

## question of ML for exam :

b. I  $\rightarrow$  Entropy (measure of impurity of attribute)  
 $\rightarrow$  Gini

a). Original dataset

	Yes	NO	total
count	8	10	18
$p_i$	$\frac{8}{18} = 0.44$	$\frac{10}{18} = 0.56$	
$-p_i \log_2 p_i$	$-0.44 \log_2 0.44$ $= 0.52$	$-0.56 \log_2 0.56$ $= 0.47$	

$$\text{Total Entropy} = 0.99$$

(b) splitted dataset (based on the feature (GIPA))

	High	medium	Low	total
GIPA = High				18
	Yes	No		total
count	4	2		6
$p_i$	$\frac{4}{6} = 0.67$	$\frac{2}{6} = 0.33$		
$-p_i \log_2 p_i$	0.39	0.53		

$$\text{Entropy} = 0.92$$

GIPA = medium

	Yes	No	total
count	4	3	7
$p_i$	$\frac{4}{7}$	$\frac{3}{7}$	
$-p_i \log_2 p_i$	$-\frac{4}{7} \log_2 \frac{4}{7}$	$-\frac{3}{7} \log_2 \frac{3}{7}$	
	$\Rightarrow 0.46$	$\Rightarrow 0.52$	

$$\text{Entropy} = 0.99$$

GIPA = Low

	Yes	No	total
count	0	5	5
$p_i$	0	1	
$-p_i \log_2 p_i$	0	0	

$$\text{Entropy} = 0$$

Combined Entropy =  $P(x) E(x)$

$$\frac{6}{18} \times 0.92 + \frac{7}{18} \times 0.99 + \frac{5}{18} \times 0$$

$$0.30 + 0.385 + 0 \Rightarrow 0.685$$

Information gain = Original data set - Combined Entropy  
 $0.99 - 0.685$   
 $\Rightarrow 0.30$

Inf gain for comm

comm = good	Yes	NO	total
count	7	2	9
$p_i$	$\frac{7}{9} = 0.77$	$\frac{2}{9} = 0.22$	
$-p_i \log_2 p_i$	$-0.77 \log_2 0.77$	$-0.22 \log_2 0.22$	
	$\Rightarrow 0.290$	$0.480$	$\Rightarrow 0.77$

comm = Bad	Yes	NO	total
count	1	8	9
$p_i$	0.11	0.88	
$-p_i \log_2 p_i$	$-0.11 \log_2 0.11$	$-0.88 \log_2 0.88$	
	$\Rightarrow 0.350$		

Info Gain (GPA) = 0.30

Info Gain (Communication) = 0.36

—— ( Aptitude ) = 0.47

—— ( Prog Skills ) = 0.04

(3marks)

(5marks)

ya toh information gain aage ya fir two factors

Gini Index ÷

$$Gini(t) = 1 - \sum_j [p(i/x)]^2$$

$C_1$	0	$P(C_1) = \frac{0}{6} = 0$
$C_2$	6	$P(C_2) = \frac{6}{6} = 1$

$$\begin{aligned} Gini &= 1 - [P(C_1)^2 + P(C_2)^2] \\ &= 1 - [0 + 1] \\ &= 1 - 1 = 0 \end{aligned}$$

$C_1$	1
$C_2$	5

$$P(C_1) = \frac{1}{6} = 0.166$$

$$P(C_2) = \frac{5}{6} = 0.833$$

$$\begin{aligned} Gini &= 1 - [0.166 \times 0.166 + 0.833 \times 0.833] \\ &\Rightarrow 1 - [0.0275 + 0.6939] \\ &\quad 1 - 0.7214 \\ &\Rightarrow 0.278 \end{aligned}$$

$C_1$	2	$P(C_1) = 0.333 = 0.110 (0.333 \times 0.333)$
$C_2$	4	$P(C_2) = 0.666 = 0.443$

$$\begin{aligned} Gini &= 1 - [\cancel{0.110} + \cancel{0.435}] \Rightarrow 1 - 0.543 \\ &= \cancel{0.457} \quad 0.44 \end{aligned}$$

Highest value of Gini = 0.5  
Entropy = 1

Important  
Page no. 10.

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Date   /  /  

cluster the following 8 points with any representing location into three clusters.

(x, y)  $A_1(2, 10)$   $A_2(2, 5)$   $A_3(8, 4)$  ,  $A_4(5, 8)$   
 $A_5(7, 5)$   $A_6(6, 4)$   $A_7(1, 2)$  ,  $A_8(4, 9)$

three clusters means  $K=3$

if Pabari not tell you about cluster toh Aabkar hisab se  
do.

but how given Initial cluster are :-

$A_1(2, 10)$

$A_4(5, 8)$

$A_7(1, 2)$

two choice distance  $fk$  given but you need to choose.

in this equation  $f(a, b) = |x_1 - x_2| + |y_1 - y_2|$

→ use Kmean clustering Algo. to find out three clusters.

	$C_1$	$C_2$	$C_3$	
Point	$A_1(2, 10)$	$A_4(5, 8)$	$A_7(1, 2)$	cluster
$A_1(2, 10)$	0	5	9	$C_1$
$A_2(2, 5)$	5	6	4	$C_3$
$A_3(8, 4)$	12	7	9	$C_2$
$A_4(5, 8)$	5	0	10	$C_2$
$A_5(7, 5)$	10	5	9	$C_2$
$A_6(6, 4)$	10	5	7	$C_2$
$A_7(1, 2)$	9	10	0	$C_3$
$A_8(4, 9)$	3	2	10	$C_2$

$C_1 \rightarrow A_1 \longrightarrow A_1(2, 10)$

$C_2 \rightarrow A_3, A_4, A_5, A_6, A_8$

$C_3 \rightarrow A_2, A_7$



$$\begin{array}{l}
 (8,4) \\
 (5,8) \\
 (7,5) \\
 (6,4) \\
 (4,9)
 \end{array}
 \Rightarrow \frac{8+5+7+6+4}{5} = \frac{30}{5} = 6, \quad \frac{4+8+5+4+9}{5} = \frac{30}{5} = 6$$

$$\Rightarrow (6,6)$$

$$\begin{array}{l}
 C3 \Rightarrow A2 = (2,5) \\
 A7 = (1,2)
 \end{array}
 \quad \left( \frac{3}{2}, \frac{7}{2} \right) \Rightarrow (1.5, 3.5)$$

Point	C1	C2	C3	cluster
A1(2,10)	0	8	7	C1
A2(2,5)	5	5	2	C3
A3(8,4)	12	4	7	C2
A4(5,8)	5	3	8	C2
A5(7,5)	10	2	7	C2
A6(6,4)	10	2	5	C2
A7(1,2)	9	9	2	C3
A8(4,9)	3	5	2.5+5.5 (8)	C1

$$C1 \rightarrow A1, A8 \quad \left( \frac{6}{2}, \frac{19}{2} \right) \Rightarrow (3, 9.5)$$

$$\begin{array}{l}
 C2 \rightarrow A3, A4, A5, A6 \quad \frac{8+5+7+6}{4}, \frac{4+8+5+4}{4} \\
 \Rightarrow \left( \frac{26}{4}, \frac{21}{4} \right) \Rightarrow 6.5, 5.25
 \end{array}$$

$$C3 \rightarrow A2, A7 \quad \frac{2+1}{2}, \frac{5+2}{2} \Rightarrow (1.5, 3.5)$$

Point	(3, 9.5)	(6.5, 5.25)	(1.5, 3.5)	cluster
A1 (2, 10)	1.5	9	7	
A2 (2, 5)	5.5	4.75	2	
A3 (3, 4)	10.5			
A4 (5, 8)	3.5			
A5 (7, 5)	8.5			
A6 (6, 4)	8.5			
A7 (1, 2)	9.5			
A8 (4, 9)				

21/11/22

Region what is a Region?

→ group of connected pixel with similar property.

Basic formulation

- $\bigcup_{i=1}^n R_i = R$
- $R_i$  is a connected region  $i=1, 2, \dots, n$
- $R_i \cap R_j = \emptyset$  for all  $i$  and  $j, i \neq j$
- $P(R_i) = \text{TRUE}$  for  $i=1, 2, \dots, n$
- 

Region growing:

$$P(R_i | K) \cup \{x, y\} = \text{TRUE}$$

→ if we add different colour to some field we find Arithmetic deviation, standard mean.

Theory question

OR tags

★ Region growing  
★ Region splitting

Problems  $\frac{3}{2}$  Large execution time.

The selection of the property to be satisfied

KNN is supervised and K-Mean is unsupervised.  
In both algorithm we can find out value of K using  
Elbow method.

## Basic clustering methods :-

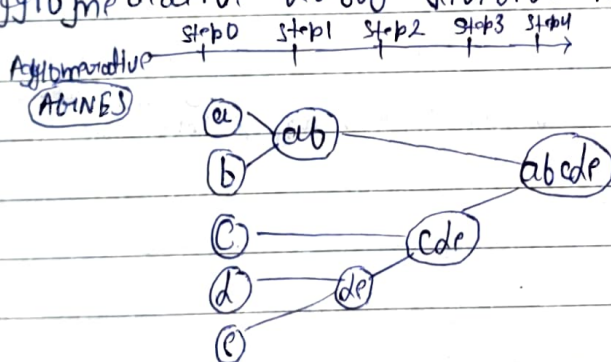
1. Partitioning methods  
K-means.

2. Hierarchical methods.

Agglomerative (bottom-up) or divisive (top-down).

3. Density-based methods } not in syllabus.  
4. Grid-based

## Agglomerative versus divisive Hierarchical clustering.



## # dendrogram

steps to perform Hierarchical clustering.

## Distance-based Algorithm :-

### Proximity matrix

Student_ID	Marks	1	2	3	4	5
1	10	0	9	18	10	25
2	7	9	0	21	13	28
3	28	18	21	0	8	7
4	20	10	13	8	0	15
5	35	25	28	7	15	0

(max)  
(min)  
(Avg)



(1,2) } begin  
(3,5)

Student-ID	Marks	ID	(1,2)	3	4	5
(1,2)	10	(1,2)	0	18	10	25
3	28	3	18	0	8	7
4	20	4	10	8	0	15
5	35	5	25	7	15	0

Q. Proximity draw key.  
Difference b/w Algorithm and dendrogram.

22/11/22

Setting the DOM:

→ value

→ innerHTML

→ innerText

→ href

→ setAttribute

→ attributes

document.getElementById('id').removeAttribute('class', 'a');

190 Reverse Bits:

Automata:

Imp.

Church Turing Thesis:

→ 1913

Some common input...

Ques

Q. Diff. Algorithmic and naive clustering  
 what is naive clustering

⇒ Ensemble model :-

Ensemble methods uses collection of models to improve the accuracy.

↳ Max voting

↳ Min voting

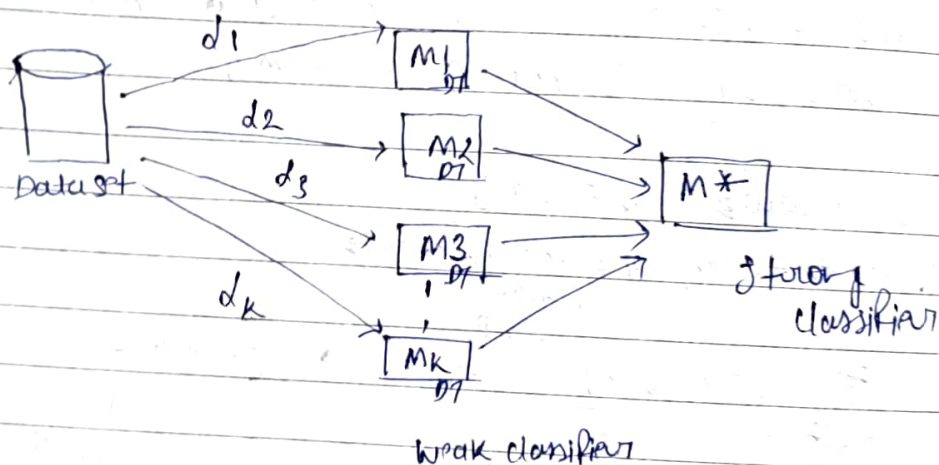
↳ Average voting

↳ weighted Average voting.

Advance Ensemble methods :-

i). Bagging

ii). Boosting.

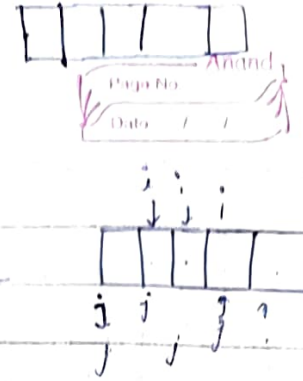
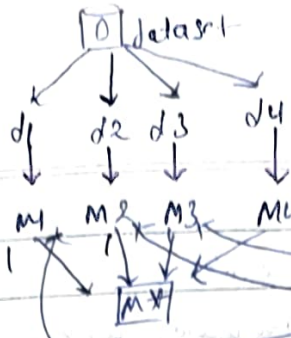


If all the models are of same type then the Ensemble classifier is homogeneous. otherwise heterogeneous.

# Bagging ⇒ Training a bunch of individual model in a parallel way. Each model is trained by the random subset of data.

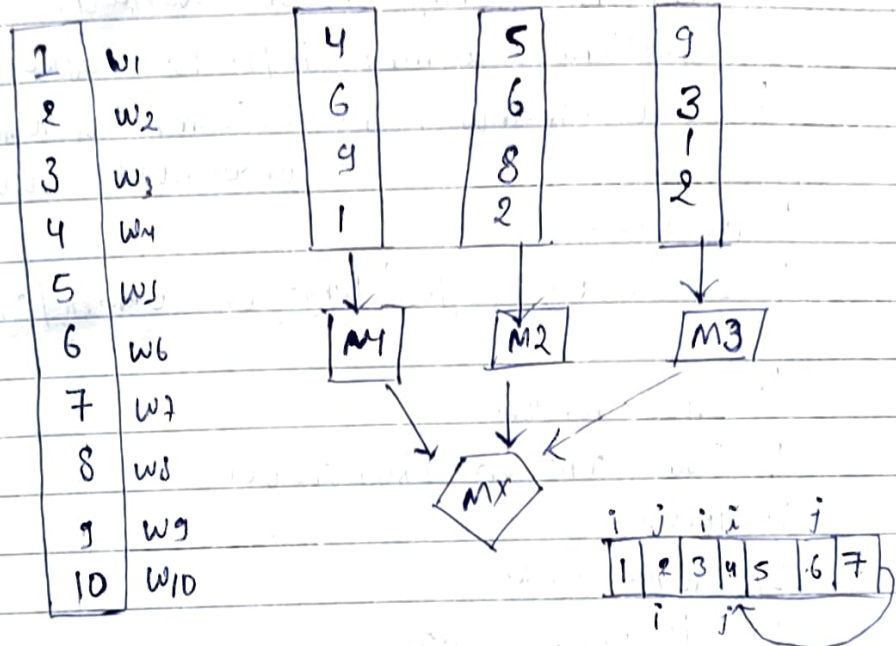
The result uses averaging the prediction over a collection of classifiers.

# Boosting ⇒ Training a bunch of individual model in a sequential way. Each individual model learn from their mistakes made by the base model. The result uses weighted vote with the weight of classifier.



Ex: of Boosting  $\Rightarrow$  Random forest.

# Boosting  $\div$



Ex: of Boosting is AdaBoost Algorithm.

left SUM  
regularisation

HTML ka parent - Parent element + Null  
Parent Null  $\rightarrow$  document

Roll Stack  $\div$  Difference b/w  $\bullet$  Parent element &  $\bullet$  parent node  
 $\downarrow$   $\downarrow$   
 null document  
 $\bullet$  setAttribute  
 $\bullet$  innerHTML  
 $\bullet$  parentElement  
 $\bullet$  child (no. of child)  
 $\downarrow$   
 element count (just use the count)  
 $\bullet$  children  
 $\bullet$  childNodes

# Event Listener.

$\pm$  Event bubbling  $\div$   
Event handling

Important  
benefit of event listener



$$A \rightarrow a_2 / b_2 / d_2$$

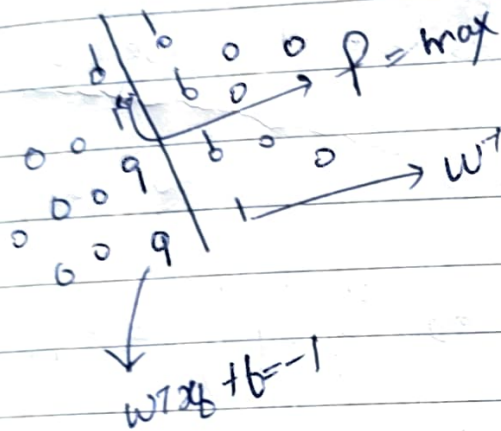
$$Z \rightarrow d / d_2$$

Machine Learning

SVM classifier (to find out the hyperplane b/w the data-points it will be a line when there are two points only).

$$w^T x_i + b \geq 1 \quad \text{if } y_i = 1$$

$$w^T x_i + b \leq -1 \quad \text{if } y_i = -1$$



$$\begin{aligned} w^T x_b + b &= -1 \\ w^T x_a + b &= 1 \\ \hline w^T (x_b - x_a) &= -2 \\ w^T (x_a - x_b) &= 2 \end{aligned}$$

$$x_a - x_b = \frac{2}{w^T}$$

$$p = |x_a - x_b| = \frac{2}{\|w\|}$$

Non Linear  
Kernel Trick  
Gaussian Trick



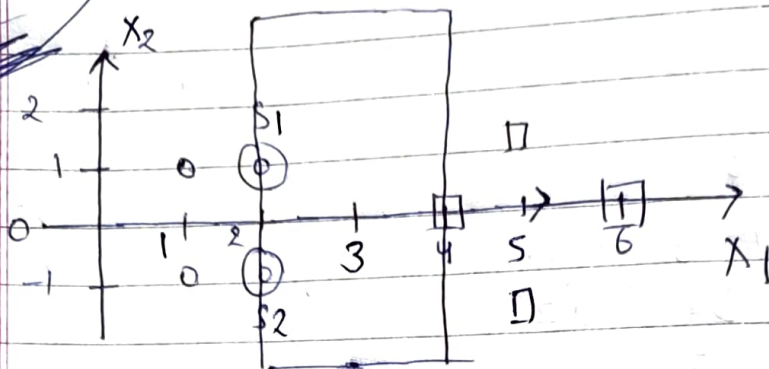
Question:

point hai. draw kon

Reduction wala

w and v wala.

Instant  
class



$$S_1 = \begin{pmatrix} 2 \\ 1 \end{pmatrix} \quad S_2 = \begin{pmatrix} 2 \\ -1 \end{pmatrix} \quad S_3 = \begin{pmatrix} 4 \\ 0 \end{pmatrix}$$

add bias  $\Rightarrow \tilde{S}_1 = \begin{pmatrix} 2 \\ 1 \\ 1 \end{pmatrix} \quad \tilde{S}_2 = \begin{pmatrix} 2 \\ -1 \\ 1 \end{pmatrix} \quad \tilde{S}_3 = \begin{pmatrix} 4 \\ 0 \\ 1 \end{pmatrix}$

$$\alpha_1 \tilde{S}_1 \cdot \tilde{S}_1 + \alpha_2 \tilde{S}_2 \cdot \tilde{S}_1 + \alpha_3 \tilde{S}_3 \cdot \tilde{S}_1 = -1 \quad (-ve \text{ class})$$

$$\alpha_1 \tilde{S}_1 \cdot \tilde{S}_2 + \alpha_2 \tilde{S}_2 \cdot \tilde{S}_2 + \alpha_3 \tilde{S}_3 \cdot \tilde{S}_2 = -1 \quad (-ve \text{ class})$$

$$\alpha_1 \tilde{S}_1 \cdot \tilde{S}_3 + \alpha_2 \tilde{S}_2 \cdot \tilde{S}_3 + \alpha_3 \tilde{S}_3 \cdot \tilde{S}_3 = +1 \quad (+ve \text{ class})$$

$$\begin{bmatrix} 2 \\ 1 \\ 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 1 \end{bmatrix} \quad \alpha_1 \begin{pmatrix} 2 \\ 1 \\ 1 \end{pmatrix} \cdot \begin{pmatrix} 2 \\ 1 \\ 1 \end{pmatrix} + \alpha_2 \begin{pmatrix} 2 \\ -1 \\ 1 \end{pmatrix} \cdot \begin{pmatrix} 2 \\ 1 \\ 1 \end{pmatrix} + \alpha_3 \begin{pmatrix} 4 \\ 0 \\ 1 \end{pmatrix} \cdot \begin{pmatrix} 2 \\ 1 \\ 1 \end{pmatrix} = -1$$

$$\begin{bmatrix} 2 \times 2 + 1 \times 1 + 1 \times 1 \end{bmatrix} \quad \alpha_1 \begin{pmatrix} 2 \\ 1 \\ 1 \end{pmatrix} \cdot \begin{pmatrix} 2 \\ -1 \\ 1 \end{pmatrix} + \alpha_2 \begin{pmatrix} 2 \\ -1 \\ 1 \end{pmatrix} \cdot \begin{pmatrix} 2 \\ -1 \\ 1 \end{pmatrix} + \alpha_3 \begin{pmatrix} 4 \\ 0 \\ 1 \end{pmatrix} \cdot \begin{pmatrix} 2 \\ -1 \\ 1 \end{pmatrix} = -1$$

$\Rightarrow 6$

$$\alpha_1 \begin{pmatrix} 2 \\ 1 \\ 1 \end{pmatrix} \cdot \begin{pmatrix} 4 \\ 0 \\ 1 \end{pmatrix} + \alpha_2 \begin{pmatrix} 2 \\ -1 \\ 1 \end{pmatrix} \cdot \begin{pmatrix} 4 \\ 0 \\ 1 \end{pmatrix} + \alpha_3 \begin{pmatrix} 4 \\ 0 \\ 1 \end{pmatrix} \cdot \begin{pmatrix} 4 \\ 0 \\ 1 \end{pmatrix} = +1$$

After simplification we get :-

$$6d_1 + 4d_2 + 9d_3 = -1$$

$$4d_1 + 6d_2 + 9d_3 = -1$$

$$9d_1 + 9d_2 + 17d_3 = 1$$

By solving no above 3,

$$d_1 = d_2 = -3.25 \quad d_3 = 3.5$$

$(\tilde{w} = \sum_i d_i \tilde{S}_i)$  w find konho ku formula.

$$\tilde{w} = d_1 \tilde{S}_1 + d_2 \tilde{S}_2 + d_3 \tilde{S}_3$$

$$\tilde{w} = d_1 \begin{pmatrix} 2 \\ 1 \\ 1 \end{pmatrix} + d_2 \begin{pmatrix} 2 \\ -1 \\ 1 \end{pmatrix} + d_3 \begin{pmatrix} 4 \\ 0 \\ 1 \end{pmatrix}$$

$$= (-3.25) \begin{pmatrix} 2 \\ 1 \\ 1 \end{pmatrix} + (-3.25) \begin{pmatrix} 2 \\ -1 \\ 1 \end{pmatrix} + (3.5) \begin{pmatrix} 4 \\ 0 \\ 1 \end{pmatrix}$$

$$\Rightarrow \begin{pmatrix} 1 \\ 0 \\ -3 \end{pmatrix}$$

$$y = wx + b$$

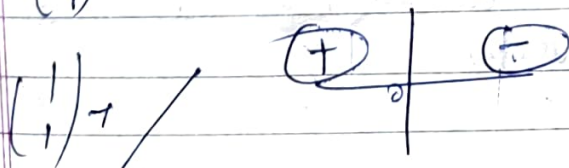
$$w \Rightarrow \begin{pmatrix} 1 \\ 0 \end{pmatrix} \quad b = -3$$

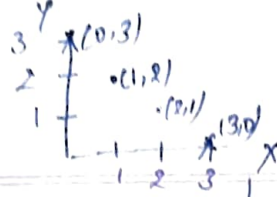
last topic :-

regularisation,

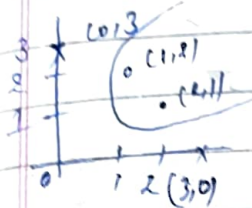
\*  $\begin{pmatrix} 1 \\ 0 \end{pmatrix}$  + vertical line.

$\rightarrow \begin{pmatrix} 0 \\ 1 \end{pmatrix}$  + horizontal line.





## Machine Learning :- Kernel Trick



	X	0	0	X
	(0,3)	(1,2)	(2,1)	(3,0)
$x+y$	3	3	3	3
$x \times y$	0	2	2	0
$x^2$	6	1	4	9

Q. What is the uses of kernel trick  
↳ to transformation of the values  
to linear space

- Polynomial kernel fn.
- Gaussian kernel fn.
- Radial Basis fn.

Q. What is SVM

Q. types of kernel tricks

Q. Use of SVM

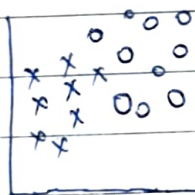
Q. type of SVM

Q. support vector  
hyper plane

Q. why kernel tricks needed.

Q. numerical.

## Regularization :-



Technique is to prevent the model from over fitting  
by adding extra information.

like :- Penalty term (Extra Info) / our complexity term

$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n + b$$

$$\sum_{i=1}^n (y_i - \hat{y}_i)^2 = \sum_{i=1}^n \left( y_i - \sum_{j=0}^n \beta_j x_{ij} \right)^2$$

## Types of Regularization :-

- Ridge (L2 - Regularization)
- Lasso (L1 - regularization)



Ridge → In this technique the cost fn is altered by adding the penalty term to it the amount of bias added to the model is called Ridge Penalty, we can calculate it by multiply  $\lambda$  to the squared weights of each individual feature.  
 The equation of cost function for Ridge is  $\frac{1}{2}$

$$\frac{1}{2} \sum_{i=1}^m (y_i - \hat{y}_i)^2 = \frac{1}{2} \sum_{i=1}^m \left( y_i - \sum_{j=0}^n \beta_j X_{ij} \right)^2 + \lambda \sum_{j=0}^n \beta_j^2$$

↓  
weights

Lasso → Least Absolute and selection operator.

It is similar to Ridge except that the penalty term contains only absolute weights instead of square of weight.

$$\frac{1}{2} \sum_{i=1}^m (y_i - \hat{y}_i)^2 = \frac{1}{2} \sum_{i=1}^m \left( y_i - \sum_{j=0}^n \beta_j X_{ij} \right)^2 + \lambda \sum_{j=0}^n |\beta_j|$$

① Regularization, types of regularization  
 trade off bias vs Variance.

## # Agglomerative Hierarchical clustering :

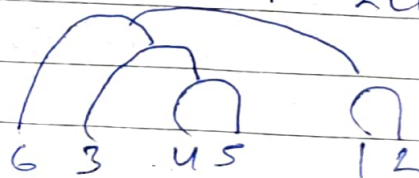
Drawback ↙

k mean depends upon the distance to centroid.

Agglomerative clustering :

→ In start think every point a cluster.

2 cluster after 2 cluster.



← Dendrogram  
 ↓  
 store info how  
 to merge.