

content for today

- Pick from Both Sides
- ✓ Bulbs
- Alternating Sub-arrays.
- ✓ Even Sub-arrays
- ✓ Good sub-arrays (# discuss)
- ✓ Sub-arrays with Least Average.
of size K (# discuss)

Q: Given an array of size N.

You have to pick B elements in total. (Some from left and some from right) to get the maximum sum.
 → possibly it can zero.

Q: $[5, 2, 8, 3, 6, 11, 1, 4]$, $B=4$

left.

4
3
2
1
0

right.

0
1
2
3
4

$$\Rightarrow 5 + 2 + 8 + 3 = 18$$

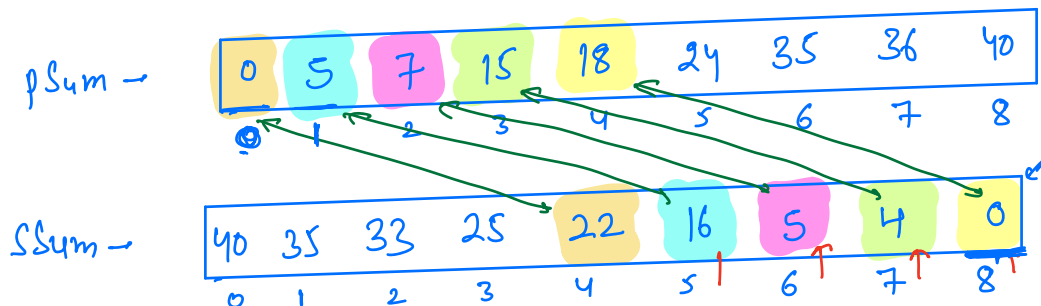
$$\Rightarrow 5 + 2 + 8 + 4 = 19$$

$$\Rightarrow 5 + 2 + 1 + 4 = 12$$

$$\Rightarrow 5 + 11 + 1 + 4 = 21$$

$$\Rightarrow 6 + 11 + 1 + 4 = 22$$

$$\underline{\underline{\text{Ans} = 22.}}$$



pSum = new int [n+1] , sSum = new int [n+1];

for (i = 1 ; i ≤ n ; i++) {

 psum[i] = psum[i-1] + a[i-1];

for (i = n-1 ; i ≥ 0 ; i--) {

 sSum[i] = sSum[i+1] + a[i];

ans = INT-MIN;

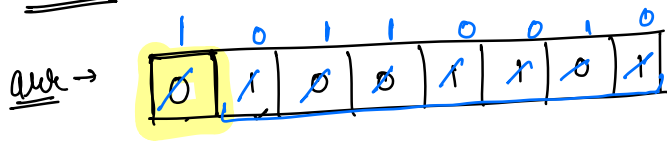
for (int i = 0 ; i ≤ B ; i++) {

 ans = max (ans , pSum[i] + sSum[n-B+i]);

T.C → $O(N)$
S.C → $O(N)$

{ # + do → $O(1)$ space complexity. }

① Bulbs.

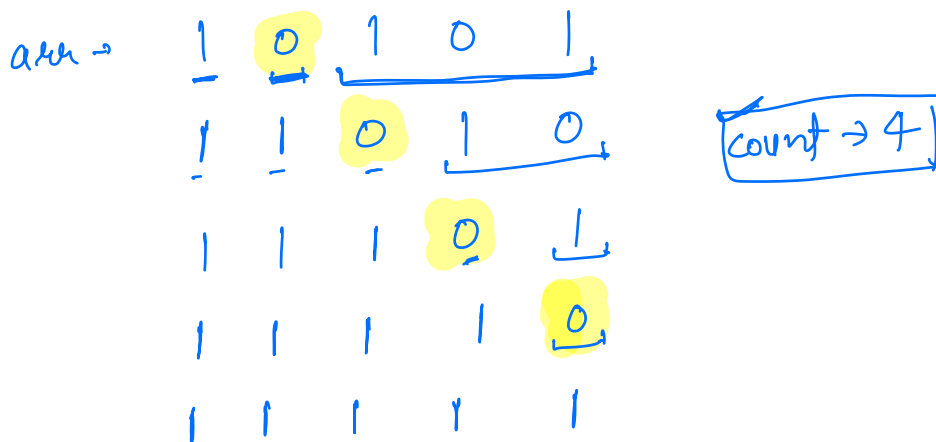


0 → bulb is off

1 → bulb is ON.

All bulbs are connected through 'a' circuit & the circuit is faulty → All the bulbs on r.h.s will be toggled.

Min no. of switch pressing such that all the bulbs are finally "ON".



pseudo-code

count = 0;

for (i = 0 ; i < n ; i++) {

if (a[i] == 0) {

count++;

for (j = i ; j < n ; j++) {

a[j] = 1 - a[j];

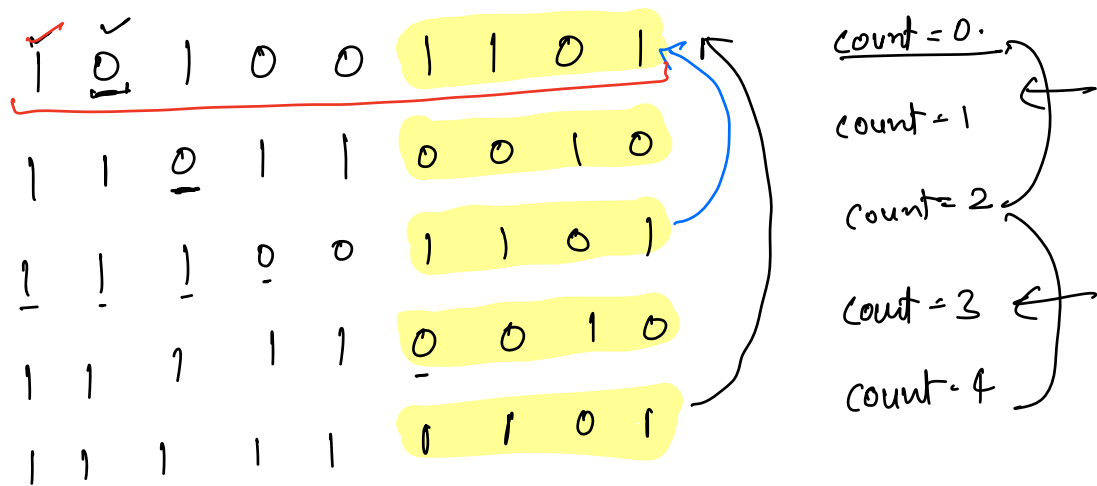
}

return count;

T.C → $O(N^2)$

S.C → $O(1)$

optimization.



→ state of a bulb is dependent on count.
→ if count is even \Rightarrow state will be similar to what it was in original array.
odd \Rightarrow state will be toggled.

pseudo-code:

```
count = 0, curr = 0;  
for (i = 0; i < N; i++) {  
    if (count % 2 == 0) {  
        curr = a[i];  
    }  
    else {  
        curr = 1 - a[i];  
    }  
    if (curr == 0) {  
        count++;  
    }  
}  
return count;
```

// switching ON the current bulb.

T.C $\rightarrow O(n)$
S.C $\rightarrow O(1)$

Q1) Given an array of size N which contains only 0's & 1's.

Find indices of all the alternating sub-arrays with

length = $2*B+1$.

[B is given]

\downarrow
 $[0-1-0-1]$
 $[1-0-1-0]$

eg: $n=5$
 $[1 \ 0 \ 1 \ 0 \ 1]$, $B=1$ length = $(2*1)+1 = 3$
 $\begin{matrix} & 0 & 1 & 2 & 3 & 4 \end{matrix}$

→ Consider all sub-arrays with length = $(2*B)+1$.

len = $(2*B)+1$; list <int> ans;

for(i = 0 ; i < n-l+1 ; i++) {
 prev = -1, flag = true;

for(j = i ; j < i + len ; j++) {
 if(a[j] == prev) {
 flag = false;
 break;
 }
 prev = a[j];

if (flag == true) ans.add(i+B);

prev = -1

\downarrow
 $[1 \ 0 \ 1 \ 0 \ 1]$
1 0 1 0 1 0 1 0 1

[for alternating, prev & curr they should be different.]

T.C → $O(n*l)$
 S.C → $O(1)$

$l = 2B+1$

Even Sub-arrays.

Q: Integer array : A

Can we divide the array into even length subarrays such that first & last elements of subarrays are even.

\Rightarrow "YES" , "NO"

a:

4	8	12	16	2	20	24
0	1	2	3	4	5	6

odd \Rightarrow "NO"

b:

17	20	4	16	18	8
0	1	2	3	4	5

\Rightarrow "NO"

c:

4	6	8	10	12	5
0	1	2	3	4	5

\Rightarrow "NO"

d:

8		20	40				4
0	1	2	3	4	5	6	7

\Rightarrow YES.

[len \rightarrow even, first element & last element \Rightarrow even]

Good Sub-arrays

Q: Good sub-array

→ length → even, sum of all elements $< B$

→ length → odd, sum of all elements $> B$

Count of good subarrays in array?

$B = 15$

eg: $\begin{bmatrix} 6 & 4 & 3 & 7 & 8 & 1 \\ 0 & 1 & 2 & 1 & 4 & 5 \end{bmatrix}$

ans →

pseudo-code.

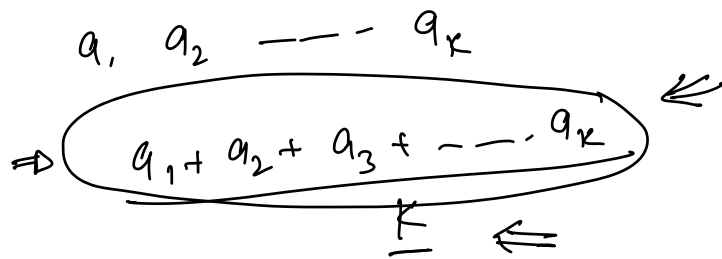
```
for (i = 0; i < N; i++) {  
    sum = 0;  
    for (j = i; j < N; j++) {  
        sum += a[j];  
        len = j - i + 1;  
        if (len is even && sum < B) count++;  
        if (len is odd && sum > B) count++;  
    }  
}
```

T.C → $O(N^2)$

S.C → $O(1)$



Q.1 Sub-array of size - K with least average. //



[sub array of size - K which is having the least sum.]

Doubts : $A \rightarrow [1, 2, 3, 4, 5]$
 $B \rightarrow [2, 3]$

$$\begin{array}{ccccc} 5 & 4 & 3 & 2 & 1 \\ \hline [4 & 5 & 1 & 2 & 3] \\ [3 & 4 & 5 & 1 & 2] \end{array}$$

int[][] ans = new int [B.length] [A.length]

traversal →

m

[i, j]

A ⇒

	0	1	2	3
0	3	12	5	11
1	7	1	15	4
2	17	0	6	27
3	37	-2	8	9
4	0	41	0	16

n

```

for (col = 0; col < m; col++) {
    arr[i][col] = 0;
}
for (row = 0; row < n; row++) {
    arr[row][j] = 0;
}

```

list 1 → [

]

list 2 → [

arr →

3	2	5	4	1	6	8
0	1	2	3	4	5	6



i j
 → $[1, 4]$
 → $[0, 5]$
 → $[3, 6]$
 → $[2, 4]$

psum →

3	5	10	14	15	21	29
0	1	2	3	4	5	6

sum of subarray from
1 to 4



3	2	5	4	1
0	1	2	3	4

3
0

sum of subarray from 0 to 4
 -
 sum of subarray from 0 to 0

$$= \text{psum}[j] - \text{psum}[i-1]$$

$$(i, j) \Rightarrow \text{psum}[j] - \text{psum}[i-1]$$