

Quantity Index Numbers (Q_i)

Ques (1) Calculate Paasche's and Laspeyres's Quantity Index from the following data

Commodity	Quantity (Units)		Values in Rs	
	1995	1999	1995	1999
A	100	150	500	900
B	80	100	320	500
C	60	72	120	360
D	30	33	360	297

Solution: Value = Price \times Quantity \Rightarrow Price = $\frac{\text{Value}}{\text{Quantity}}$

Commodity	q_0	q_1	$p_0 q_0$	$p_1 q_1$	p_0	p_1	$p_1 q_0$	$p_0 q_1$
A	100	150	500	900	5	6	600	750
B	80	100	320	500	4	5	400	400
C	60	72	120	360	2	5	300	144
D	30	33	360	297	12	9	270	396
			$\Sigma p_0 q_0 = 1300$	$\Sigma p_1 q_1 = 2057$			$\Sigma p_1 q_0 = 1570$	$\Sigma p_0 q_1 = 1690$

Paasche's Quantity Index $Q_{01} = \frac{\Sigma p_1 q_1}{\Sigma p_1 q_0} \times 100 = \frac{2057}{1570} \times 100 = 131.02$

Laspeyres's Quantity Index $Q_{01} = \frac{\Sigma p_0 q_1}{\Sigma p_0 q_0} \times 100 = \frac{1690}{1300} \times 100 = 130$ Ans

Value Index Numbers (V_i)

$$V_{01} = \frac{\Sigma p_1 q_1}{\Sigma p_0 q_0} \times 100 = \frac{\Sigma V_1}{\Sigma V_0} \times 100$$

ΣV_1 = Total value of all items in the given period

ΣV_0 = Total value of same items in base period.

Test of consistency or adequacy

Used to select most suitable method in a given condition

(I) Unit Test: Method must be independent from the units in which price and quantities are quoted.

Note: Except simple aggregate method all the method satisfies this test.

(II) Time Reversal Test: $P_{01} \times P_{10} = 1$ (omitting the factor 100)

Note: Laspeyres's and Paasche's method does not satisfied time reversal test.

(III) Factor Reversal Test: $P_{01} \times Q_{01} = \frac{\sum p_1 q_1}{\sum p_0 q_0}$

Note: This factor reversal test is satisfied only by Fisher's Ideal Index.

(IV) Circular Test: $P_{01} \times P_{12} \times P_{20} = 1$

Note: Simple aggregate method, Kelly's method satisfies the circular Test.

Note: Fisher's Ideal Index satisfies both time reversal and factor reversal test.