

Assignments (CS551 DL 2021)

Q1. Find out the eigen value and eigen vector of a given matrix using python library

$X = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 4 \\ 4 & 5 & 6 \end{bmatrix}$

Q2. Find the dot product of two vectors $v = [1,2]$ and $w = [1,1]$

Q3. Find out the trace of a matrix given below using python.

$X = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$

Q2: Write a python program to perform the following set of operations on the augmented matrix derived from the system of linear equations given below.

- (a) Generate Row Echelon Form (**REF**)
- (b) Generate Reduced Row Echelon Form (**RREF**)
- (c) Perform **Gaussian elimination** to solve the below system of linear equation
- (d) Perform **Gauss–Jordan elimination** to solve the below system of linear equation

Test Case:

Input:

$X + y + 2z = 9$
 $2x + 4y - 3z = 1$
 $3x + 6y - 5z = 0$

Output:

$x = 1, y = 2, z = 3$

Matrix factorization using SGD

Q2. Assume R is a $m \times n$ matrix with each entry is an integer in $[0, 5]$ i.e. moving rating m users have given to n movies. Find the factorization of matrix $R = P^T Q$ using approximation method.

Where P and Q have size $(k \times m)$ and $(k \times n)$ and $k < m$ and $k < n$.

Update rule for P_c and Q_c (column vectors of P, Q respectively) are as follows:

$P_c \leftarrow P_c + s * (e_{Q_c} - t * P_c)$

$Q_c \leftarrow Q_c + s * (e_{P_c} - t * Q_c)$

Where s, t are from $[0, 1]$. $e = R_{\{i, j\}} - (Pc)^T Qc$.

$$E = \|R - P^T Q\|_F$$

1) Find k, s and t for least E . (use hyperopt or sklearn library for gridsearch.)

2) Plot graph for E vs k .

*Each user (P_c) and movie (Q_c) are defined by k features (k sized 1-d vector) which best describes their characteristics in latent space.

Q3. Find the partial derivative of $\|LU - A\|_F$ (a function of squared frobenius norm) with respect to U . Where L, U and A are all matrices.

Linear Regression

Link: <https://raw.githubusercontent.com/manishbhnau/Repo/master/Advertising.csv>

Q1. Find the linear regression model which best predicts the dependent variable ("sales") on validation dataset.

- Divide data in 80-20 % for training and testing set.
- Use 10 fold cross validation set (10% of training dataset).

Find regression co-efficients and intercepts. Report confusion matrix on test dataset.

Q2. This question involves the use of multiple linear regression on the Auto data set (<https://www.kaggle.com/uciml/autompg-dataset>).

Compute the matrix of correlations between the variables

- Fit a least square linear model, You will need to exclude the name variable which is qualitative.
- Use the multiple linear regression with mpg as the response and all other variables except name as the predictors.

Logistic Regression:

Q5. The objective is to build a classifier that can predict whether an application will be admitted to the university (class 0) or not (class 1).

Dataset details :The data consists of marks of two exams for 100 applicants. The target value takes on binary values 1,0. 1 means the applicant was admitted to the university whereas 0 means the applicant didn't get an admission. Download data from the following link.

Dataset link:

<https://github.com/animesh-agarwal/Machine-Learning/blob/master/LogisticRegression/data/marks.txt>

- (a) Calculate precision, recall, accuracy and f1 score.
- (b) Visualize the confusion matrix using Heatmap.