

# Rendering 3D Scenes

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IMPA

## Outline

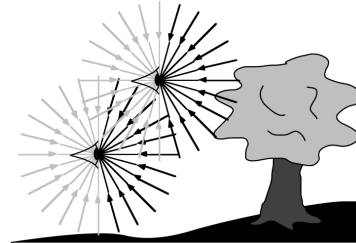
- Plenoptic Function / Light Fields
- Illumination
- Cameras
- Viewing Pipeline
- Rendering Architectures

# Plenoptic Function

*Complete description of Visual Information in a 3D environment*

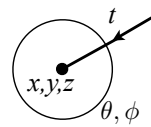
- $I_\lambda = P(x, y, z, \theta, \phi, t)$

Holographic Image



- $P : \mathbb{R}^3 \times \mathbb{S}^2 \times \mathbb{R} \mapsto \mathcal{E}$

6D Phase Space



*OBS: No Explicit Geometry - Scene Modeling to the Rescue !*

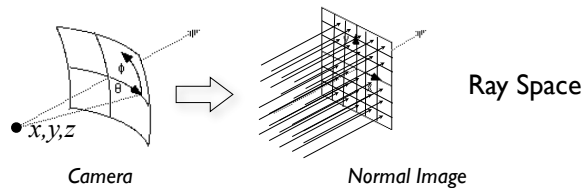
## Light Field

*A Slice of the Plenoptic Function*

\* Structured Sampling of  $P$

- Point Sampling ( Inverse Rendering )

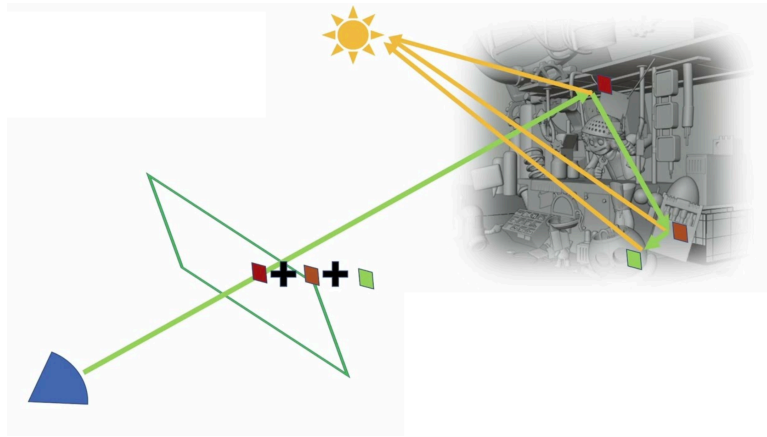
- Pinhole Camera Model



$(x, y, z)$  Viewpoint /  $(\theta, \phi)$  Field of View (FOV)

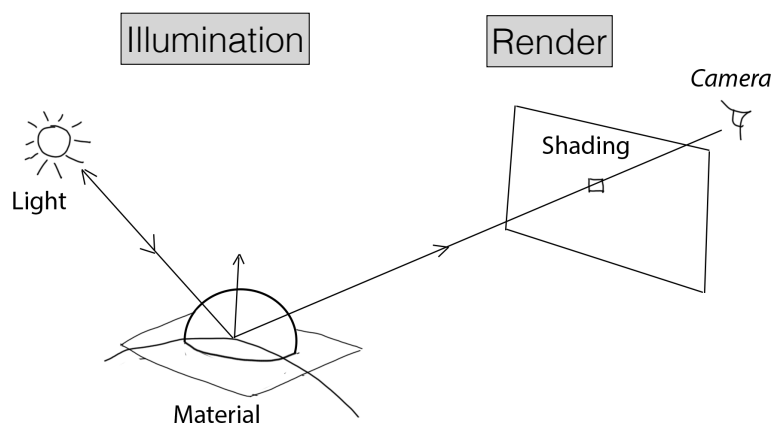
# Synthesizing the Plenoptic Function

- Illumination
  - Light Sources
  - Materials
- Rendering
  - Shading



## Conceptual Model

- **Data Driven Computation**



# *Illumination*

## **Illumination**

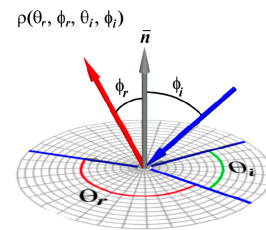
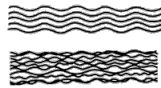
*Study of Light Emission and Propagation*

- Light
- Materials
-

# Local Illumination

## Illumination Mechanisms

- Light Transport
  - Coherent
  - Incoherent
- Bidirectional Transport Function
  - *BRDF* - Reflection
  - *BTDF* - Transmission



## Study Topics



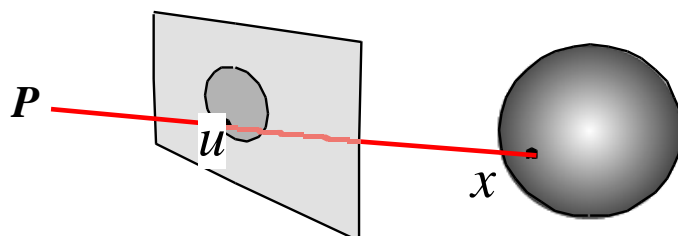
- Projective Geometry
- Camera Calibration

# *Projective Geometry & Cameras*

## Mathematical Fundamentals

- Projective Geometry

$$2D \leftrightarrow 3D$$



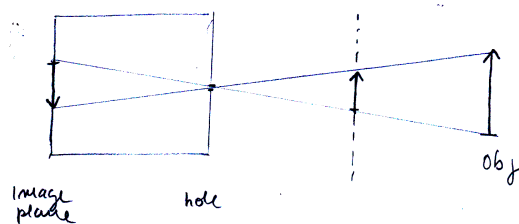
$$u = Px$$

$$u \in \mathbb{R}^2, \quad x \in \mathbb{R}^3$$

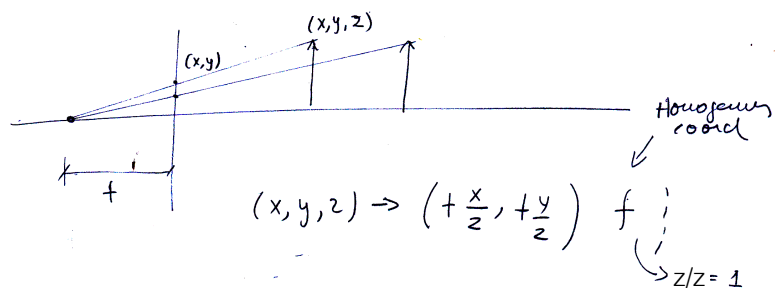
# Projective Geometry

- Camera Transform
  - Projection (3D  $\Rightarrow$  2D)
    - 2D Image  $u \in I \subset \mathbb{R}^2$
    - 3D Space  $x \in \mathbb{R}^3$
    - Camera  $u = Px$
- Types of Projection
  - Orthographic (Affine)
  - Perspective
  - Etc..

## Pinhole Camera Model

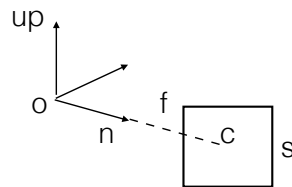


- Perspective Projection.



# Vision / Graphics

- Camera Model



- Camera Parameters

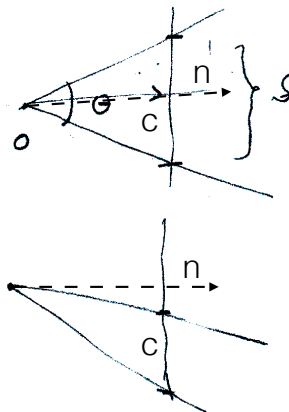
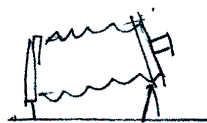
- Position:  $o$
- Orientation:  $up, n$
- Focal Distance:  $f$
- Image Center:  $c$
- Image Size:  $s$

# Field of View

- Pinhole Camera



- View Camera





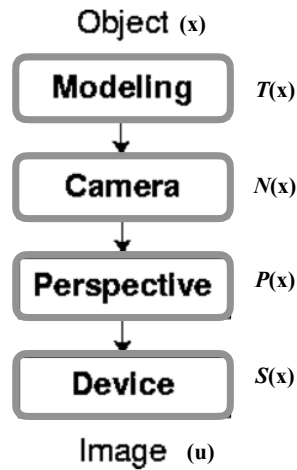
# Viewing Transformations

## Viewing Operations

- **Camera Transformation**
- **Clipping**
- **Projection**
- **Rasterisation**
- **Visibility**

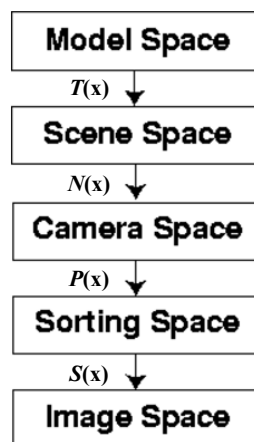
# Viewing Pipeline

*“Sequence of transformations mapping 3D objects to viewport”*



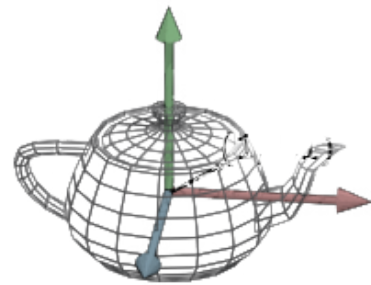
# Reference Spaces

*“Objects are transformed to coordinate systems where viewing operations are performed”*



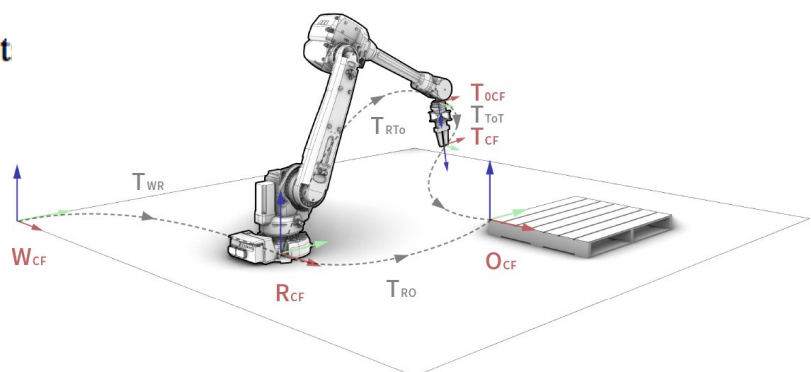
## Model Space

- Characteristics
  - Object Coordinate System
  - Origin: Center of Object
  - Principal Axis (Object)
  - Normalized
- Operation
  - Modeling Ops



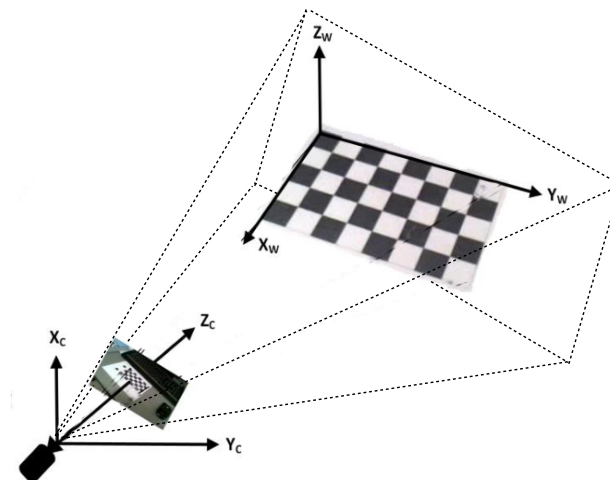
## Scene Space

- Characteristics
  - Global Coordinate System
  - All Objects
  - Application Unit
- Operation
  - Shading



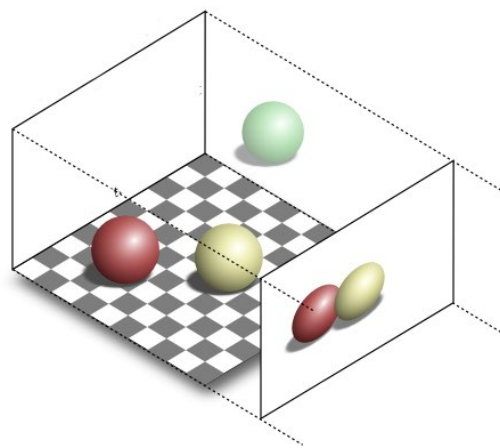
## Camera Space

- Characteristics
  - Camera Coordinate System
  - XY Plane: Image Plane
  - Z Axis: View Direction
  - Normalized Fustrum
- Operation
  - Clipping



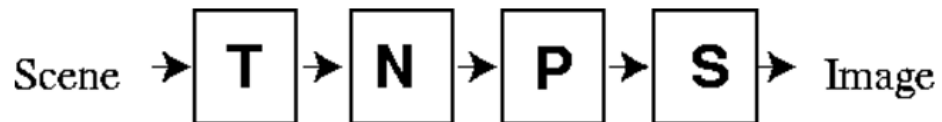
## Sorting Space

- Characteristics
  - Sorting Coordinate System
  - Viewpoint at Infinity
  - Preserve Linear Structures
- Operation
  - Visibility Computation

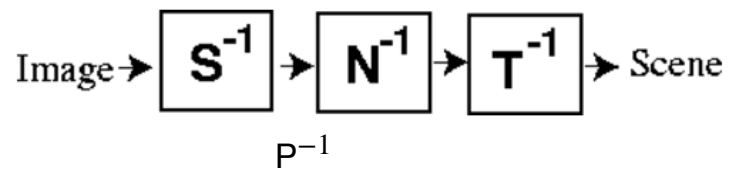


# Viewing Pipeline

- Parametric Models

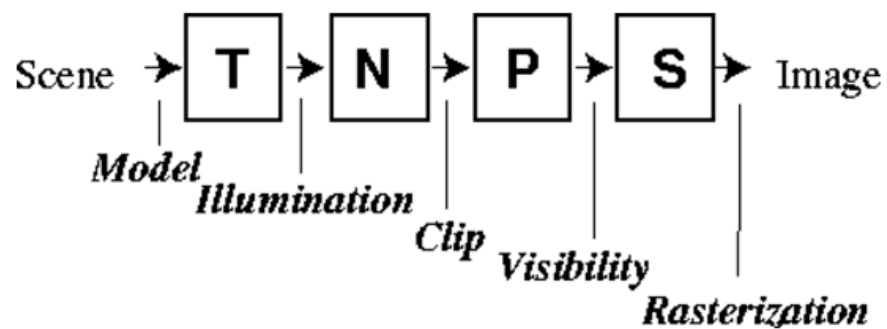


- Implicit Models



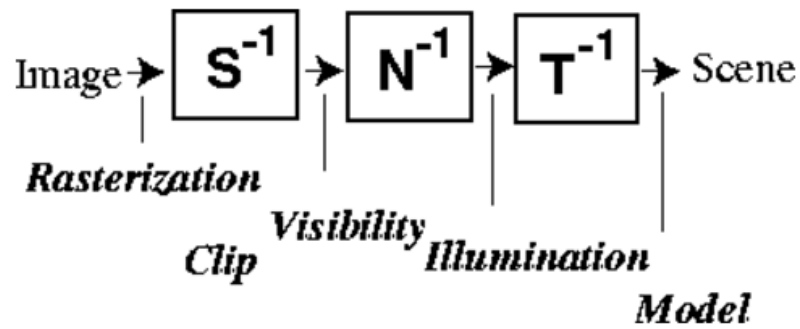
# Object Centered Pipeline

- Projection + Raster



# Image Centered Pipeline

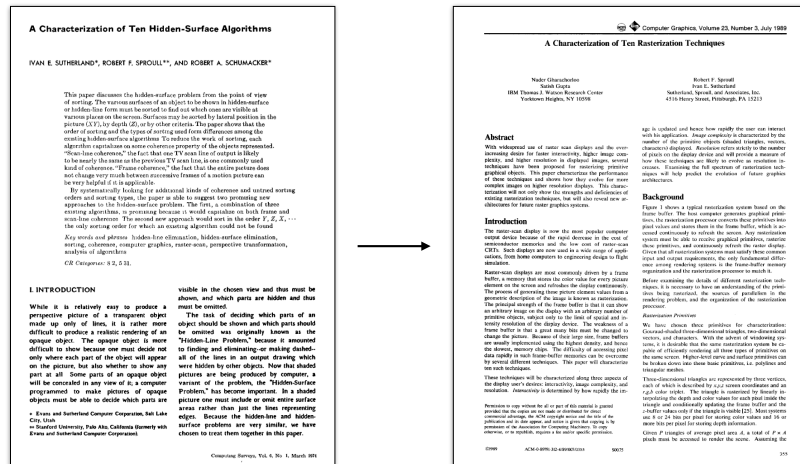
- Ray Casting



*Rendering Architectures*

# A Bit of History

- From Visibility to Rasterization



1974

1989

# Main Algorithms

## ♦ Projection + Rasterization

- Object Space
  - Pre-Compute Order of Pieces
  - (Visibility First)

## ♦ Ray Casting

- Image Space
  - Ordering at Each Ray
  - (Visibility Last)

# Looking Ahead

- **Sistemas Gráficos 3D**

- [Descrição](#)
- [Conteúdo](#)
- [Software](#)
- [Notas de Aula](#)
- [Metodologia](#)
- [Padrões Gráficos](#)

