### **NAME**

CUTEST\_ugreh\_threaded - CUTEst tool to evaluate the gradient and sparse Hessian matrix in finite element format.

#### **SYNOPSIS**

CALL CUTEST\_ugreh\_threaded( status, n, X, G, ne, lhe\_ptr, HE\_row\_ptr, HE\_val\_ptr, lhe\_row, HE\_row, lhe\_val, HE\_val, byrows, thread)

For real rather than double precision arguments, instead

CALL CUTEST\_ugreh\_threaded\_s( ... )

and for quadruple precision arguments, when available,

CALL CUTEST\_ugreh\_threaded\_q( ... )

#### DESCRIPTION

The CUTEST\_ugreh\_threaded subroutine evaluates the gradient and Hessian matrix of the objective function of the problem decoded from a SIF file by the script *sifdecoder* at the point X. This Hessian matrix is stored as a sparse matrix in finite element format

$$H = \sum_{e=1}^{ne} H_{e},$$

where each square symmetric element *H* sub *e* involves a small subset of the rows of the Hessian matrix.

The problem under consideration is to minimize or maximize an objective function f(x) over all  $x \in \mathbb{R}^n$  subject to the simple bounds  $x^l \le x \le x^u$ . The objective function is group-partially separable.

# **ARGUMENTS**

The arguments of CUTEST\_ugreh\_threaded are as follows

status [out] - integer

the outputr status: 0 for a successful call, 1 for an array allocation/deallocation error, 2 for an array bound error, 3 for an evaluation error, 4 for an out-of-range thread,

n [in] - integer

the number of variables for the problem,

**X** [in] - real/double precision

an array which gives the current estimate of the solution of the problem,

G [out] - real/double precision

an array which gives the value of the gradient of the objective function evaluated at X

ne [out] - integer

the number, ne, of "finite-elements" used,

**lhe ptr** [in] - integer

the actual declared dimensions of HE\_row\_ptr and HE\_val\_ptr,

### **HE\_row\_ptr** [out] - integer

HE\_row\_ptr(i) points to the position in HE\_row of the first row index involved with element number e: the row indices of element number e are stored in HE\_row between the indices HE\_row\_ptr(e) and HE\_row\_ptr(e+1)-1. HE\_row\_ptr(ne+1) points to the first empty location in HE\_row,

### **HE\_val\_ptr** [out] - integer

HE\_val\_ptr(i) points to the position in HE\_val of the first nonzero involved with element number i: the values involved in element number e are stored in HE\_val between the indices HE\_val\_ptr(e) and HE\_val\_ptr(e+1)-1. HE\_val\_ptr(ne+1) points to the first empty location in HE\_val,

# lhe\_row [in] - integer

the actual declared dimension of HE\_row,

### **HE\_row** [out] - integer

an array which holds a list of the row indices involved which each element. Those for element e directly preced those for element e+1, e=1, ..., ne-1. Since the elements are symmetric,  $HE_row$  is also the list of column indices involved with each element.

# lhe\_val [in] - integer

the actual declared dimension of HE\_val,

### **HE\_val** [out] - real/double precision

an array of the nonzeros in the upper triangle of  $H_e$ , evaluated at X and stored by rows, or by columns. Those for element e directly proceed those for element, e+1, i=1, ..., ne-1. Element number e contains the values stored between

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HE_val( HE_val_ptr(e) ) and HE_val( HE_val_ptr(e+1)-1 )
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and involves the rows/columns stored between

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HE row (HE row ptr(e)) and HE row (HE row ptr(e+1)-1).
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### byrows [in] - logical

must be set to .TRUE. if the upper triangle of each H\_i is to be stored by rows, and to .FALSE. if it is to be stored by columns,

# thread [in] - integer

thread chosen for the evaluation; threads are numbered from 1 to the value threads set when calling CUTEST\_usetup\_threaded.

# NOTE

Calling this routine is more efficient than separate calls to CUTEST\_ugr and CUTEST\_ueh\_threaded.

## **AUTHORS**

I. Bongartz, A.R. Conn, N.I.M. Gould, D. Orban and Ph.L. Toint

### **SEE ALSO**

CUTEst: a Constrained and Unconstrained Testing Environment with safe threads,

N.I.M. Gould, D. Orban and Ph.L. Toint,

Computational Optimization and Applications 60:3, pp.545-557, 2014.

CUTEr (and SifDec): A Constrained and Unconstrained Testing Environment, revisited,

N.I.M. Gould, D. Orban and Ph.L. Toint,

ACM TOMS, 29:4, pp.373-394, 2003.

CUTE: Constrained and Unconstrained Testing Environment,

I. Bongartz, A.R. Conn, N.I.M. Gould and Ph.L. Toint,

ACM TOMS, 21:1, pp.123-160, 1995.

cutest\_csgreh\_threaded(3M), sifdecoder(1).