

Answer 4.4

X is normal is nature

We have to run iterations n=1000

```
In [1]: 1 import numpy as np
        2
        3 n = 1000
        4 mu_x = 0
        5 sigma_x = 1
        6 X = np.random.normal(mu_x, sigma_x, n)
        7 beta = 5
        8 sigma = 3
        9 Yandx = []
       10 for i in range (n):
       11     mu = beta* X[i]
       12     temp = np.random.normal(mu, sigma, 1)[0]
       13     Yandx.append(temp)
```

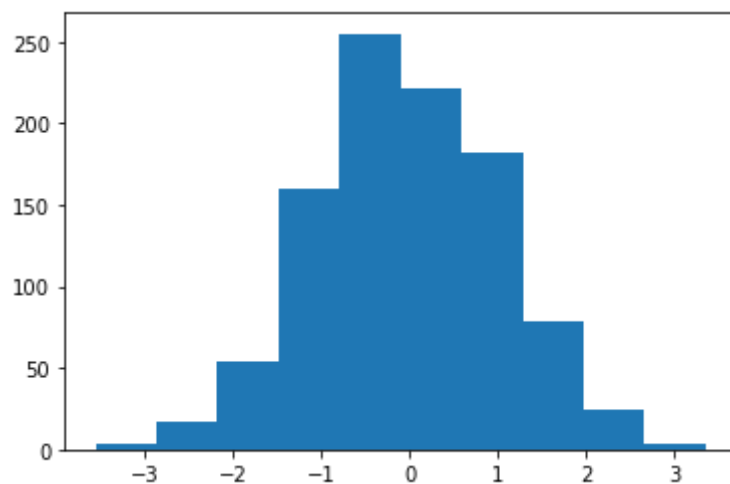
```
In [ ]: 1
```

```
In [19]: 1 missing_val_ind = np.where(np.abs(X)>2 , 1,0)
2 def filter_data(X,Yandx,missing_idx):
3     X_new = []
4     Y_new = []
5     for i in range(len(missing_idx)):
6         if missing_val_ind[i] == 0 :
7             X_new.append(X[i])
8             Y_new.append(Yandx[i])
9     return X_new,Y_new
10 # beta_hat = sum xiyi/sum xi**2
11 def get_beta_hat(X,Y):
12     numer = 0
13     denom = 0
14     for i in range(len(X)):
15         numer+= X[i]*Y[i]
16         denom+= X[i]**2
17     beta_hat = numer/denom
18     return beta_hat
19 X_new,Y_new = filter_data(X,Yandx,missing_val_ind)
20 beta_hat = get_beta_hat(X_new,Y_new)
21
22 print("Beta Hat= {:.1f}".format(beta_hat))
23
```

Beta Hat= 5.0

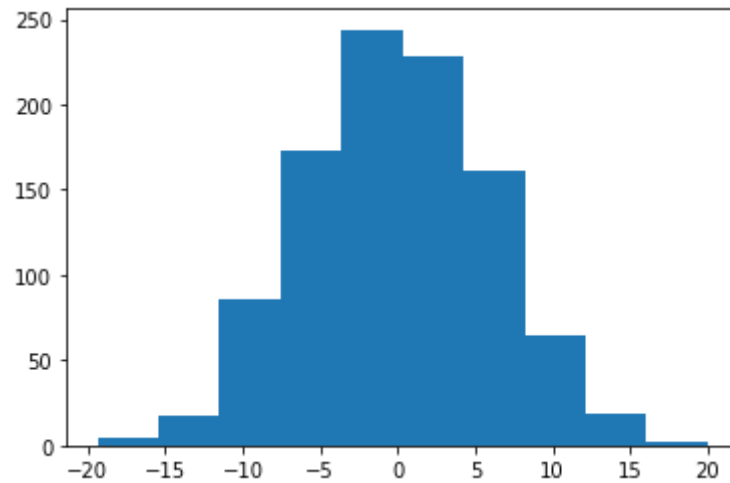
```
In [38]: import seaborn as sns
import matplotlib.pyplot as plt
plt.hist(X_new)
```

```
Out[38]: (array([ 3., 17., 54., 160., 255., 222., 182., 79., 24., 4.]),
array([-3.56244834, -2.87000028, -2.1775222, -1.48510416, -0.7926561 ,
        -0.10020803,  0.59224003,  1.28468809,  1.97713615,  2.66958421,
         3.36203228]),
<BarContainer object of 10 artists>)
```



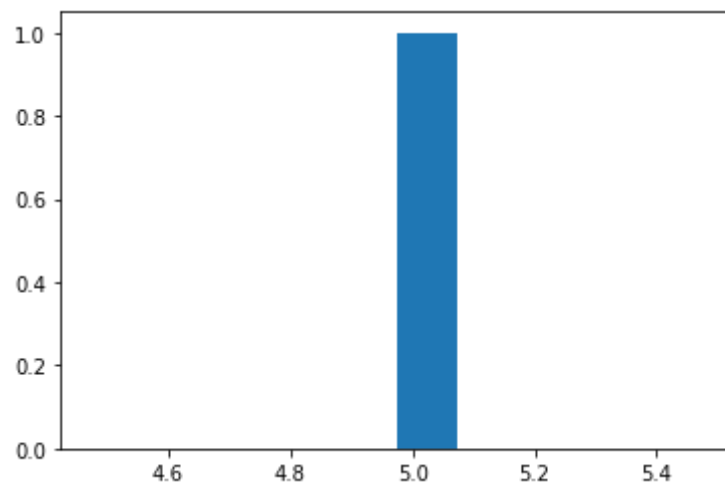
```
In [52]: 1 plt.hist(Y_new)
```

```
Out[52]: (array([ 5., 18., 86., 173., 244., 228., 161., 64., 19., 2.]),  
array([-19.37088293, -15.43266722, -11.49445151, -7.55623579,  
-3.61802008, 0.32019564, 4.25841135, 8.19662706,  
12.13484278, 16.07305849, 20.01127421]),  
<BarContainer object of 10 artists>)
```



```
In [57]: 1 plt.hist(beta_hat)
```

```
Out[57]: (array([0., 0., 0., 0., 0., 1., 0., 0., 0., 0.]),
 array([4.47340283, 4.57340283, 4.67340283, 4.77340283, 4.87340283,
        4.97340283, 5.07340283, 5.17340283, 5.27340283, 5.37340283,
        5.47340283]),
 <BarContainer object of 10 artists>)
```



The beta hat is consistent with the original beta with is set at = 5, (on rounding off as noticed)

Answer 4.5

```
In [20]: 1 gamma_0 = 1
          2 gamma_1 = 2
          3 a = gamma_0 + gamma_1*X
          4 missingProbability = np.exp(a)/(1+np.exp(a))
          5 missing_val_ind = np.where(missingProbability==1.0 , 1,0)
          6 X_new,Y_new = filter_data(X,Yandx,missing_val_ind)
          7 beta_hat = get_beta_hat(X_new,Y_new)
          8 print("Beta Hat={:0.1f}".format(beta_hat))
          9
```

Beta Hat=5.0

When the missing values are removed based on the condition in 4.5 we can still use $\hat{\beta}$ as a consistent estimator.

```
In [58]: 1 plt.hist(beta_hat)
```

```
Out[58]: (array([0., 0., 0., 0., 0., 1., 0., 0., 0., 0.]),  
          array([4.47340283, 4.57340283, 4.67340283, 4.77340283, 4.87340283,  
                4.97340283, 5.07340283, 5.17340283, 5.27340283, 5.37340283,  
                5.47340283]),  
          <BarContainer object of 10 artists>)
```

