

## BULK QUEUES

This is a class of queues in which arrival or service (or both) is in bulks. This scenario is commonly found in ticket booking counters where a group of people arrive for ticket booking but they are served one at a time. This is referred to as BULK ARRIVAL. Another form of it is commonly seen in tourist places where a group of people arrive and a single tourist guide takes them through the place. This is referred to as BULK SERVICE, since one server, the tourist guide servers a group of people at the same time.

### Bulk Arrival:

This form of the queue is an extension of the  $M/M/1$  queuing system whereby we now make an additional assumption that  $x$  ( $x \geq 1$ ) customers arrive, with probability  $c_x$ , for service and are served one at a time by the server (assuming 1 server). It is denoted by:  $M^{[X]}/M/1$ . If  $\lambda_x$  is the arrival rate of a batch of size  $X$ , then

$c_x = \frac{\lambda_x}{\lambda}$ ,  $\lambda$  being the composite arrival rate of all the batches and equals  $\sum_{x=1}^{\infty} \lambda_x$ . This is also known as compound

Poisson process. We can similarly extend  $M/M/c, M/M/c/c, M/M/c/k$  models in terms of bulk arrivals.

For an  $M^{[X]}/M/1$  system, the measures of effectiveness are

- a) Average number of customers in the system:

$$L = \frac{r(E(X) + E(X^2))}{2(1-\rho)} = \frac{\rho + rE(X^2)}{2(1-\rho)}, \left( \rho = \frac{\lambda E(X)}{\mu}, r = \frac{\lambda}{\mu} \right)$$

- b) Average number of customers in the queue: By Little's formula, we get:

$$L_q = L - \rho = \frac{\rho^2 + (r-1)\rho}{2(1-\rho)} \text{ for a batch of size } \left( \rho = \frac{\lambda E(X)}{\mu}, r = \frac{\lambda}{\mu} \right)$$

- c) Steady State Probability: The probability of  $n$  customers in the system is given by:

$$p_n = (1-\rho) \{ [\alpha + (1-\alpha)\rho]^{n-1} [(1-\alpha)\rho] \}$$

### Bulk Service:

In this form of queuing system, the customers arrive to the server one at a time and the server is capable of serving  $K$  customers at a time. This shows two possibilities: (a) the server waits to serve till there are  $K$  customers to be served or (b) the server performs service if there are  $0 < i \leq K$  customers awaiting service. Hence, depending on the system, anyone of the disciplines is applicable. We denote a single server, bulk service by  $M/M^{[X]}/1$ . The other queuing models can be similarly extended.

It should be noted that the Markovian nature in these forms of queuing systems is maintained since the inter-arrival and service times are assumed to follow exponential distribution.