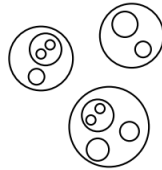


Problem 1. [8] Consider the drawing below.



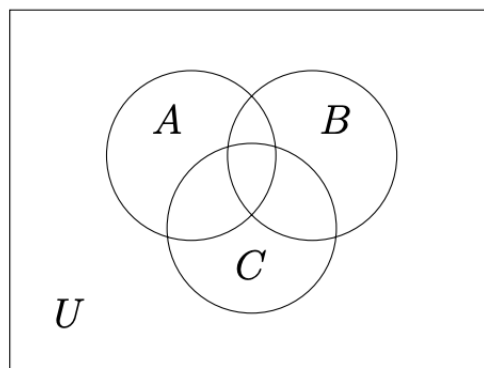
Let X be the set of circles in the drawing and define a binary relation \sim on X by

$$x \sim y \Leftrightarrow x \text{ and } y \text{ contain the same number of circles.}$$

The relation \sim is actually an equivalence relation on X (you do not need to prove this).

- How many elements are there in the set X ? Just write the number, no explanation needed.
- How many equivalence classes does the equivalence relation have? Write the number and then provide an explanation.
- How many elements does each equivalence class have? Just write the numbers, no explanation needed.

Problem 2. [3] Clearly shade the set $(A \cup B) \cap (A \cap C)^c \cap (B \cup C)^c$ in the following Venn diagram. Do your rough work outside this diagram and only shade your final answer in the below diagram.



Problem 3. [9] Determine whether or not each of the following relations is a partial order on $\mathbb{N} \times \mathbb{N}$. If it is not a partial order then give a counterexample. If it is a partial order then

- provide a proof,
- check if it is also a total order,
- find all maximal and minimal elements if it has any,
- find the greatest and least elements if it has.

(a) $(a, b) \leq (c, d)$ if and only if $a \leq c$.

(b) $(a, b) \leq (c, d)$ if and only if $a \leq c$ and $b \geq d$.