Integrales formas basica

1)
$$\int x^n dx = \frac{1}{n+1} x^{n+1}$$

$$2) \int \frac{1}{x} dx = \ln|x|$$

3)
$$\int u dv = uv - \int v du$$

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$$\int_{0}^{x} u dv = uv - \int_{0}^{x} v du$$
4)
$$\int_{0}^{x} \frac{1}{ax+b} dx = \frac{1}{a} \ln|ax+b|$$

Integrales de funciones racionales

5)
$$\int \frac{1}{(x+a)^2} dx = -\frac{1}{x+a}$$

6)
$$\int (x+a)^n dx = \frac{(x+a)^{n+1}}{n+1}, n \neq -1$$

$$5) \int (x+a)^{2} dx = \frac{x+a}{n+1}, n \neq -1$$

$$7) \int x(x+a)^{n} dx = \frac{(x+a)^{n+1}}{(n+1)(n+2)}, n \neq -1$$

8)
$$\int \frac{1}{1+x^2} dx = \tan^{-1} x$$

9)
$$\int \frac{1}{a^2 + x^2} dx = \frac{1}{a} \tan^{-1} \frac{x}{a}$$

9)
$$\int \frac{1+x}{a^2+x^2} dx = \frac{1}{a} \tan^{-1} \frac{x}{a}$$
10)
$$\int \frac{x}{a^2+x^2} dx = \frac{1}{2} \ln |a^2 + x^2|$$

11)
$$\int \frac{x^2}{a^2 + x^2} dx = x - a \tan^{-1} \frac{x}{a}$$

12)
$$\int \frac{x^3}{a^2 + x^2} dx = \frac{1}{2}x^2 - \frac{1}{2}a^2 \ln|a^2 + x^2|$$

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13)
$$\int \frac{1}{ax^2 + bx + c} dx = \frac{2}{\sqrt{4ac - b^2}} \tan^{-1} \frac{2ax + b}{\sqrt{4ac - b^2}}$$
14)
$$\int \frac{1}{(x+a)(x+b)} dx = \frac{1}{b-a} \ln \frac{a+x}{b+x}, \ a \neq b$$

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15)
$$\int \frac{x}{(x+a)^2} dx = \frac{a}{a+x} + \ln|a+x|$$

16)
$$\int \frac{x}{ax^2 + bx + c} dx = \frac{1}{2a} \ln|ax^2 + bx + c| - \frac{b}{a\sqrt{4ac - b^2}} \tan^{-1} \frac{2ax + b}{\sqrt{4ac - b^2}}$$

Integrales con raíces

17)
$$\int \sqrt{x-a} dx = \frac{2}{5}(x-a)^{3/2}$$

17)
$$\int \sqrt{x-a} dx = \frac{2}{3}(x-a)^{3/2}$$

18) $\int \frac{1}{\sqrt{x\pm a}} dx = 2\sqrt{x\pm a}$

$$19) \int \frac{1}{\sqrt{a-x}} dx = -2\sqrt{a-x}$$

20)
$$\int x\sqrt{x-a}dx = \frac{2}{3}a(x-a)^{3/2} + \frac{2}{5}(x-a)^{5/2}$$
21)
$$\int \sqrt{ax+b}dx = \left(\frac{2b}{3a} + \frac{2x}{3}\right)\sqrt{ax+b}$$
22)
$$\int (ax+b)^{3/2}dx = \frac{2}{5a}(ax+b)^{5/2}$$
23)
$$\int \frac{x}{\sqrt{x\pm a}}dx = \frac{2}{3}(x\mp 2a)\sqrt{x\pm a}$$

21)
$$\int \sqrt{ax+b}dx = \left(\frac{2b}{3a} + \frac{2x}{3}\right)\sqrt{ax+b}$$

22)
$$\int (ax+b)^{3/2} dx = \frac{2}{5a}(ax+b)^{5/2}$$

23)
$$\int \frac{x}{\sqrt{x \pm a}} dx = \frac{2}{3} (x \mp 2a) \sqrt{x \pm a}$$

24)
$$\int \sqrt{\frac{x}{a-x}} dx = -\sqrt{x(a-x)} - a \tan^{-1} \frac{\sqrt{x(a-x)}}{x-a}$$

25)
$$\int \sqrt{\frac{x}{a+x}} dx = \sqrt{x(a+x)} - a \ln \left[\sqrt{x} + \sqrt{x+a} \right]$$

26)
$$\int x\sqrt{ax+b}dx = \frac{2}{15a^2}(-2b^2+abx+3a^2x^2)\sqrt{ax+b}$$

27)
$$\int \sqrt{x(ax+b)} dx = \frac{1}{4a^{3/2}} \left[(2ax+b)\sqrt{ax(ax+b)} - b^2 \ln \left| a\sqrt{x} + \sqrt{a(ax+b)} \right| \right]$$

28)
$$\int \sqrt{x^3(ax+b)} dx = \left[\frac{b}{12a} - \frac{b^2}{8a^2x} + \frac{x}{3} \right] \sqrt{x^3(ax+b)} + \frac{b^3}{8a^{5/2}} \ln \left| a\sqrt{x} + \sqrt{a(ax+b)} \right|$$

29)
$$\int \sqrt{x^2 \pm a^2} dx = \frac{1}{2} x \sqrt{x^2 \pm a^2} \pm \frac{1}{2} a^2 \ln |x + \sqrt{x^2 \pm a^2}|$$

30)
$$\int x\sqrt{x^2 \pm a^2} dx = \frac{1}{3} (x^2 \pm a^2)^{3/2}$$

31)
$$\int \frac{1}{\sqrt{x^2 + a^2}} dx = \ln \left| x + \sqrt{x^2 \pm a^2} \right|$$

32)
$$\int \frac{1}{\sqrt{a^2 - x^2}} dx = \sin^{-1} \frac{x}{a}$$

33)
$$\int \frac{x}{\sqrt{x^2 \pm a^2}} dx = \sqrt{x^2 \pm a^2}$$

34)
$$\int \frac{x}{\sqrt{a^2 - x^2}} dx = -\sqrt{a^2 - x^2}$$

35)
$$\int \frac{x^2}{\sqrt{x^2 + a^2}} dx = \frac{1}{2} x \sqrt{x^2 \pm a^2} \mp \frac{1}{2} a^2 \ln |x + \sqrt{x^2 \pm a^2}|$$

36)
$$\int \sqrt{ax^2 + bx + c} dx = \frac{b + 2ax}{4a} \sqrt{ax^2 + bx + c} + \frac{4ac - b^2}{8a^{3/2}} \ln \left| 2ax + b + 2\sqrt{a(ax^2 + bx + c)} \right|$$