

## Robotics [IIT-Jodhpur]

### Practical 1: Introduction to MATLAB through Force Analysis (Inverse Dynamics) of 1-link robot

#### Part A: Demonstration of MATLAB

Brief Demonstration of features of MATLAB

#### Part B: Force Analysis (Inverse Dynamics) of 1-link robot Using MATLAB

Equation of motion of the 1-link robot, shown in Fig. 1, is given by

$$I_{zz}\ddot{\theta} = \tau - mgl_c \cos \theta \text{ or}$$

*Inverse Dynamics* :  $\tau = I_{zz}\ddot{\theta} + mgl_c \cos \theta$   
(or Force Analysis) [Inputs:  $\theta, \dot{\theta}, \ddot{\theta}$ ] [Output:  $\tau$ ]

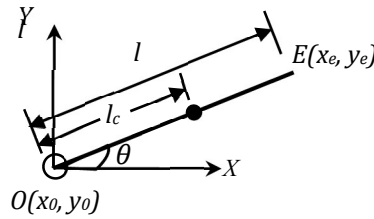


Figure 1: A 1-link robot

The robot is commanded to follow the cycloidal trajectory:

$$\begin{aligned}\theta_{des} &= \theta(0) + \frac{\theta(T) - \theta(0)}{T} \left[ t - \frac{T}{2\pi} \sin\left(\frac{2\pi}{T}t\right) \right] \\ \dot{\theta}_{des} &= \frac{\theta(T) - \theta(0)}{T} \left[ 1 - \cos\left(\frac{2\pi}{T}t\right) \right] \\ \ddot{\theta}_{des} &= \frac{\theta(T) - \theta(0)}{T} \left[ \frac{2\pi}{T} \sin\left(\frac{2\pi}{T}t\right) \right]\end{aligned}$$

where  $\theta(0) = 0^\circ$ ,  $\theta(T) = 120^\circ$  and  $T = 3$  sec.

Perform the following:

- Plot the commanded joint position, velocity and acceleration vs. time for time period  $T = 3$  s
- Plot linear velocity and acceleration of the end-effector of the robot
- Find joint torque ( $\tau$ ) required to follow the above trajectory and plot joint torque vs time
- Animate the system for the commanded trajectories.

Assume  $m = 1\text{kg}$ ,  $l = 1\text{m}$ ,  $l_c = 0.5\text{m}$ ,  $I_{zz} = \frac{1}{3}ml^2$  and  $g = 9.81\text{ m/s}^2$ .