

## Using Manhattan Distance for 8 puzzle game

### Input:

```
import heapq
```

```
class PuzzleState:
```

```
    def __init__(self, board, g, h):
```

```
        self.board = board # The current state of the board
```

```
        self.g = g # Cost to reach this node (depth)
```

```
        self.h = h # Heuristic cost (Manhattan distance)
```

```
        self.f = g + h # Total cost ( $f(n) = g(n) + h(n)$ )
```

```
    def __lt__(self, other):
```

```
        return self.f < other.f # For priority queue to sort by  $f(n)$ 
```

```
def print_board(board):
```

```
    """Print the current board state."""
```

```
    for row in board:
```

```
        print(" ".join(str(num) for num in row))
```

```
    print() # Empty line for better readability
```

```
def get_blank_position(board):
```

```
    for i in range(3):
```

```
        for j in range(3):
```

```
            if board[i][j] == 0: # Find the blank space (0)
```

```
                return (i, j)
```

```
def get_successors(state):
```

```
    successors = []
```

```
    x, y = get_blank_position(state.board) # Get position of blank tile
```

```
    directions = [(-1, 0), (1, 0), (0, -1), (0, 1)] # Possible moves
```

```

for dx, dy in directions:
    new_x, new_y = x + dx, y + dy
    if 0 <= new_x < 3 and 0 <= new_y < 3: # Valid move
        new_board = [row[:] for row in state.board] # Copy the current board
        new_board[x][y], new_board[new_x][new_y] = new_board[new_x][new_y], new_board[x][y]
# Swap
        successors.append(PuzzleState(new_board, state.g + 1, 0)) # Create new state
return successors

```

```

def heuristic_manhattan_distance(board):
    distance = 0
    for i in range(3):
        for j in range(3):
            if board[i][j] != 0:
                target_x = (board[i][j] - 1) // 3
                target_y = (board[i][j] - 1) % 3
                distance += abs(i - target_x) + abs(j - target_y)
    return distance

```

```

def is_goal_state(board):
    return board == [[1, 2, 3],
                     [8, 0, 4],
                     [7, 6, 5]] # Check if the board is in the goal state

```

```

def a_star_search_manhattan_distance(start_board):
    start_state = PuzzleState(start_board, 0, heuristic_manhattan_distance(start_board))
    open_set = []
    heapq.heappush(open_set, start_state)
    closed_set = set()

    while open_set:

```

```

current_state = heapq.heappop(open_set)

# Print current board state and details
print("Current board state:")
print_board(current_state.board)
print(f'g(n): {current_state.g}, h(n): {current_state.h}, f(n): {current_state.f}\n')

# Check if we've reached the goal
if is_goal_state(current_state.board):
    print("Goal state reached!")
    return current_state.g # Return the cost to reach the goal

closed_set.add(tuple(map(tuple, current_state.board)))

for successor in get_successors(current_state):
    successor.h = heuristic_manhattan_distance(successor.board)
    successor.f = successor.g + successor.h

    if tuple(map(tuple, successor.board)) in closed_set:
        continue

    heapq.heappush(open_set, successor)

return None # No solution found

def get_user_input():
    board = []
    for i in range(3):
        while True:
            row = input(f"Enter row {i + 1} (3 numbers separated by space): ")
            nums = list(map(int, row.split()))

```

```

        if len(nums) == 3 and all(0 <= num <= 8 for num in nums):
            board.append(nums)
            break
        else:
            print("Invalid input. Please enter 3 numbers between 0 and 8.")
    return board

```

```

if __name__ == "__main__":
    start_board = get_user_input()
    steps = a_star_search_manhattan_distance(start_board)
    print(f"Steps to solve with Manhattan Distance heuristic: {steps}")

```

## Output:

Enter row 1 (3 numbers separated by space): 2 8 3

Enter row 2 (3 numbers separated by space): 1 6 4

Enter row 3 (3 numbers separated by space): 7 0 5

Current board state:

2 8 3

1 6 4

7 0 5

$g(n)$ : 0,  $h(n)$ : 9,  $f(n)$ : 9

Current board state:

2 8 3

1 6 4

7 5 0

$g(n)$ : 1,  $h(n)$ : 8,  $f(n)$ : 9

Current board state:

2 8 3

1 6 4

0 7 5

$g(n)$ : 1,  $h(n)$ : 10,  $f(n)$ : 11

Current board state:

2 8 3

1 0 4

7 6 5

$g(n)$ : 1,  $h(n)$ : 10,  $f(n)$ : 11

Current board state:

2 8 3

1 6 0

7 5 4

$g(n)$ : 2,  $h(n)$ : 9,  $f(n)$ : 11

Current board state:

2 0 3

1 8 4

7 6 5

$g(n)$ : 2,  $h(n)$ : 9,  $f(n)$ : 11

Current board state:

2 8 3

1 0 6

7 5 4

$g(n): 3, h(n): 8, f(n): 11$

Current board state:

0 2 3

1 8 4

7 6 5

$g(n): 3, h(n): 8, f(n): 11$

Current board state:

2 0 3

1 8 6

7 5 4

$g(n): 4, h(n): 7, f(n): 11$

Current board state:

2 8 3

1 4 0

7 6 5

$g(n): 2, h(n): 9, f(n): 11$

Current board state:

2 8 3

1 5 6

7 0 4

$g(n): 4, h(n): 7, f(n): 11$

Current board state:

1 2 3

0 8 4

7 6 5

$g(n)$ : 4,  $h(n)$ : 7,  $f(n)$ : 11

Current board state:

2 8 3

1 5 6

7 4 0

$g(n)$ : 5,  $h(n)$ : 6,  $f(n)$ : 11

Current board state:

2 8 3

1 4 5

7 6 0

$g(n)$ : 3,  $h(n)$ : 8,  $f(n)$ : 11

Current board state:

0 2 3

1 8 6

7 5 4

$g(n)$ : 5,  $h(n)$ : 6,  $f(n)$ : 11

Current board state:

2 8 3

1 4 5

7 0 6

$g(n): 4, h(n): 7, f(n): 11$

Current board state:

1 2 3

0 8 6

7 5 4

$g(n): 6, h(n): 5, f(n): 11$

Current board state:

2 8 3

0 6 4

1 7 5

$g(n): 2, h(n): 11, f(n): 13$

Current board state:

2 8 3

0 1 6

7 5 4

$g(n): 4, h(n): 9, f(n): 13$

Current board state:

2 8 3

1 4 5

0 7 6



$g(n): 5, h(n): 8, f(n): 13$

Current board state:

1 2 3

7 8 6

0 5 4

$g(n): 7, h(n): 6, f(n): 13$

Current board state:

1 2 3

8 0 6

7 5 4

$g(n): 7, h(n): 6, f(n): 13$

Current board state:

2 3 0

1 8 4

7 6 5

$g(n): 3, h(n): 10, f(n): 13$

Current board state:

2 8 3

1 0 5

7 4 6

$g(n): 5, h(n): 8, f(n): 13$

Current board state:

1 2 3

7 8 4

0 6 5

$g(n): 5, h(n): 8, f(n): 13$

Current board state:

2 8 0

1 4 3

7 6 5

$g(n): 3, h(n): 10, f(n): 13$

Current board state:

2 8 3

1 5 6

0 7 4

$g(n): 5, h(n): 8, f(n): 13$

Current board state:

2 8 3

1 5 0

7 4 6

$g(n): 6, h(n): 7, f(n): 13$

Current board state:

2 8 3

1 5 0

7 4 6

$g(n): 6, h(n): 7, f(n): 13$

Current board state:

2 8 0

1 6 3

7 5 4

$g(n): 3, h(n): 10, f(n): 13$

Current board state:

2 3 0

1 8 6

7 5 4

$g(n): 5, h(n): 8, f(n): 13$

Current board state:

1 2 3

8 0 4

7 6 5

$g(n): 5, h(n): 8, f(n): 13$

Goal state reached!

Steps to solve with Manhattan Distance heuristic: 5