

CLASS-II → 13/09/2023

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SEARCHING & SORTING

LEVEL-01

1. Linear search

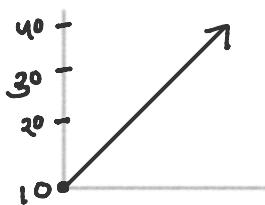
array	10	20	30	40	50	60	70	80	Target = 70
	0	1	2	3	4	5	6	7	

Time Complexity: $O(N)$, where N is Length of array.

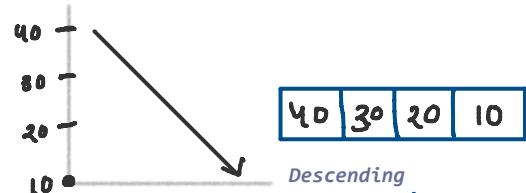
```
func int i=0; i< arr.size(); i++) {
    if( arr[i] == target) {
        return true;
    }
}
return false;
```

2. Binary search

- Binary search is always work on MONOTONIC array
- MONOTONIC → Ascending or Descending order of array



10	20	30	40
Ascending			

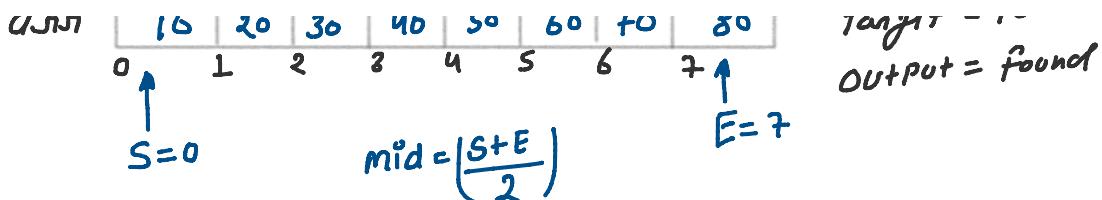


40	30	20	10
Descending			

EXAMPLE ①

array	10	20	30	40	50	60	70	80
	0	1	2	3	4	5	6	7

Target = 70
Output = found



Rules

- ① $\text{arr}[\text{mid}] == \text{target}$
 return true
 - ② $\text{arr}[\text{mid}] < \text{target}$
 $s = \text{mid} + 1$
 - ③ $\text{arr}[\text{mid}] > \text{target}$
 $E = \text{mid} - 1$

Note

BEST PRACTICE FOR FINDING MID

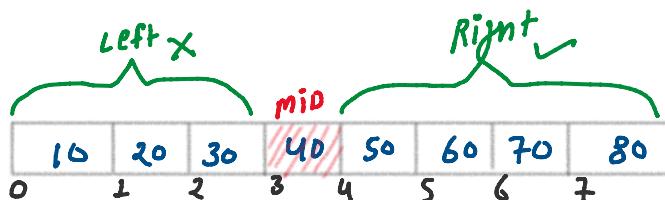
$$\leftarrow \text{mid} = s + \left(\frac{e-s}{2} \right)$$

④ Terminating conditions

may be \rightarrow (sc e)
OR
(sc = e)

DRY RUN

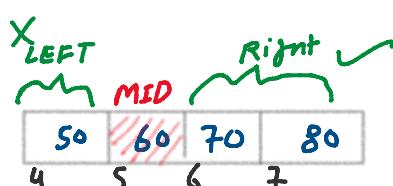
Iteration: 0



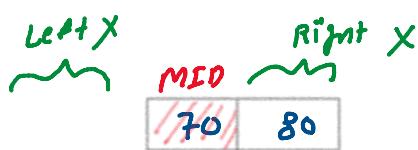
$$s=0 \quad e=7 \quad \text{mid} = 3 \quad \text{target} = 70 \quad \text{Rule} \Rightarrow \textcircled{2} \checkmark$$

$40 < 70$
 ↳ right

Iteration: 1



Itnation:2



Iteration: 2



$$s=6 \quad e=7 \quad \text{mid} = 6 \quad \text{target} = 70 \quad \text{Rule} \Rightarrow (1) \quad 70 == 70 \quad \hookrightarrow \text{return True}$$

Output: found

EXAMPLE (2)

array

10	20	30	40	50	60	70	80
0	1	2	3	4	5	6	7

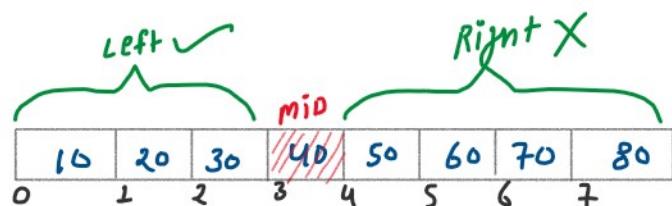
$\uparrow S=0$ $\uparrow E=7$

$\text{mid} = \left(\frac{S+E}{2} \right)$

$$\text{target} = 20 \\ \text{output} = \text{found}$$

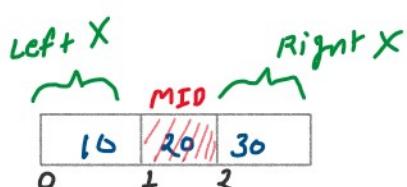
DRY RUN

Iteration: 0



$$s=0 \quad e=7 \quad \text{mid} = 3 \quad \text{target} = 20 \quad \text{Rule} \Rightarrow (3) \quad 40 > 20 \quad \hookrightarrow \text{left +}$$

Iteration: 1



$$s=0 \quad e=2 \quad \text{mid} = 1 \quad \text{target} = 20 \quad \text{Rule} \Rightarrow (1) \quad 20 == 20 \quad \hookrightarrow \text{return True}$$

Output: found

```

// Binary Search
bool binarySearch(vector<int> arr, int target){
    int n=arr.size();
    int start=0;
    int end=n-1;

    // Best practice of finding mid index
    int mid=start+((end-start)/2);

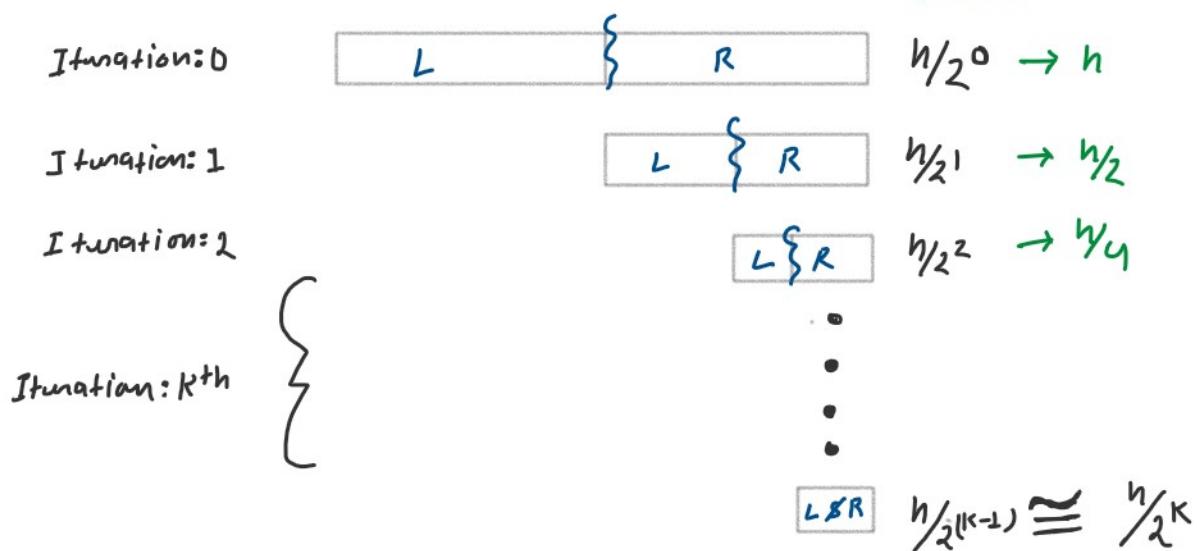
    bool ans=false;

    // Rule 04: Terminating condition to outside of loop
    while(start<=end){
        // Rule 01: When target found the return true
        if(arr[mid]==target){
            ans = true;
            return ans;
        }
        // Rule 02: When target is greater than mid of array value then skip the left part
        else if(arr[mid]<target){
            start=mid+1;
        }
        // Rule 03: When target is less than mid of array value then skip the right part
        else if(arr[mid]>target){
            end=mid-1;
        }
        // Update the mid index (HIGH CHANCE:---->Yaha par me galti kar skta hun)
        mid=start+((end-start)/2);
    }
    // When target not found then return false
    return ans;
}

```

3. Find Time Complexity of Binary Search

size = h



$$\Rightarrow \frac{h}{2^K} = 1$$

$$\Rightarrow h = 2^K$$

$$\Rightarrow h = 2^k$$

$$\Rightarrow \log_2 h = \log_2 (2^k)$$

$$\Rightarrow \log_2 h = k \xrightarrow{\text{T.C.}} O(k) \Rightarrow O(\log n)$$

RULE ↗

$$\log_{A^A} A = 1$$

5. Find first occurrence of a number in sorted array

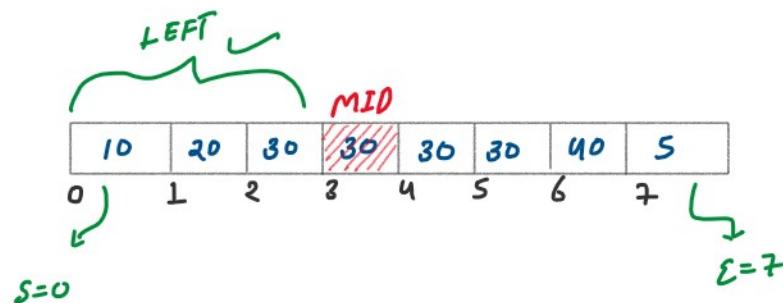
array	<table border="1" style="display: inline-table; vertical-align: middle;"> <tr><td>10</td><td>20</td><td>30</td><td>30</td><td>30</td><td>30</td><td>40</td><td>5</td></tr> <tr><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td></tr> </table>	10	20	30	30	30	30	40	5	0	1	2	3	4	5	6	7
10	20	30	30	30	30	40	5										
0	1	2	3	4	5	6	7										

$$\text{target} = 30$$

$$\text{output} = ?$$

DRY RUN

Iteration: 0



$$\text{Mid} = \frac{0+7}{2} = 3$$

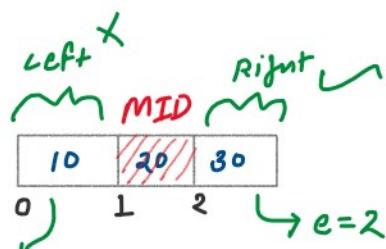
Ans = 3

$$\textcircled{1} \quad \text{array}[mid] == \text{target}$$

$$\begin{cases} \text{Ans} = \text{mid} \\ \text{e} = \text{mid}-1 \end{cases}$$

mid ko Ans main store karlo AND Right part ko skip kardo

Iteration: 1



$$\text{Mid} = \frac{0+2}{2} = 1$$

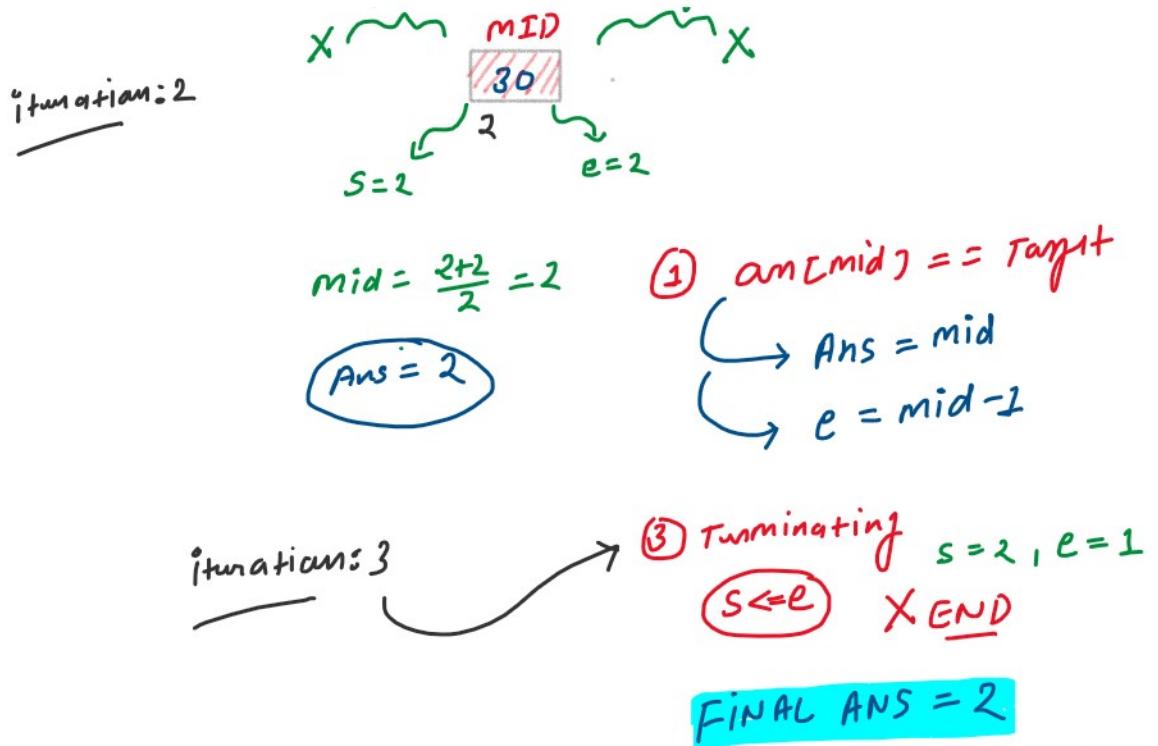
Ans = 3

$$\textcircled{2} \quad \text{array}[mid] < \text{target}$$

$$\rightarrow s = \text{mid} + 1$$

Iteration: 2





```
// First occurrence
int findFirstOccurrence(vector<int> arr, int target){
    int n=arr.size();
    int start=0;
    int end=n-1;
    int ans=-1;

    while(start<=end){

        int mid=start+((end-start)/2);

        // Rule 01: When target is equal to mid of array then store possible index in ans and skip the right part
        if(arr[mid]==target){
            ans=mid;
            end=mid-1;
        }
        // Rule 02: When target is greater than mid of array value then skip the left part
        else if(arr[mid]<target){
            start=mid+1;
        }
        // Rule 03: When target is less than mid of array value then skip the right part
        else if(arr[mid]>target){
            end=mid-1;
        }
    }
    // When first occurrence of a number is found then return ans=index otherwise ans=-1
    return ans;
}
```

6. Find Last occurrence of a number in sorted array

array	10	20	30	30	30	30	40	5
0	1	2	3	4	5	6	7	

target = 30
output = 5

7. Find total occurrence of a number in sorted array

array	10	20	30	30	30	30	40	5	
0	1	2	3	4	5	6	7		

$\text{target} = 30$
 $\text{output} = 4$

$$\begin{aligned}
 \text{Total OC} &= \text{Last OC} - \text{First OC} + 1 \\
 &= 5 - 2 + 1 \\
 &= 4 \quad \text{Ans}
 \end{aligned}$$

```
// First occurrence
int findTotalOccurrence(vector<int> arr, int target){
    int lastIndex=findLastOccurrence(arr,target); // 5
    int firstIndex=findFirstOccurrence(arr,target); // 2
    int totalOccurrence=lastIndex-firstIndex+1; // 5-2+1=6-2=4
    return totalOccurrence; // 4
}
/*
EXAMPLE 01:
INPUT: arr[10,20,30,30,30,30,40,50], target=30
OUTPUT: Total occurrence of target is 4
*/
```

OUTPUT: Total occurrence of target is 4
*/

8. Find missing element in sorted array (GFG)

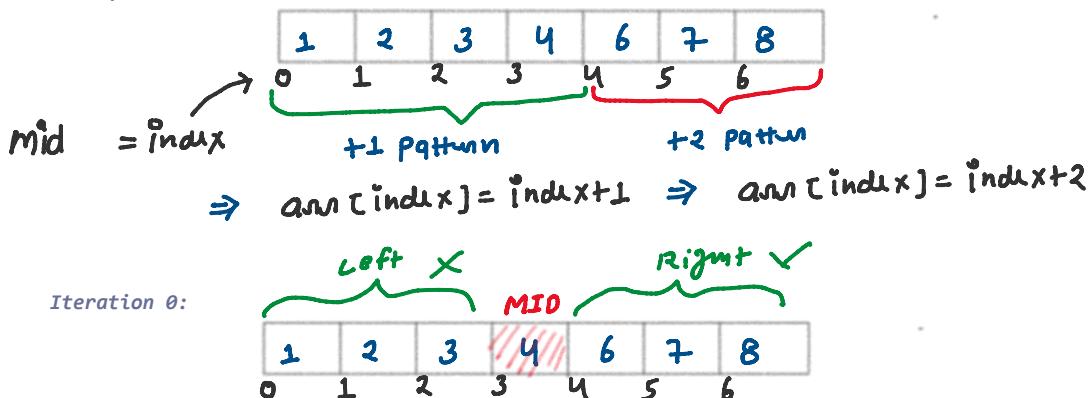
- Given a list of $n-1$ integers and these integers are in the range of 1 to n .
- There are **no duplicates** in list.
- One of the integers is missing in the list.

Example 01:
Input : arr[] = [1, 2, 3, 4, 6, 7, 8]
Output : 5

Example 02:
Input : arr[] = [1, 2, 3, 4, 5, 6, 8, 9]
Output : 7

DRY RUN

Example 01:



$$s = 0 \\ e = 6 \\ \text{mid} = \frac{0+6}{2} = 3$$

AB pattern check karna htae difference
 nikai ke
 $\text{difference} = arr[\text{mid}] - \text{mid}$
 $= 4 - 3$
 $= 1$

when (difference = 1) then skip left side
 $s = \text{mid} + 1;$

Iteration 1:

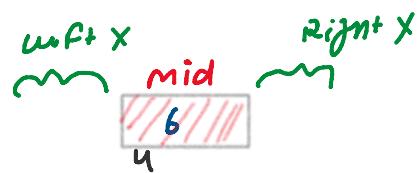


$$s = 4 \\ e = 6 \\ \text{mid} = \frac{4+6}{2} = 5$$

$\text{difference} = arr[5] - 5$
 $= 7 - 5$
 $= 2$
 when (difference = 2) then skip right part
 and store mid in ans
 $\text{ans} = 5$ and

\hookrightarrow $ans = 5$ and
 $e = mid - 1$

Iteration 2:



$$s = 4$$

$$e = 4$$

$$mid = \frac{s+e}{2} = 4$$

$$\begin{aligned} \text{difference} &= arr[mid] - mid \\ &= 6 - 4 \\ &= 2 \end{aligned}$$

\hookrightarrow ($\text{difference} == 2$)
 $ans = 4$ and
 $e = mid - 1$

\hookrightarrow RUK jao... Kyunki
 $s = 4, e = 3$ Lakin ($s <= e$)

($s > e$) XEND

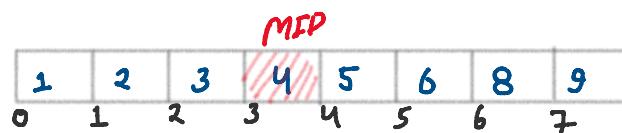
\hookrightarrow AB Ans Return Kando

\hookrightarrow return (ans + 1); (5) missing number

DRY RUN

Output = ?

Example 02:



$$s = 0$$

$$e = 7$$

$$mid = \frac{s+e}{2} = 3$$

$$\begin{aligned} ① \text{difference} &= arr[mid] - mid \\ &= 4 - 3 \\ &= 1 \end{aligned}$$

($\text{difference} == 1$)

$\hookrightarrow s = mid + 1$

Iteration 1:



Iteration 1:

$$\begin{aligned} s &= 4 \\ e &= 7 \\ \text{mid} &= \frac{s+e}{2} = 5 \end{aligned}$$

MID				
5	6	8	9	
4	5	6	7	

$$\begin{aligned} \textcircled{1} \quad \text{diff}_1 &= arr[\text{mid}] - \text{mid} \\ &= 6 - 5 \\ &= 1 \\ \textcircled{2} \quad (\text{diff}_1 &= 1) \\ \hookrightarrow s &= \text{mid} + 1 \end{aligned}$$

Iteration 2:

$$\begin{aligned} s &= 6 \\ e &= 7 \\ \text{mid} &= \frac{s+e}{2} = 6 \end{aligned}$$

MID		
8	9	
6	7	

$$\begin{aligned} \textcircled{1} \quad \text{diff}_1 &= arr[\text{mid}] - \text{mid} \\ &= 8 - 6 \\ &= 2 \\ \textcircled{2} \quad (\text{diff}_1 &= 2) \\ \hookrightarrow \text{Ans} &= \text{mid} \\ &= 6 \\ e &= \text{mid}-1 \end{aligned}$$

QUK jao... \Rightarrow $s > e$ X END

Ans return Random
 \Rightarrow medium (Ans+1); Output \Rightarrow 7 missing no.

```

// Find missing element
int findMissingElement(int arr[], int size){
    int start=0;
    int end=size-1;
    int mid=start+((end-start)/2);
    int ans=-1;

    while(start<=end){
        // Rule 01: Find the pattern
        int difference=arr[mid]-mid;

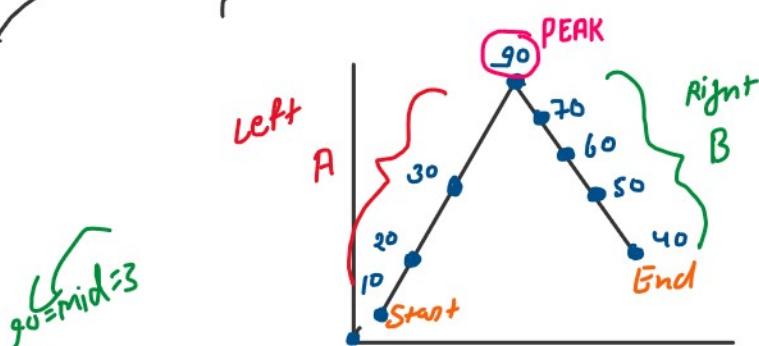
        // Rule 02: When difference is equal to 1 then skip the left part
        if(difference==1){
            start=mid+1;
        }
        // Rule 03: When difference is equal to 2 then store mid index in ans and skip the right part
        else if(difference==2){
            ans=mid;
            end=mid-1;
        }
        // Updated mid index
        mid=start+((end-start)/2);
    }
    return ans+1;
}

```

Most Imp 9. Peak element/index in a mountain array (Leetcode-852)

EXAMPLE 1

arr	10	20	30	90	70	60	50	40
i	0	1	2	3	4	5	6	7



Rule:1

$$arr[mid] < arr[mid+1]$$

Shift to Right $start = mid + 1$

Rule:2

$$arr[mid] > arr[mid+1]$$

Shift to Left / Peak point
 $End = mid$

$(End = mid - 1)$

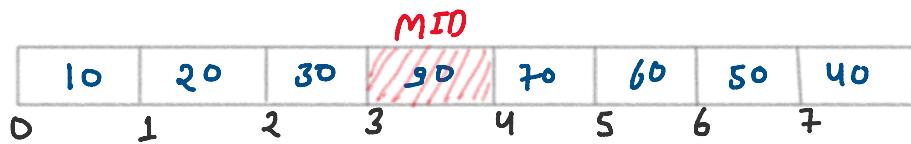
YEH KYUN NAHI KIY? KYUN HAI
HO SKTQ HAI XI YEH
KANN SE PEAK POINT
NA MILE.

DRY RUN

MID

DRY RUN

Iteration: 0



$$S=0$$

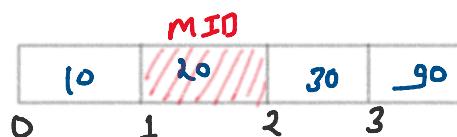
$$E=7$$

$$\text{mid} = \frac{0+7}{2} = 3$$

$\text{arr}[\text{mid}] > \text{arr}[\text{mid}+1]$

$90 > 70 \quad \begin{cases} \text{① main B line par HU yaq} \\ \text{② main PEAK par HU} \end{cases}$

Iteration: 1



$$S=0$$

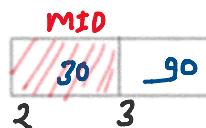
$$E=3$$

$$\text{mid} = \frac{0+3}{2} = 1$$

$\text{arr}[\text{mid}] < \text{arr}[\text{mid}+1]$

$20 < 30 \quad \begin{cases} \text{① main A line par HU AND} \\ \text{② Right me PEAK hai} \end{cases}$

Iteration: 2



$$S=2$$

$$E=3$$

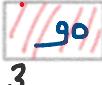
$$\text{mid} = \frac{2+3}{2} = 2$$

$\text{arr}[\text{mid}] < \text{arr}[\text{mid}+1]$

$20 < 90$
 $\text{Start} = \text{mid}+1$

Iteration: 3

MID



$$S=3$$

$$E=3$$

$$\text{mid} = \frac{3+3}{2} = 3$$

AB RUK jao... Kya Kri
 $S=3, E=3, S==E$

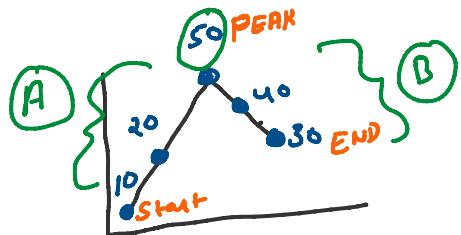
$S < E$
END

return mid
return S ;

- IMPLEMENTATION

EXAMPLE 2

arr	10	20	50	40	30
0	1	2	3	4	



Iteration: 1

MID	10	20	50	40	30
0	1	2	3	4	

$$S = 0$$

$$E = 4$$

$$\text{Mid} = \frac{0+4}{2} = 2$$

$$\text{arr}[\text{mid}] > \text{arr}[\text{mid}+1]$$

$\hookrightarrow 50 > 40 \left\{ \begin{array}{l} \text{① B line part HU ya} \\ \text{② PEAK part HU} \end{array} \right.$
 $\text{End} = \text{mid}$

Iteration: 0

MID	10	20	50
0	1	2	

$$S = 0$$

$$E = 2$$

$$\text{Mid} = \frac{0+2}{2} = 1$$

$$\text{arr}[\text{mid}] < \text{arr}[\text{mid}+1]$$

$\hookrightarrow 20 < 50 \left\{ \begin{array}{l} \text{① A line part HU} \\ \text{② Right nu PEAK HAI} \end{array} \right.$
 $\text{Start} = \text{mid} + 1$

Iteration: 2

50
2

$$\left. \begin{array}{l} S = 2 \\ E = 2 \end{array} \right\} \text{RUK jao } \dots \dots (S < E)$$

$\hookrightarrow \text{Return Kan do } S \text{ KO}$

$\text{return } S$

return

return value return KAN DO start always PEAK

Note

So hamara return karne ki kyunki start always peak point par exist karne hai at the end ml.

```
● ● ●

// Program 06: Peak element/index in a mountain array (Leetcode-852)
class Solution {
public:
    int peakIndexInMountainArray(vector<int>& arr) {
        int n=arr.size();
        int start=0;
        int end=n-1;

        // Termination condition
        while(start<end){
            int mid=start+(end-start)/2;

            if(arr[mid]>arr[mid+1]){
                // Me B line par hu
                // Yaa me PEAK par hu
                end=mid;
            }
            else if(arr[mid]<arr[mid+1]){
                // Me A line par hu
                // And PEAK right me exist karta hai
                start=mid+1;
            }
        }

        return start;
    };
}

/*
Example 1:
Input: arr = [0,1,0]
Output: 1

Example 2:
Input: arr = [0,2,1,0]
Output: 1

Example 3:
Input: arr = [0,10,5,2]
Output: 1

Example 4:
Input : arr[] = [10,20,30,90,70,60,50,40]
Output : 3

Example 5:
Input : arr[] = [10,20,50,40,30]
Output : 2
*/
```