

Today's Content :-

- a) How -ve no's are stored
- b) Significance of MSB
- c) datatype ranges.

8 bit number

→ sign bit → Concept of storing
-ve no is
wrong,

	7	6	5	4	3	2	1	0
10 :	0	0	0	0	1	0	1	0
-10 :	1	0	0	0	1	0	1	0

4 :	0	0	0	0	0	1	0	0
-4 :	1	0	0	0	0	1	0	0
10 :	0	0	0	0	1	0	1	0
-14	1	0	0	0	1	1	0	

1 more problem :-

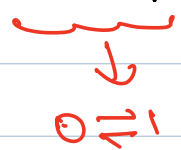
0 0 0 0 0 0 0 0 → 0

1 0 0 0 0 0 0 0 → -0

2's complement :-

$a = -a$ = 2's complement of a
(in binary)

\Rightarrow 1's comp $a + 1$

\Rightarrow 

$\left\{ \begin{array}{l} -10 = 1's \text{ of } 10 + 1 \\ = \sim 10 + 1 \end{array} \right.$

8 bit no's.

10 : 0 0 0 0 1 0 1 0

~ 10 : 1 1 1 1 0 1 0 1

+1 : 0 0 0 0 0 0 0 1

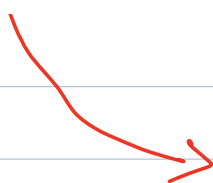
$-10 \Rightarrow$ 1 1 1 1 0 1 1 0

$-2^7 \quad 2^6 \quad 2^5 \quad 2^4 \quad 2^3 \quad 2^2 \quad 2^1 \quad 2^0$
1 1 1 1 0 1 1 0

\downarrow

$2^7 + 2^6 + 2^5 + 2^4 + 2^2 + 2^1$

\Rightarrow 246



$$-2^7 + 2^6 + 2^5 + 2^4 + 2^2 + 2^1$$

$$\Rightarrow \underline{-10}$$

// 4 bit no.

$$\begin{array}{cccc} 3 & 2 & 1 & 0 \\ \hline -2^3 & 2^2 & 2^1 & 2^0 \end{array}$$

8 bit no.

$$\begin{array}{ccccccc} -2^7 & & 2^5 & & 2^3 & & 2^1 \\ \hline & 2^6 & & 2^4 & & 2^2 & 2^0 \end{array}$$

$$\downarrow$$

 128

$$\downarrow$$

MSB \rightarrow most significant bit.



MSB base value is negative.

8 bit no

$$\begin{array}{r}
 -2^7 \quad 2^6 \quad 2^5 \quad 2^4 \quad 2^3 \quad 2^2 \quad 2^1 \quad 2^0 \\
 10 : \quad 0 \quad 0 \quad 0 \quad 0 \quad 1 \quad 0 \quad 1 \quad 0 \\
 -4 : \quad 1 \quad 1 \quad 1 \quad 1 \quad 1 \quad 1 \quad 0 \quad 0 \\
 \hline
 6 \quad 1 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 1 \quad 1 \quad 0
 \end{array}$$

$$\begin{array}{cccccccc} 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \end{array} \leftarrow +4$$

$$\begin{array}{cccccccc} 1 & 1 & 1 & 1 & 0 & 1 & 1 & \end{array} \leftarrow \sim 4$$

$$ + 1$$

$$\begin{array}{cccccccc} 1 & 1 & 1 & 1 & 1 & 1 & 0 & 0 \end{array} \leftarrow -4$$

$$\begin{array}{r} 11 \\ - 7 \\ \hline 4 \end{array}$$

4

	2^7	2^6	2^5	2^4	2^3	2^2	2^1	2^0
$11 \rightarrow$	0	0	0	0	1	0	1	1
$-7 \rightarrow$	1	1	1	1	1	0	0	1
	1	0	0	0	0	0	1	0

Convert Binary to decimal:-

4 bit no

$-2^3 \quad 2^2 \quad 2^1 \quad 2^0$

1 0 1 1 $\rightarrow -5$

1 0 1 0 $\rightarrow -6$

0 0 1 1 $\rightarrow 3$

1 0 0 0 $\rightarrow -8$

1 1 1 1 $\rightarrow -1$

8 bit Numbers:-

Decimal

$\frac{-2^7}{\quad} \quad \frac{2^6}{\quad} \quad \frac{2^5}{\quad} \quad \frac{2^4}{\quad} \quad \frac{2^3}{\quad} \quad \frac{2^2}{\quad} \quad \frac{2^1}{\quad} \quad \frac{2^0}{\quad}$

0 0 0 1 0 1 0 1 $\rightarrow 21$

1 0 0 1 0 1 0 1 $\rightarrow -107$

1 0 0 1 0 0 0 1 $\rightarrow -111$

0 0 0 1 0 0 0 1 $\rightarrow 17$

10 bit Numbers:-

$\frac{2^{n-1}}{\quad} \quad \frac{2^{n-2}}{\quad} \quad \frac{2^{n-3}}{\quad} \quad \frac{2^2}{\quad} \quad \frac{2^1}{\quad} \quad \frac{2^0}{\quad}$
 $-2^{n-1} \quad \quad \quad 2^3 \quad 2^2 \quad 2^1 \quad 2^0$

\downarrow

Max Neg \rightarrow 1 0 0 0 0 0 $\rightarrow -2^{n-1}$

Max pos \rightarrow 0 1 1 1 1 1 $\rightarrow 1$

will MSB base value be always -ve?

unsigned

Declare unsigned 4 bit
no'

2^3 2^2 2^1 2^0
— — — —

Declare unsigned 8
bit no'

2^7 2^6 2^5 2^4 2^3 2^2 2^1 2^0

signed

Declare signed 4 bit
no'

-2^3 2^2 2^1 2^0
— — — —

Declare signed 8 bit,

-2^7 2^6 2^5 2^4 2^3 2^2 2^1 2^0

How will system know signed/
unsigned,

C/C++/C#

unsigned

unsigned int x
unsigned long x
unsigned short x

{ Base value of MSB is +ve

↳ we can't store -ve
numbers.

Default

int x
long x
short x

By default they
are signed:

Base value of
MSB bit is -ve.

In java: There is no
such that as unsigned,

There are only signed
data types.

Break : 10:05 → 10:15 pm ,



Ranges in Signed Datatypes.

2 bit Signed no.

-2^1	2^0	Decimal	→ [-2, 1]
0	0	→ 0	min max
0	1	→ 1	
1	0	→ -2	
1	1	→ -1	

Can we store -5 or 10 in
a 2 bit no. [no]

3 bit Signed no.

-2^2	2^1	2^0	Decimal	Min	Max
0	0	0	= 0	[-4, 3]	
0	0	1	= 1		
0	1	0	= 2		
0	1	1	= 3		
1	0	0	= -4		
1	0	1	= -3		
1	1	0	= -2		
1	1	1	= -1		

n bit signed no.

	<u>Min</u>	<u>Max</u>
2 bits	-2	1
3 bits	-4	3

n-1 ... 3 2 1 0

Min \Rightarrow 1 0 0 0 0 0 ... $\rightarrow -2^{n-1}$

Max \Rightarrow 0 1 1 1 1 ... 1 1 1 \rightarrow

\downarrow
 2^{n-2}

\downarrow
 2^2

\downarrow
 2^1

\downarrow
 2^0

$$\Rightarrow 2^0 + 2^1 + 2^2 + \dots + 2^{n-2}$$

$$\Rightarrow a = 1, r = 2, \text{ Terms} = \underline{n-1}$$

$$S = \frac{a(r^{n-1})}{r-1} \Rightarrow \frac{1(2^{n-1}-1)}{2-1}$$

$$\Rightarrow \underline{2^{n-1}-1}$$

Range of n bit no. :- $[-2^{n-1} \text{ to } 2^{n-1}]$

	bytes	bits	min	max
byte / char	1	8	$[-128, 127]$	

\hookrightarrow can we store 130, 240, 10^5
 \hookrightarrow overflows.

short int	2	16 \Rightarrow	$\{-2^{15}, 2^{15}-1\}$ $[-32768, 32767]$
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int	4	32 \Rightarrow	$\{-2^{31}, 2^{31}-1\}$ close app $\rightarrow \{-2 \cdot 10^9, 2 \cdot 10^9\}$
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long int	8	64 \Rightarrow	$\{-2^{63}, 2^{63}-1\}$ close app $\rightarrow \{-8 \cdot 10^{18}, 8 \cdot 10^{18}\}$
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$$2^{10} = 1024 \approx 1000$$

$$(2^{10})^3 \approx (1000)^3$$

$$2^{30} \approx 10^9 \xrightarrow{\cdot 2} 2^{31} \approx 2 \cdot 10^9$$

\downarrow

$$2^{60} \approx 10^{18} \xrightarrow{\cdot 2^3} 2^{63} \approx 8 \cdot 10^{18}$$

Importance of Constraints :-

Q1) Given an array, calculate sum of it.

Constraints :-

$$1 \leq N \leq 10^5$$

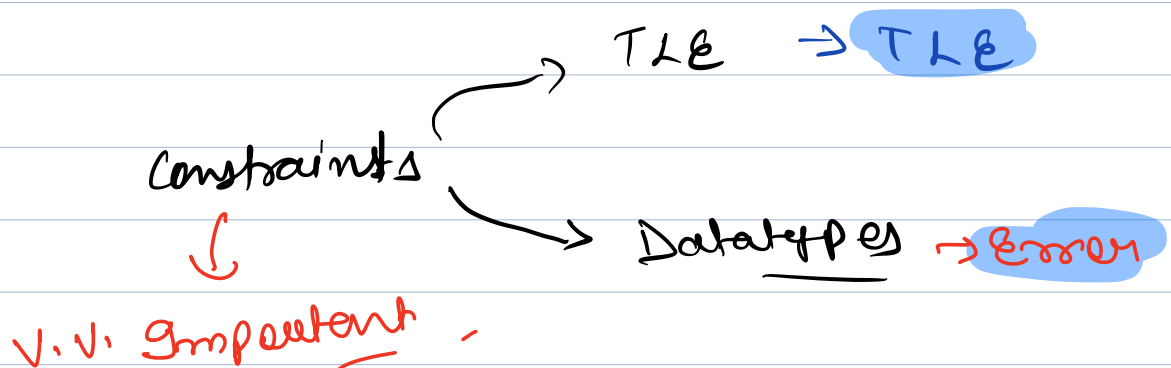
$$1 \leq \text{arr}[i] \leq 10^6$$

$$1 \leq \text{sum} \leq 10^{11}$$

↓

Can we store in int + int
we need to use long.

```
long  
int sum(int arr[]) {  
    int n = arr.length  
    long sum = 0  
    for (i = 0; i < n; i++)  
    {  
        sum = sum + arr[i]  
    }  
    return sum;  
}
```



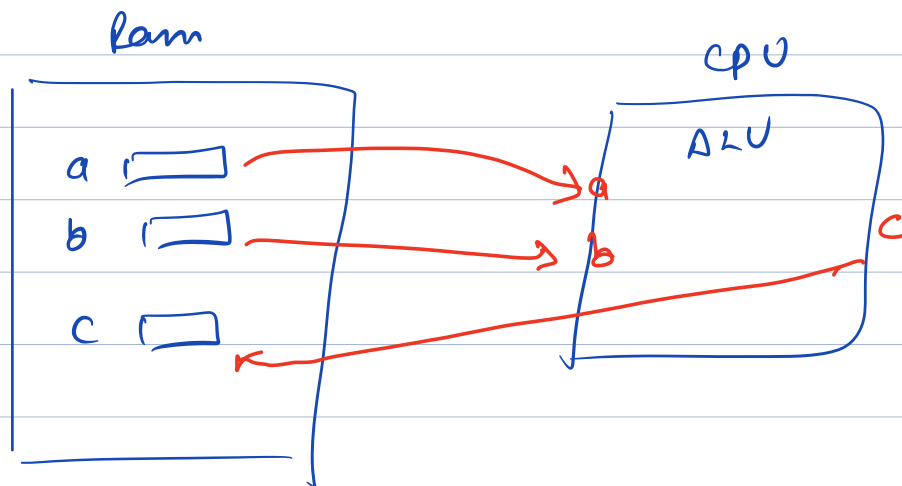
Ques Given 2 numbers a & b,
return their prod.

$$1 \leq a, b \leq 10^6$$

```

prod (int a, int b) {
    int c = a * b
    long c = (a * b);
    long c = long(a * b)
    long c = (long)a * b
    long a1 = a, b1 = b
    return a1 * b1
}

```



Take care :-

- when we multiply int * int.
- when we multiply long * long.

Ans (Long. max-value < B):

$$(01111) < B$$

Ques, given N & i , unset i th bit in N .

$N = 23$
 $i = 2,$

4	3	2	1	0	
1	0	1	1	1	
		↓			
1 0 0 1 1					

→

1	0	1	1	
		↓		
1 1 0 1 1				

→ 1 1 0 1 1

~ (0 0 1 0 0) → 1 1 0 1 1

no:-

1	1	1	1	0	0	1	1
1	1	1	0	1	1	1	1
1 1 1 0 0 0 1 1							

→ 1 1 1 0 1 1 1 1

→ (0 0 0 1 0 0 0 0)

Ques) Given x, y set x continuous bits & y unset bits.

$$x = 8, y = 2 \quad \therefore \quad \begin{matrix} 4 & 3 & 2 & 1 & 0 \\ 1 & 1 & 1 & 0 & 0 \end{matrix} \rightarrow 28$$

$$\hookrightarrow \quad 111 < \leq 2$$

$$x = 5, y = 3$$

$$\hookrightarrow \quad \begin{matrix} 1 & 1 & 1 & 1 & 0 & 0 & 0 \end{matrix}$$

$$11111 < \leq 3$$

$$11111 < \leq y$$

$$\begin{matrix} \rightarrow & 1 & 1 & 1 & \rightarrow & 7 \\ \rightarrow & 1 & 0 & 0 & 0 & \downarrow & 8 \end{matrix}$$

$$\left(\frac{1 < \leq 3}{-1} \right)$$

$$\begin{matrix} \rightarrow & \overbrace{1111}^x & \rightarrow & 15 \\ \rightarrow & 10000 & \rightarrow & 16 \end{matrix}$$

$$\downarrow$$

$$(1 < \leq 4)$$

$$\left((1 < \leq n) - 1 \right) < \leq y$$

→

7	6	5	4	3	2	1	0
1	1	0	0	0	1	1	1

→ 8 bit.