

Recap: Association Rule Mining

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STUDY LOCALLY. LIVE GLOBALLY.

Association Rule Mining

- Given a set of transactions, find rules that will predict the occurrence of an item based on the occurrences of other items in the transaction

Market-Basket transactions

TID	Items
1	Bread, Milk
2	Bread, Diaper, Beer, Eggs
3	Milk, Diaper, Beer, Coke
4	Bread, Milk, Diaper, Beer
5	Bread, Milk, Diaper, Coke

Example of Association Rules

$\{Diaper\} \rightarrow \{Beer\},$
 $\{Milk, Bread\} \rightarrow \{Eggs, Coke\},$
 $\{Beer, Bread\} \rightarrow \{Milk\},$

Implication means co-occurrence,
not causality!

Definitions

- **Itemset**

- A collection of one or more items
 - ◆ Example: {Milk, Bread, Diaper}
- k-itemset
 - ◆ An itemset that contains k items

- **Support count (σ)**

- Frequency of occurrence of an itemset
- E.g. $\sigma(\{\text{Milk, Bread, Diaper}\}) = 2$

- **Support**

- Fraction of transactions that contain an itemset
- E.g. $s(\{\text{Milk, Bread, Diaper}\})$
 $= \sigma(\{\text{Milk, Bread, Diaper}\}) / |T| = 2/5$

- **Frequent Itemset**

- An itemset whose support is greater than or equal to a *minsup* threshold

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$$s(X) = \frac{\sigma(X)}{|T|}$$

Definitions

- **Association Rule**

- An implication expression of the form $X \rightarrow Y$, where X and Y are itemsets
- Example:
 $\{Milk, Bread\} \rightarrow \{Diaper\}$

- **Rule Evaluation Metrics**

- Support (s)
 - ◆ Fraction of transactions that contain both X and Y
- Confidence (c)
 - ◆ Measures how often items in Y appear in transactions that contain X

TID	Items
1	Bread, Milk
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Example:

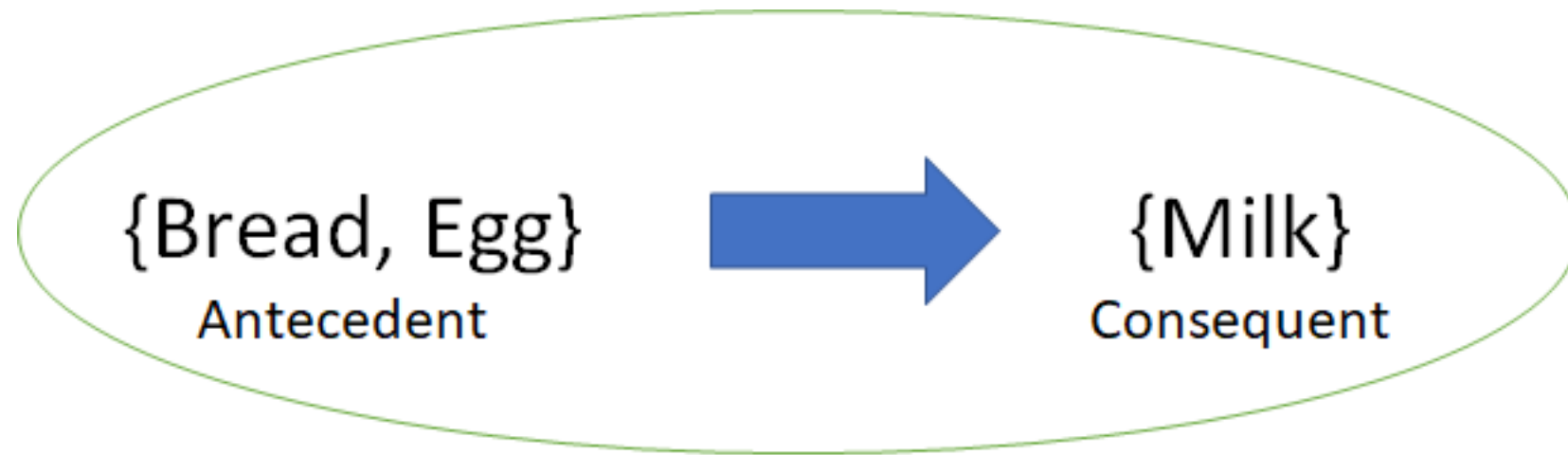
$\{Milk, Bread\} \rightarrow \{Diaper\}$

$$s = \frac{\sigma(\{Milk, Bread, Diaper\})}{|T|} = \frac{2}{5} = 0.4$$

$$c = \frac{\sigma(\{Milk, Bread, Diaper\})}{\sigma(\{Milk, Diaper\})} = \frac{2}{3} = 0.67$$

$$c(X \rightarrow Y) = \frac{\sigma(X \cup Y)}{\sigma(X)} = \frac{s(X \cup Y)}{s(X)}$$

Definitions



Itemset = {Bread, Egg, Milk}

Association Rule Mining Tasks

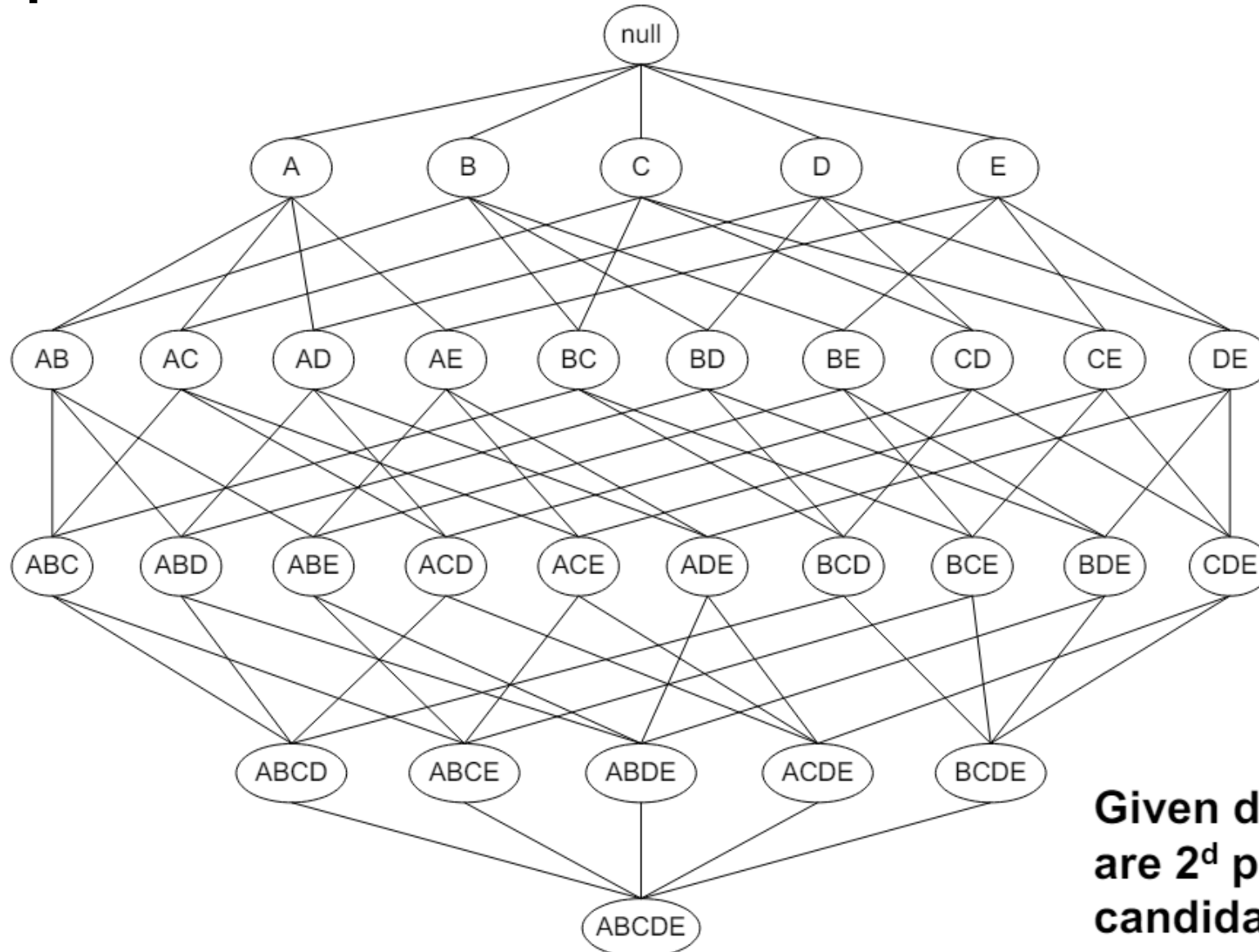
- Given a set of transactions T , the goal of association rule mining is to find all rules having
 - support $\geq \textit{minsup}$ threshold
 - confidence $\geq \textit{minconf}$ threshold
- Brute-force approach:
 - List all possible association rules
 - Compute the support and confidence for each rule
 - Prune rules that fail the *minsup* and *minconf* thresholds

⇒ **Computationally prohibitive!**

Association Rule Mining Tasks

- Two-step approach:
 1. Frequent Itemset Generation
 - Generate all itemsets whose support \geq minsup
 2. Rule Generation
 - Generate high confidence rules from each frequent itemset, where each rule is a binary partitioning of a frequent itemset
- Frequent itemset generation is still computationally expensive

Frequent Itemset Generation



Given d items, there are 2^d possible candidate itemsets

Illustrating Apriori Principle

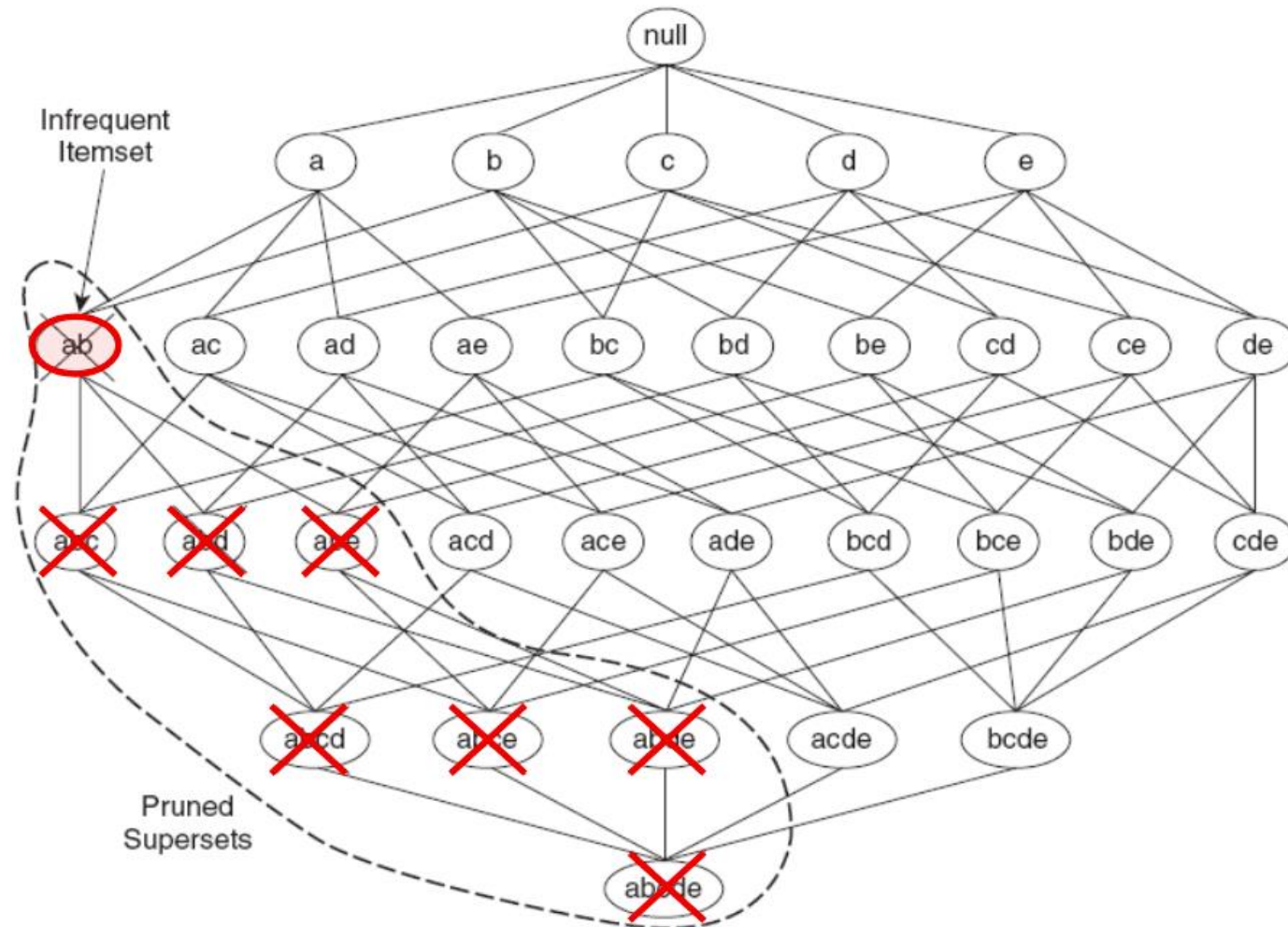
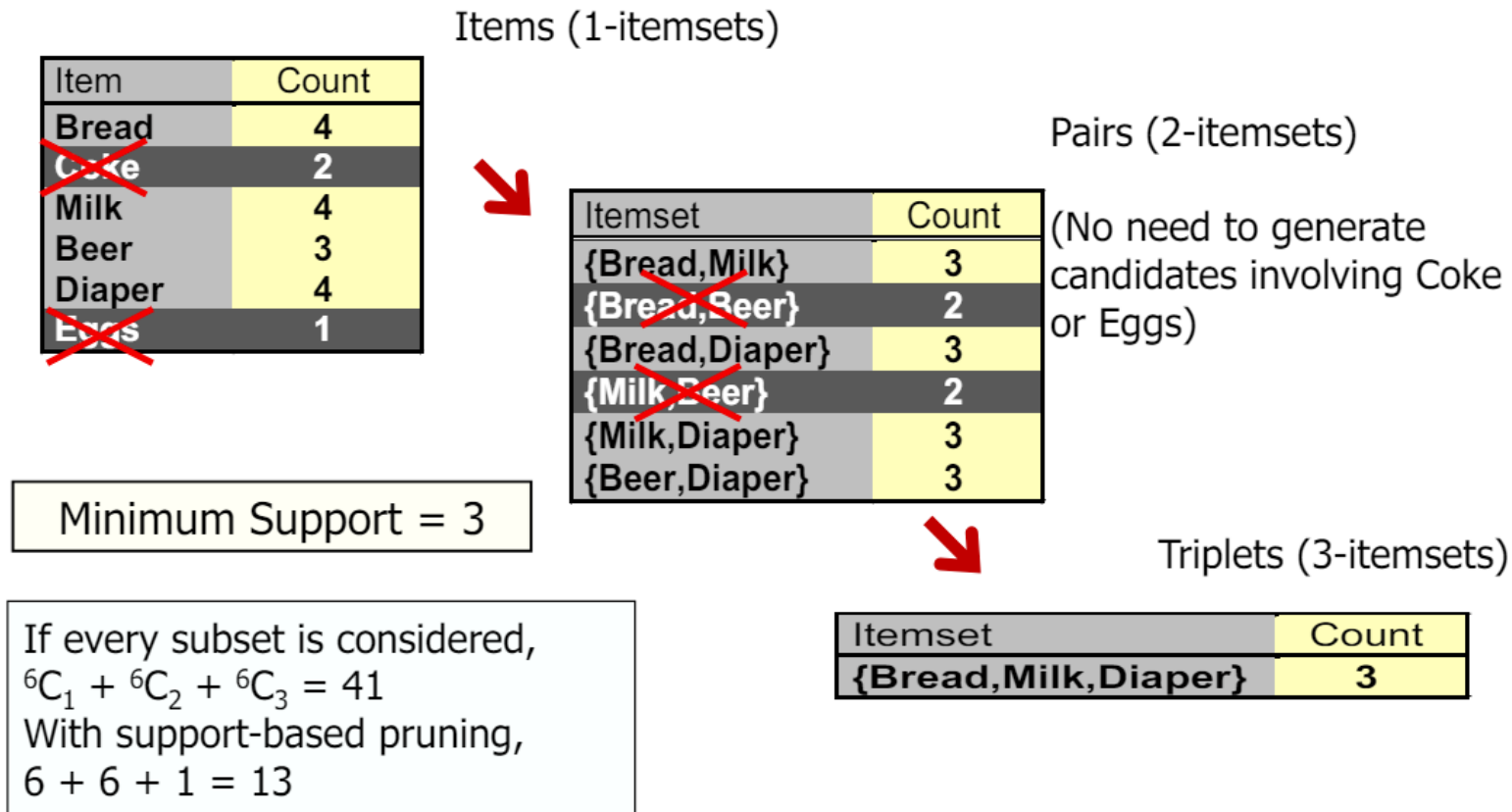


Figure 6.4. An illustration of support-based pruning. If $\{a, b\}$ is infrequent, then all supersets of $\{a, b\}$ are infrequent.

Illustrating Apriori Principle



Apriori Aglorithm

- Method:

- Let $k=1$
- Generate frequent itemsets of length 1
- Repeat until no new frequent itemsets are identified
 - ◆ Generate length $(k+1)$ candidate itemsets from length k frequent itemsets
 - ◆ Prune candidate itemsets containing subsets of length k that are infrequent
 - ◆ Count the support of each candidate by scanning the DB
 - ◆ Eliminate candidates that are infrequent, leaving only those that are frequent