

Ques (1) Calculate Coefficient of correlation from the following informations

$$n=10, \quad \Sigma X = 100, \quad \Sigma Y = 150, \quad \Sigma (X-10)^2 = 180$$

$$\Sigma (Y-15)^2 = 215 \quad \text{and} \quad \Sigma (X-10)(Y-15) = 60.$$

Solution: Here, $\bar{X} = \frac{\Sigma X}{n} = \frac{100}{10} = 10$, $\bar{Y} = \frac{\Sigma Y}{n} = \frac{150}{10} = 15$

Therefore, we have $\Sigma (X-\bar{X})^2 = 180$, $\Sigma (Y-\bar{Y})^2 = 215$

$$\Sigma (X-\bar{X})(Y-\bar{Y}) = 60.$$

$$r = \frac{\Sigma (X-\bar{X})(Y-\bar{Y})}{\sqrt{\Sigma (X-\bar{X})^2} \cdot \sqrt{\Sigma (Y-\bar{Y})^2}}$$

$$= \frac{60}{\sqrt{180} \times \sqrt{215}} = \frac{60}{13.42 \times 14.66} = \frac{60}{196.74} = 0.305 \text{ Ans}$$

Ques (2) Find the Coefficient of Correlation between X and Y for the following data

$$n=25, \quad \Sigma X = 125, \quad \Sigma Y = 100, \quad \Sigma X^2 = 650, \quad \Sigma Y^2 = 436, \quad \Sigma XY = 520$$

Solution: The Correlation coefficient r is given by

$$r = \frac{n \Sigma XY - \Sigma X \Sigma Y}{\sqrt{n \Sigma X^2 - (\Sigma X)^2} \sqrt{n \Sigma Y^2 - (\Sigma Y)^2}}$$

$$= \frac{25 \times 520 - 125 \times 100}{\sqrt{25 \times 650 - (125)^2} \cdot \sqrt{25 \times 436 - (100)^2}}$$

$$= \frac{13000 - 12500}{\sqrt{16250 - 15625} \times \sqrt{10900 - 10000}}$$

$$= \frac{500}{\sqrt{625} \times \sqrt{900}} = \frac{500}{25 \times 30} = \frac{500}{750} = \frac{2}{3}$$

$$r = 0.67 \text{ Ans}$$

Ques (3) Find the coefficient of correlation between x and y for the following data

$$n=10, \Sigma x=55, \Sigma y=40, \Sigma x^2=385, \Sigma y^2=192, \Sigma xy=185$$

Ques (4) Find the coefficient of Correlation, from the following data

$$x: \quad 6 \quad 2 \quad 10 \quad 4 \quad 8$$

$$y: \quad 9 \quad 11 \quad 5 \quad 8 \quad 7$$

Solution: Here, we have $n=5$

x	$x = x - \bar{x}$	$x^2 = (x - \bar{x})^2$	y	$y = y - \bar{y}$	$y^2 = (y - \bar{y})^2$	$xy = (x - \bar{x})(y - \bar{y})$
6	$6 - 6 = 0$	0	9	$9 - 8 = 1$	1	0
2	$2 - 6 = -4$	16	11	$11 - 8 = 3$	9	-12
10	$10 - 6 = 4$	16	5	$5 - 8 = -3$	9	-12
4	$4 - 6 = -2$	4	8	$8 - 8 = 0$	0	0
8	$8 - 6 = 2$	4	7	$7 - 8 = -1$	1	-2
$\Sigma x = 30$		$\Sigma x^2 = 40$	40		$\Sigma y^2 = 20$	-26

$$\Sigma x = 30 \Rightarrow \bar{x} = \frac{\Sigma x}{n} = \frac{30}{5} = 6$$

$$\Sigma y = 40 \Rightarrow \bar{y} = \frac{\Sigma y}{n} = \frac{40}{5} = 8$$

$$\begin{aligned} r &= \frac{\Sigma (x - \bar{x})(y - \bar{y})}{\sqrt{\Sigma (x - \bar{x})^2} \sqrt{\Sigma (y - \bar{y})^2}} = \frac{\Sigma xy}{\sqrt{\Sigma x^2} \cdot \sqrt{\Sigma y^2}} = \frac{-26}{\sqrt{40} \cdot \sqrt{20}} \\ &= \frac{-26}{6.32 \times 4.47} = \frac{-26}{28.25} = -0.92 \text{ Ans} \end{aligned}$$

Ques (5) The following table gives the supply and price figures for a commodity for 6 days. Calculate correlation coefficient between price and supply

Days:	Mon	Tue	Wed	Th	Fri	Sat
Price:	22	30	25	20	15	8
Supply:	10	12	15	20	23	28