3. If
$$\beta_n = X$$
 is used \overline{O}_n

where $\overline{O}_n \geq \overline{O}_{n-1} + \alpha \left(1 - \overline{O}_{n-1} \right)$ then, show that, where $\overline{O}_0 = c$

On is an exponential receney weighted average without bias,

=) On will be independant of Qo

 $\overline{D}_{n} = \overline{O}_{n-1} + \propto ([-\overline{O}_{n-1}))$ $= ([-\alpha)\overline{O}_{n-1} + \propto$

 $= (1-\alpha)^2 \overline{O}_{n-2} + \alpha + \alpha(1-\alpha)$

 $=) \overline{O}_{N} = (1-x)^{2} \overline{O}_{0} + x + x(1-x) + - - -$

 $=) \overline{O}_n = \propto \left[\frac{1 - (1 - \infty)^n}{(-1 + \infty)} \right]$

 $=) \quad \overline{O}_{\eta} = \quad 1 - (1 - x)^{\eta}$

 $\Rightarrow \beta_n = \frac{\alpha}{1 - (1 - \alpha)^n} - \frac{\alpha}{1 - \alpha}$

$$= (1-\alpha)^{n} \frac{\overline{O}_{n-1}}{\overline{O}_{n}} \cdot \frac{\overline{O}_{n-2}}{\overline{O}_{n-1}} \cdot \frac{\overline{O}_{0}}{\overline{O}_{k}}$$

$$\stackrel{\sim}{\prod} (1-\beta_{i}) = 0 \quad \text{if } \overline{O}_{0} = 0$$

Since, coeff of do = 0

=) On is an exponentially weighted recency average without mittal bios.

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