# CP

## **▼** DP tricks

### 1. 1D1D Optimize

- $ullet \ dp[i] = \min_{0 \leq j < i} dp[j] + w(j,i)$
- w(j,i) is cost whice need to satisfies quadrangle inequality:

$$\circ \ \ w(a,c) + w(b,d) \leq w(a,d) + w(b,c)$$
 with  $a \leq b \leq c \leq d$ 

· Example cost:

```
1. w(j,i)=b[j]\cdot a[i], providing that a[i]< a[j] and b[i]>b[j] satisfy for all i< j.   
2. w(j,i)=(x[i]-x[j])^2+C, providing that x[j]< x[i] satisfies for all j< i.   
3. w(j,i)=b[j]\cdot a[i]+b[j]^2\cdot a[i]^2+b[j]^3\cdot a[i]^3, providing that the following is true for all i< j: 0< a[i]< a[j] and b[i]>b[j]>0.
```

#### 2. Knuth

- $ullet \ dp[i][j] = \min_{i < k < j} dp[i][k] + dp[k][j] + w(j,i)$
- Call A(i,j) is optimize k give min dp[i][j] then:

$$A(i, j - 1) \le A(i, j) \le A(i + 1, j)$$

### 3. Divide and Conquer

- $\bullet \ dp[i][k] = \min_{j < i} dp[j][k-1] + w(j,i)$
- Call A(i,k) is optimize j give min dp[i][k] then:

$$\circ \ A(i,k) \leq A(i,k+1)$$

#### 4. ConvexHull Trick

#### 5. AlienTrick

- Often combine with above trick in binary search phase.
- ullet Problem: Use at most K so that the answer is max or min.
- Call ans(i) is the maximum when using **exactly** i then

$$\circ \ ans(i+1) - ans(i) <= ans(i) - ans(i-1).$$

#### 6. **SOS**

- Given a fixed array **A** of  $2^N$  integers, we need to calculate  $\forall x$  function F(x) = Sum of all A[i] such that **i** is a subset of **x**.
- 7. Open and Close Interval Trick
- 8. BerlekampMassey

## ▼ Data Structure

- 1. Walking on ST.
- 2. Segment Tree Beast
  - Solve problem with this type of query:
    - $\circ$  For all  $i \in [l,r]$  , change  $A_i$  to  $max(A_i,\,x)$ .
    - $\circ$  For all  $i \in [l,r]$  , change  $A_i$  to  $min(A_i,\,x)$ .
    - $\circ$  Get sum of  $A_i$

### 3. Splays Tree

• <a href="http://poj.org/problem?id=3580">http://poj.org/problem?id=3580</a>

## **▼** Tree

#### 1. DSU on Tree

- Answer how many vertices in the subtree of vertex v has some property in time O(nlogn).
- 2. **HLD**:
  - Update and query on path from vertex u to v.
- 3. Compress Tree:
  - Only consider important node.
- 4. DP on Tree

- O(n^3) seem but O(n^2).
- <a href="https://usaco.guide/adv/comb-sub#problem-cf-815C">https://usaco.guide/adv/comb-sub#problem-cf-815C</a>

# **▼** Others

- Divide and Conquer Tricks when you want to **ignore 1 element**.
  - Problem: <a href="https://codeforces.com/gym/104555/problem/D">https://codeforces.com/gym/104555/problem/D</a>.
- GCD
  - Inclusion Exclusion : <a href="https://codeforces.com/contest/1559/problem/E">https://codeforces.com/contest/1559/problem/E</a>

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