

Assignment-3

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Abstract—This document explains the concept of balancing the chemical equations using linear algebra.

Download all python codes from

<https://github.com/vipulmalik8569/MT-EE5609>

and latex-tikz codes from

<https://github.com/vipulmalik8569/MT-EE5609>

1 PROBLEM

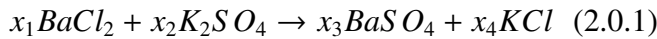
Write the balanced chemical equations for the following reaction :



2 SOLUTION

We know that the number of atoms of each element remains the same, before and after a chemical reaction.

Equation (1.0.1) can be written as:



Element wise contribution in forming the respective chemical compound can be written in the form of equation as :

$$Ba : x_1 + 0x_2 - x_3 - 0x_4 = 0 \quad (2.0.2)$$

$$Cl : 2x_1 + 0x_2 - 0x_3 - 1x_4 = 0 \quad (2.0.3)$$

$$K : 0x_1 + 2x_2 - 0x_3 - 1x_4 = 0 \quad (2.0.4)$$

$$S : 0x_1 + 1x_2 - 1x_3 - 0x_4 = 0 \quad (2.0.5)$$

$$O : 0x_1 + 4x_2 - 4x_3 - 0x_4 = 0 \quad (2.0.6)$$

In matrix form this can be written as:

$$\begin{pmatrix} 1 & 0 & -1 & 0 \\ 2 & 0 & 0 & -1 \\ 0 & 2 & 0 & -1 \\ 0 & 1 & -1 & 0 \\ 0 & 4 & -4 & 0 \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \quad (2.0.7)$$

Using Gaussian Elimination method :

$$\xleftrightarrow{R_2 \leftrightarrow R_5} \begin{pmatrix} 1 & 0 & -1 & 0 & : & 0 \\ 0 & 4 & -4 & 0 & : & 0 \\ 0 & 2 & 0 & -1 & : & 0 \\ 0 & 1 & -1 & 0 & : & 0 \\ 2 & 0 & 0 & -1 & : & 0 \end{pmatrix} \quad (2.0.8)$$

$$\xleftrightarrow{R_5 \leftarrow 2R_1 - R_5} \begin{pmatrix} 1 & 0 & -1 & 0 & : & 0 \\ 0 & 4 & -4 & 0 & : & 0 \\ 0 & 2 & 0 & -1 & : & 0 \\ 0 & 1 & -1 & 0 & : & 0 \\ 0 & 0 & -2 & 1 & : & 0 \end{pmatrix} \quad (2.0.9)$$

$$\xleftrightarrow{\begin{matrix} R_3 \leftarrow 2R_3 - R_2 \\ R_4 \leftarrow 4R_4 - R_2 \end{matrix}} \begin{pmatrix} 1 & 0 & -1 & 0 & : & 0 \\ 0 & 4 & -4 & 0 & : & 0 \\ 0 & 0 & 4 & -2 & : & 0 \\ 0 & 0 & 0 & 0 & : & 0 \\ 0 & 0 & -2 & 1 & : & 0 \end{pmatrix} \quad (2.0.10)$$

$$\xleftrightarrow{R_5 \leftrightarrow R_5} \begin{pmatrix} 1 & 0 & -1 & 0 & : & 0 \\ 0 & 4 & -4 & 0 & : & 0 \\ 0 & 0 & 4 & -2 & : & 0 \\ 0 & 0 & -2 & 1 & : & 0 \\ 0 & 0 & 0 & 0 & : & 0 \end{pmatrix} \quad (2.0.11)$$

$$\xleftrightarrow{R_4 \leftarrow 2R_4 - R_3} \begin{pmatrix} 1 & 0 & -1 & 0 & : & 0 \\ 0 & 4 & -4 & 0 & : & 0 \\ 0 & 0 & 4 & -2 & : & 0 \\ 0 & 0 & 0 & 0 & : & 0 \\ 0 & 0 & 0 & 0 & : & 0 \end{pmatrix} \quad (2.0.12)$$

By solving this we get :

$$x_1 = x_2 = x_3 = 1, x_4 = 2 \quad (2.0.13)$$

Hence by putting the values of x_1, x_2, x_3, x_4 in equation (1.0.1) we get our balanced chemical equation as follows :

