

Ratio and Proportion

Ratio and proportion



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This Video Completely covers Ratio and Proportion which is more than sufficient for all kind of placement Exams eg: TCS/WIPRO/AMCAT/ELITMUS/CoCubes and all other placement Exams.

Ratio and proportion

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Ratio and Proportion

Q1. If $A:B = 5:7$, $B:C = 6:11$ then $A:B:C$ is ?

Solution:

$$\begin{array}{l} A:B = 5:7 \\ B:C = 6:11 \end{array} \left. \begin{array}{l} \times 6 \\ \times 7 \end{array} \right\}$$

A:B:C

$$\begin{array}{l} A:B = 30:42 \\ B:C = 42:77 \end{array}$$

$$\underline{A:B:C = 30:42:77} \checkmark$$

$$\boxed{A:B = \frac{A}{B}}$$

Ratio and Proportion

Q2. If $A:B = 3:4$ and $B:C = 8:9$, then $A:C$ is ?

A. 6:8

C. 9:6

e. None

~~B. 6:9~~ : 2:3

D. 3:8

Solution:

$$\begin{array}{l} A:B = 3:4 \\ B:C = 8:9 \end{array}$$

A:C ✓

$$\left[\begin{array}{l} 2:3 \checkmark \\ 4:6 \checkmark \\ 6:9 \checkmark \end{array} \right]$$

$$\begin{array}{l} 1:2 \\ 2 \times 1: 2 \times 2 \\ \hline 2:4 \end{array}$$

$$\frac{A}{B} = \frac{3}{4} \quad \frac{B}{C} = \frac{8}{9}$$

$$\frac{A}{B} \times \frac{B}{C} = \frac{3}{4} \times \frac{8}{9} = \frac{2}{3} = \underline{2:3} \checkmark$$

Ratio and Proportion

Q3. If $A:B = 8:15$, $B:C = 5:8$ and $C:D = 4:5$, then $A:D$ is equal to ?

- A. ~~8:30~~ 4:5
B. 8:15

- C. 8:24
D. 4:5

Solution:

~~A:D~~

$$A:B = 8:15, \quad B:C = 5:8, \quad C:D = 4:5$$

$$\frac{A}{B} \times \frac{B}{C} \times \frac{C}{D} = \frac{8}{15} \times \frac{5}{8} \times \frac{4}{5}$$

$$\frac{A}{D} = \frac{4}{15} \Rightarrow \frac{A}{D} = \frac{8}{30} \Rightarrow 8:30$$

Ratio and Proportion

Q4. If $2A=3B=4C$, then $A:B:C$ is ?

- A. 2:4:6
B. 2:3:4

- C. ~~6:4:3~~
D. 4:3:2

Solution:

$$A:B:C = 2:3:4 \quad \times$$

$$2A = 3B = 4C, \quad A:B:C$$

$$\frac{2A}{12} = \frac{3B}{12} = \frac{4C}{12} \quad \begin{array}{l} 2, 3, 4 \\ 1, 3, 2 \end{array} = 12$$

$$\frac{A}{6} = \frac{B}{4} = \frac{C}{3} \quad \begin{array}{l} 2 \times 3 \times 2 = 12 \\ A:B:C \\ 6:4:3 \end{array}$$

$$\frac{A}{3} = \frac{B}{2} \Rightarrow 2A = 3B$$

$$A:B = \frac{3}{2} \Rightarrow A:B = 3:2 \checkmark$$

Ratio and Proportion

Q5. If $(A/3) = (B/4) = (C/5)$ then $A:B:C$ is ?

- A. 5:4:3
B. ~~3:4:5~~

- C. 4:3:5
D. None of these

Solution:

$$\text{Format} \rightarrow \frac{A}{3} = \frac{B}{4} = \frac{C}{5} \Rightarrow A:B:C$$

$$3:4:5 \checkmark$$

Ratio and Proportion

Q6. Find the fourth proportional to 4, 9 and 12? x

- A) 18 B) 21 C) 24 D) 27

Answer: Let the fourth proportional to the numbers 4, 9, and 12 be x . Then from the definition of the fourth proportional, we must have:

$$4, 9, 12, x$$

$$\rightarrow \overset{M}{4} : \overset{W}{9} :: \overset{M}{12} : \overset{W}{x}$$

$$\Rightarrow \frac{4 \times x}{x} = \frac{9 \times 12}{3}$$

$$x = 27$$

Ratio and Proportion

Q8. Two numbers are respectively 20% and 50% more than a third number. the ratio of the two numbers is:

- A) 3:4 B) 4:5 C) 5:6 D) 6:7

Solution:

$$\begin{array}{l} \text{3rd} : 100 \\ \text{1st} : 2^{\text{nd}} \\ 120 : 150 \\ \hline 4 : 5 \end{array}$$

$$\begin{array}{l} \text{Third no} = x \\ \text{Calculation} \\ \text{lengthy} \\ \text{2-mth} \end{array}$$

Trick

$$\begin{array}{l} \text{Third} = 100 \\ \text{1st} : 120, \text{2nd} : 150 \\ \hline 120 : 150 \\ 4 : 5 \end{array}$$

Ratio and Proportion

Q9. Salaries of Ravi and Sumit are in the ratio 2:3. If the salary of each is increased by Rs. 4000, the new ratio becomes 40:57. What is Sumit's salary?

- A) 38000 B) 46800 TCS
C) 36700 D) 50000

Solution:

$$\begin{array}{l} R:S = 2:3 \\ R = 2x, S = 3x \\ \Rightarrow \frac{2x+4000}{3x+4000} = \frac{40}{57} \\ \Rightarrow 114x + 57 \times 4000 = 120x + 40 \times 4000 \\ \Rightarrow 6x = 57 \times 4000 - 40 \times 4000 \\ \Rightarrow 6x = 4000(57-40) \end{array}$$

* data - given in terms of ratio

$$\begin{array}{l} A:B = 2:3 \\ A=2x \\ B=3x \end{array}$$

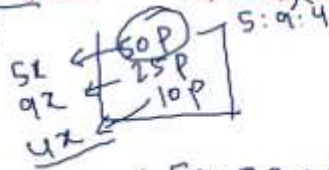
$$\begin{array}{l} 6x = 4000 \times 17 \\ \frac{6x}{6} = \frac{4000 \times 17}{2} \\ 3x = \frac{2000 \times 17}{1} \\ 3x = 34000 \end{array}$$

Ratio and Proportion

Q10. A bag contains 50 P, 25 P and 10 P coins in the ratio 5:9:4, amounting to Rs. 206. Find the number of coins of each type respectively.

- A) 360, 160, 200
B) 160, 360, 200
C) 200, 360, 160
D) 200, 160, 300

Solution:



$$100P = 125$$

$$1P = \frac{1}{100}$$

$$10rs \times 2 + 20rs \times 5 = 20 + 100 = 120$$

$$50 \times 5x + 25 \times 9x + 10 \times 4x = 206 \times 100$$

$$5 \times 40 = 200$$

$$9 \times 40 = 360$$

$$4 \times 40 = 160$$

$$\frac{1}{2} \times \frac{50}{100} \times 5x + \frac{1}{4} \times \frac{25}{100} \times 9x + \frac{1}{5} \times \frac{10}{100} \times 4x = 206$$

$$\frac{5x}{2} + \frac{9x}{4} + \frac{2x}{5} = 206$$

$$\frac{50x + 45x + 8x}{20} = 206$$

$$103x = 206 \times 20$$

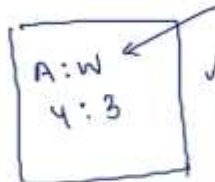
$$x = 40$$

Ratio and Proportion

Q11. A mixture contains alcohol and water in the ratio 4:3. If 5 liters of water is added to the mixture, the ratio becomes 4:5. Find the quantity of alcohol in the given mixture.

- A) 10 B) 12
C) 15 D) 18

Solution:



$$A = 4x$$

$$W = 3x \text{ lit}$$

$$= 4x$$

$$4x \times \frac{2}{3} = 8x$$

$$\Rightarrow \frac{4x}{3x+5} \times \frac{4}{5}$$

$$\Rightarrow 20x = 12x + 20$$

$$8x = 20$$

$$x = \frac{20}{8}$$

Ratio and Proportion

Q12. If Rs. 782 be divided into three parts, proportional to $\frac{1}{2} : \frac{2}{3} : \frac{3}{4}$, then the first part is?

- A) Rs. 182 B) Rs. 190
C) Rs. 192 D) Rs. 204

Solution:

$$6x + 8x + 9x = 782$$

$$23x = 782$$

$$x = \frac{782}{23}$$

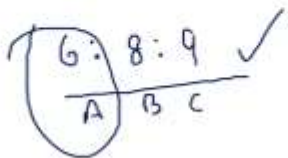
$$= 34$$

$$6 \times 34 = 204$$



$$\frac{1}{2} : \frac{2}{3} : \frac{3}{4}$$

$$12 \times \frac{1}{2} : 12 \times \frac{2}{3} : 12 \times \frac{3}{4}$$



$$200$$

$$A:B = 2:3$$

$$2x + 3x = 200$$

$$5x = 200$$

$$x = 40$$

Ratio and Proportion

Q13. Seats for Mathematics, Physics and Biology in a school are in the ratio 5:7:8. There is a proposal to increase these seats by 40%, 50% and 75% respectively. What will be the ratio of increased seats?

- A) 1:2:3 B) 2:3:4
C) 3:4:5 D) 4:5:6

Solution:

$$M = 5x$$

$$P = 7x$$

$$B = 8x$$

$$\Rightarrow 5x \times \frac{140}{100} : 7x \times \frac{150}{100} : 8x \times \frac{175}{100}$$

$$\Rightarrow 7 : \frac{21}{2} : 14$$

$$\Rightarrow 2 \times 7 : 2 \times \frac{21}{2} : 14 \times 2$$

$$2:3:4 \quad 14:21:28$$

$$\begin{aligned} A &= 120 \\ B &\text{ is } 40\% \text{ more than } A \\ B &= 120 \times \frac{(100+40)}{100} \\ &= \frac{120 \times 140}{100} \\ &= 168 \checkmark \end{aligned}$$

Ratio and Proportion

Q14. The salaries of A, B, and C are in the ratio of 1 : 2 : 3. The salary of B and C together is Rs. 6000. By what percent is the salary of C more than that of A?

- A) 100% B) 200%
C) 300% D) 600%

Solution:

$$A : B : C = 1 : 2 : 3$$

$$A = x$$

$$B = 2x$$

$$C = 3x$$

$$B + C = 6000$$

$$2x + 3x = 6000$$

$$5x = 6000$$

$$x = \frac{6000}{5}$$

$$x = 1200$$

$$A = 1200, C = 3600$$

$$3600 - 1200 = 2400$$

$$\Rightarrow \frac{2400}{1200} \times 100$$

$$\Rightarrow 200$$

$$3 \times 1200 = 3600$$

Ratio and Proportion

Q15. A sum of Rs. 427 is to be divided among A, B and C such that 3 times A's share, 4 times B's share and 7 times C's share are all equal. The share of C is:

- A) 84 B) 140
C) 196 D) 240

Solution:

$$427 \checkmark$$

$$A \quad B \quad C$$

$$28x + 21x + 12x = 427$$

$$61x = 427$$

$$x = \frac{427}{61} = 7$$

$$3, 4, 7 \quad 84$$

$$3A = 4B = 7C$$

$$\frac{3A}{84} = \frac{4B}{84} = \frac{7C}{84}$$

$$A : B : C =$$

$$28 : 21 : 12$$

$$12 \times 7 = 84$$

$$2A = 3B = 4C$$

Ratio and Proportion

Q16. The incomes of two persons A and B are in the ratio 3 : 4. If each saves Rs.100 per month, the ratio of their expenditures is Rs. 1 : 2. Find their incomes.

A) Rs. 100 and Rs.150 B) Rs. 150 and Rs.200

C) Rs.200 and Rs.250 D) Rs.250 and Rs.300

Solution:

$$\begin{array}{l} I \\ E \\ 100 - 20 = 80 \\ 100 - 80 = 20 \end{array}$$

$$\begin{array}{l} \text{Income} \quad A:B = 3:4 \\ I_A = 3x \quad \rightarrow 3 \times 50 = 150 \\ I_B = 4x \quad \rightarrow 4 \times 50 = 200 \\ \text{Saving} = 100x \end{array}$$

$$E_A = \frac{3x - 100}{4x - 100} \times \frac{1}{2}$$

$$E_B =$$

$$\Rightarrow 6x - 200 = 4x - 100$$

$$2x = -100 + 200$$

$$2x = 100 \Rightarrow x = 50$$

Ratio and Proportion

(Ages) ✓

Q17. Ratio of Arun's age to Vinod's age is 4:3. Vinod will be 20 years old after 5 years. what was Arun Age before 3 years?

a) 20years b) 21years c) 17years d) 15years

Solution:

$$A:V = 4:3$$

$$\begin{array}{l} 4 \times 5 = 20 = A = 4x \\ V = 3x \end{array}$$

$$20 - 3 = 17$$

after 5 years.

$$3x + 5 = 20 \checkmark$$

$$3x = 15$$

$$x = 5 \checkmark$$

Ratio and Proportion

Q18. A sum of Rs. 312 was divided among 100 boys and girls in such a way that the boy gets Rs. 3.60 and each girl Rs. 2.40 the number of girls is

- A) 35 B) 40 C) 45 D) 50

Solution:

Boys = b
Girls = g

$$b + g = 100 \quad \text{--- (i)} \times 3.6$$

$$3.6b + 2.4g = 312 \quad \text{--- (2)}$$

$$3.6b + 3.6g = 360$$

$$3.6b + 2.4g = 312$$

$$\hline 1.2g = 48$$

$$g = \frac{48}{1.2} = \frac{480}{12} = 40$$

$$100 \times 3.6 = 360$$

Ratio and Proportion

Q19. The ratio of male and female in a city is 7 : 8 respectively and percentage of children among male and female is 25 and 20 respectively. If number of adult females is 156800, what is the total population of the city?

- A) 4,12,480 B) 3,67,500 C) 5,44,700 D) 2,98,948

$M:F = 7:8$ $M = 7x$ $F = 8x$ \hline Total pop = $15x$	<table border="1"> <thead> <tr> <th colspan="2">Children</th> <th colspan="2">Adults</th> </tr> </thead> <tbody> <tr> <td>M</td> <td>F</td> <td>M</td> <td>F</td> </tr> <tr> <td>25%</td> <td>20%</td> <td>75%</td> <td>80%</td> </tr> </tbody> </table>	Children		Adults		M	F	M	F	25%	20%	75%	80%	$\Rightarrow 8x \times \frac{80}{100} = 156800$ $\Rightarrow 8x \times 5 = 156800$ $\Rightarrow 8x = \frac{156800}{5}$ $\Rightarrow 8x = 31360$ $\Rightarrow x = \frac{31360}{8}$ $\Rightarrow x = 3920$
Children		Adults												
M	F	M	F											
25%	20%	75%	80%											

$15x = \frac{4900 \times 5 \times 15}{8}$ $= \frac{4900 \times 75}{8}$ $= 367500$
