0	2.0	4.0	3.0	0.0	0.0	1.0	4.0	3.0
2.0	6.0	2.0	2.0	4.0	3.0	1.0	1.0	0.0	1.0	2.0	282.0	12.0	1.0	1.0	0.0	8.0	4.0	3.0	2.0
8.0	8.0	2.0	27.0	15.0	4.0	7.0	13.0	8.0	1.0	1.0	10.0	230.0	8.0	14.0	2.0	1.0	3.0	2.0	1.0
8.0	0.0	4.0	0.0	0.0	2.0	0.0	3.0	7.0	4.0	3.0	2.0	12.0	302.0	7.0	7.0	6.0	2.0	5.0	7.0
11.0	8.0	9.0	2.0	4.0	5.0	0.0	6.0	7.0	1.0	3.0	4.0	9.0	4.0	289.0	2.0	8.0	2.0	11.0	6.0
44.0	1.0	1.0	0.0	2.0	1.0	2.0	1.0	5.0	6.0	2.0	4.0	2.0	7.0	5.0	319.0	11.0	11.0	3.0	63.0
6.0	2.0	2.0	0.0	3.0	0.0	4.0	3.0	4.0	1.0	4.0	12.0	3.0	4.0	6.0	0.0	243.0	6.0	86.0	20.0
13.0	2.0	3.0	0.0	0.0	0.0	1.0	5.0	2.0	0.0	1.0	3.0	2.0	6.0	2.0	1.0	9.0	283.0	7.0	6.0
8.0	1.0	6.0	3.0	1.0	0.0	2.0	6.0	6.0	7.0	0.0	12.0	2.0	7.0	7.0	3.0	21.0	15.0	145.0	10.0
26.0	0.0	3.0	0.0	0.0	2.0	1.0	1.0	2.0	0.0	3.0	4.0	2.0	3.0	0.0	20.0	12.0	3.0	10.0	79.0

1.1.4 Bernoulli Baseline

1. Train/test loss

- Train accuracy 0.598727240587
- Test accuracy 0.457912904939

2 SVM

2.1 SVM test

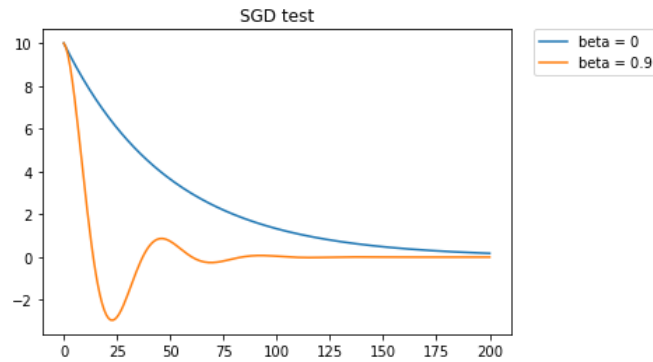


Figure 1: Plot of test SVM

2.2 SVM code

see code

2.3 SVM on MNIST

2.3.1 without momentum

1. Train loss= 0.400699029921
2. Test loss= 0.37243523202
3. classification accuracy on training set = 0.826985854189
4. classification accuracy on testing set = 0.818503401361
5. Plot of w

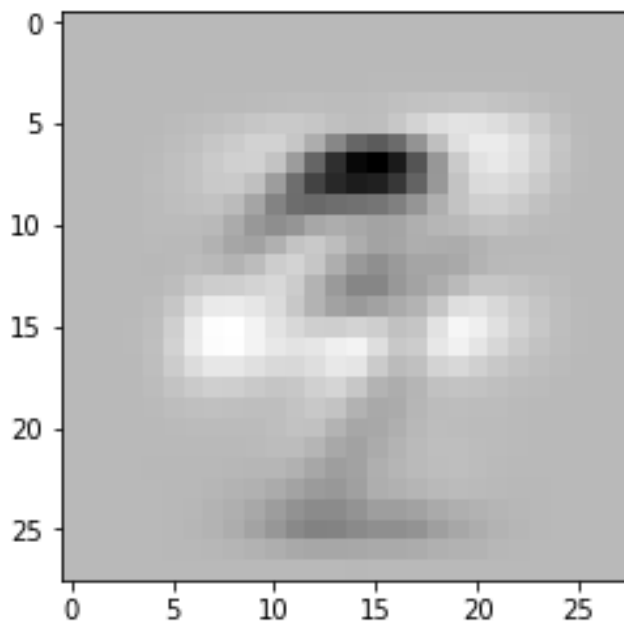


Figure 2: Plot momentum = 0

2.3.2 with momentum

1. Train loss = 0.424045274211
2. Test loss = 0.394698671058
3. classification accuracy on training set = 0.817555313747
4. classification accuracy on testing set = 0.809977324263
5. Plot of w

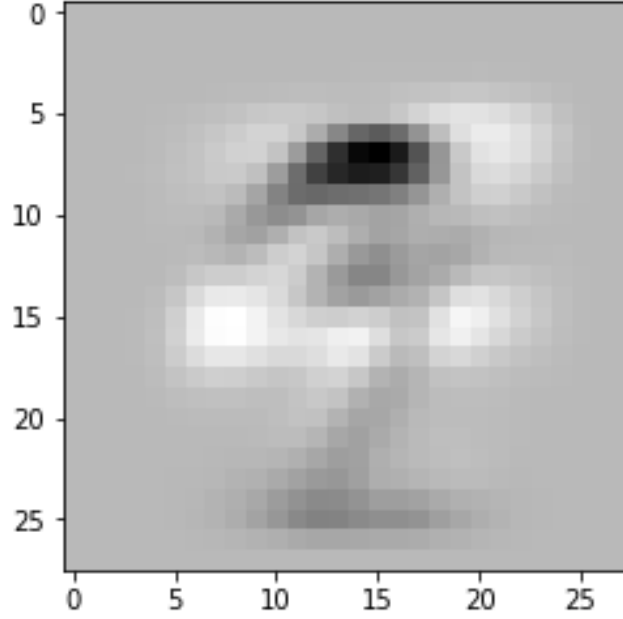


Figure 3: Plot momentum = 0.1

3 Kernels

3.1 Positive semidefinite and quadratic form

Assume K is symmetric, we can decompose K into $U\Lambda U^T$

$$x^T K x = x^T (U\Lambda U^T) x = (x^T U) \Lambda (U^T x)$$

Λ has the eigenvalues λ_i , and if K is positive, and all $\lambda_i > 0$,

$$x^T K x = \sum_{i=1}^d \lambda_i ([x^T U_i])^2 \geq 0$$

Then $x^T K x \geq 0$ for all x in \mathbb{R}^d iff K is positive semidefinite

3.2 Kernel properties

3.2.1 α

Define mapping $\phi(x) = \sqrt{\alpha}$, $\alpha > 0$, and the kernel $\langle \phi(x), \phi(y) \rangle = \alpha$. The resulting matrix K has item $K_{ij} = \alpha$, the matrix K has equal number of row and columns, and element is α . Since $\alpha > 0$, and all elements are equal, K is positive semidefinite

3.2.2 $f(x), f(y)$

$$K_{ij} = \langle \phi(x), \phi(y) \rangle,$$

define $\phi(x) = f(x), \forall f : \mathbb{R}^d \rightarrow \mathbb{R}$

define $\phi(y) = f(y), \forall f : \mathbb{R}^d \rightarrow \mathbb{R}$

Since $f(x)$ and $f(y)$ produce a scalar, $\langle \phi(x), \phi(y) \rangle = f(x) \cdot f(y)$

3.2.3 k1 and k2

If the gram matrix, K_1 of kernel k1 and gram matrix, K_2 of kernel k2 are positive semidefinite, by scaling them and adding each element, the new gram matrix of $a \cdot k_1(x, y) + b \cdot k_2(x, y)$, call it K , each element of K is positive since $a, b > 0$.

K is also symmetric because K_1 and K_2 are symmetric with the same dimension, and element wise addition and linear combination preserve the symmetric property.

3.2.4 $k(x, y) = \frac{k_1(x, y)}{\sqrt{k_1(x, x)}\sqrt{k_1(y, y)}}$

Let ϕ_1 be the mapping defined by k_1

We define a new mapping, ϕ for $k(x, y)$

We let $\phi(x) = \frac{\phi_1(x)}{\|\phi_1(x)\|}$

$$\begin{aligned}
 k(x, y) &= \langle \phi(x), \phi(y) \rangle \\
 &= \frac{\phi_1(x)}{\|\phi_1(x)\|} \cdot \frac{\phi_1(y)}{\|\phi_1(y)\|} \\
 &= \frac{\phi_1(x)}{\sqrt{\phi_1(x) \cdot \phi_1(x)}} \cdot \frac{\phi_1(y)}{\sqrt{\phi_1(y) \cdot \phi_1(y)}} \\
 &= \frac{\phi_1(x)}{(\sqrt{\phi_1(x)} \cdot \sqrt{\phi_1(y)})} \cdot \frac{\phi_1(y)}{(\sqrt{\phi_1(x)} \cdot \sqrt{\phi_1(y)})} \\
 &= \frac{\phi_1(x)}{\sqrt{\phi_1(x) \cdot \phi_1(y)}} \cdot \frac{\phi_1(y)}{\sqrt{\phi_1(x) \cdot \phi_1(y)}} \\
 k(x, y) &= \frac{k_1(x, y)}{\sqrt{k_1(x, x)}\sqrt{k_1(y, y)}}
 \end{aligned}$$

Therefore, there is a new mapping $\phi(x)$ that supports $k(x, y)$ and it is a kernel because $\phi(x)$ is the product of two kernel mappings