

Gautam Buddha University
Engineering Mathematics-III (MA-201)
Second semester (2016-2017)
Tutorial Sheet-2

Differential Equation Reducible to Separable Form, Exact Differential equation.

Q. 1 Solve the following differential equations by first reducing to separable form:

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| (a) $\cos(x+y)dy = dx$ | (i) $(x^2 - y^2)dx + 2xydy = 0$, |
| (b) $\frac{dy}{dx} = \cos(x+y) + \sin(x+y)$ | (j) $(x^2 + y^2)dx + 2xydy = 0$, |
| (c) $\sin^{-1}\left(\frac{dy}{dx}\right) = x + y$ | (k) $x\frac{dy}{dx} + \frac{y^2}{x} = x$. |
| (d) $\log\left(\frac{dy}{dx}\right) = ax + by$ | (l) $\frac{dy}{dx} = \frac{y}{x} + \tan \frac{y}{x}$ |
| (e) $\frac{dy}{dx} = e^{x+y}$, $y(1) = 1$. | (m) $\frac{dy}{dx} = \frac{y-x+1}{y+x+5}$, |
| (f) $\frac{dy}{dx} = \sin^2(x-y+1)$ | (n) $\frac{2x-y+1}{x+2y-3} - \frac{dy}{dx} = 0$, |
| (g) $x + y\frac{dy}{dx} = 2y$, | (o) $\frac{dy}{dx} = \frac{x+y+4}{x+y-6}$, |
| (h) $\frac{x-2y}{2x-y} + \frac{dy}{dx} = 0$, | |

Q. 2 Find the equation of the curve that passes through the point (1, 2) and has slope at any point (x, y)

$$\frac{dy}{dx} = -\frac{2xy}{x^2 + 1}$$

Q. 3 Check whether the following differential equations are exact or not if happen to be exact then find their general solution:

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| (a) $(x + \frac{2}{y})dy + ydx = 0$ | (d) $(2xy^4 + \sin y)dx + (4x^2y^3 + x \cos y)dy = 0$ |
| (b) $(y + y \cos xy)dx + (x + x \cos xy)dy = 0$ | (e) $2x(1 + \sqrt{x^2 - y})dx = (\sqrt{x^2 - y})dy$ |
| (c) $(\sin x \sin y - xe^y)dy = (e^y + \cos x \cos y)dx$ | |

Q. 4 Define an integrating factor. Show that the $M(x, y)dx + N(x, y)dy = 0$ always has an IF $\mu(x, y)$ if it has a general solution. Moreover in this case there are infinitely many IFs.

Q. 5 Under what conditions, the differential equation $(ax + by)dx + (kx + ly)dy$ is exact? Hence solve the exact equation.