

# SS-ZG548: ADVANCED DATA MINING

## Lecture-03: Incremental Mining



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Jan 13, 2018

(WILP @ BITS-Pilani Jan-Apr 2018)

# Recap: Association Rule Mining

Association Rule Mining does link analysis

- Set of items  $I = \{i_1, i_2, \dots, i_m\}$ , set of transactions  $T = \{t_1, t_2, \dots, t_n\}$  where  $t_i \subseteq I$
- An association rule  $X \Rightarrow Y$  has a **support**  $s$  in set  $T$  if  $s\%$  of the transactions in  $T$  contains  $X \cup Y$

$$\text{support}(X \Rightarrow Y) = P(X \cup Y)$$

- The association rule  $X \Rightarrow Y$  holds in the transaction set  $T$  with **confidence**  $c$  if  $c\%$  of the transactions in  $T$  that contain  $X$  also contain  $Y$ .

$$\text{confidence}(X \Rightarrow Y) = P(Y|X)$$

- An association rule is an implication of the form  $X \Rightarrow Y$ , where  $X \subseteq I$ ,  $Y \subseteq I$  and  $X \cap Y = \phi$

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- 1 Find all frequent item sets:  $\{X : \text{support}(X) \geq S_{min}\}$

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Second step is straight forward so most of the research interest lies in solving the first part.

### Apriori algorithm

- Starting from set of 1-item frequent sets  $L_1$
- Uses  $k$ -item set to levelwise explore  $(k+1)$ -item set
- Process continues until there is no more candidate item sets

# Recap: Apriori at work

Consider  
transactions T

$T_1 = (A, B, C)$
$T_2 = (A, F)$
$T_3 = (A, B, C, E)$
$T_4 = (A, B, D, F)$
$T_5 = (C, F)$
$T_6 = (A, B, C)$
$T_7 = (A, B, C, E)$
$T_8 = (C, D, E)$
$T_9 = (B, D, E)$

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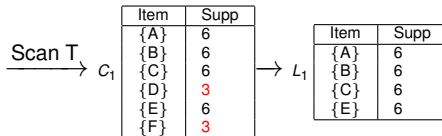
Scan T  $\rightarrow C_1$

Item	Supp
{A}	6
{B}	6
{C}	6
{D}	3
{E}	6
{F}	3

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Consider transactions T

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$T_8 = (C, D, E)$
$T_9 = (B, D, E)$

Item
{A, B}
{A, C}
{A, E}
{B, C}
{B, E}
{C, E}

$C_2$

Scan T  $\rightarrow C_1$

Item	Supp
{A}	6
{B}	6
{C}	6
{D}	3
{E}	6
{F}	3

$\rightarrow L_1$

Item	Supp
{A}	6
{B}	6
{C}	6
{E}	6

# Recap: Apriori at work

Consider transactions T

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$T_9 = (B, D, E)$

Item
{A,B}
{A,C}
{A,E}
{B,C}
{B,E}
{C,E}

Scan T

Item	Supp
{A,B}	5
{A,C}	4
{A,E}	2
{B,C}	4
{B,E}	3
{C,E}	3

Scan T

Item	Supp
{A}	6
{B}	6
{C}	6
{D}	3
{E}	6
{F}	3

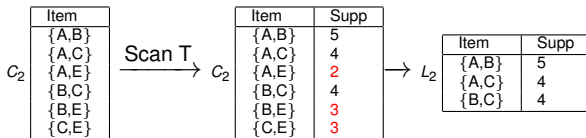
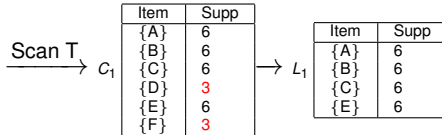
$L_1$

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Scan T  $\rightarrow C_1$

Item	Supp
{A}	6
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{E}	6
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$\rightarrow L_1$

Item	Supp
{A}	6
{B}	6
{C}	6
{E}	6

$C_2$

Item
{A, B}
{A, C}
{A, E}
{B, C}
{B, E}
{C, E}

Scan T  $\rightarrow C_2$

Item	Supp
{A, B}	5
{A, C}	4
{A, E}	2
{B, C}	4
{B, E}	3
{C, E}	3

$\rightarrow L_2$

Item	Supp
{A, B}	5
{A, C}	4
{B, C}	4

$C_3$

Item
{A, B, C}

# Recap: Apriori at work

Consider transactions T

$T_1 = (A, B, C)$
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{B,E}	3
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$\rightarrow L_2$

Item	Supp
{A,B}	5
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$C_3$

Item
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$C_3$

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Scan T  $\rightarrow C_3$

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# Generate Association Rules

If  $X \subset W$  &  $\text{support}(X)/\text{support}(W) \geq C_{min}$ , then  $X \Rightarrow W - X$

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$T_7=(A,B,C,E)$
$T_8=(C,D,E)$
$T_9=(B,D,E)$



# Generate Association Rules

If  $X \subset W$  &  $\text{support}(X)/\text{support}(W) \geq C_{min}$ , then  $X \Rightarrow W - X$

- Our frequent item contains

- ▶  $\{A\}_6 \{B\}_6 \{C\}_6 \{E\}_6 \{A,B\}_5 \{A,C\}_4 \{B,C\}_6$   
 $\{A,B,C\}_4$

Transactions

$T_1=(A,B,C)$
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 $\{A,B,C\}_4$

- Possibilities are

$A \Rightarrow B, B \Rightarrow A, A \Rightarrow C, C \Rightarrow A, B \Rightarrow C, C \Rightarrow B,$   
 $A \Rightarrow \{B, C\}, B \Rightarrow \{A, C\}, C \Rightarrow \{B, A\},$   
 $\{A, B\} \Rightarrow C, \{A, C\} \Rightarrow B, \{B, C\} \Rightarrow A$

- Let's take  $C_{min} = 1.22$

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If  $X \subset W$  &  $\text{support}(X)/\text{support}(W) \geq C_{min}$ , then  $X \Rightarrow W - X$

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$A \Rightarrow B, B \Rightarrow A, A \Rightarrow C, C \Rightarrow A, B \Rightarrow C, C \Rightarrow B,$   
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 $\{A, B\} \Rightarrow C, \{A, C\} \Rightarrow B, \{B, C\} \Rightarrow A$

- Let's take  $C_{min} = 1.22$
- Association rules that qualifies as valid rule are shown green

$A \Rightarrow B, B \Rightarrow A, A \Rightarrow C, C \Rightarrow A, B \Rightarrow C, C \Rightarrow B, A \Rightarrow \{B, C\},$   
 $B \Rightarrow \{A, C\}, C \Rightarrow \{B, A\}, \{A, B\} \Rightarrow C, \{A, C\} \Rightarrow B, \{B, C\} \Rightarrow A$

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- Similar to Apriori. Uses hash to reduce the size of set C's.

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T	
$T_1 = (A, B, C)$	$\{A, B\} \{A, C\} \{B, C\}$
$T_2 = (A, F)$	$\{A, F\}$
$T_3 = (A, B, C, E)$	$\{A, B\} \{A, C\} \{A, E\} \{B, C\} \{B, E\} \{C, E\}$
$T_4 = (A, B, D, F)$	-
$T_5 = (C, F)$	-
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$T_5 = (C, F)$	-
$T_6 = (A, B, C)$	-
$T_7 = (A, B, C, E)$	-
$T_8 = (C, D, E)$	-
$T_9 = (B, D, E)$	-

hash	Bucket
0	$\{C, E\} \{A, D\} \{C, E\}$ (4)
1	$\{A, E\} \{C, F\} \{A, E\}$ (3)
2	$\{B, C\} \{A, F\} \{B, C\} \{A, F\}$ $\{B, C\} \{B, C\} \{D, E\} \{D, E\}$ (8)
3	$\{B, D\} \{B, D\}$ (2)
4	$\{B, E\} \{D, F\} \{B, E\}$ $\{B, E\}$ (4)
5	$\{A, B\} \{A, B\} \{B, F\} \{B, F\}$ $\{A, B\}$ (5)
6	$\{A, C\} \{A, C\} \{A, C\} \{A, C\}$ $\{C, D\}$ (5)



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- Assume a hash function  $h(x, y) = (10 * ID(x) + ID(y)) \bmod 7$

T	
$T_1 = (A, B, C)$	$\{A, B\} \{A, C\} \{B, C\}$
$T_2 = (A, F)$	$\{A, F\}$
$T_3 = (A, B, C, E)$	$\{A, B\} \{A, C\} \{A, E\} \{B, C\} \{B, E\} \{C, E\}$
$T_4 = (A, B, D, F)$	-
$T_5 = (C, F)$	-
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$T_8 = (C, D, E)$	-
$T_9 = (B, D, E)$	-

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2	$\{B, C\} \{A, F\} \{B, C\} \{A, F\}$ $\{B, C\} \{B, C\} \{D, E\} \{D, E\}$ (8)
3	$\{B, D\} \{B, D\}$ (2)
4	$\{B, E\} \{D, F\} \{B, E\}$ $\{B, E\}$ (4)
5	$\{A, B\} \{A, B\} \{B, F\} \{B, A\}$ $\{A, B\}$ (5)
6	$\{A, C\} \{A, C\} \{A, C\} \{A, C\}$ $\{C, D\}$ (5)

Note that the total counts for buckets 1 and 3 cannot satisfy the minimum support constraint, therefore,  $\{A, E\}$ , should not be included in  $C_2$ .

# Partition Based Algorithm

- Essentially based on a partition-based heuristic.
- A frequent item set in database  $D$  having  $n$  partitions  $p_1, p_2, \dots, p_n$  must be a frequent item set in at least one of the  $n$  partitions

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P1	$T_1 = (A, B, C)$
	$T_2 = (A, F)$
	$T_3 = (A, B, C, E)$
P2	$T_4 = (A, B, D, F)$
	$T_5 = (C, F)$
	$T_6 = (A, B, C)$
P3	$T_7 = (A, B, C, E)$
	$T_8 = (C, D, E)$
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A handwritten table with three sections labeled P1, P2, and P3 on the left. Each section contains one or more rows of item sets  $T_i$ . Red horizontal lines separate the sections.

P1	$T_1 = (A, B, C)$
	$T_2 = (A, F)$
	$T_3 = (A, B, C, E)$
P2	$T_4 = (A, B, D, F)$
	$T_5 = (C, F)$
	$T_6 = (A, B, C)$
P3	$T_7 = (A, B, C, E)$
	$T_8 = (C, D, E)$
	$T_9 = (B, D, E)$

Partition	Frequent Item set
$P_1$	$\{A\} \{B\} \{C\} \{AB\} \{AC\} \{BC\} \{ABC\}$
$P_2$	$\{A\} \{B\} \{C\} \{F\} \{AB\}$
$P_3$	$\{B\} \{C\} \{D\} \{E\} \{BE\} \{CE\} \{DE\}$

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Partition	Frequent Item set
$P_1$	$\{A\} \{B\} \{C\} \{AB\} \{AC\} \{BC\} \{ABC\}$
$P_2$	$\{A\} \{B\} \{C\} \{F\} \{AB\}$
$P_3$	$\{B\} \{C\} \{D\} \{E\} \{BE\} \{CE\} \{DE\}$

Union is taken

Candidate item sets
$\{A\} \{B\} \{C\} \{D\} \{E\} \{F\} \{AB\} \{AC\}$ $\{BC\} \{CE\} \{DE\} \{ABC\} \{ABC\}$

Second scan of  $D$  examines the required support



# Incremental Association Rule Mining

- Real databases are generally dynamic (not static)

# Incremental Association Rule Mining

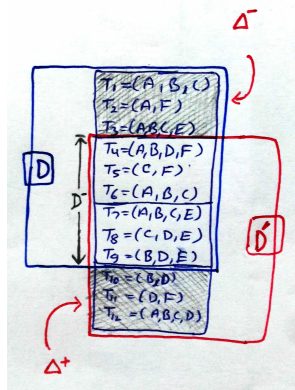
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- New transactions are generated and old transactions may be obsolete over time

# Incremental Association Rule Mining

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- New transactions are generated and old transactions may be obsolete over time

## Premittives:

- Let  $D$  be the initial database
- $\Delta^-$  portion of the database becomes obsolete
- Therefore, the database is left with  $D^- = D - \Delta^-$
- $\Delta^+$  more transactions are added
- The database becomes  
 $D' = D^- + \Delta^+ = D - \Delta^- + \Delta^+$



Incremental update can avoid redoing mining on updated database

# Incremental Association Rule Mining (contd..)

- 1 The update problem can be reduced to finding the new set of frequent item sets. After that, the new association rules can be computed from the new frequent item sets.
- 2 An old frequent item set has the potential to become infrequent in the updated database.
- 3 Similarly, an old infrequent item set could become frequent in the new database.
- 4 In order to find the new frequent item sets “exactly”, all the records in the updated database, including those from the original database, have to be checked against every candidate set.

We would evaluate two algorithms *viz.* FUP and FUP2

# Algorithm FUP

- FUP stands for **F**ast **U**pdate.
- Can handle insertions only
- Specifically, given the original database  $D$  and its corresponding frequent item set  $L = \{L_1, L_2, \dots, L_k\}$ .
  - ▶ The goal is to reuse the information to efficiently obtain  $L' = \{L'_1, L'_2, \dots, L'_k\}$  for new database  $D' = D \cup \Delta^+$

By utilizing the definition of support and constraint of minimum support  $S_{min}$ , following is used by FUP.

- An original frequent item set  $X \in L$ , becomes infrequent in  $D'$  iff  $support(X)_{D'} < S_{min}$
- An item set  $X \notin L$ , becomes frequent in  $D'$  iff  $support(X)_{\Delta^+} \geq S_{min}$
- If a  $k$ -item set  $X$  whose  $(k-1)$ -subset(s) becomes infrequent, i.e., the subset is in  $L_{k-1}$  but not in  $L'_{k-1}$ , then  $X$  must be infrequent in  $D'$ .

# FUP at work

Consider the database  $D$  and the related frequent set discovered with Apriori

$T_1 = (A, B, C)$   
 $T_2 = (A, F)$   
 $T_3 = (A, B, C, E)$   
 $T_4 = (A, B, D, F)$   
 $T_5 = (C, F)$   
 $T_6 = (A, B, C)$   
 $T_7 = (A, B, C, E)$   
 $T_8 = (C, D, E)$   
 $T_9 = (B, D, E)$

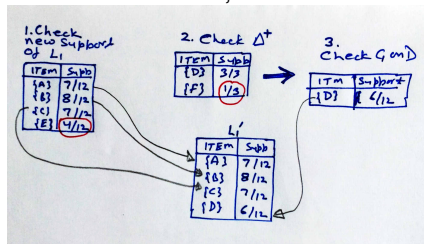
Item set	Support
{A}	6/9
{B}	6/9
{C}	6/9
{E}	4/9
{AB}	5/9
{AC}	4/9
{BC}	4/9
{ABC}	4/9

Consider the arrival of  $\Delta^+$  more transactions

$T_1 = (A, B, C)$   
 $T_2 = (A, F)$   
 $T_3 = (A, B, C, E)$   
 $T_4 = (A, B, D, F)$   
 $T_5 = (C, F)$   
 $T_6 = (A, B, C)$   
 $T_7 = (A, B, C, E)$   
 $T_8 = (C, D, E)$   
 $T_9 = (B, D, E)$

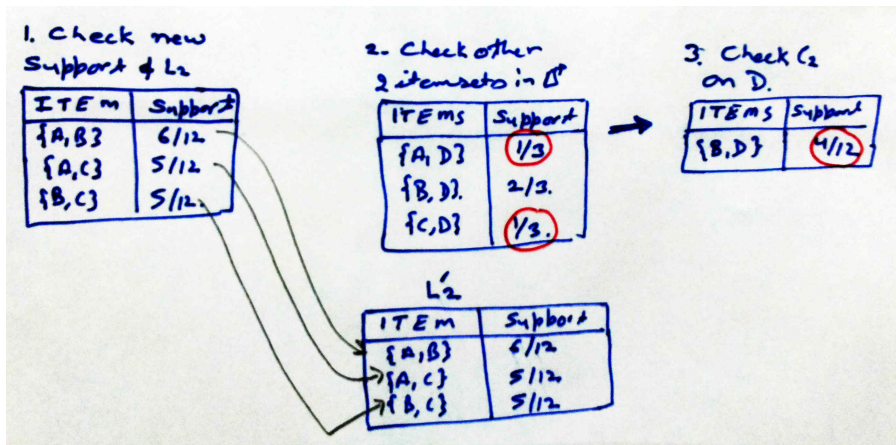
$\Delta^+ \rightarrow$   
 $T_{10} = (B, D)$   
 $T_{11} = (D, F)$   
 $T_{12} = (A, B, C, D)$

The first iteration, is as below.



# FUP at work (contd...)

The second iteration, is as below.

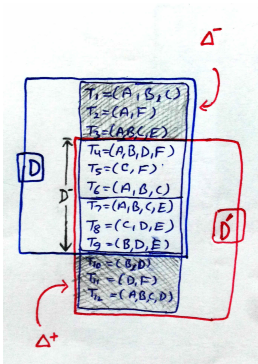


Similarly it is executed for next levels.

- FUP<sub>2</sub> can work for both  $\Delta^-$  and  $\Delta^+$
- $L_k$  from previous mining result is used for dividing candidate itemset  $C_k$  into two parts
  - ▶  $P_k = C_k \cap L_k$
  - ▶  $Q_k = C_k - P_k$
- Itemset that is frequent in  $\Delta^-$ , must be infrequent in  $D^-$ .
- Further if itemset in  $Q_k$  is infrequent in  $\Delta^+$  then it is infrequent in  $D^-$ .
- This technique helps to effectively reduce number of candidate itemsets.

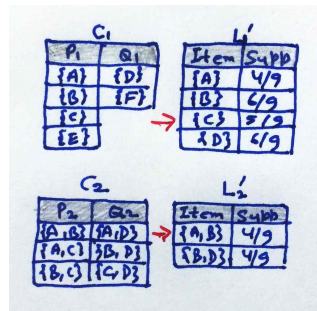


# FUP<sub>2</sub> at work



Item set	Support
{A}	6/9
{B}	6/9
{C}	6/9
{E}	4/9
{A B}	5/9
{A C}	4/9
{B C}	4/9
{A B C}	4/9

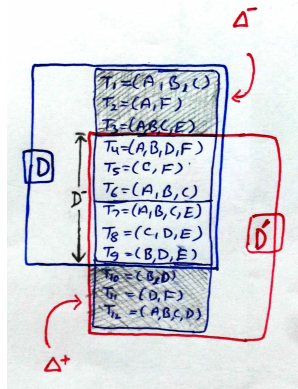
Frequent itemsets of D



- $C_1$  is set of all items. It is divided in  $P_i$  and  $Q_i$
- Being frequent, support for all items in  $P_i$  is known. It could be updated using  $\Delta^-$  and  $\Delta^+$  only.
- $\text{Count}(\{A\})_{D'} = \text{Count}(\{A\})_D - \text{Count}(\{A\})_{\Delta^-} + \text{Count}(\{A\})_{\Delta^+}$   
 $= 6 - 3 + 1 = 4$

## FUP<sub>2</sub> at work

- In some cases only the scan of  $\Delta^-$  and  $\Delta^+$  is required.
- For example,  $\text{Count}(\{F\})_{\Delta^+ -}$   
 $\text{Count}(\{F\})_{\Delta^-} = 0$  showing that support of  $\{F\}$  can not be improved.
- Consequently, fewer itemsets have to be further scanned
- An iteration finishes when all the itemsets in  $P_i$  and  $Q_i$  are verified, and new set of frequent itemsets  $L'_i$  is generated



## FUP<sub>2</sub>H

Uses hashing for performance improvement

# Thank You!

**Thank you very much for your attention!**

**Queries ?**