

Mensuration

Mensuration



OnlineStudy4u

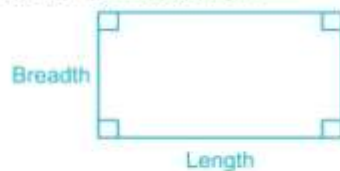
Placement for ALL. All for Placement

This Video Completely covers the problems on "Mensuration" which is more than sufficient for all kind of placement Exams eg: TCS/WIPRO/AMCAT/ELITMUS/CoCubes and all other placement Exams.

Mensuration by : Pratik Shrivastava (10 years of industry experience and best Aptitude trainer)

Mensuration:

1. Mensuration Formulas for RECTANGLE



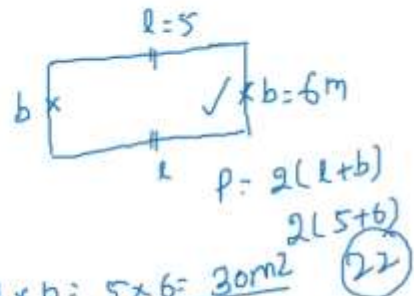
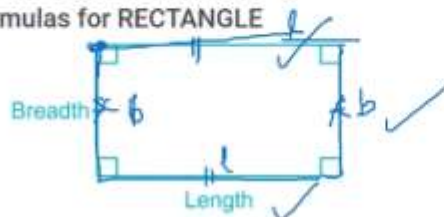
Area of Rectangle = Length * Breadth

Perimeter of Rectangle = 2 * (Length * Breadth)

Length of the Diagonal = $\sqrt{\text{Length}^2 + \text{Breadth}^2}$

Mensuration:

1. Mensuration Formulas for RECTANGLE



Area of Rectangle = Length * Breadth

$$\text{Area} = l \times b = 5 \times 6 = 30\text{m}^2$$

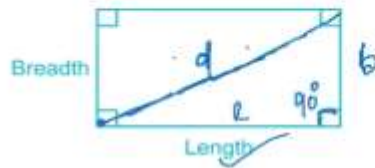
Perimeter of Rectangle = 2 * (Length + Breadth)

$$2l + 2b \\ l + b + l + b = 2(l + b) \checkmark$$

Length of the Diagonal = $\sqrt{\text{Length}^2 + \text{Breadth}^2}$

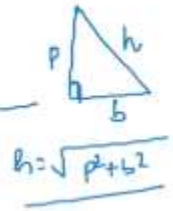
Mensuration:

1. Mensuration Formulas for RECTANGLE



Pythagoras theorem

$$d = \sqrt{l^2 + b^2}$$



Area of Rectangle = Length \times Breadth

Perimeter of Rectangle = $2 \times (\text{Length} + \text{Breadth})$

Length of the Diagonal = $\sqrt{\text{Length}^2 + \text{Breadth}^2}$

Mensuration:

2. Mensuration Formulas for Square:

side



side

Area of Square = side \times side

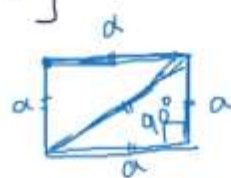
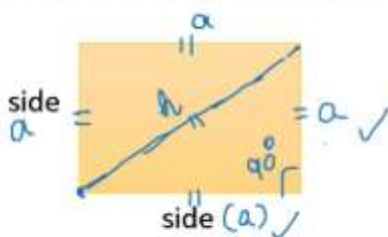
Perimeter of Square = $4 \times \text{side}$

Length of the Diagonal = $\sqrt{2} \times \text{side}$

Area (in terms of diagonal) = $(\text{diagonal})^2 / 2$

Mensuration:

2. Mensuration Formulas for Square:



$$[a + a + a + a = 4a = 4 \times \text{side}]$$

Area of Square = side \times side

Perimeter of Square = $4 \times \text{side}$

Length of the Diagonal = $\sqrt{2} \times \text{side}$

Area (in terms of diagonal) = $(\text{diagonal})^2 / 2$

$$\text{Area} = \text{side} \times \text{side} = a \times a = a^2$$

Pythagoras \checkmark $h = \sqrt{p^2 + b^2}$

$$\Rightarrow h = \sqrt{l^2 + b^2} \checkmark$$

$$h: \text{diagonal} = \frac{\sqrt{a^2 + a^2}}{\sqrt{2}a}$$

Mensuration:

2. Mensuration Formulas for Square:

side



side

$$\text{side} = a$$

$$\text{Area} = (\text{side})^2$$

$$\text{diagonal} = \sqrt{2} \text{ side}$$

$$\text{Area} = a^2, \quad d = \sqrt{2} a$$

$$(d)^2 = (\sqrt{2} a)^2$$

$$d^2 = 2a^2$$

$$\frac{d^2}{2} = \frac{2}{2} a^2$$

$$\boxed{\frac{d^2}{2} = a^2 = \text{Area}}$$

$$\text{Area of Square} = \text{side} \times \text{side}$$

$$\text{Perimeter of Square} = 4 \times \text{side}$$

$$\text{Length of the Diagonal} = \sqrt{2} \times \text{side}$$

$$\text{Area (in terms of diagonal)} = \frac{(\text{diagonal})^2}{2}$$

Mensuration

Q1. The length and breadth of a rectangle are in ratio 9:5. If the area is 720 m^2 , find its perimeter.

1) 112m 2) 115m 3) 110m 4) 118m

Solution:

x x x

Trick:

Perimeter = $2(l+b)$
 $2(9+5)$
 2×14
 $= 28$

Perimeter = $2(l+b)$
 $= 2(9x+5x)$
 $= 2 \times 14x$
 $= 2 \times 14 \times 4$
 $= 112 \text{ m}$

Normal

$$l:b = 9:5 \checkmark$$

$9x = l$
 $5x = b$
 $\begin{cases} l = 9x \\ b = 5x \end{cases}$

$$\text{Area} = l \times b$$

$$\Rightarrow 720 = 9x \times 5x$$

$$x = 4$$

$$x^2 = 16$$

$$x = \pm 4$$

$$x = 4$$

Mensuration

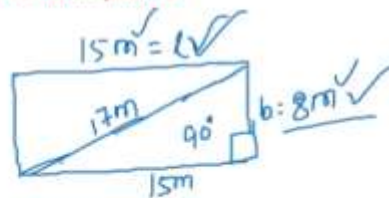
Q2. One side of a rectangular field is 15m and one of its diagonal is 17m. Find the area of the field.

a) 60 msquare b) 110 msquare c) 120 msquare d) 140 msquare

Solution:

$$\Rightarrow \text{Area} = l \times b$$

$$\Rightarrow 15 \times 8 = 120 \text{ m}^2$$



Pythagoras

$$h^2 = p^2 + b^2$$

$$\Rightarrow (17)^2 - (15)^2 = p^2$$

$$\Rightarrow 289 - 225 = p^2$$

$$64 = p^2$$

$$\sqrt{p} = 8 \text{ m}$$

Mensuration

Q3. The length of rectangle is twice the breadth. If the length is decreased by 5cm and breadth is increased by 5cm, the area of the rectangle is increased by 75cmsquare. Find the length of the rectangle.

a)10cm b)20cm c)30cm d)40 cm

Solution:

$$l = 2x \quad 2 \times 20 = 40 \text{ cm} \quad b = x, \quad l = 2x$$

$$\checkmark \quad l = 2b$$

$$\Rightarrow A_2 - A_1 = 75$$

$$\Rightarrow (2x-5)(x+5) - 2x \times x = 75$$

$$\Rightarrow 2x^2 + 10x - 5x - 25 - 2x^2 = 75$$

$$5x = 100$$

$$x = 20$$

$$\begin{cases} (l-5) = (2x-5) \\ (b+5) = (x+5) \end{cases}$$

Mensuration

Q4. Find the cost of carpeting a room 13m long and 9m broad with a carpet 75cm wide at the rate of 12.40rs per square meter.

a)1720rs b)1934.40rs c)2120rs d)1220rs

Solution:

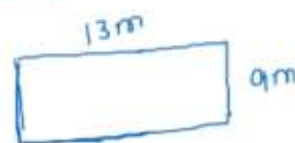
$$\begin{aligned} \text{Area} &= l \times b \\ &\Rightarrow 13 \times 9 = 117 \text{ m}^2 \end{aligned}$$

$$156 \times 12.4 = 1934.4$$

$$\text{length of carpet} = \frac{117 \text{ m}^2}{75 \text{ cm}}$$

$$\Rightarrow 156 \times 12.4 = 1934.4 \text{ rs}$$

[Placement]



$$\begin{aligned} 39 &= \frac{117 \times 100}{75} \\ &= 156 \text{ m} \checkmark \end{aligned}$$

$$\begin{aligned} 1 \text{ m} &= 100 \text{ cm} \\ 1 \text{ cm} &= \frac{1}{100} \text{ m} \end{aligned}$$

$$\begin{array}{r} 156 \\ 124 \\ \hline 624 \\ 312 \\ \hline 156 \\ \hline 19344 \end{array}$$

Mensuration

Q5. Find the largest size of bamboo that can be placed in a square of area 100sqm.

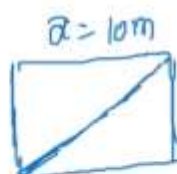
a)7.7m b)14.14m c)24.24m d)None

Solution:

$$\text{Area} = 100 \text{ m}^2$$

$$a^2 = 100$$

$$a = 10 \text{ m}$$



$$\text{diagonal} = \sqrt{2} a$$

$$= 10 \times 1.414$$

$$\Rightarrow 14.14 \text{ m}$$

Mensuration

Q6. If the diagonal of a square is increased by 15%, find the percentage increase in the area.

- a) 25% b) 32.25% c) 40% d) 35%

Solution:

old Area

assume $a = 5\sqrt{2}$
 $d = \sqrt{2}a = \sqrt{2} \times 5\sqrt{2} = 10$

$A = \frac{1}{2}(d)^2 = \frac{10 \times 10}{2} = 50$

new Area

$d = 11.5$

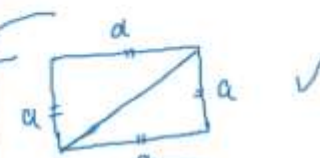
$A = \frac{1}{2}(d)^2 = \frac{11.5 \times 11.5}{2} = 65.875$

$\frac{65.875 - 50}{50} \times 100 = 32.25\%$

common sense

5 min

placement



$d = a\sqrt{2}$

$A = \frac{1}{2}(d)^2$

$\frac{10 + 10 \times 15}{100} = 11.5$

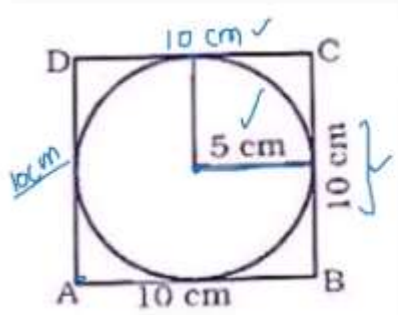
Mensuration

Q7. From a square piece of paper having each side equal to 10cm, the largest possible circle is being cutout. The ratio of the area of the circle to the area of the original square is nearly.

- a) 4:5 b) 3:5 c) 5:6 d) 6:7

$\frac{4}{5} = 0.8$

Solution:



$\frac{A_{\text{circle}}}{A_{\text{square}}} = \frac{\frac{22}{7} \times 5 \times 5}{10 \times 10} = \frac{11}{14} \approx 0.8$

$\frac{22}{28} \times \frac{11}{14} \approx 0.8$

πr^2

$\pi = \frac{22}{7}$

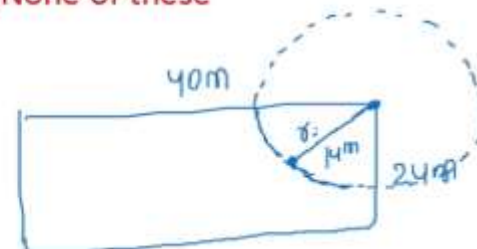
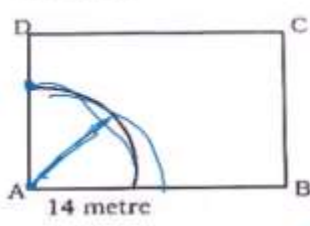
$14 \times 8 = 112$

Mensuration

Q8. A horse is tethered to one corner of a rectangular grassy field 40m by 24m with a rope 14m long. Over how much area of the field can it graze?

- a) 154 cmsquare b) 308 cmsquare c) 150 cmsquare d) None of these

Solution:



$A = \pi r^2$
 $\pi = \frac{22}{7}$

$\frac{1}{4} \text{th of Area of circle}$
 $\frac{1}{4} \times \pi r^2 = \frac{1}{4} \times \frac{22}{7} \times 14 \times 14 = 154$

Mensuration

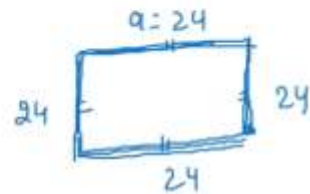
Q9. The area of a square field is 576kmsquare. How long it take for a horse to run around at the speed of 12km/h.

a)12h b)10h c)8h d)6h

Solution:

Speed = 12 km/hr ✓

\Rightarrow Area = 576 kmsquare
 $a^2 = 576$ $\sqrt{576} = 24$
 $a = 24$



Total distance = perimeter = $24 \times 4 = 96$ km ✓

$D = S \times t \Rightarrow 96 = 12 \times t \Rightarrow t = \frac{96}{12} = 8h$

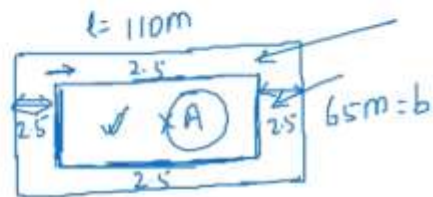
Mensuration

Q10. A rectangular grassy field 110m by 65m has a gravel path 2.5m wide all around it on the inside. Find the cost of gravelling the path at 80 paise per sqm.

a)700 b)800 c)680 d)740

Solution:

Area of rectangle $k = l \times b$
 $= 110 \times 65$
 $= 7150 m^2$ ✓

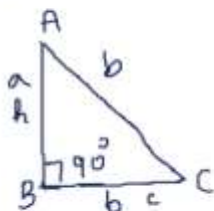


Area of inner rectangle = $(110 - 5) \times (65 - 5)$

Area of path needs to gravel = 105×60
 $= 7150 - 6300$
 $= 850 m^2$
 $\Rightarrow 850 m^2 \times \frac{80}{100} = 680 \text{ paise}$ ✓

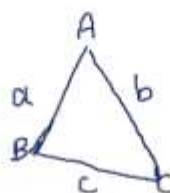
Mensuration

Triangle:

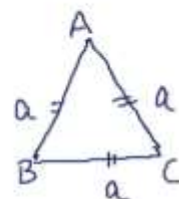


Area of $\triangle ABC$
 $= \frac{1}{2} \times b \times h$

Perimeter = $\frac{\text{sum of all sides}}{a+b+c}$



\checkmark Area of $\triangle ABC$
 $= \sqrt{s(s-a)(s-b)(s-c)}$
 $\left[s = \frac{a+b+c}{2} \right]$



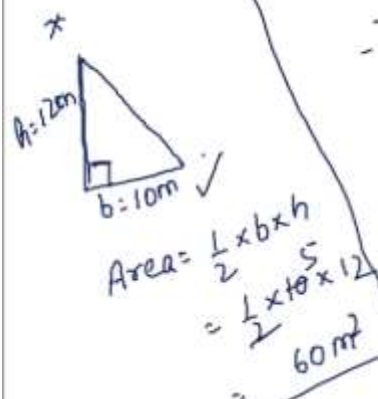
$\Rightarrow \text{Area} = \frac{\sqrt{3}}{4} a^2$

\Rightarrow perimeter
 $= a + a + a$
 $= 3a$

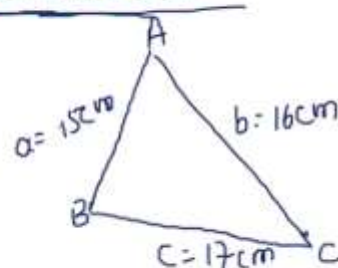
Mensuration

Q11. Find the area of triangle whose sides are 15cm, 16cm and 17cm.

Solution:



$$\begin{aligned} \text{Area} &= \sqrt{s(s-a)(s-b)(s-c)} \\ &= \sqrt{24(24-15)(24-16)(24-17)} \\ &= \sqrt{24 \times 9 \times 8 \times 7} \\ &= \sqrt{8 \times 3 \times 3 \times 3 \times 8 \times 7} \\ &= 8 \times 3 \sqrt{21} \\ &= 24\sqrt{21} \end{aligned}$$



$$\begin{aligned} s &= \frac{a+b+c}{2} \quad \leftarrow \text{Perimeter} \\ &\downarrow \\ &\text{semi perimeter} \\ s &= \frac{15+16+17}{2} = \frac{48}{2} = 24 \end{aligned}$$

Mensuration

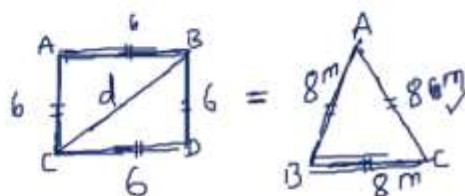
Q12. The cost of fencing an equilateral triangular park and a square park is the same. If the area of the triangular park is $16\sqrt{3} \text{ m}^2$, find the length of the diagonal of the square park.

a. 8.484 b. 8 c. 9 d. 12

Solution:

$$\begin{aligned} \text{Area of } \Delta ABC &= \frac{\sqrt{3}}{4} a^2 = 16\sqrt{3} \\ a^2 &= 64 \Rightarrow a = 8 \end{aligned}$$

$$\begin{aligned} \text{perimeter of square} &= \text{perimeter of } \Delta \\ \Rightarrow 4 \times a &= 24 \\ 4 \times a &= \frac{24}{4} = 6 \end{aligned}$$

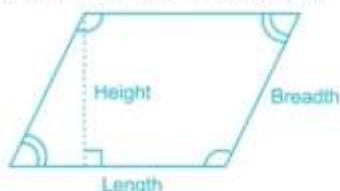


$$\begin{aligned} \text{perimeter} &\checkmark \\ &= 8+8+8 \\ &= 3 \times 8 = 24 \text{ m} \end{aligned}$$

$$\begin{aligned} d &= a\sqrt{2} \\ &= 6\sqrt{2} \\ 6 \times 1.414 &= 8.484 \end{aligned}$$

Mensuration:

3. Mensuration Formulas for PARALLELOGRAM

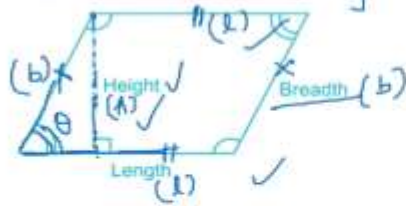


Area of parallel gram = Length * Height

Perimeter of Rectangle = 2 * (Length * Breadth)

Mensuration:

Q. Mensuration Formulas for PARALLELOGRAM



[Quadrilateral]

① Area of parallelogram
 $= l \times h$

Area of parallelogram = Length * Height ✓

Perimeter of parallelogram = $2 * (\text{Length} + \text{Breadth})$

Sum of sides: $l + b + l + b$

$2l + 2b = 2(l + b)$

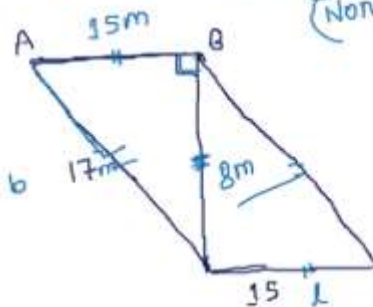
② Area of parallelogram
 $a \times b \times \sin \theta$

Mensuration

Q13. In a diagram shown, Quadrilateral ABCD is parallelogram. Find its Area.

- a) 700 b) 800 c) 680 d) 740 (e) 120m^2
 (None of these)

Solution:



Area of $\square = l \times h$

$\Rightarrow 8\text{m} \times 15\text{m} = 120\text{m}^2$

Pythagoras $\Rightarrow h^2 = p^2 + b^2$
 $17^2 = p^2 + 15^2$
 $= 289 - 225 = p^2$
 $= 64 = p^2$
 $p = 8$

Mensuration

Q14. A parallelogram has sides 30m and 14m and one of its diagonal is 40m long. Then its area is .

- a) 168msquare b) 336msquare c) 370msquare d) 480msquare

Solution:

Area = $l \times h$

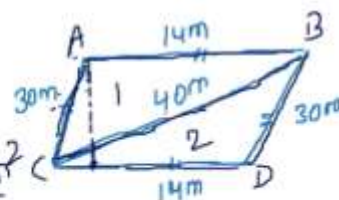
$= \triangle ABC + \triangle BCD$ ✓

$= 2 \triangle ABC = 2 \times 168 = 336\text{m}^2$

$A = \sqrt{s(s-a)(s-b)(s-c)}$

$= \sqrt{42 \times (42-30) \times (42-40) \times (42-14)}$

$= \sqrt{6 \times 7 \times 6 \times 2 \times 2 \times 28}$



$s = \frac{30 + 14 + 40}{2}$

$= \frac{84}{2} = 42$

$= \sqrt{6 \times 6 \times 2 \times 2 \times 7 \times 7 \times 2 \times 2}$
 $= 6 \times 2 \times 7 \times 2$

$6 \times 2 \times 7 \times 2$
 $= 6 \times 28$
 $= 168\text{m}^2$

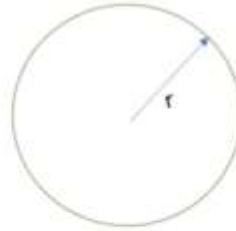
$= 168 \times 2$

Mensuration:

r = radius

d = diameter = $2r$

- Area of circle : πr^2
- Circumference of Circle = $2\pi r$
- Circumference of semi circle = $(\pi r + d)$
- Area of Semi circle : $\pi r^2 / 2$



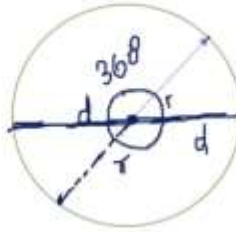
Circle

Mensuration:

r = radius ✓

d = diameter = $2r$

- Area of circle : πr^2 ✓
- Circumference of Circle = $2\pi r$
- Circumference of semi circle = $(\pi r + d)$ $2\pi r$
- Area of Semi circle : $\pi r^2 / 2$



$$\frac{360^\circ}{2\pi r}$$

Circle

Circumference = Perimeter

πr

radius = r

diameter = $2r$

$$\pi = \frac{22}{7} \approx 3.14$$



Mensuration

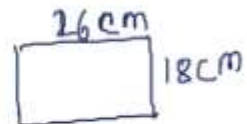
Q15. A circle and A rectangle have the same perimeter. The sides of the rectangle are 18cm and 26cm. what is the area of the circle?

a) 88 cmsqaure b) 154 cmsqaure c) 1250 cmsqaure d) 616 cmsqaure ✓

Solution:

$$\checkmark \text{ Perimeter } \bigcirc = \text{ Perimeter } \square$$

$$2\pi r = 2(l+b)$$



$$\text{Area of } \bigcirc = \pi r^2$$

$$14 \times (40+4) = \frac{22}{7} \times 14 \times 14 = 44 \times 14 = 560 + 56 = 616 \text{ cm}^2$$

$$2 \times \frac{22}{7} \times r = 2(26+18)$$

$$\frac{22}{7} \times r = 442$$

$$r = 14 \text{ cm}$$

Mensuration

Q16 When the circumference and area of a circle are numerically equal, then the diameter is numerically equal to _____

a) Area b) circumference c) 4 d) 2π

Solution:

$$\Rightarrow \text{Circumference } O = \text{Area } O$$

$$\Rightarrow 2\pi r = \pi r^2$$

$$\boxed{r = 2}$$

$$d = 2 \times r$$

$$= 2 \times 2 = 4$$

Mensuration

Q17 If the area of a circle decreased by 36%, then the radius of a circle decreased by _____

a) 20% b) 18% c) 36% d) 64%

Solution:

Option

assume

Important

Common sense

$$r = 10 \text{ cm}$$

$$A = \pi r^2 = \pi \times 10 \times 10 = 100\pi$$

$$\text{Now } A = \pi \times 8 \times 8 = 64\pi$$

$$100 - 36 = 64$$

$$10 - 8$$

$$\frac{100 - 80}{20 \text{ diff}} = 20\%$$

Mensuration

Q18 A wire can be bent in the form of a circle of radius 56cm. If it is bent in the form of a square, then its area will be _____

A) 7744

B) 8844

C) 5544

D) 4444

Solution:

concept

good

Perimeter (length)

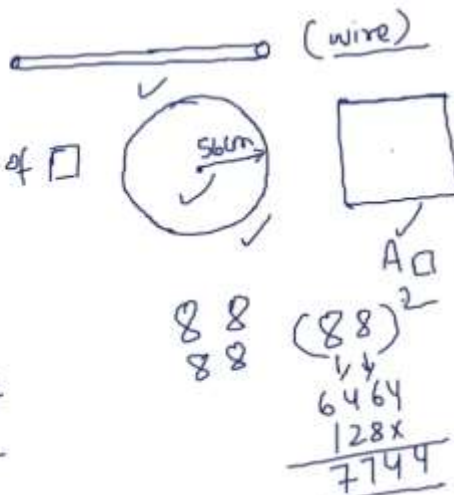
Perimeter of O = perimeter of \square

$$\Rightarrow 2\pi r = 4 \times a$$

$$2 \times \frac{22}{7} \times 56 = 4 \times a$$

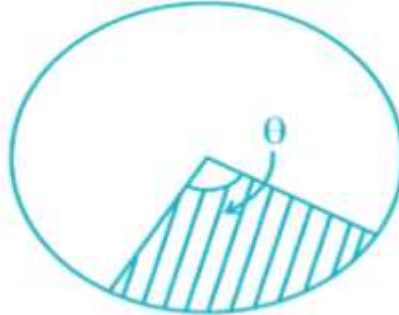
$$a = 22 \times 2 \times 2 = 88 \text{ cm}$$

$$\text{Area} = (\text{Side})^2 = (88)^2 = 7744$$



Mensuration:

➤ Length of Arc = $(2\pi r\theta) / 360$ where θ is the central angle in degrees.



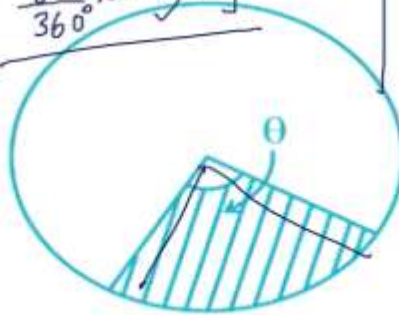
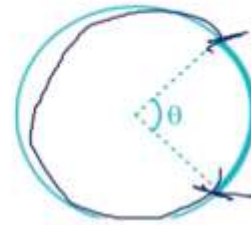
- Area of a sector = $(1/2) \times (\text{length of arc}) \times r = (\pi r^2 \theta) / 360$

Mensuration:

➤ Length of Arc = $(2\pi r\theta) / 360$ where θ is the central angle in degrees.

① Length of Arc = $\frac{\theta}{360} \times 2\pi r$ ✓

② Area of sector = $\frac{\theta}{360} \times \pi r^2$ ✓



- Area of a sector = $(1/2) \times (\text{length of arc}) \times r = (\pi r^2 \theta) / 360$

Mensuration

Q19. In a circle of radius 7cm, an arc subtends an angle of 108° at the center. The area of the sector is.

- A) 43.2cmsquare B) 44.2cmsquare
C) 45.2cmsquare ✓ D) 46.2cmsquare

Solution:

$$\text{Area of sector} = \frac{\theta}{360} \times \pi r^2$$

$$= \frac{3 \times 108}{10 \times 360} \times \frac{22}{7} \times 7 \times 7$$

$$\frac{66 \times 7}{10} = \frac{46.2 \text{ cm}^2}{1}$$



Mensuration

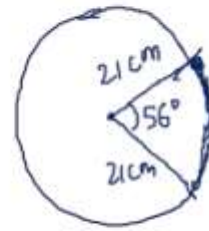
Q20. If in a circle of radius 21cm, an arc subtends an angle of 56° at the center, the length of the arc is .

- A) 15.53cm B) 16.53cm
C) 18.53cm D) 20.53cm

Solution:

$$\text{Length of Arc} = \frac{\theta}{360^\circ} \times 2\pi r$$

$$= \frac{56^\circ}{360^\circ} \times 2 \times \frac{22}{7} \times 21$$

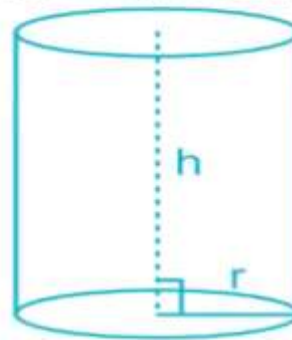


$$\frac{616}{30} = 20.53\text{cm}$$

Mensuration:

Mensuration formula for CYLINDER:

In the following formulae, r = radius of base, h = height of cylinder



- Curved surface area of a cylinder = $2\pi rh$
- Total surface area of a cylinder = $2\pi r(r + h)$
- Volume of a cylinder = $\pi r^2 h$

Mensuration:

Mensuration formula for CYLINDER:

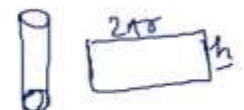
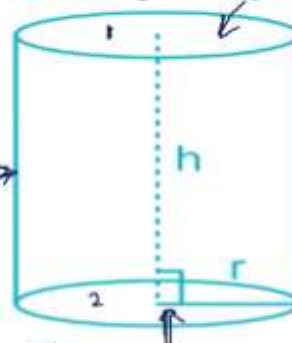
In the following formulae, r = radius of base, h = height of cylinder

① $\pi r^2 h$ ✓

② $2\pi rh$

③ $2\pi rh + 2\pi r^2$
 $2\pi r(r + h)$

Curved
Surface



placement

cylinder

[two circles + rectangle]

✓ Curved surface area of a cylinder = $2\pi rh$

✓ Total surface area of a cylinder = $2\pi r(r + h)$

✓ Volume of a cylinder = $\pi r^2 h$

Mensuration

Q21. The radius and height of a cylinder are in the ratio 5:7 and its volume is 4400cm^3 . then its radius will be?

- A) 4cm B) 10cm
C) 5cm D) 12cm

Solution:

$$\text{volume of cylinder} = \pi r^2 h$$

$$8 \quad 2 \times 4400 = \frac{22}{7} \times 5x \times 7x \times 7x$$

$$5 \times 2 = 10\text{cm}$$

$$x^3 = 8\text{cm}^3$$

$$x = 2\text{cm}$$



Mensuration

Q22. The volume of a right circular cylinder whose curved surface area is 2640cm^2 and circumference of its base is 66cm is?

- A) 3465cm^3 B) 13860cm^3
C) 7720cm^3 D) 55440cm^3

Solution:

$$\text{Curved surface} = 2\pi r h = 2640$$

$$\Rightarrow 2 \times \frac{22}{7} \times \frac{66}{2} \times h = 2640$$

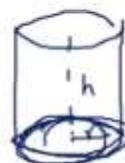
$$h = 40\text{cm}$$

$$\begin{array}{r} 63 \\ 22 \\ \hline 126 \\ 126 \\ \hline 1386 \end{array}$$

$$\text{Circumference of base (C)} = 2\pi r$$

$$2 \times \frac{22}{7} \times r = 66$$

$$r = \frac{21}{2}\text{cm}$$



$$2\pi r h +$$

$$\pi r^2 h \Rightarrow \frac{22}{7} \times \frac{21}{2} \times \frac{21}{2} \times 40$$

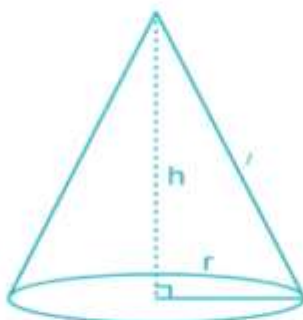
$$= 22 \times 63 \times 10$$

$$= 13860$$

Mensuration:

Mensuration formula for Cone:

In the following formulae, r = radius of base, l = slant height of cone and h = height of the cone (perpendicular to base)



- Slant height of a cone = $l = \sqrt{h^2 + r^2}$
- Curved surface area of a cone = $C = \pi \times r \times l$
- Total surface area of a cone = $\pi \times r \times (r + l)$

Mensuration:

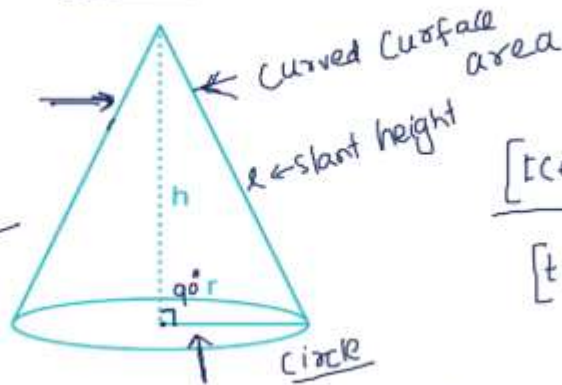
Mensuration formula for Cone:

In the following formulae, r = radius of base, l = slant height of cone and h = height of the cone (perpendicular to base)



Pythagoras
 $l = \sqrt{h^2 + r^2}$

$\frac{1}{3} \pi r^2 h$



[icecream]
 [tent] ✓

- ✓ Slant height of a cone = $l = \sqrt{h^2 + r^2}$
- ✓ Curved surface area of a cone = $C = \pi \times r \times l$
- ✓ Total surface area of a cone = $\pi \times r \times (r + l)$ ✓

$\pi r l + \pi r^2$
 $\pi r (r + l)$

Mensuration

Q23 Find the slant height, volume, curved surface area and the whole surface area of a cone of radius 21cm and height 28cm?

Solution:

① $l = \sqrt{h^2 + r^2} = \sqrt{28^2 + 21^2} = \sqrt{784 + 441} = \sqrt{1225} = 35 \text{ cm}$



② $\pi r l = \frac{22}{7} \times 21 \times 35 = 22 \times 105 = 2200 + 110 = 2310 \text{ cm}^2$

③ $\frac{1}{3} \pi r^2 h = \frac{1}{3} \times \frac{22}{7} \times 21 \times 28 = 22 \times 21 \times 28 = 12936 \text{ cm}^3$

④ $\pi r l + \pi r^2 = 2310 + 1386 = 3696$

$\frac{22}{7} \times 21 \times 28^3$
 22×63
 1320
 1386

OnlineStudyHub & Complete Placement Solution

Mensuration

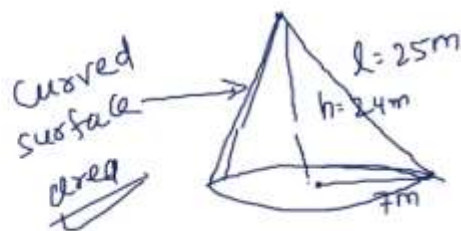
Q24 How many meters of cloth 5m wide will be required to make a conical tent, the radius of whose base is 7m and height is 24m?

- A) 100m B) 110m
 C) 120m D) 150m

Solution:

Curved Surface area = $\pi r l$
 $= \frac{22}{7} \times 7 \times 25$
 $= 22 \times 25$

$l = \sqrt{h^2 + r^2}$
 $= \sqrt{24^2 + 7^2}$
 $= \sqrt{576 + 49}$
 $= \sqrt{625} = 25$



Required cloth = $\frac{22 \times 25 \times 5}{5} = 110 \text{ m}$

Mensuration:

Mensuration formula for Sphere:

Surface Area of sphere = $4\pi r^2$

Volume of sphere = $(4/3)\pi r^3$

$$\frac{4}{3} \pi r^3$$



Sphere

football

Mensuration

Q25 find out the volume and Surface area of a sphere of radius 10.5cm.

Solution:

$$r = 10.5 \text{ cm} = \frac{21}{2} \text{ cm}$$

$$\textcircled{1} \quad \frac{4}{3} \pi r^3 = \frac{4}{3} \times \frac{22}{7} \times \frac{21}{2} \times \frac{21}{2} \times \frac{21}{2}$$

$$= 11 \times 4 \times 11$$

$$\textcircled{2} \quad 4\pi r^2 = 4 \times \frac{22}{7} \times \frac{21}{2} \times \frac{21}{2}$$

$$= 21 \times 66 = 1386 \text{ cm}^2$$

Mensuration

Q26 A copper sphere of radius 3cm is beaten and drawn into a wire of diameter 0.2cm. The length of the wire is

a) 9m b) 12m c) 18m d) 36m

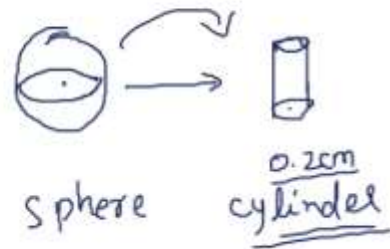
Solution:

$$\Rightarrow V_{\text{sphere}} = V_{\text{cylinder}}$$

$$\frac{4}{3} \times \frac{22}{7} \times 3 \times 3 \times 3 = \pi \times 0.1 \times 0.1 \times h$$

$$\Rightarrow 36 = \frac{1}{10} \times \frac{1}{10} \times h$$

$$h = \frac{3600 \text{ cm}}{h = 36 \text{ m}}$$



Sphere

cylinder

$$1 \text{ m} = 100 \text{ cm} \quad d = 0.2 \text{ cm}$$

$$3600 \quad r = \frac{d}{2} = 0.1 \text{ cm}$$

Mensuration

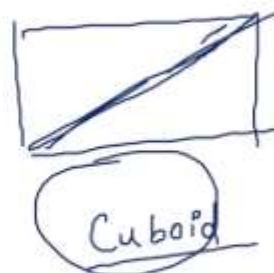
Q27. The length of longest rod that can be placed in a room which is 12m long, 9m broad and 8m high is

a) 27m b) 19m c) 17m d) 13m

Placement

Solution:

$$\begin{aligned}\text{longest rod} &= \sqrt{l^2 + b^2 + h^2} \\ &= \sqrt{12^2 + 9^2 + 8^2} \\ &= \sqrt{144 + 81 + 64} \\ &= \sqrt{289} \\ &= 17\text{m}\end{aligned}$$



Mensuration

Q28. A cube has a surface area 150 msquare. The length of its diagonal is?

a) $5\sqrt{3}$ b) 5m c) $10/\sqrt{3}$ d) 15m

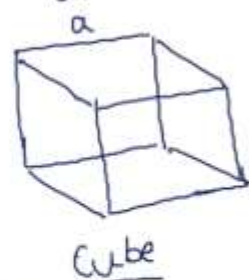
Solution: $5\sqrt{3}\text{m}$

a) Surface area of cube = $6a^2$

b) Volume of cube = a^3

$$6a^2 = \frac{150\text{m}^2}{25}$$

$$a = 5\text{m}$$



$$\sqrt{3}a$$

$$5\sqrt{3}$$