



UNIVERSITÄT
KOBLENZ · LANDAU

Business Process Management

Exercise 4

Group 04

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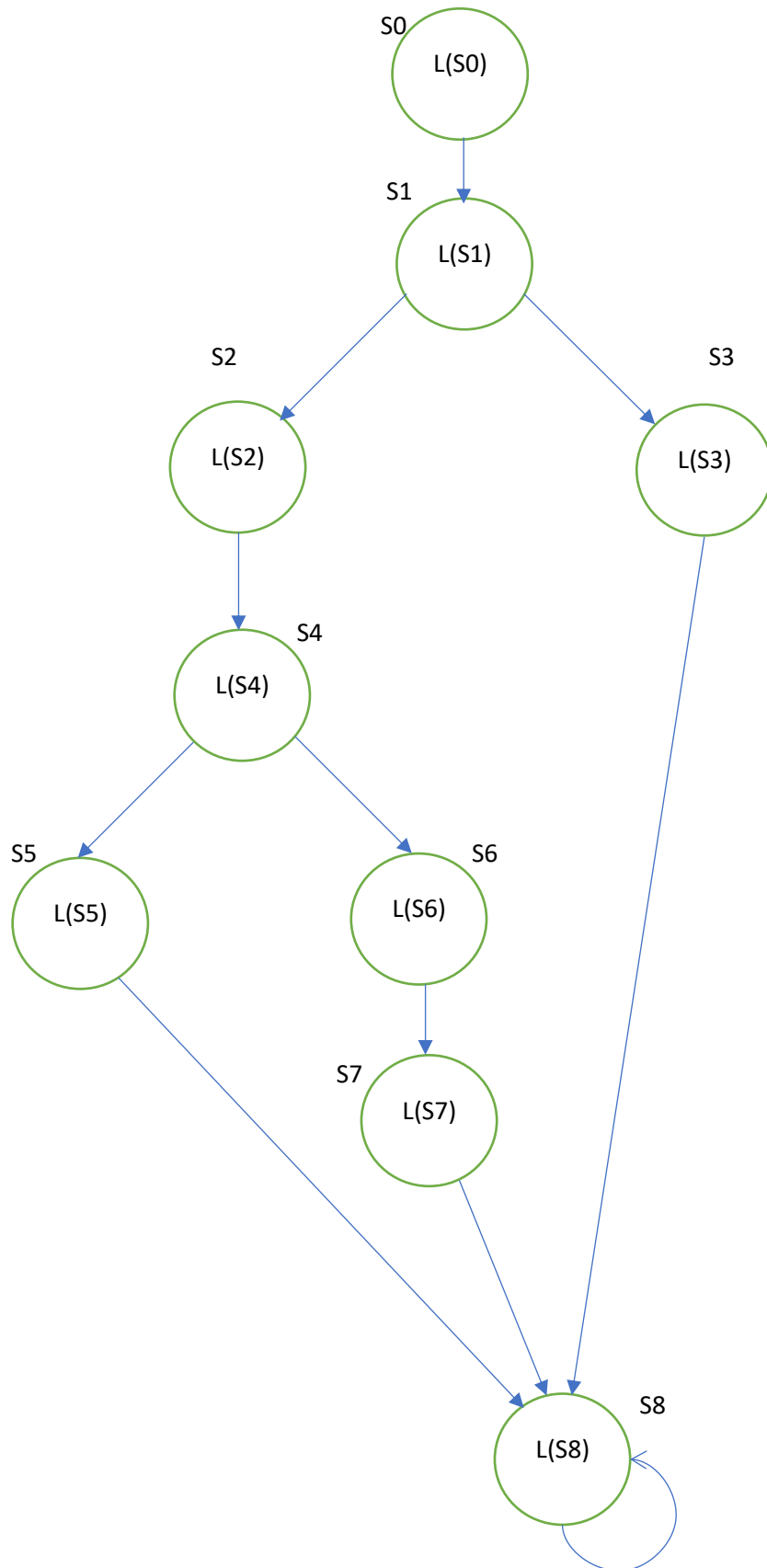
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TOTAL: 9,5/10

TASK 1 5,5/6

- **Transition System:**



$M = (S, R_t, L)$

$S = \{s_0, s_1, s_2, s_3, s_4, s_5, s_6, s_7, s_8\}$

$R_t = \{ (s_0, s_1), (s_1, s_2), (s_1, s_3), (s_2, s_4), (s_4, s_5), (s_4, s_6), (s_6, s_7), (s_7, s_8), (s_5, s_8), (s_3, s_8), (s_8, s_8) \}$

$L(s_0) = \{\text{start}\}$

$L(s_1) = \{\text{n_check_order}\}$

$L(s_2) = \{\text{n_process_order}\}$

$L(s_3) = \{\text{n_inform_customer}\}$

$L(s_4) = \{\text{n_verify_order}, \text{o_boss}\}$

$L(s_5) = \{\text{n_ship_order}\}$

$L(s_6) = \{\text{n_write_report}\}$

$L(s_7) = \{\text{n_inform_employee}, \text{o_employee}\}$

$L(s_8) = \{\text{end}\}$

- **CTL formulas**

1. The order has to be verified, before it can be shipped.

→ $M, s_0 = A [\neg \text{n_ship_order} \cup \text{n_verify_correctness}]$

2. The order has to be verified by the boss.

- $M, s_0 = \neg EF (\text{n_verify_order} \wedge \neg \text{o_boss})$

3. If the order is not correct, an employee has to be informed about this.

- $M, s_0 = AG (\text{n_write_report} \rightarrow AF(\text{n_inform_employee}))$

EF (-0,25)

4. If the customer is informed that the product is unavailable, the order needn't be verified by the boss (to save time).

- $M, s_0 = AG (\text{n_inform_customer} \rightarrow AF (\neg \text{n_verify_order}))$

EF (-0,25)

TASK 2 2/2

1. Depicted is a transition system $M = (S, R, L)$. Please explain, if the following CTL formulas satisfy M in regard to the respective $s \in S$: (If yes, you can simply make a checkmark. If no, please explain why not.)

- $M, s_1 \models EX(\neg p) \rightarrow \checkmark$ (True)
 - $M, s_1 \models AX(\neg p) \rightarrow \times$ (There exist a path from S_1 to S_0 where p is present)
 - $M, s_1 \models AG(q \vee r) \rightarrow \checkmark$ (True)
 - $M, s_0 \models A[q \cup r] \rightarrow \checkmark$ (True)
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TASK 3 2/2

- 1) In the lecture, a transition system M was defined as a tuple $M = (S, R, L)$. S is the set of states and R is the set of relations. L is a labeling function. More specific, this labelling is defined as a function $L: S \rightarrow 2^{AP}$. Briefly explain this function L in your own words. What does it do and why does it say 2^{AP} ? For your solution, you can assume the atomic propositions are a set $AP = \{A, B, C\}$

$L: S \rightarrow 2^{AP}$ (L = Labeling Function, S = States, AP = Atomic Proposition)

$AP = \{A, B, C\}$

We have three labels A , B and C . Now we have to assign labels to the states we have in the model (could be any number of states). L is the labeling function that assigns to any state S one element from 2^{AP} which is the power set of atomic propositions i.e all the possible combinations of labels.

Suppose we have 2 states s_0 and s_1 such that $S = \{s_0, s_1\}$

and $AP = \{A, B, C\} = 3$,

Then 2^{AP} will be 8

Power set will be of 8 elements :

$\{ -, A, B, C, AB, BC, AC, ABC \}$

Now L will assign any one element from this power set to a state. For e.g :

$L(s_0) = AB$

$L(s_1) = ABC$