

# Chapter 1. The Role of Algorithms in Computing

1.1-2.

Memory usage is a significant factor of consideration in a real-world setting.

1.1-4.

Shortest path problem finds a shortest path between two nodes. Traveling salesman problem finds a shortest path that visits each city and returns to the origin city.

1.1-5.

The longest increasing subsequence problem is the problem in which only the best solution will do. The A\* algorithm is the problem in which the heuristic solution will be enough.

1.2-2.

For  $n < 44$ , insertion sort beat merge sort.

1.2-3.

$n = 15$  is the smallest value such that  $100n^2 < 2^n$ .

1-1.

For  $n = 10^{10000}$ , algorithm with  $\log n$  complexity solves in 0.033 seconds.

For  $n = 10^{10000}$ , algorithm with  $\sqrt{n}$  complexity solves in  $10^{4985}$  centuries.

For  $n = 10^{30}$ , algorithm with  $\log n$  complexity solves in 0.0001 seconds.

For  $n = 10^{30}$ , algorithm with  $\sqrt{n}$  complexity solves in 0.315 centuries.

For  $n = 10^{30}$ , algorithm with  $n$  complexity solves in  $3.170 \cdot 10^{14}$  centuries.

For  $n = 10^{15}$ , algorithm with  $\sqrt{n}$  complexity solves in 31.62 seconds.

For  $n = 10^{15}$ , algorithm with  $n$  complexity solves in 0.317 centuries.

For  $n = 10^{15}$ , algorithm with  $n \log n$  complexity solves in 15.798 centuries.  
 For  $n = 10^{13}$ , algorithm with  $\sqrt{n}$  complexity solves in 3.162 seconds.  
 For  $n = 10^{13}$ , algorithm with  $n$  complexity solves in 4 months.  
 For  $n = 10^{13}$ , algorithm with  $n \log n$  complexity solves in 0.1371 centuries.  
 For  $n = 10^{10}$ , algorithm with  $\sqrt{n}$  complexity solves in 0.1 seconds.  
 For  $n = 10^{10}$ , algorithm with  $n$  complexity solves in 3 hours.  
 For  $n = 10^{10}$ , algorithm with  $n \log n$  complexity solves in 4 days.  
 For  $n = 10^8$ , algorithm with  $n$  complexity solves in 2 minutes.  
 For  $n = 10^8$ , algorithm with  $n \log n$  complexity solves in 1 hours.  
 For  $n = 10^8$ , algorithm with  $n^2$  complexity solves in 3.2 centuries.  
 For  $n = 10^7$ , algorithm with  $n$  complexity solves in 10 seconds.  
 For  $n = 10^7$ , algorithm with  $n \log n$  complexity solves in 3.9 minutes.  
 For  $n = 10^7$ , algorithm with  $n^2$  complexity solves in 3.2 years.  
 For  $n = 10^6$ , algorithm with  $n$  complexity solves in 1 seconds.  
 For  $n = 10^6$ , algorithm with  $n \log n$  complexity solves in 0.33 minutes.  
 For  $n = 10^6$ , algorithm with  $n^2$  complexity solves in 11.6 days.  
 For  $n = 10^5$ , algorithm with  $n \log n$  complexity solves in 1.66 seconds.  
 For  $n = 10^5$ , algorithm with  $n^2$  complexity solves in 3 hours.  
 For  $n = 10^5$ , algorithm with  $n^3$  complexity solves in 0.317 centuries.  
 For  $n = 10^4$ , algorithm with  $n \log n$  complexity solves in 0.13 seconds.  
 For  $n = 10^4$ , algorithm with  $n^2$  complexity solves in 2 minutes.  
 For  $n = 10^4$ , algorithm with  $n^3$  complexity solves in 11.6 days.  
 For  $n = 10^3$ , algorithm with  $n^2$  complexity solves in 1 seconds.  
 For  $n = 10^3$ , algorithm with  $n^3$  complexity solves in 17 minutes.  
 For  $n = 10^2$ , algorithm with  $n^3$  complexity solves in 1 seconds.  
 For  $n = 10^2$ , algorithm with  $2^n$  complexity solves in 420000000000000 centuries.  
 For  $n = 50$ , algorithm with  $2^n$  complexity solves in 36 years.  
 For  $n = 40$ , algorithm with  $2^n$  complexity solves in 13 days.  
 For  $n = 30$ , algorithm with  $2^n$  complexity solves in 18 minutes.  
 For  $n = 20$ , algorithm with  $2^n$  complexity solves in 1.1 seconds.  
 For  $n = 20$ , algorithm with  $n!$  complexity solves in 771 centuries.  
 For  $n = 18$ , algorithm with  $n!$  complexity solves in 2.03 centuries.  
 For  $n = 17$ , algorithm with  $n!$  complexity solves in 11.3 years.  
 For  $n = 16$ , algorithm with  $n!$  complexity solves in 243 days.  
 For  $n = 15$ , algorithm with  $n!$  complexity solves in 16 days.  
 For  $n = 14$ , algorithm with  $n!$  complexity solves in 25 hours.  
 For  $n = 13$ , algorithm with  $n!$  complexity solves in 2 hours.

For  $n = 12$ , algorithm with  $n!$  complexity solves in 8 minutes.  
For  $n = 11$ , algorithm with  $n!$  complexity solves in 40 seconds.  
For  $n = 10$ , algorithm with  $n!$  complexity solves in 4 seconds.