

Recursion – 4

Lecture-30

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Finding subarrays *→ vo subsequence jo ki continuous fashion me ho*

Find out all the subarrays of an array.

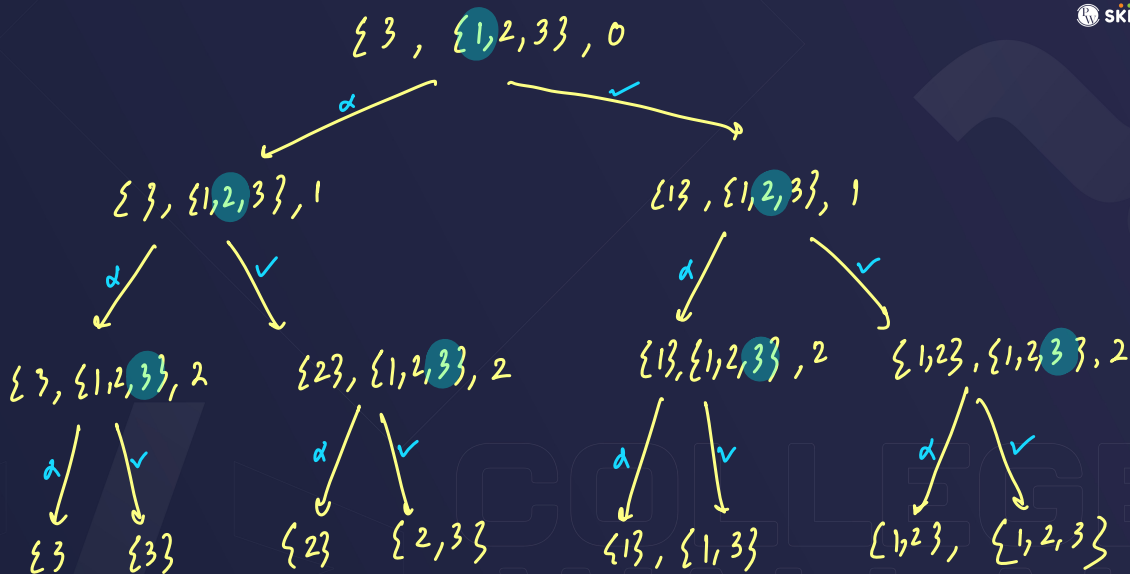
$arr = \{1, 2, 3, 4\}$

→ $\{1\}, \{2\}, \{3\}, \{4\}, \{1, 2\}, \{1, 3\}, \{1, 4\}, \{2, 3\}, \{2, 4\}, \{3, 4\},$
 $\{1, 2, 3\}, \{1, 2, 4\}, \{1, 3, 4\}, \{2, 3, 4\}, \{1, 2, 3, 4\}$

1	2		
1 2	2 3	3	
1 2 3	2 3 4	3 4	4
1 2 3 4			

```
for(int i=0;i<n;i++){ // start
    for(int k=i;k<n;k++){
        for(int j=i;j<=k;j++){
            cout<<arr[j];
        }
        cout<<endl;
    }
}
```

→ k only denotes no. of rounds in loop {1,2,3,4}



Will work in unique elements only.

Palindrome using recursion

Find out whether a given string is palindrome or not using recursion

dad

mom

aba

abcdcba

racecar

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Greatest Common Divisor

Calculate Greatest Common Divisor of two numbers.

$$\text{hcf}(24, 60) = 12$$

```
for(int i = 24; i >= 2; i--) {
    if (24 % i == 0 && 60 % i == 0) return i;
}
return 1; → T.C. = O(min(a, b))
```

$$\text{hcf}(a, b) \leq \min(a, b)$$

$$\text{lcm}(a, b) \geq \max(a, b)$$

Euclid's Division Algo (long division method)

$$\begin{array}{r}
 24 \overline{) 60} \quad 2 \\
 \underline{48} \\
 12 \overline{) 24} \quad 2 \\
 \underline{24} \\
 0
 \end{array}$$

HCF

$$\begin{array}{r}
 10000 \overline{) 10001} \quad 1 \\
 \underline{10000} \\
 1 \overline{) 10000} \quad 10000 \\
 \underline{10000} \\
 0
 \end{array}$$

HCF

$$\begin{array}{r}
 27 \overline{) 45} \quad 1 \\
 \underline{27} \\
 18 \overline{) 27} \quad 1 \\
 \underline{18} \\
 9 \overline{) 18} \quad 2 \\
 \underline{18} \\
 0
 \end{array}$$

HCF

Time Complexity of $\gcd(a, b)$ is $O(\log(a+b))$

HCF \rightarrow 27 & 45

$$\gcd(27, 45)$$

$$\downarrow$$

$$\gcd(45 \% 27, 27) = \gcd(18, 27)$$

$$\downarrow$$

$$\gcd(27 \% 18, 18) = \gcd(9, 18)$$

$$\downarrow$$

$$\gcd(18 \% 9, 9) = \gcd(0, 9)$$

$$\gcd(\underset{a}{45}, \underset{b}{27}) = \gcd(27, 45)$$

$$27 \% 45$$

$$a \% b = a \text{ if } a < b$$

HCF
 \uparrow

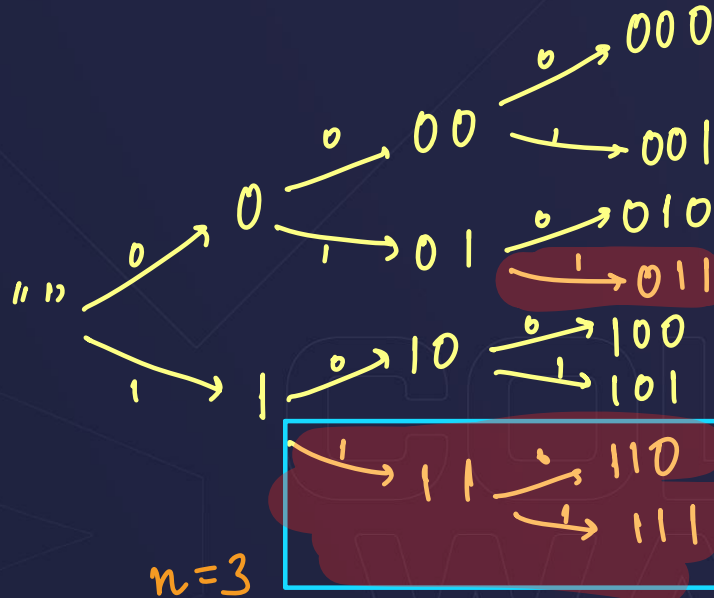
Practice

Generate all **binary strings** of length n without consecutive 1's

$$2^n$$

$$n = 2$$

\rightarrow "00"
 "01"
 "10"
 "11"



Ques: Combination Sum

[Leetcode - 39]

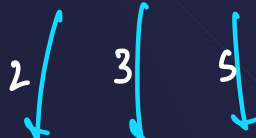
$\{\}, \{2, 3, 5\}, 8$



$\{2\}, \{2, 3, 5\}, 6$

$\{3\}, \{2, 3, 5\}, 5$

$\{5\}, \{1, 2, 3\}, 3$



$\{2, 2\}, 4$

$\{2, 3\}, 3$

$\{2, 5\}, 1$

$\{3, 2\}, 2$



$\{2, 2, 2\}, 2$

$\{2, 2, 5\}, -1$

$\{2, 2, 3\}, 1$

Ques: Generate Parentheses

[Leetcode - 22]

Input: $n = 3$

Output: ["((()))", "(()())", "(())()", "()(())", "()()()"]

$n=1 \rightarrow ()$

$n=2 \rightarrow ()(), (())$

$n=3 \rightarrow ()()(), (())(), (())(), (())(), ()()()$

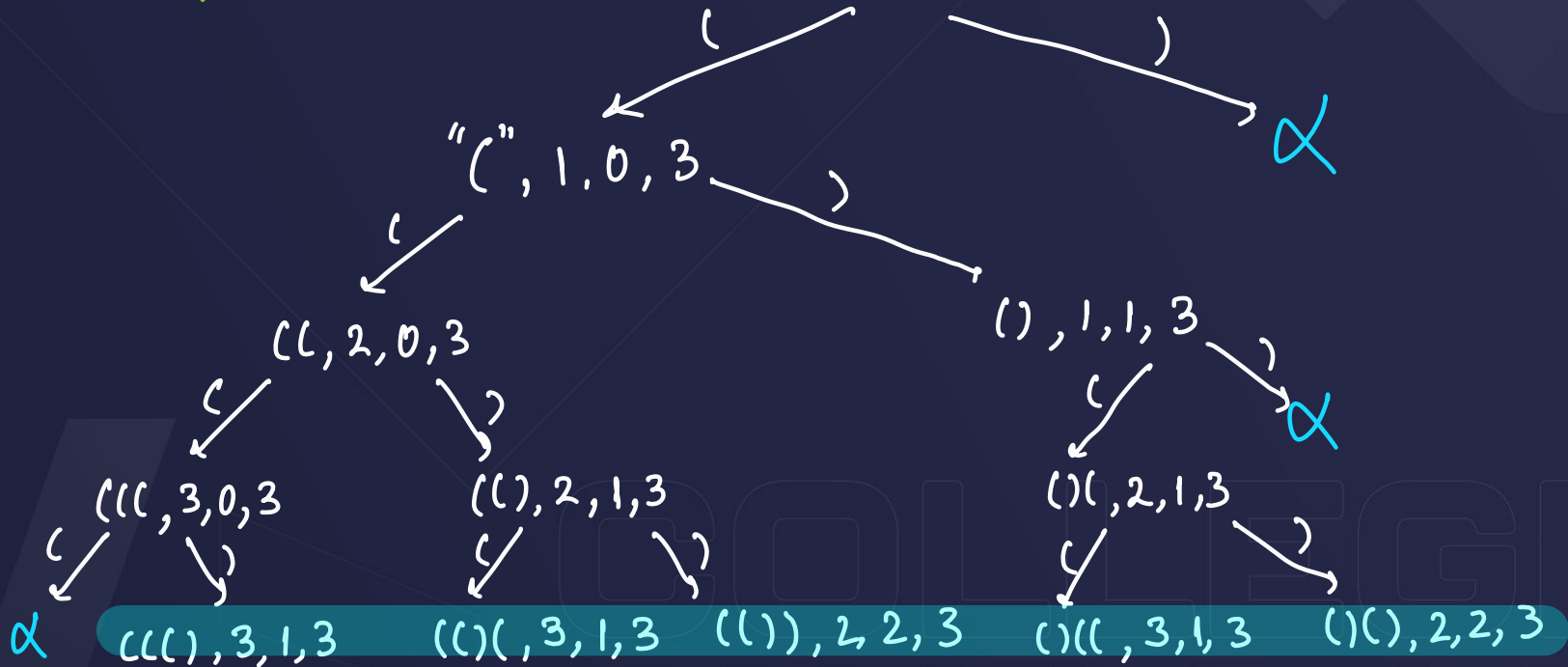
VIMP observations

at every instant,
no. of opening bckts \geq
no. of closing bckts.

Ques: Generate Parentheses [Leetcode - 22]

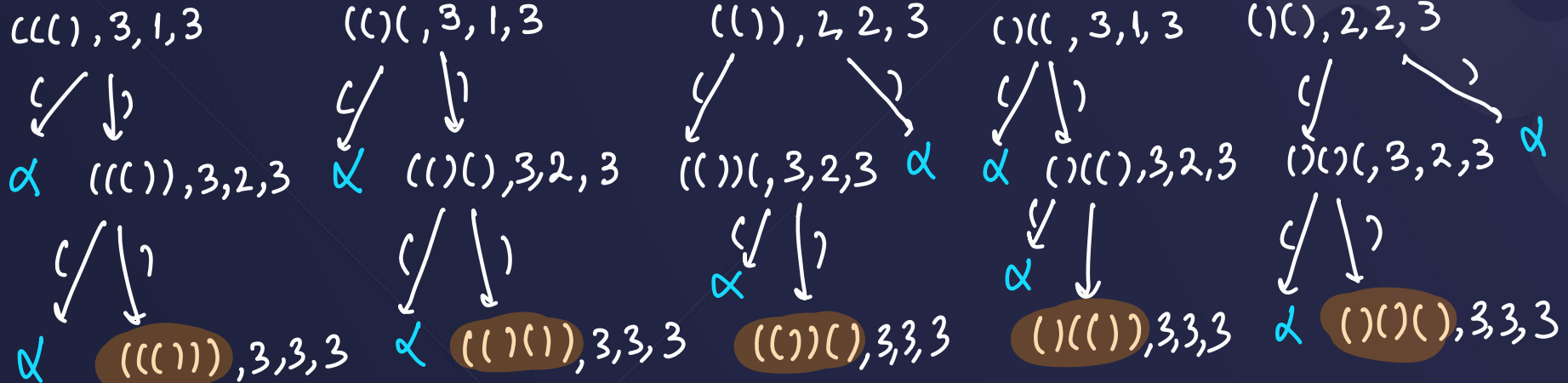
$n = 3 \rightarrow (, (, (,),),)$

str op cl n
" ", 0, 0, 3



Ques: Generate Parentheses

[Leetcode - 22]



Input: $n = 3$

Output: `["((()))", "(()())", "(())()", "()(())", "()()()"]`

Ques: Kth Symbol in Grammar

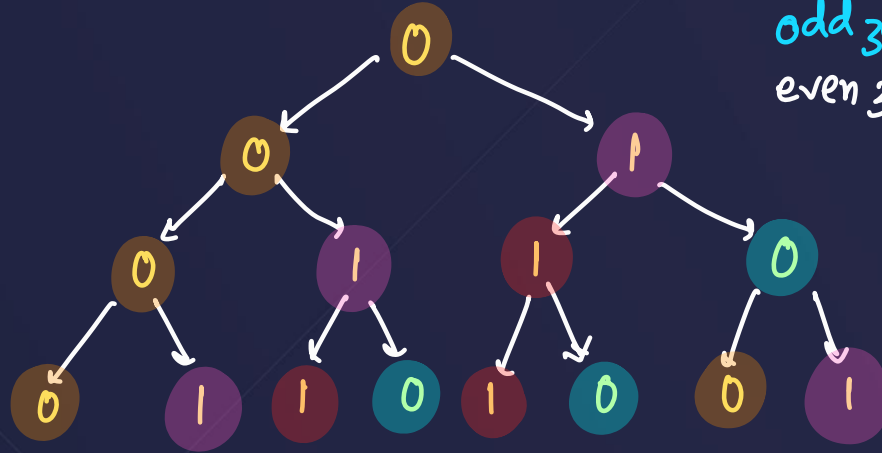
[Leetcode - 779]

1 →

2 →

3 →

4 →



odd zeroes → 0 se gen
even zeroes → 1 se gen

$$T.C. = O(n)$$

$n = 4, k = 5$

$0 \rightarrow 01$

$1 \rightarrow 10$

odd ones → 1 se

even ones → 0 se

$kth(n, k) \rightarrow \text{if}(k \% 2 == 0) \rightarrow kth(n-1, \frac{k}{2})$

$kth(n, k) \rightarrow \text{if}(k \% 2 != 0) \rightarrow kth(n-1, \frac{k}{2} + 1)$

Ques: Kth Symbol in Grammar

[Leetcode - 779]

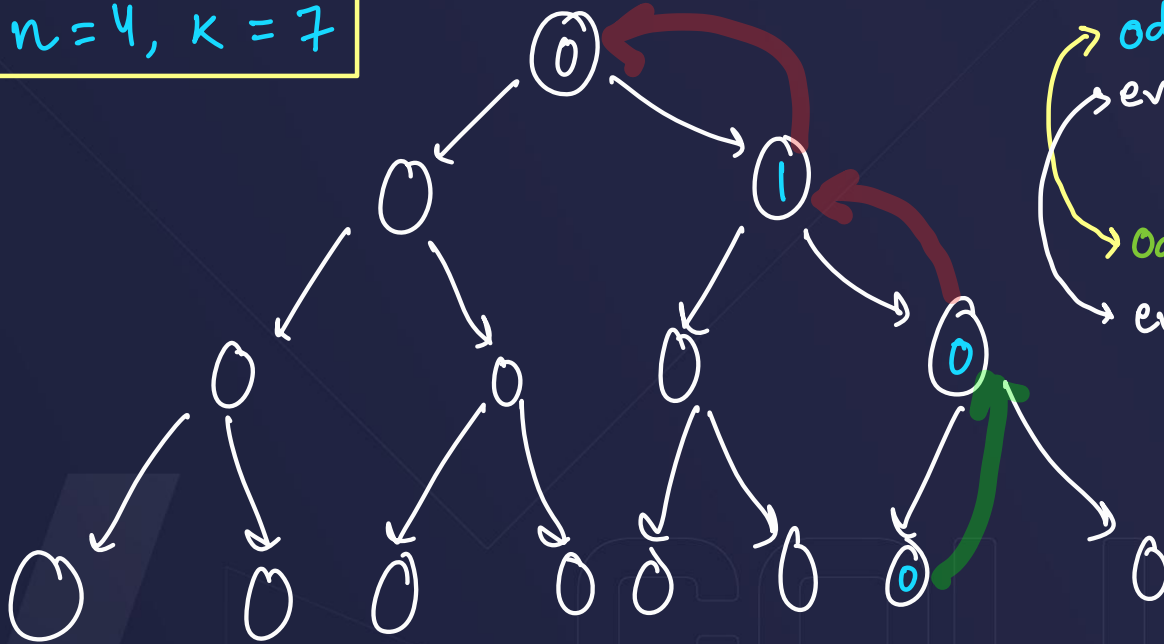
1

$n = 4, k = 7$

2

3

4



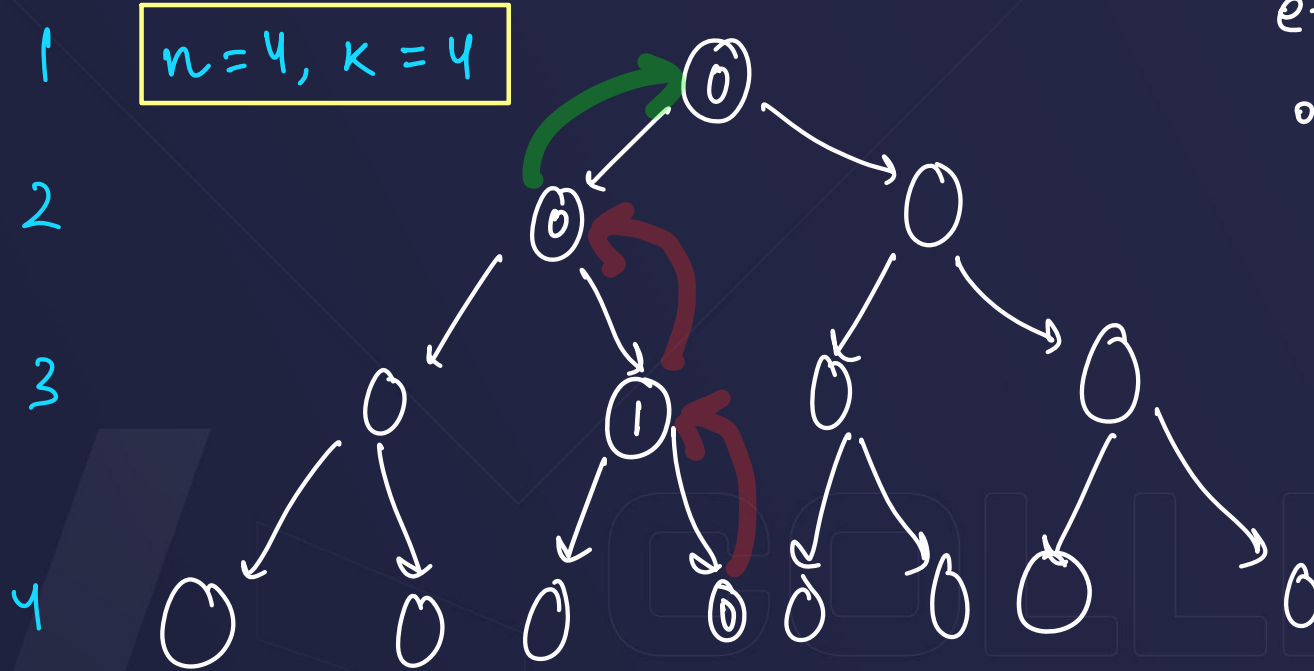
odd zeroes → 0 se gen
even zeroes → 1 se gen
odd ones → 1 se
even one → 0 se

$$kth(n, k) \rightarrow \text{if } (k \% 2 == 0) \rightarrow kth(n-1, \frac{k}{2})$$

$$kth(n, k) \rightarrow \text{if } (k \% 2 != 0) \rightarrow kth(n-1, \frac{k}{2} + 1)$$

Ques: Kth Symbol in Grammar

[Leetcode - 779]



even \rightarrow flip
odd \rightarrow same

Ques: Count and Say

[Leetcode - 38]

cas(n) = the way you would speak cas(n-1)

cas(1) = "1";

cas(7) = "13112221"

cas(2) = one 1 → "11"

cas(8) = "1113213211"

cas(3) = two 1 ⇒ "21"

cas(4) = "1211"

cas(5) = "111221"

cas(6) = "312211"

"3322251"

two 3's, three 2's, one 5, and one 1

2 3 + 3 2 + 1 5 + 1 1

"23321511"

Ques: Permutation Sequence

[Leetcode - 60]

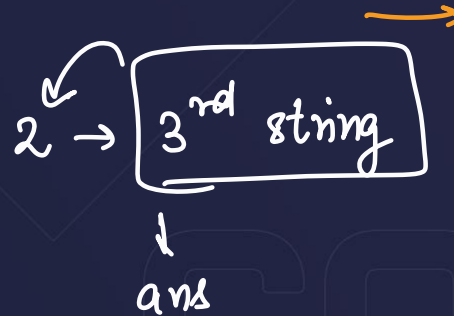
$n = 4 \rightarrow 4! = 24$ permutations
 $k = 9$

ori n ans idx k
 \hookrightarrow "1234", 4, "", 0, 9

\rightarrow 134, 3, 2, , 3

\rightarrow 14, 2, 23,

1 se start $\rightarrow 6$



2 ---
 1, 3, 4

134

143

314

341

413

431

\rightarrow 14

1234

1243

1324

1342

1423

1432

2134

2143

2314

2341

2413

2431

3124

3142

3214

3241

3412

3421

4123

4132

4213

4231

4312

4321

$n=4$
 $k=18 \rightarrow \text{fact} = (n-1)! = 3! = 6$

1234

1243

1324

1342

1423

1432

2134

2143

2314

2341

2413

2431

3124

3142

3214

3241

3412

3421

4123

4132

4213

4231

4312

4321

str

n

k

ans

\rightarrow

1234

4

18

" "

\rightarrow

124

3

fact

3

$$\text{fact} = (4-1)! = 6$$

$$\text{idx} = \frac{18}{6} - 1 = 2$$

if ($k \% \text{fact} \neq 0$) $\text{idx} = k / \text{fact};$

if ($k \% \text{fact} == 0$) $\text{idx} = k / \text{fact} - 1$

$n=4$
 $k=17 \rightarrow \text{fact} = (n-1)! = 3! = 6$

1234
 1243
 1324
 1342
 1423
 1432
 2134
 2143
 2314
 2341
 2413
 2431

3124
 3142
 3214
 3241
 3412
 3421
 4123
 4132
 4213
 4231
 4312
 4321

	str	n	k	ans
\rightarrow	1234	4	17	""
\rightarrow	124	3	5	3

$\text{fact} = 6$

$\text{idx} = \frac{17}{6} = 2$

$k\text{-fact}$
 $17 \% 6 = 5$

$\text{if}(k \% \text{fact} \neq 0) \text{idx} = k / \text{fact};$

$\text{if}(k \% \text{fact} == 0) \text{idx} = k / \text{fact} - 1$

$$n=4$$

$$K=4 \rightarrow \text{fact} = (n-1)! = 3! = 6$$

1234

1243

1324

1342

1423

1432

2134

2143

2314

2341

2413

2431

3124

3142

3214

3241

3412

3421

4123

4132

4213

4231

4312

4321

str

n

K

ans

→ 1234

4

4

""

→ 234

3

4

1

fact = 6

$$\text{idx} = \frac{K}{\text{fact}} = \frac{4}{6} = 0$$

$$n = 3$$

$$K = 3$$

1 2 3

1 3 2

2 1 3

2 3 1

3 1 2

3 2 1

	str	n	K	ans
→	123	3	3	""
→	13	2	1	2
→	3	1	1	21

$$\text{fact} = (2-1)! = 1! = 1$$

$$\text{idx} = \frac{K-1}{\text{fact}} = \frac{1-1}{1} = 0$$

$$n = 4$$

$$K = 2$$

Str	n	K	ans
1234	4	2	111
234	3		1

$$fact = 6$$

$$\boxed{idx} = \frac{2}{6} = 0$$

$$q = 1;$$

$$\text{if } (K \% fact == 0) \quad q = fact$$

$$\text{else } (K > fact) \quad q = K \% fact$$

Next Lecture

Advanced Sorting Algorithms

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