

Question

In the Quant test of CAT exam, the population standard deviation is known to be 100. A sample of 25 test takers has a mean of 520. Construct a 80% Confidence Interval about the mean ?

Answer

$\sigma = 100$, $\bar{x} = 520$, $n = 25$, Confidence Interval = 80%

Calculate Significance level

Significance Value(α) = 1 - Confidence Interval

$$\alpha = 1 - 0.80 = 0.20$$

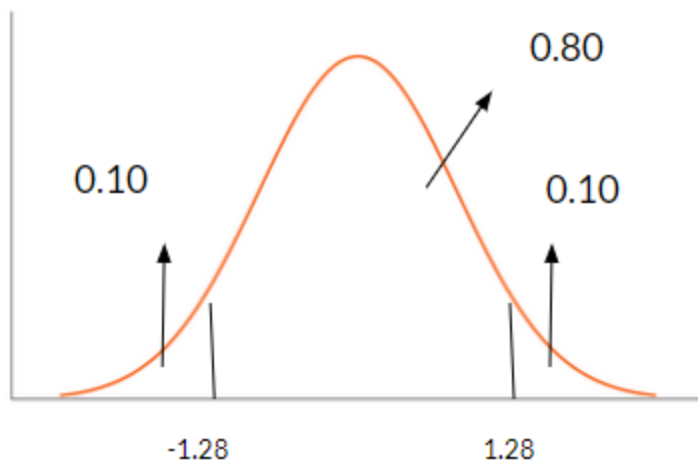
$$\alpha = 0.20$$

$$z_{\alpha/2} = z_{0.20/2} = z_{0.10}$$

$$1 - 0.10 = 0.90$$

Therefore, from the z table(if population standard deviation is given)value is 1.28

$$z_{\alpha/2} = 1.28$$



$$\text{Lower Fence} = \bar{x} - z \alpha/2 \left(\frac{\sigma}{\sqrt{n}} \right)$$

$$\begin{aligned} \text{Lower Fence} &= 520 - 1.28 (100/\sqrt{25}) \\ &= 520 - 1.28 \times 20 \\ &= 520 - 25.6 \\ &= 494.4 \end{aligned}$$

$$\text{Higher Fence} = \bar{x} + z \alpha/2 \left(\frac{\sigma}{\sqrt{n}} \right)$$

$$\begin{aligned} \text{Higher Fence} &= 520 + 1.28 (100/\sqrt{25}) \\ &= 520 + 1.28 \times 20 \\ &= 520 + 25.6 \\ &= 545.6 \end{aligned}$$

The Lower and Higher Fence in Distribution

